

Eli - TAARG

- DUCTED PROPELLER'S FUNCTION - TOTAL THRUST

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1 Algorithm

In this brief document, we will describe the algorithm of the function `ducted_prop_thrust.m` based on the semi - empirical method proposed by McCormick. First, the function that calculates the universal function f is called.

```
1 % Use function Feature_RVortexInt to evaluate universal function f
2 f = Feature_RvortexInt(ch,D14,D34);
3 % -----
```

Listing 1: Calling the `Feature_RvortexInt.m` function

Then, the Propeller's induced velocity is calculated.

```
1 % eq 4.24
2 w0 = .5*(-Vinf + sqrt(Vinf^2 + 2*TR/(rho*pi*R^2)));
```

Listing 2: Propeller's induced velocity. `ducted_prop_thrust.m`

Is now possible to evaluate the elicoidal vortex induced axial velocity at $(3/4)c$.

```
1 % eq 3.15
2 w34 = w0*[1 + (0.75*ch/R)/sqrt(1+(0.75*ch/R)^2)];
```

Listing 3: w at $(3/4)c$. `ducted_prop_thrust.m`

Next, is calculated the rotor's induced radial velocity at $(3/4)c$.

```
1 % eq 4.23
2 vi34 = -0.5*(D34/2)*w0*(R^2/((R^2 + (0.25*ch)^2)^1.5));
```

Listing 4: Induced radial velocity v_{iR} at $(3/4)c$. `ducted_prop_thrust.m`

Angular vortex induced velocity is calculated using tangency condition at $(3/4)c$.

```
1 % eq 4.25
2 vi = -vi34 - theta*(w34 + Vinf);
```

Listing 5: Angular vortex induced velocity at $(3/4)c$. `ducted_prop_thrust.m`

Next, the circulation around the shroud is calculated.

```
1 % eq 4.26
2 Gamma = (pi*D14/f)*[-vi34 - theta*(Vinf + w34)];
```

Listing 6: Circulation around the shroud Γ . `ducted_prop_thrust.m`

Rotor's induced radial velocity at $c/4$ is calculated.

```
1 % eq 4.23
2 vi14 = -0.5*(D14/2)*w0*(R^2/((R^2 + (-0.25*ch)^2)^1.5));
```

Listing 7: Induced radial velocity v_{iR} at $c/4$. `ducted_prop_thrust.m`

At the end of the code, thrust's calculations are performed.

```
1 % -----
2 % Thrust component due to the shroud
3 TS = -rho*vi14*Gamma*pi*D14;
4 % -----
5 % Total thrust
6 T = TR + TS;
7 % -----
8 end
```

Listing 8: Thrust's calculations. `ducted_prop_thrust.m`

1.1 Inputs

The function accepts the following inputs:

- flow density ρ ;
- shroud chord c ;
- stream velocity V_∞ ;
- quarter diameter D_{14} ;
- $(3/4)c$ diameter D_{34} ;
- tangency condition's angle θ
- rotor's radius R ;
- free rotor's thrust T_R .

1.2 Outputs

The function generates the following outputs:

- total thrust T_{total} ;
- shroud thrust T_S .

A test case for the function `ducted_prop_thrust.m` is shown, with relative outputs.

```

1 % =====
2 % | Input      : |
3 % |           (rho) = 1.225 [kg/m^3] |
4 % |           (ch) = 2.40 [m] |
5 % |           (Vinf) = 35 [m/s] |
6 % |           (D14) = 1.50 [m] |
7 % |           (D34) = 1.50 [m] |
8 % |           (theta) = 0 [deg] |
9 % |           (R) = 0.75 [m] |
10 % |           (TR) = 500 [N] |
11 % | Output     : (T) = 566.3129 [N] |
12 % |           (TS) = 66.3129 [N] |
13 % | Note       : |
14 % =====
15
16 rho = 1.225;
17 ch = 2.40;
18 Vinf = 35;
19 D14 = 1.5;
20 D34 = 1.5;
21 theta = 0;
22 R = 0.75;
23 TR = 500;
24
25 [T, TS] = ducted_prop_thrust(rho, Gamma, Vinf, Dquarter, R, TR)

```

Listing 9: Test case for the `ducted_prop_thrust.m`

1.3 Use of the function

This function must be used in conjunction with another program that provides ring vortex circulation and, thus, the isolated rotor's thrust.

2 Code listing

```

1 %% \ducted_prop_thrust.m
2 % \brief: A function that calculates total thrust of a ducted propeller.
3 % It generates a vector with total thrust and shroud thrust as output.
4 % \author: Claudio Mirabella, Christian Salzano
5 % \version: 1.04
6 %
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23 %
24 % =====
25 % |Name      : ducted_prop_thrust.m |
26 % |Author    : Claudio Mirabella, Christian Salzano |
27 % |          : University of Naples Federico II. |
28 % |Version   : 1.04 |
29 % |Date      : 25/11/2020 |
30 % |Modified  : 18/02/2021 |
31 % |Description : A function that calculates total thrust of a |
32 % |            : ducted propeller. |
33 % |            : It generates a vector with total thrust and |
34 % |            : shroud thrust as output. |
35 % |Reference  : Lezioni di Aerodinamica dell'Ala Rotante |
36 % |Input      : |
37 % |            : (rho) = Density |
38 % |            : (ch) = Chord of the shroud |
39 % |            : (Vinf) = Stream velocity |
40 % |            : (D14) = Shroud diameter at c/4 |
41 % |            : (D34) = Shroud diameter at 3c/4 |
42 % |            : (theta) = Angle of tangent between velocity and mean |
43 % |            : camber line at 3c/4 |
44 % |            : (R) = Rotor radius |
45 % |            : (TR) = Isolated rotor thrust |
46 % |Output     : (T) = Total thrust generated |
47 % |            : (TS) = Thrust generated by the shroud |
48 % |Note       : |
49 % |=====
50

```

```

51 function [T, TS] = ducted_prop_thrust(rho, ch, Vinf, D14, D34, theta, R, TR)
52 % Use function Feature_RVortexInt to evaluate universal function f
53 f = Feature_RvortexInt(ch,D14,D34);
54 % -----
55 % Propeller's induced velocity calculations
56 % eq 4.24
57 w0 = .5*(-Vinf + sqrt(Vinf^2 + 2*TR/(rho*pi*R^2)));
58 % -----
59 % Elicoidal vortex induced axial velocity at 3c/4
60 % eq 3.15
61 w34 = w0*[1 + (0.75*ch/R)/sqrt(1+(0.75*ch/R)^2)];
62 % -----
63 % Rotor's induced radial velocity at 3c/4
64 % eq 4.23
65 vi34 = -0.5*(D34/2)*w0*(R^2/((R^2 + (0.25*ch)^2)^1.5));
66 % -----
67 % Annular vortex induced velocity calculated using tangency condition at
68 % 3c/4
69 % eq 4.25
70 vi = -vi34 - theta*(w34 + Vinf);
71 % -----
72 % Circulation around the shroud
73 % eq. 4.26
74 Gamma = (pi*D14/f)*[-vi34 - theta*(Vinf + w34)];
75 % -----
76 % Rotor's induced radial velocity at c/4
77 % eq 4.23
78 vi14 = -0.5*(D14/2)*w0*(R^2/((R^2 + (-0.25*ch)^2)^1.5));
79 % -----
80 % Thrust component due to the shroud
81 TS = -rho*vi14*Gamma*pi*D14;
82 % -----
83 % Total thrust
84 T = TR + TS;
85 % -----
86 end

```

Listing 10: Function ducted_prop_thrust.m

Listings

1	Calling the <code>Feature_RvortexInt.m</code> function	1
2	Propeller's induced velocity. <code>ducted_prop_thrust.m</code>	1
3	w at $(3/4)c$. <code>ducted_prop_thrust.m</code>	1
4	Induced radial velocity v_{iR} at $(3/4)c$. <code>ducted_prop_thrust.m</code>	1
5	Anular vortex induced velocity at $(3/4)c$. <code>ducted_prop_thrust.m</code>	1
6	Circulation around the shroud Γ . <code>ducted_prop_thrust.m</code>	1
7	Induced radial velocity v_{iR} at $c/4$. <code>ducted_prop_thrust.m</code>	1
8	Thrust's calculations. <code>ducted_prop_thrust.m</code>	1
9	Test case for the <code>ducted_prop_thrust.m</code>	2
10	Function <code>ducted_prop_thrust.m</code>	3

References

- [1] Tognaccini Renato. *Lezioni di Aerodinamica dell'ala rotante*. Università degli Studi Ferico II, 2020.