

If we assume the steering angle δ is small:

$$u = \begin{bmatrix} \delta \\ F \end{bmatrix}, s_1 = \begin{bmatrix} y \\ \dot{y} \\ \psi \\ \dot{\psi} \end{bmatrix}, s_2 = \begin{bmatrix} x \\ \dot{x} \end{bmatrix}$$

$$\begin{aligned} \ddot{y} &= -\dot{\psi}\dot{x} + \frac{2Ca}{m} \left(\cos\delta \left(\delta - \frac{\dot{y} + f\dot{\psi}}{\dot{x}} \right) \right) - \frac{2Ca\dot{y}}{m\dot{x}} - \frac{lr\dot{\psi}}{m\dot{x}} \\ &= -\dot{\psi}\dot{x} + \frac{2Ca}{m} \delta - \frac{2Ca\dot{y}}{m\dot{x}} + \frac{2Ca(f\dot{\psi})}{m\dot{x}} - \frac{2Ca\dot{y}}{m\dot{x}} - \frac{2Calr\dot{\psi}}{m\dot{x}} \\ &= \dot{y} \left(-\frac{2Ca}{m\dot{x}} - \frac{2Ca}{m\dot{x}} \right) + \dot{\psi} \left(-\dot{x} - \frac{lr}{m\dot{x}} + \frac{2Calf}{m\dot{x}} \right) + \delta \left(\frac{2Ca}{m} \right) \\ &= \dot{y} \left(-\frac{4Ca}{m\dot{x}} \right) + \dot{\psi} \left(-\dot{x} + \frac{2Calr + 2Calf}{m\dot{x}} \right) + \delta \left(\frac{2Ca}{m} \right) \end{aligned}$$

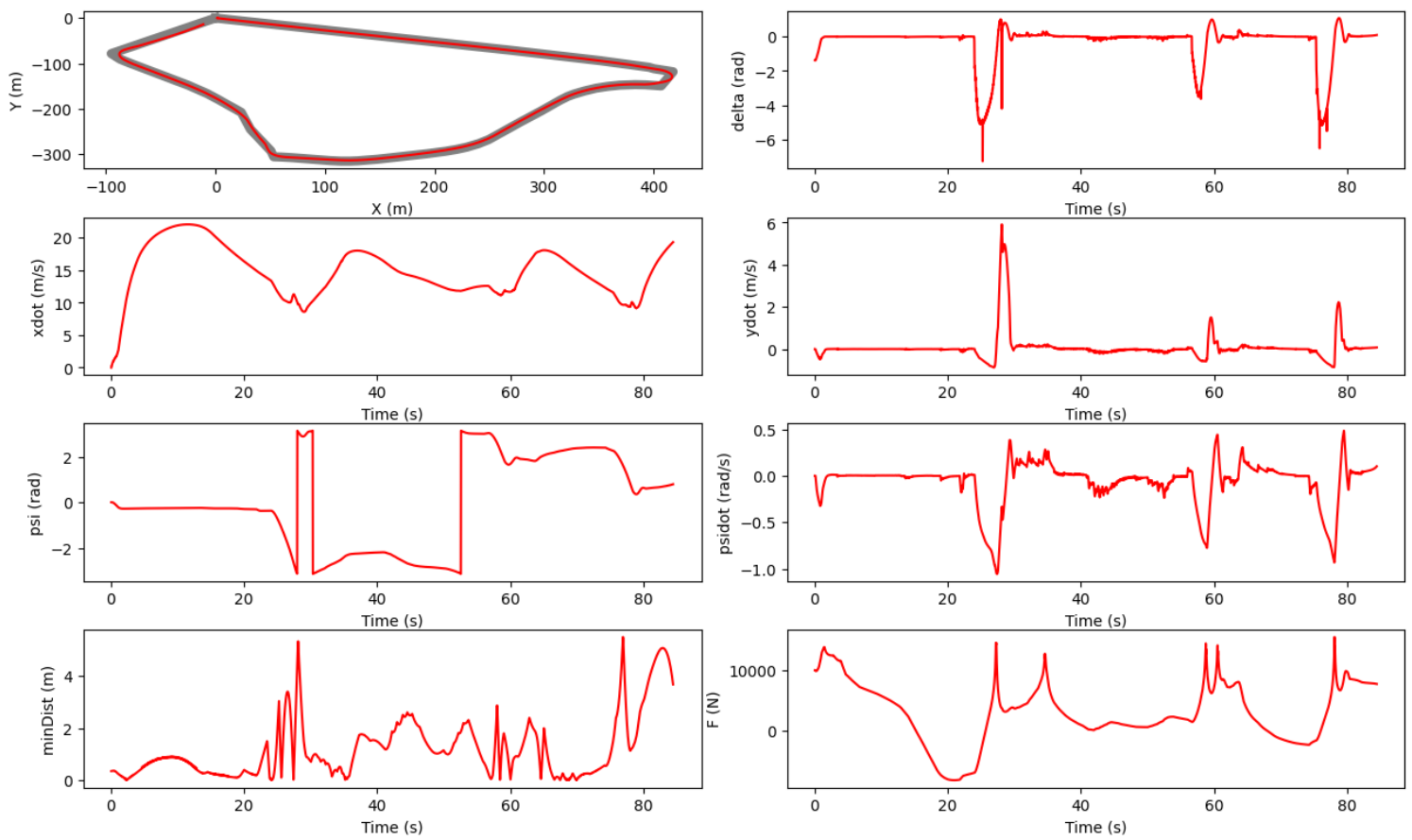
$$\begin{aligned} \ddot{\psi} &= \frac{2lfCa}{I_2} \delta - \frac{2lfCa\dot{y}}{I_2\dot{x}} - \frac{2lf^2\dot{\psi}Ca}{I_2\dot{x}} + \frac{2lrCa\dot{y}}{I_2\dot{x}} - \frac{2lr^2Ca\dot{\psi}}{I_2\dot{x}} \\ &= \dot{y} \left(\frac{2lrCa - 2lfCa}{I_2\dot{x}} \right) + \dot{\psi} \left(-\frac{2lf^2Ca + 2lr^2Ca}{I_2\dot{x}} \right) + \left(\frac{2lfCa}{I_2} \right) \delta \end{aligned}$$

So the linearized equation is:

$$\dot{s}_1 = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & -\frac{4Ca}{m\dot{x}} & 0 & -\dot{x} + \frac{2Calr + 2Calf}{m\dot{x}} \\ 0 & 0 & 0 & 1 \\ 0 & \frac{2lrCa - 2lfCa}{I_2\dot{x}} & 0 & -\frac{2lf^2Ca + 2lr^2Ca}{I_2\dot{x}} \end{bmatrix} \begin{bmatrix} y \\ \dot{y} \\ \psi \\ \dot{\psi} \end{bmatrix} + \begin{bmatrix} 0 & 0 \\ \frac{2Ca}{m} & 0 \\ 0 & 0 \\ \frac{2lfCa}{I_2} & 0 \end{bmatrix} \begin{bmatrix} \delta \\ F \end{bmatrix}$$

$$\ddot{x} = \dot{\psi}\dot{y} + \frac{F}{m} - fg$$

$$\dot{s}_2 = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} x \\ \dot{x} \end{bmatrix} + \begin{bmatrix} 0 & 0 \\ 0 & \frac{1}{m} \end{bmatrix} \begin{bmatrix} \delta \\ F \end{bmatrix} + \dot{\psi}\dot{y} - fg$$



Score for completing the loop: 30.0/30.0
 Score for Score for completing the loop: 30.0/30.0
 Score for average distance: 30.0/30.0
 Score for maximum distance: 30.0/30.0
 Your time is 84.44800000000001
 Your total score is : 100.0/100.0
 total steps: 84448
 maxMinDist: 5.4831341545966525
 avgMinDist: 1.2185331031845643