IOITC 2021

Hidden Cell

There is an $N \times N$ matrix. The rows are numbered $0, 1, 2, \ldots, N-1$ top to bottom and the columns are numbered $0, 1, 2, \ldots, N-1$ left to right. There is a hidden cell (a, b). It is known that this cell doesn't lie on the boundary, that is $\min(a, b) > 0$ and $\max(a, b) < N-1$.

Your task is to recover the hidden cell. You can ask queries, in which you give the judge a matrix M of size $N \times N$, consisting of zeroes and ones. Let's call a cell (i,j) valid if (i,j)=(a,b) or M[i][j]=1. The judge replies whether there exists a path from (0,0) to (N-1,N-1) consisting of only valid cells, and going either down or right. Formally, it tells whether there exists a sequence of 2N-1 cells $(0=u_0,0=v_0),(u_1,v_1),\ldots,(N-1=u_{2N-2},N-1=v_{2N-2}),$ such that (u_i,v_i) is a valid cell for all i and either $(u_{i+1}=u_i,v_{i+1}=v_i+1)$ or $(u_{i+1}=u_i+1,v_{i+1}=v_i)$. To make such a query, you can call the function:

```
bool doesPathExist(const vector<string>& M)
```

where you pass the matrix M as a vector of strings of length N each, consisting of characters 0 and 1. The function returns true if there is a path as described above and false otherwise.

You have to implement the function:

```
pair<int, int> findHiddenCell(int N)
```

that makes queries and returns the cell (a, b).

Do NOT read anything from stdin or write something to stdout/stderr.

Test Data and Scoring

Each testfile consists of ≤ 25 testcases, all having N = 50.

If in any testcase of any testfile, you make an invalid query (where M is not an $N \times N$ matrix consisting of only zeroes and ones) or if you return incorrect hidden cell, you get a score of 0. Else, let Q be the maximum number of queries asked by you over all the testcases of all the testfiles.

- If Q > 120, you get 0 points.
- If $61 \le Q \le 120$, you get 9 points.
- If $51 \le Q \le 60$, you get 24 points.
- If $Q \le 50$, you get $54 + \left\lfloor \frac{46 \times (50 \max(Q, 14))}{36} \right\rfloor$ points, where $\lfloor x \rfloor$ denotes the largest integer $\le x$. In particular, you get 54 points if Q = 50 and 100 points if $Q \le 14$.

Local testing

You are provided with a dummy grader with the name dummy_grader.cpp.You should compile your solution (assumed to be in the file solution.cpp) as:

```
g++ solution.cpp dummy_grader.cpp -o grader
```

Then you can run ./grader, and give input of the form as given in the sample input:

- \bullet The first line contains T, the number of test cases.
- \bullet The first line of each testcase contains N.
- ullet The second line contains two integers, a and b, the row and column numbers of the hidden cell.

Limits

Time: 1 seconds Memory: 256 MB