CICd_XRotor.m function user guide

1 Introduction and description

This function evaluates the aerodynamic model of a propeller's or rotor's element blade according to the software XRotor [1], by Prof. M. Drela at MIT. The theory uses the following law to build the polar parabola representing the drag coefficient as function of the lift coefficient. The meaning of each one of these quantities is presented in the I/O section.

$$C_d = \left\{ C_{d_{min}} + \frac{dC_d}{dC_l^2} \cdot \left[C_l (C_{d_{min}}) - C_l \right]^2 \right\} \cdot \left(\frac{Re_{\infty}}{Re_{ref}} \right)^f$$

2 1/0

The function is intended to take in *input* the following values. Note that, if the contrary is not stated, the values are represented by scalar quantities.

- $\frac{dc_d}{dc_l^2}$ quadratic coefficient of the parable that approximates the $C_d(C_l)$ law
- $C_l(C_{d_{min}})$ blade element's lift coefficient for which the drag coefficient assumes its minimum value
- \bullet Re_{ref}

blade element's Reynolds number computed taking into account the radius at which the blade element is intended to be (i.e. the reference velocity is Ωr where Ω is the propeller's angular velocity and r is the radial position of the blade element taken into account)

- ullet Re_{∞} asymptotic Reynolds number of the phenomena
- f
 Reynolds number scaling exponent, according to XRotor documentation
- $oldsymbol{c}_{l_{max}}$ maximum blade element's lift coefficient
- ullet $oldsymbol{\mathcal{C}_{l_{min}}}$ minimum blade element's lift coefficient

C_l breakpoints

blade element's lift coefficient breakpoints; this input can be both a vector or a single value; a breakpoint is the value at which the drag coefficient evaluation is requested, according to the $\mathcal{C}_d(\mathcal{C}_l)$ law built through the function script

Input data inserting mode is very strict: the function must be carefully called because the order of the input vectors can only be the following one. Input data given in a different order could result in wrong outputs.

The function takes 2 inputs; the first one must be ordered in the following way:

- 1. Cd_min
- 2. dCd_dCl2
- 3. Cl_Cd_min
- 4. Re_ref
- 5. Re_inf
- 6. *f*
- 7. Cl_max
- 8. Cl_min

the second input can be either a vector or a single value, representing the blade element's lift coefficient breakpoints (i.e. it is the variable previously called C_l breakpoints)

The *outputs* of the function are:

• C_l vector

this is the lift coefficients vector used to build the $C_d(C_l)$ law; it is through this vector that the parable is plotted

\bullet C_d

this is the drag coefficients vector evaluated at C_l vector

• C_d breakpoints

this is a vector or a single value, depending on the nature of the \mathcal{C}_l breakpoints input, whose components are the drag coefficients requested at lift coefficients breakpoints

3 Code description

Once the inputs are stored, the script firstly generates a lift coefficient vector through the line:

```
Cl vec = Cl min:.01:Cl max;
```

and then builds the aerodynamic model implementing the above-mentioned formula:

Cd = (Cd min + dCd dCl2*(Cl Cd min - Cl vec).^2)*(Re inf/Re ref)^f;

After these first passages, the script evaluates the requested drag coefficients breakpoints at the given lift coefficients input values. To do that, the code firstly define an anonymous function through the *handle* command in MATLAB (@) using the built-in function *interp1* applying a piecewise cubic Hermite interpolating polynomial, and then uses this interpolation to evaluates the desired drag coefficients values. The lines referred in this explanation are:

The function finally plots the $C_d(C_l)$ law.

4 Usage examples

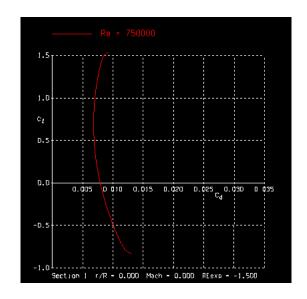
An useful test case input is represented by the following values:

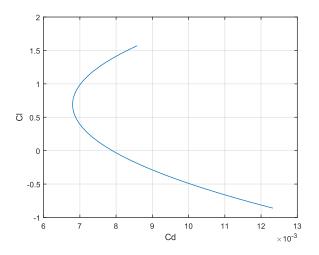
```
input_vec = [.0068, .0023, .69, 750000, 750000, -1.5, 1.57, -.86];
Cl_bp = [0.8,1];
[Cl_vec, Cd, Cd_bp] = ClCd_XRotor(input_vec, Cl_bp);
```

Note that, to work, this calling must be in the same directory as the *ClCd_XRotor.m* script. Results obtained in this case have been validated through the software XRotor itself. Outputs from XRotor and from the *ClCd_XRotor.m* script are reported below: note that the scale of the diagrams is different but pivotal values can be detected to state the conformity of results. In

particular the values to compare are the lift coefficient values at drag coefficients equal to: (0.01, 0.007, 0.0083). It is also reported the display of the aerodynamics parameter of the blade element used in XRotor: values not modified as written above are set as default by the MIT software.

```
Zero-lift alpha (deg):
                     0.00
                               Minimum Cd
                                                 : 0.0068
d(Cl)/d(alpha)
                    6.280
                               Cl at minimum Cd
                                                  : 0.690
d(Cl)/d(alpha)@stall
                                                  : 0.0023
                    0.100
                               d(Cd)/d(C1**2)
                    1.57
Maximum Cl
                               Reference Re number
                                                   750000
Minimum Cl
                   -0.86
                               Re scaling exponent
                                                   -1.5000
                                                  : -0.100
Cl increment to stall: 0.100
                               Cm
                               Mcrit
                                                    0.800
 ------
```





5 References

[1] XRotor software user guide http://web.mit.edu/drela/Public/web/xrotor/xrotor_doc.txt

6 Complete script

The above explained script is thus reported in the following lines.

```
function [Cl vec, Cd, Cd bp] = ClCd XRotor(input v, Cl bp)
    % taking input data
    Cd min = input v(1);
    dCd \ dC12 = input \ v(2);
    Cl Cd min = input v(3);
    Re ref = input v(4);
    Re inf = input v(5);
            = input_v(6);
    f
   Cl_max = input_v(7);
Cl_min = input_v(8);
    % lift coefficient vector creation
    Cl vec = Cl min:.01:Cl max;
    % aerodynamic model building
    Cd = (Cd min + dCd dCl2*(Cl Cd min -
Cl vec).^2)*(Re inf/Re ref)^f;
    %% evaluation of Cd values @ requested Cl breakpoints
    % note that Cl bp can be both a single value or a vector
    % definition of an anonymous function through the handle (@)
symbol
    Cd interp = @(Cl interp) interp1(Cl vec, Cd, Cl interp, 'pchip');
    % anonymous fcn used to compute requested Cd
    Cd bp = Cd interp(Cl bp);
    %% plots section -----
    % blade element's polar diagram
    % along x: drag coefficient
    % along y: lift coefficient
    plot(Cd, Cl vec);
end
```