DOCUMENTATION OF AXIAL_DESCENT_ASCENT_OPERATING_ CURVES_ROTOR FUNCTION

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Contents

1	Documentation			
	1.1	Algorithm Introduction	2	
	1.2	Algorithm Description	3	
	1.3	Input and Output	4	
	1.4	Test Case	5	
Appendices			8	
A Function's code			9	

Chapter 1

Documentation

1.1 Algorithm Introduction

The function plots $w(V_{\infty})$ and $P(V_{\infty})$ curves according to rotor's simply impulsive theory.

To achieve this objective in the first step we defined the following vectors:

- ALTITUDE
- ASCENT VELOCITY
- DESCENT VELOCITY

Density is then calculated from the altitude vector with the MATLAB function atmosisa.

After calculated the density, the axial hovering induction is obtained from the following relation derived by rotor's simply impulsive theory:

$$w_h = \sqrt{\frac{Mg}{2\rho(h)\pi r^2}} \tag{1.1}$$

From this value, we calculated the non-dimensional variables:

•
$$\widetilde{V} = \frac{V_{\infty}}{w_h}$$

•
$$\widetilde{w}_{ascent} = -\frac{\widetilde{V}}{2} + \sqrt{\frac{\widetilde{V}^2}{4} + 1}$$

•
$$\widetilde{w}_{descent} = -\frac{\widetilde{V}}{2} + \sqrt{\frac{\widetilde{V}^2}{4} - 1}$$

•
$$\widetilde{P}_{ascent} = \widetilde{V} + \widetilde{w}_{ascent}$$

•
$$\widetilde{P}_{descent} = \widetilde{V} + \widetilde{w}_{descent}$$

Then, we used some cycles to obtain the matrices including the values of induction and power that are two variables functions.

Subsequently these functions are plotted. In the code the user has also the possibility to insert the interest altitude.

1.2 Algorithm Description

The code begins at line 40 with the function call, where are defined the inputs as well as described in section 1.3.

Dimensional variables, as the altitude and the velocity, are defined in the lines [42-45].

The density as a function of altitude is calculated in line 49 through the MAT-LAB function *atmosisa*. In line 51 this variable is interpolated in a function handle to obtain a numerical law to use whit any altitude that the user choice in line 152.

From the line 55 to line 59 the code calculates the non-dimensional variables as mentioned in section 1.1.

At lines [61-62] the matrices which will contain the numerical value of induction as a function of velocity and altitude are initialized. Subsequently (lines [66-81]) those matrices are filled with *for loops* as show below, where you can see that is respected the limit of simply impulsive rotor theory:

Subsequently (lines [88-108]) the same thing is done for the non-dimensional power

The first type of outputs are the 3D plots of the induction and power as a function of altitude and velocity, which are in line [113-144]. After that, in lines [148-152] the user has the possibility to choose the altitude of interest to obtain the 2d plots of induction and power as function of only velocity at the entered altitude. In the following lines [154-185] the matrices containg the numerical value of induction and power are initialized and till as function of velocity at the entered altitude as show below:

```
prompt = {'Insert interest altitude in metres [min=0, Max=6000]: '};
dlgtitle = 'Altitude';
dims = [1 \ 35];
answer = inputdlg(prompt,dlgtitle,dims);
hnew = str2double(answer{1});
WTSnew = zeros(1,length(VVs));
WTDnew = zeros(1,length(VVd));
% Matrices fill
for j = 1 : length(VVs)
    WTSnew(1,j) = w_tilde_salita(VVs(j),hnew);
for j = 1 : length(VVd)
    if V_tilde(VVd(j),hh(i)) < -2</pre>
        WTDnew(1,j) = w_tilde_discesa(VVd(j),hnew);
        aanew = j;
        break
    end
end
PTSnew = zeros(1,length(VVs));
PTDnew = zeros(1,length(VVd));
for j = 1 : length(VVs)
    PTSnew(1,j) = P_tilde_salita(VVs(j),hnew);
for j = 1 : length(VVd)
    if V_tilde(VVd(j),hh(i)) < -2</pre>
        PTDnew(1,j) = P_tilde_discesa(VVd(j),hnew);
        bbnew = j;
    else
        break
    end
```

The values of induction and power as function of velocity at the entered altitude are plotted through the command in line[188-207].

1.3 Input and Output

The function takes in input:

- ROTORCRAFT'S MASS
- Rotor's radius

The outputs are the plots of induction and power and these are reported in section *Test Case*

1.4 Test Case

The numerical values in input for those plots are:

- Rotorcraft's mass = 5000 kg
- Rotor's radius = 7m

The outputs of the test case are the following plots:

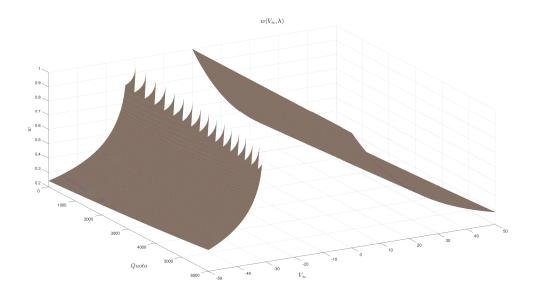


Figure 1.1: Induction

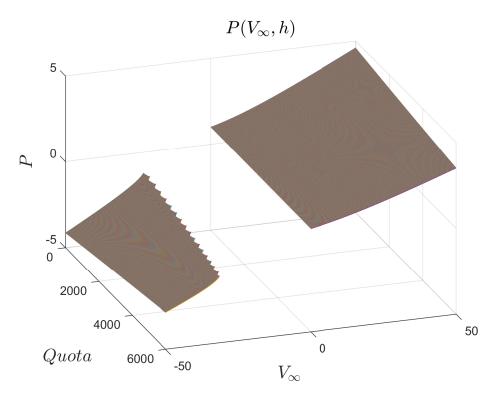


Figure 1.2: Power

In the code the user has also the possibility to insert the interest altitude: for example, choosing an altitude of 2000 metres we are obtained the following curves:

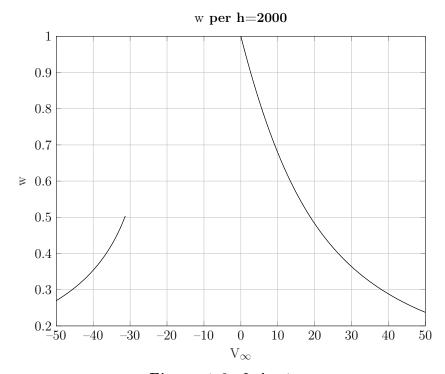


Figure 1.3: Induction

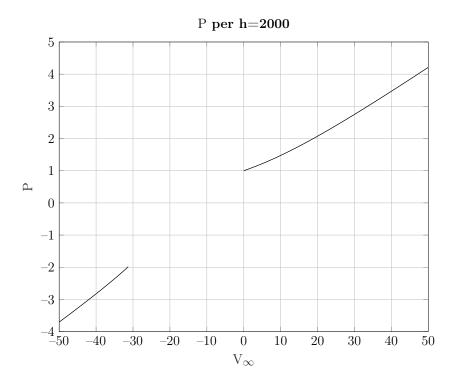


Figure 1.4: Power

Appendices

Appendix A

Function's code

```
\%\% \Axial_Descent_Ascent_Operating_Curves_Rotor.m \% \brief: the function plots w(V_infty) and P(V_infty) curves according to \% Impulsive theory. \% aerodynamic model
           \author: Colled\tilde{A} Moreno , Veneruso Salvatore \version: 1.00
       % Eli-TAARG is free software; you can redistribute it and/or % modify it under the terms of the GNU General Public % License as published by the Free Software Foundation; either % version 3 of the License, or (at your option) any later version.
       % Eli-TAARG is developed by the TAARG Educational organization for % educational purposes only. % Theoretical and Applied Aerodynamic Research Group - University of Naples Federico II. %
       % Eli-TAARG GitHub link: <https://github.com/TAARG-Education/Eli-TAARG>
       %
K Eli-TAARG is distributed in the hope that it will be useful,
% but WITHOUT ANY WARRANTY; without even the implied warranty of
% MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU
% General Public License for more details.
% <a href="http://www.gnu.org/licenses/">http://www.gnu.org/licenses/</a>>.
%
      25
30
35
       % Input
% Output
% Note
       function [Power,Induction] = Axial_Descent_Ascent_Operating_Curves_Rotor(M,R)
42
       hh = linspace(0,6000,1000);

VVs = linspace(0, 50, 100);

VVd = linspace(-50, 0, 100);

g = 9.81;
       [~, ~, ~, rho1] = atmosisa(hh);
       rho = @(h) interp1(hh,rho1,h, 'pchip');
wh = @(h) sqrt((M*g)/(2*rho(h)*pi*R^2));
53
54
55
       % Non-Dimensional Variables Definition
V_tilde = @(V,h) V/wh(h);
       % Matrices fill
       % hatrices iiii
for i = 1 : length(hh)
    for j = 1 : length(VVs)
        WTS(i,j) = w_tilde_salita(VVs(j),hh(i));
       end
end
```

```
WTD(i,j) = w_tilde_discesa(VVd(j),hh(i));
aa(1,i) = j;
 75
76
77
78
79
                  else
WTD(i,j) = 0;
                   end
       end
end
 80
 81
82
83
84
       %Non-Dimensional Power
       88
 89
90
 91
92
93
       94
95
96
97
98
99
100
       101
      .i.()
bb(1,i) =
else
break
end
end
102
103
104
105
107
108
110
111
       %%
% 3D Plots of Induction [output]
figure(1)
plot3(hh(1)*ones(1,length(WTS(1,:))),VVs,WTS(1,:))
hold on
for i = 2 : length(hh)
    plot3(hh(i)*ones(1,length(WTS(i,:))),VVs,WTS(i,:))
end
113
114
115
116
117
118
         end
for i = 1 : length(hh)
    plot3(hh(i)*ones(1,length(WTD(i,1:aa(i)))), VVd(1,1:aa(i)), WTD(i,1:aa(i)))
120
121
       end
xlabel('$Quota$','Interpreter','latex', 'FontSize',15)
ylabel('$V_{\infty}$','Interpreter','latex', 'FontSize',15)
zlabel('$w$','Interpreter','latex', 'FontSize',15)
123
124
       title('$w (V_{\infty}, h)$','Interpreter','latex', 'FontSize', 15)
view(71,32)
127
128
        % 3D Plots of Power [output]
       figure (2)
plot3(hh(1)*ones(1,length(PTS(1,:))),VVs,PTS(1,:))
hold on
for i = 2 : length(hh)
130
131
131 \\ 132 \\ 133
       for 1 = 2 : length(hh)
    plot3(hh(i)*ones(1,length(PTS(i,:))),VVs,PTS(i,:))
end
for i = 1 : length(hh)
    plot3(hh(i)*ones(1,length(PTD(i,1:bb(i)))),VVd(1,1:bb(i)),PTD(i,1:bb(i)))
end
xlabel('$Quota$','Interpreter','latex', 'FontSize',15)
ylabel('$V {\intropyreter','latex', 'FontSize',15)
134
135
136
137
       ylabel('$\[ \infty\\ '\]. 'Interpreter', 'latex', 'FontSize',15)
zlabel('\$P\$', 'Interpreter', 'latex', 'FontSize',15)
140
141
       grid on
title('$P (V_{\infty}, h)$','Interpreter','latex', 'FontSize', 15)
view(71,32)
142
143
144
145
146
       %% Insertion of Interes Altitude;
147
       prompt = {'Insert interest altitude in metres [min=0,Max=6000]: '};
dlgtitle = 'Altitude';
dims = [1 35];
answer = inputdlg(prompt,dlgtitle,dims);
hnew = str2double(answer{1});
148
150
151
153
       154
155
156
        % Matrices fill
157
158
159
       for j = 1 : length(VVs)
    WTSnew(1,j) = w_tilde_salita(VVs(j),hnew);
        end
160
161
162
163
       for j = 1 : length(VVd)
  if V_tilde(VVd(j),hh(i)) < -2
     WTDnew(1,j) = w_tilde_discesa(VVd(j),hnew);</pre>
                                                                                 %Validity limit of simply impulsive theory;
164
165
166
                  aanew = j;
            else
break
167
       end
end
168
\frac{170}{171}
       PTSnew = zeros(1,length(VVs));
PTDnew = zeros(1,length(VVd));
172
173
       for j = 1 : length(VVs)
    PTSnew(1,j) = P_tilde_salita(VVs(j),hnew);
174
175
176
        end
```

```
178 \\ 179 \\ 180
181
182
       bbnew = J;
else
break
end
%%
% 2D Plots of induction [Output]
183
184
185
186
187
       % 2D Plots of induction [Output]
figure(3)
plot(VVs, WTSnew, '-k')
hold on
plot(VVd(1:aanew), WTDnew(1:aanew), '-k')
grid on
xlabel('$V_{\infty}$','Interpreter','latex','FontSize',15)
ylabel('$W$','Interpreter','latex','FontSize',15)
title(['$w$ per h=' num2str(hnew)],'Interpreter','latex')
matlab2tikz('D:\Università \Magistrale\AerodinamicaAlaRotante\Matlab\EliiTAARG\Figure\Induzione2d.tex');
188
189
190
191
192
193
194
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197
198
       % 2D Plots of power [Output]
       199
200
201
202
203
204
205
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207
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211
212
213
```

Bibliography

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