

Ex3)

linear separation with the least square principle:

$x^{(n)} \Rightarrow$ training vector, $y^{(n)}$ class label

$\hat{y} = W^T X \Rightarrow$ linear classifier, $w_0 = 0$

* the cost/loss function

$$E(w) = \sum_{n=1}^N (y^{(n)} - W^T x^{(n)})^2 \quad \text{--- (1)}$$

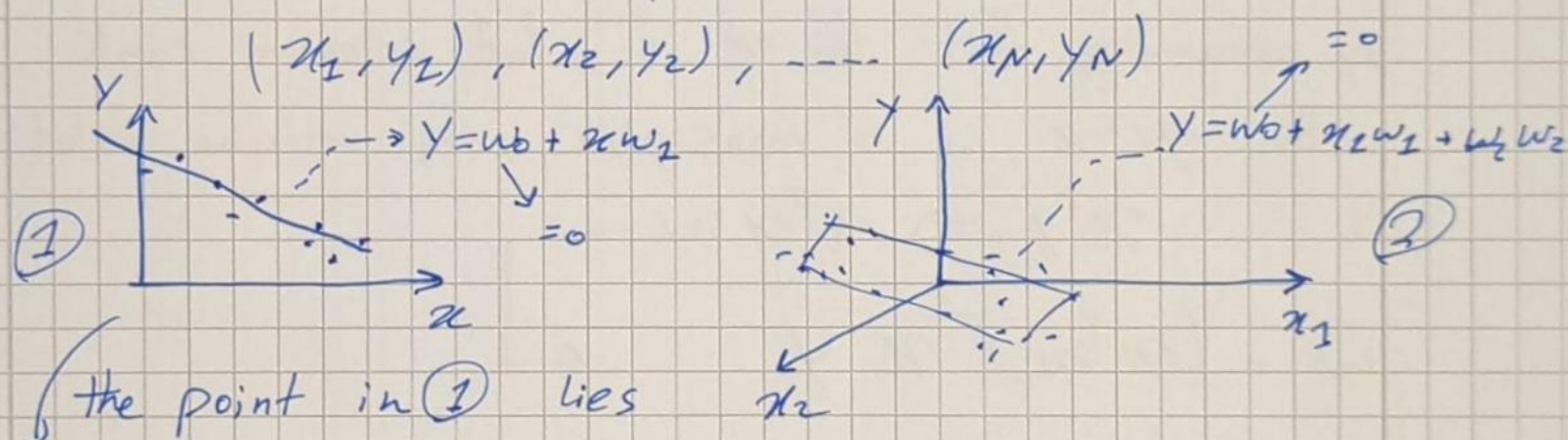
$$E(w) = (y - W^T x)(y - W^T x)^T \quad \text{--- (2)}$$

(a) The $E(w)$ function minimum is always exists but not unique.

The training vectors represent independent random draws.

Therefore, the X represents a $N \times p$ matrix with each row an input vector and y is an N -vector of the outputs in the training set.

The ⁱⁿput/output of observation pairs:



the point in (1) lies in (x_p, y_p) of the slope w_1 as in the two dimensions as $w_0 + x w_1 = y$ is close to $w_0 + x_p w_1 = y$

the point in (2) a data of three dimensions is defined as $w_0 + x_1 w_1 + x_2 w_2 + \dots + x_N w_N = y$ which holds to a hyperplane coordinate slope of $N=2$

By presenting the linear models and least squares and giving a X^T as an input vector $X^T = (x_1, x_2, \dots, x_p)$ the summation would be used as:

$$\hat{y} = \hat{w}_0 + \sum_{n=1}^N X^{(n)} \hat{w}$$

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