

# Union-like constructs

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# 1. Dealing with multiple types

- Union: one name can stand for multiple types ('Here are some bits; now pretend they are an integer; now pretend they are a float')  
This existed in C, C++ has better ways
- Tuples: pack together a char & int & string under one variable

# Tuples

## 2. C++11 style tuples

Use `get` to unpack a `std::tuple` or `std::pair`:

```
1 #include <tuple>
2
3 std::tuple<int,double,char> id = \
4     std::make_tuple<int,double,char>( 3, 5.12, 'f' );
5     // or:
6     std::make_tuple( 3, 5.12, 'f' );
7 double result = std::get<1>(id);
8 std::get<0>(id) += 1;
9
10 // also:
11 std::pair<int,char> ic = std::make_pair( 24, 'd' );
```

Annoyance: all that 'get'ing.

Note: `std::pair` has methods `first/second`

### 3. Returning two things

simple solution:

```
1 // union/optroot.cpp
2 bool RootOrError(float &x) {
3     if (x<0)
4         return false;
5     else
6         x = std::sqrt(x);
7     return true;
8 };
```

other solution: tuples

# 4. Tuples

Pack up multiple types in one variable:

```
1 // union/tuple.cpp
2 // pack:
3 tuple<int,string> intstring { 13,"fourteen" };
4 // unpack:
5 auto [i,s] = intstring;
6 println( "Int: {}, String: {}",i,s );
```

'structured binding'

## 5. Tuple solution

```
1 // union/optroot.cpp
2 #include <tuple>
3 using std::tuple, std::pair;
4     /* ... */
5 pair<bool,float> RootAndValid(float x) {
6     if (x<0)
7         return {false,x};
8     else
9         return {true,std::sqrt(x)};
10 };
11     /* ... */
12 for ( auto x : {2.f,-2.f} )
13     if ( auto [ok,root] = RootAndValid(x) ; ok )
14         cout << "Root is "
15             << root << '\n';
16     else
17         cout
18             << "could not take root of "
19                 << x << '\n';
```

# 6. Returning tuple with type deduction

Return type deduction:

```
1 // stl/tuple.cpp
2 auto maybe_root1(float x) {
3     if (x<0)
4         return make_tuple
5             <bool,float>(false,-1);
6     else
7         return make_tuple
8             <bool,float>
9                 (true,sqrt(x));
10 }
```

Alternative:

```
1 // stl/tuple.cpp
2 tuple<bool,float>maybe_root2
3             (float x) {
4     if (x<0)
5         return {false,-1};
6     else
7         return {true,sqrt(x)};
8 };
```

Note: use `pair` for `tuple` of two.

## 7. Catching a returned tuple

The calling code is particularly elegant:

Code:

```
1 // stl/tuple.cpp
2 auto [succeed,y] = maybe_root2(x);
3 if (succeed)
4     cout << "Root of " << x
5         << " is " << y << '\n';
6 else
7     cout << "Sorry, " << x
8         << " is negative" << '\n';
```

Output:

```
1 Root of 2 is 1.41421
2 Sorry, -2 is negative
```

This is known as structured binding.

# Variants

## 8. Variant methods

```
1 // union/intdoublestring.cpp
2 variant<int,double,string> union_ids;
```

Get the index of what the variant contains:

```
1 // union/intdoublestring.cpp
2 union_ids = 3.5;
3 switch ( union_ids.index() ) {
4 case 1 :
5   cout << "Double case: " << std::get<double>(union_ids) << '\n';
6 }
```

```
1 // union/intdoublestring.cpp
2 union_ids = "Hello world";
3 if ( auto union_int = get_if<int>(&union_ids) ; union_int )
4   cout << "Int: " << *union_int << '\n';
5 else if ( auto union_string = get_if<string>(&union_ids) ; union_string
       )
6   cout << "String: " << *union_string << '\n';
```

(Takes pointer to variant, returns pointer to value)

# Exercise 1

Write a routine that computes the roots of the quadratic equation

$$ax^2 + bx + c = 0.$$

The routine should return two roots, or one root, or an indication that the equation has no solutions.

Code:

```
1 // union/quadratic.cpp
2 for ( auto coefficients :
3     { quadratic{.a=2.0, .b=1.5, .c
4       =2.5},
5     quadratic{.a=1.0, .b=4.0, .c
6       =4.0},
7     quadratic{.a=2.2, .b=5.1, .c
8       =2.5}
9   } ) {
10   auto result = compute_roots(
11     coefficients);
```

Output:

```
1 With a=2 b=1.5 c=2.5
2 No root
3 With a=2.2 b=5.1
   ↪c=2.5
4 Root1: -0.703978
   ↪root2: -1.6142
5 With a=1 b=4 c=4
6 Single root: -2
```

## 9. Problem setup

Represent the polynomial

$$ax^2 + bx + c$$

as

```
1 using quadratic = tuple<double, double, double>;
```

Unpack:

```
1 auto [a, b, c] = coefficients;
```

assert something here?

# Exercise 2

Write a function

```
1 double discriminant( quadratic coefficients );
```

that computes  $b^2 - 4ac$ , and test:

```
1 // union/quadtest.cpp
2 TEST_CASE( "discriminant" ) {
3     quadratic one{0., 2.5, 0.};
4     REQUIRE( discriminant( one ) ==Catch::Approx(6.25) );
5     quadratic two{1., 0., 1.5};
6     REQUIRE( discriminant( two ) ==Catch::Approx(-6.) );
7     quadratic three{.1, .1, .1*.5};
8     REQUIRE( discriminant( three ) ==Catch::Approx(-.01) );
9 }
```

# Exercise 3

Write a function

```
1 bool discriminant_zero( quadratic coefficients );
```

that passes the test

```
1 // union/quadtest.cpp
2 quadratic coefficients{a,b,c};
3 d = discriminant( coefficients );
4 z = discriminant_zero( coefficients );
5 INFO( a << "," << b << "," << c << " d=" << d );
6 REQUIRE( z );
```

Using for instance the values:

```
1 a = 2; b = 4; c = 2;
2 a = 2; b = sqrt(40); c = 5; // !!!
3 a = 3; b = 0; c = 0.;
```

# Exercise 4

Write the function `simple_root` that returns the single root. For confirmation, test

```
1 // union/quadtest.cpp
2 auto r = simple_root(coefficients);
3 REQUIRE( evaluate(coefficients,r)==Catch::Approx(0.).margin(1.e-14) );
```

# Exercise 5

Write a function that returns the two roots as a  
indexcstdpair:

```
1 pair<double,double> double_root( quadratic coefficients );
```

Test:

```
1 // union/quadtest.cpp
2 quadratic coefficients{a,b,c};
3 auto [r1,r2] = double_root(coefficients);
4 auto
5   e1 = evaluate(coefficients,r1),
6   e2 = evaluate(coefficients,r2);
7 REQUIRE( evaluate(coefficients,r1)==Catch::Approx(0.).margin(1.e-14) );
8 REQUIRE( evaluate(coefficients,r2)==Catch::Approx(0.).margin(1.e-14) );
```

# Exercise 6

Write a function

```
1 variant< bool,double, pair<double,double> >
2     compute_roots( quadratic coefficients);
```

Test:

```
1 // union/quadtest.cpp
2 TEST_CASE( "full test" ) {
3     double a,b,c; int index;
4     SECTION( "no root" ) {
5         a=2.0; b=1.5; c=2.5;
6         index = 0;
7     }
8     SECTION( "single root" ) {
9         a=1.0; b=4.0; c=4.0;
10        index = 1;
11    }
12     SECTION( "double root" ) {
13         a=2.2; b=5.1; c=2.5;
14         index = 2;
15     }
16     quadratic coefficients{.a=a,.b=b
17         ,.c=c};
18     auto result = compute_roots(
19         coefficients);
20     REQUIRE( result.index()==index );
21 }
```

# 10. Monostate

In the previous slide the `bool` was an overspecification:  
it is enough to know that the result is a bool and the value is  
irrelevant.

For such cases, use

```
1 std::monostate{}
```

**Optional, expected**

# 11. Optional results

The most elegant solution to ‘a number or an error’ is to have a single quantity that you can query whether it’s valid.

```
1 #include <optional>
2 using std::optional;

1 // union/optroot.cpp
2 optional<float> MaybeRoot(float x) {
3     if (x<0)
4         return {};
5     else
6         return std::sqrt(x);
7 }
```

# Exercise 7

Write a function *first\_factor* that optionally returns the smallest factor of a given input.

```
1 // primes/optfactor.cpp
2 auto factor = first_factor(number);
3 if (factor.has_value())
4     cout << "Found factor: " << factor.value() << '\n';
5 else
6     cout << "Prime number\n";
```

# 12. Expected

Expect double, return info string if not:

Function returning expected:      In Use:

```
1 // union/expected.cpp
2 std::expected<double, string>
3 square_root( double x ) {
4     if (x<0)
5         return std::unexpected("negative");
6     else if (x<limits<double>::min())
7         return std::unexpected("underflow");
8     else {
9         auto result = sqrt(x);
10        return result;
11    }
12 }
```

```
1 // union/expected.cpp
2 auto root = square_root(x);
3 if (x)
4     cout << "Root=" << root.value()
              << '\n';
5 else if (root.error() == /* et cetera
6             */ )
7     /* handle the problem */
```

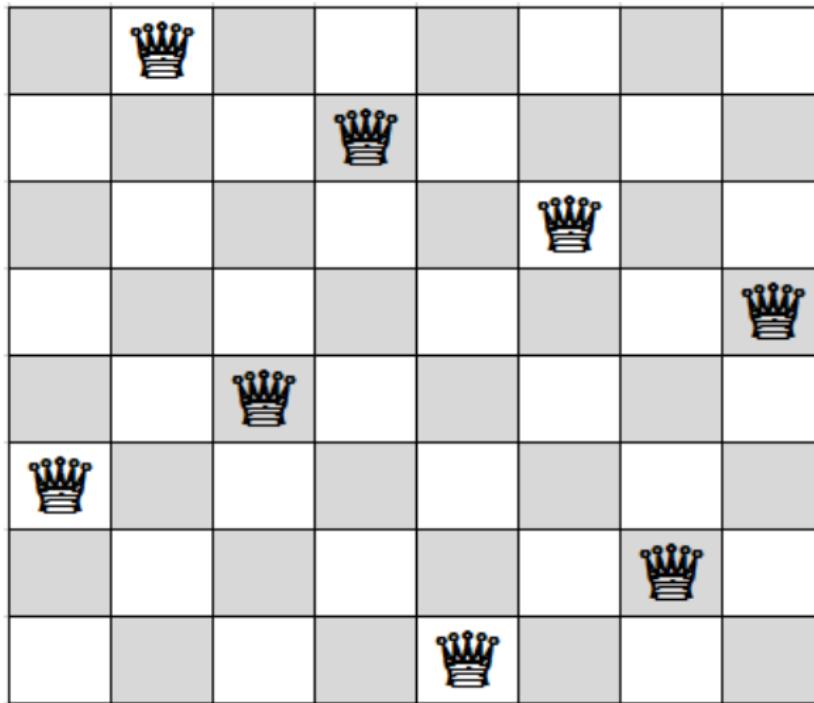
## 13. Any

If you want a variant that can be anything,  
use `std::any`.

# **Eight queens problem**

# 14. Classic problem

Can you put 8 queens on a board so that they can't hit each other?



## 15. Statement

- Put eight pieces on an  $8 \times 8$  board, no two pieces on the same square; so that
- no two pieces are on the same row,
- no two pieces are on the same column, and
- no two pieces are on the same diagonal.

## 16. Not good solution

A systematic solution would run:

1. put a piece anywhere in the first row;
2. for each choice in the first row, try all positions in the second row;
3. for all choices in the first two rows, try all positions in the third row;
4. when you have a piece in all eight rows, evaluate the board to see if it satisfies the condition.

Better: abort search early.

# Exercise 8: Board class

Class *board*:

```
1 // queens/queens.hpp
2 ChessBoard(int n);
```

Method to keep track how far we are:

```
1 // queens/queens.hpp
2 int next_row_to_be_filled()
```

Test:

```
1 // queens/queentest.cpp
2 TEST_CASE( "empty board", "[1]" ) {
3     constexpr int n=10;
4     ChessBoard empty(n);
5     REQUIRE( empty.next_row_to_be_filled()==0 );
6 }
```

# Exercise 9: Place one queen

Method to place the next queen,  
without testing for feasibility:

```
1 // queens/queens.hpp  
2 void place_next_queen_at_column(int i);
```

This test should catch incorrect indexing:

```
1 // queens/queentest.cpp  
2 INFO( "Illegal placement throws" )  
3 REQUIRE_THROWS( empty.place_next_queen_at_column(-1) );  
4 REQUIRE_THROWS( empty.place_next_queen_at_column(n) );  
5 INFO( "Correct placement succeeds" );  
6 REQUIRE_NO_THROW( empty.place_next_queen_at_column(0) );  
7 REQUIRE( empty.next_row_to_be_filled() == 1 );
```

Without this test, would you be able to cheat?

# Exercise 10: Test if we're still good

Feasibility test:

```
1 // queens/queens.hpp  
2 bool feasible()
```

Some simple cases:  
(add to previous test)

```
1 // queens/queentest.cpp  
2 ChessBoard empty(n);  
3 REQUIRE( empty.feasible() );  
  
1 // queens/queentest.cpp  
2 ChessBoard one = empty;  
3 one.place_next_queen_at_column(0);  
4 REQUIRE( one.next_row_to_be_filled()==1 );  
5 REQUIRE( one.feasible() );
```

# Exercise 11: Test collisions

```
1 // queens/queentest.cpp
2 ChessBoard collide = one;
3 // place a queen in a 'colliding' location
4 collide.place_next_queen_at_column(0);
5 // and test that this is not feasible
6 REQUIRE( not collide.feasible() );
```

# Exercise 12: Test a full board

Construct full solution

```
1 // queens/queens.hpp
2 ChessBoard( int n, vector<int> cols );
3 ChessBoard( vector<int> cols );
```

Test:

```
1 // queens/queentest.cpp
2 ChessBoard five( {0,3,1,4,2} );
3 REQUIRE( five.feasible() );
```

# Exercise 13: Exhaustive testing

This should now work:

```
1 // queens/queentest.cpp
2 // loop over all possibilities first queen
3 auto firstcol = GENERATE_COPY( range(1,n) );
4 ChessBoard place_one = empty;
5 REQUIRE_NOTHROW( place_one.place_next_queen_at_column(firstcol) );
6 REQUIRE( place_one.feasible() );
7
8 // loop over all possibilities second queen
9 auto secondcol = GENERATE_COPY( range(1,n) );
10 ChessBoard place_two = place_one;
11 REQUIRE_NOTHROW( place_two.place_next_queen_at_column(secondcol) );
12 if (secondcol<firstcol-1 or secondcol>firstcol+1) {
13     REQUIRE( place_two.feasible() );
14 } else {
15     REQUIRE( not place_two.feasible() );
16 }
```

# Exercise 14: Place if possible

You need to write a recursive function:

```
1 // queens/queens.hpp
2 optional<ChessBoard> place_queens()
```

- place the next queen.
- if stuck, return ‘nope’.
- if feasible, recurse.

```
1 class board {
2     /* stuff */
3     optional<board> place_queens() const {
4         /* stuff */
5         board next(*this);
6         /* stuff */
7         return next;
8     };
}
```

# Exercise 15: Test last step

Test `place_queens` on a board that is almost complete:

```
1 // queens/queentest.cpp
2 ChessBoard almost( 4, {1,3,0} );
3 auto solution = almost.place_queens();
4 REQUIRE( solution.has_value() );
5 REQUIRE( solution->filled() );
```

Note the new constructor! (Can you write a unit test for it?)

# Exercise 16: Sanity tests

```
1 // queens/queentest.cpp
2 TEST_CASE( "no 2x2 solutions", "[8]" ) {
3     ChessBoard two(2);
4     auto solution = two.place_queens();
5     REQUIRE( not solution.has_value() );
6 }

1 // queens/queentest.cpp
2 TEST_CASE( "no 3x3 solutions", "[9]" ) {
3     ChessBoard three(3);
4     auto solution = three.place_queens();
5     REQUIRE( not solution.has_value() );
6 }
```

## Exercise 17: O

ptional: can you do timing the solution time as function of the size of the board?