Optimizing random walks

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1. Malaria

- A mosquito flies in a straight line for some unit time,
- then it turns in a rndom direction.
- How far does it get in *N* time intervals?
- Answer: about \sqrt{N} .



```
Code:
float avg_dist{0.f};
for ( int x=0; x<experiments; x++ ) {
   Mosquito m(dim);
   for (int step=0; step<steps; step++)
        m.step();
   avg_dist += m.distance();
}
avg_dist /= experiments;</pre>
```

```
Output
[rand] vec:
D=3 after 10000
    steps, distance=
    83.7997
D=3 after 100000
    steps, distance=
    224.372
D=3 after 1000000
    steps, distance=
    922.599
product took: 2776
    milliseconds
```



```
class Mosquito {
private:
    vector<float> pos;
public:
    Mosquito( int d )
    : pos( vector<float>(d,0.f) ) { };
```



```
void step() {
  int d = pos.size();
  auto incr = random_step(d);
  for (int id=0; id<d; id++)
     pos.at(id) += incr.at(id);
};</pre>
```



```
vector<float> random_coordinate( int d ) {
  auto v = vector<float>(d);
  for ( auto& e : v )
    e = random_float();
  return v;
};
```



```
vector<float> random_step(int d) {
  for (;;) {
    auto step = random_coordinate(d);
    if ( auto l=length(step); l<=1.f ) {</pre>
      if ( l==0.f ) {
        /*
         * Zero lengths can conceivably happen for d==1
         * but should not for higher d.
         */
        assert(d==1);
      } else {
        normalize(step,1);
        return step;
};
```



7. exercise

Take the basic code, and make a version based on

```
template<int d>
class Mosquito { /* ... */
```

How much does this simplify your code? Do you get any performance improvement?

You can base this off the file walk_vec.cxx in the repository



So we move the creation of the vectors outside of the computational routines. The random coordinates are now written into an array passed as parameter:

```
void random_coordinate( vector<float>& v ) {
  for ( auto& e : v )
    e = random_float();
};
```



Likewise the random step:

```
void random_step( vector<float>& step ) {
  for (;;) {
    random_coordinate(step);
```



This process of passing the arrays in stops at the step method, which we want to keep parameterless. So we add an option cache to the constructor to store the step vector as well as the position:

```
Code:
class Mosquito {
private:
  vector<float> pos;
  vector<float> inc:
  bool cache;
public:
  Mosquito( int d,bool cache=false )
    : pos( vector<float>(d,0.f)
    ), cache(cache) {
    if (cache) inc =
     vector<float>(d,0.f);
  };
```

```
Output
[rand] pass:
D=3 after 10000
    steps, distance=
    76.7711
D=3 after 100000
    steps, distance=
    257.19
D=3 after 1000000
    steps, distance=
    956.122
run took: 2852
    milliseconds
D=3 after 10000
```

steps, distance= 2022



```
void step() {
  int d = pos.size();
  if (cache) {
    random_step(inc);
    step( inc );
  } else {
    vector<float> incr(d);
    random_step(incr);
    step( incr );
  }
};
```



12. Sum of squares

There is still a problem with the <code>length</code> calculation. Since there is no reduction operator for 'sum of squares', we need to create a temporary vector for the squares, (or do we?) so that we can do a plus-reduction on it.



13. Exercise

Explore options for this temporary. Discuss what's most elegant, and measure performance improvement.

- This temporary can be passed in as a parameter;
- it can be stored in a global variable;
- or we can declare it static.
- With the C++20 standard, you could also use the ranges header.







16. Optimization

While above we have removed all unnecessary allocation, we get an extra performance boost from optimizations from the compiler knowing the length of the array. Thus, instead of a loop of length two, the compiler will probably replace this by two explicit instructions



```
Code:
float avg_dist{0.f};
for ( int x=0; x<experiments; x++ ) {
   Mosquito<dim> m;
   for (int step=0; step<steps; step++)
        m.step();
   avg_dist += m.distance();
}
avg_dist /= experiments;</pre>
```

```
Output
[rand] arr:
D=3 after 10000
    steps, distance=
    76.3221
D=3 after 100000
    steps, distance=
    247.5
D=3 after 1000000
    steps, distance=
    959.735
product took: 358
    milliseconds
```

