





Scientific and Technical Computing

Hardware and Code Optimization

Lars Koesterke

UT Austin, 8/31/20 & 9/8/20 & ...



What are the **primary components** of a computer?



What are the **primary components** of a computer?

Can you already detect some limitations?



What are the **primary components** of a computer?

- CPU
- Memory
- (Storage)
- (Motherboard, lots of wires)
- (Keyboard, screen)

Can you already detect some limitations?

Number of pins connecting CPU and Memory to motherboard

What **sciences and technologies** are

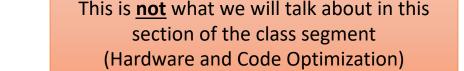
involved in designing and building a

CPU/Memory/Computer?



What sciences and technologies are involved in designing and and building a CPU?

- Electrical engineering, physics, chemistry, math ... (all the things you study)
- Cutting edge research
- A lot of institutional knowledge by people in companies and research institutions
 - Not everything is an exact science; many tricks are applied (a bit like cooking)
 - Design decisions are made on incomplete facts (humans weigh the pros and cons)
- Certainly, many computers equipped with previous generations of CPUs





What are we going to <u>explore</u> in the next 4 weeks?

High level overview of the architecture

- High level of abstraction
- Simplified implementation details
- Features that allow for a very high peak performance

How to write code that exploits the hardware features?



Matching software to hardware: Why?

Much higher performance

Orders of magnitude!

There is, of course, the idea to match the hardware to the software/purpose

This is done in other areas

In HPC the idea is not feasible (with one notable exception)

Conceptual understanding of hardware features guides software design

Assumption: You are in this class (and other TACC classes) to learn how to

- learn about high-performance computing (HPC)
- use a supercomputer (or any computer!) in an **efficient** and **effective** way
- write fast code
 - This class: exploiting parallelism of the hardware
 - Note: some/many bad code design decision cannot be reversed later
- write <u>parallel</u> code with OpenMP and MPI (PCSE in the spring semester)

Getting some scientific calculations done
Better than the competition

Terminology

Today's supercomputers are clusters

Components of a cluster

- Nodes
 - CPUs and memory
- Network
- (File system)

In this class we strongly focus on a single-node!

A cluster is build of individual computers which are called nodes

The nodes are connected through an interconnect

Nodes

Memory Cores

















What is a clock tick?

What is a clock cycle?



What is a clock tick?

What is a clock cycle?

What does this mean?

Clock frequency = 2.2 GHz

What is a clock tick?

What is a clock cycle?

Think of an assembly line

- Smallest unit of time to 'do' something
- One or multiple instructions are executed
- An instruction may take several cycles

Examples of instructions are

- Multiply two numbers
- Load data into a register

Some answers from the web

Computers use an internal clock to synchronize all of their calculations. The clock ensures that the various circuits inside a computer work together at the same time.

Same as a cycle, the smallest unit of time recognized by a device. For personal computers, clock ticks generally refer to the main system clock, which runs at 66 MHz. This means that there are 66 million clock ticks (or cycles) per second. Since modern CPUs run much faster (up to 3 GHz), the CPU can execute several instructions in a single clock tick.

"The processor clock coordinates all CPU and memory operations by periodically generating a time reference signal called a *clock cycle or tick*. Clock frequency is specified in gigahertz (GHz), which specifies billions of ticks per second. Clock speed determines how fast instructions execute. Some instructions require one tick, others multiple ticks, and some processors execute multiple instructions during one tick."



'Instruction' can mean many things. Let's leave it a bit vague for now

Intermission

Let's talk about how to proceed

I'd like to organize this class having this in mind:

What and how to learn?

What will be on the slides?

How to participate?

Give me feedback!

How participation will affect your grade?

Teamwork

Let me know (at a later point) what you are interested in



Experiment: Prepare something at home

Your tasks

- Look up what the 'Horner scheme' is
 - Wikipedia entry (English Wikipedia site) is very good
 - To be specific, Horner's notation: ((((z+...)×z+...)×z ...
- Describe the 'Horner notation'
 - Three to four sentences
 - General context (Note: you don't have to explain what a polynomial is)
 - What is the 'trick'?
 - Why would you use it when writing code?
- 'Present' in class next week
 - Nothing dramatic, I'll explain
 - Write the 3 sentences down, if that helps you



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$$a = b + c$$

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What needs to happen so that the CPU can calculate?

Where is the data coming from?

Where is the data going?

What part of the hardware performs the operation?

$$a = b + c$$

What needs to happen so that the CPU can calculate?

Where is the data coming from?

Memory

Where is the data going? Memory

What part performs the operation? Floating Point Unit (FPU) in the CPU (Central Processing Unit)

$$a = b + c$$

What needs to happen so that the CPU can calculate?

How long does it take?

Where is the data coming from?

Memory

Where is the data going?

Memory

What part performs the operation?

FPU in the CPU



$$a = b + c$$

What needs to happen so that the CPU can calculate?

How long does it take?

Where is the data coming from?

Memory

A very long time

Where is the data going?

Memory

A very long time

What part performs the operation?

FPU in the CPU

A very short time



$$a = b + c$$

What needs to happen so that the CPU can calculate?

How long does it take?

Where is the data coming from?

Memory

300 cycles

Where is the data going?

Memory

300 cycles

What part performs the operation?

FPU in the CPU

3 cycles

What a bummer! Actual work takes 0.5% of the total time We may have built the 'most ineffective computer' ever!



Does this help us?

$$a(i) = b(i) + c(i)$$

Does this help us?

$$a(i) = b(i) + c(i)$$

Hint: where would you likely find such a statement?

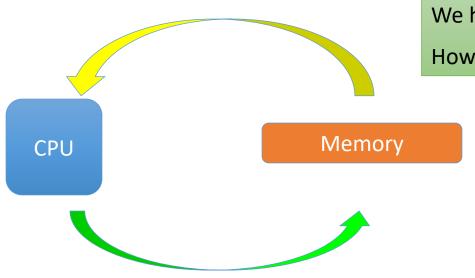
Does this help us?

$$a(i) = b(i) + c(i)$$

```
loop with index i
  a(i) = b(i) + c(i)
end loop
```

Data

$$a(i) = b(i) + c(i)$$



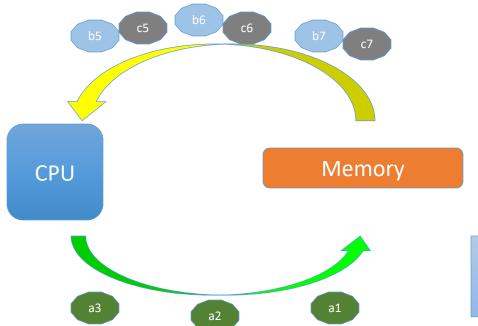
We have a lot of data to process

How can that help to **'getting more done'**?

'getting more done'

We are mostly interested in floating point operations (flops) that move the calculation closer to the solution

a(i) = b(i) + c(i)



Some data is 'en route'

b and c: from memory to CPU

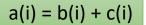
a: from CPU to memory

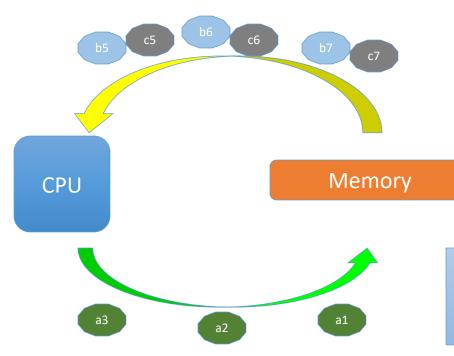
Some data is being processed

$$a(i) = b(i) + c(i)$$

How much data has to be 'en route'?

What are the main factors?





Some data is 'en route'

b and c: from memory to CPU

a: from CPU to memory

Some data is being processed

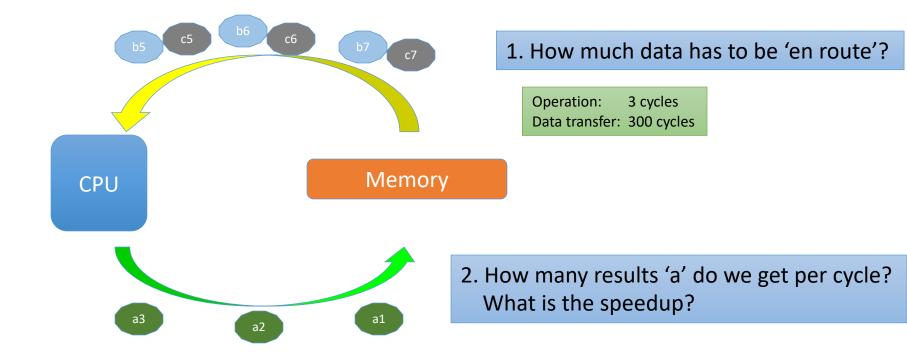
$$a(i) = b(i) + c(i)$$

How much data has to be 'en route'?

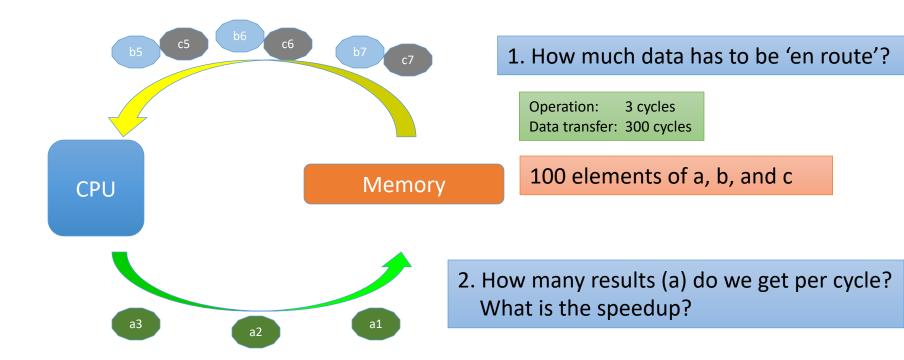
What is one of the main factors?

What if I had drawn CPU and Memory further apart?

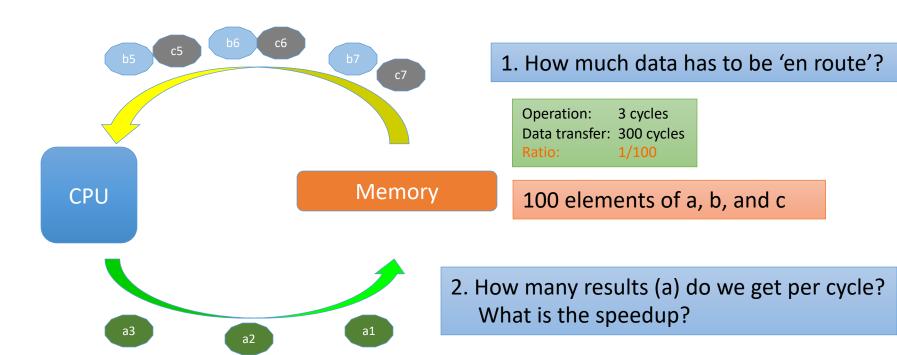
a(i) = b(i) + c(i)



a(i) = b(i) + c(i)



$$a(i) = b(i) + c(i)$$



1 result every 3 cycles Speedup is 100×

Hooray!

We have just discovered one of the most important hardware features in a CPU: Data streams

- Data Streams
 - Long distance (in terms of cycles) between main memory and CPU
 - Short time to execute 'add' operation (few cycles)
 - Streaming data: Data 'en route' filling the stream between memory and CPU
- Questions for later
 - How do we or the CPU 'organize' the data stream?
 - How does this look in code?

There are 2 fundamental bottlenecks

- 1. The data supply to the CPU
- 2. The actual operations (flops)



Hooray!

We have just discovered one of the most important hardware features in a CPU: Data streams

- Data Streams
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There are 2 fundamental bottlenecks

- 1. The data supply to the CPU
- 2. The actual operations (flops)

There are 3 major technologies that are applied (we can argue about the exact number)

- 1. Data streams
- 2. 'Improving CPU throughput'
- 3. 'Improving data movement'



Can we speed-up the actual numerical operation 'add'?

If so, **how**?

Assume

- 1. 'add' takes 3 cycles
- 2. The data streams supply data effortlessly, i.e. without delay and at infinite bandwidth



How can we speed-up the actual operation 'add'?

Assume

- 1. 'add' takes 3 cycles
- 2. The data streams supply data effortlessly

Think of Henry Ford's moving assembly line

The assembly line predates H. Ford (see R. Olds in the automotive industry; but earlier assembly lines in other industries)



Discussion: Pipelining

Simple toy model of the implementation of 'add'

'add' takes 3 cycles: For sake of argument, 'read', 'add', write'

After 2 cycles (ramp up phase) a result is produced every cycle

writ

one result

a2 a3

> b3 b4

> **c3** c4

cycle 4

One result per cycle, once the pipeline is filled 3× performance increase

Operation: 1 cycle Data transfer: 300 cycles 1/300

Ratio is now worse (no good deed goes unpunished)

write

read

b3

с3

add

one result

a2

b2

c2

cycle 3

a1

add

read

write

add

no result



no result

a1

b1

c1

c2

b2

c1

b1

time

cycle 2

cycle 1

Discussion: Pipelining

Simple toy model of the implementation of 'add'

'add' takes 3 cycles: 'read', 'add', write'

After 2 cycles a result is produced every cycle one result a2 a3 b3 b4 **c3** c4

read add one result a2 a1 b2 b3 **c3** c2

One result per cycle, once the pipeline is filled 3× performance increase

Operation: 1 cycle Data transfer: 300 cycles 1/300

Ratio is now worse (no good deed goes unpunished)

add

write write read add no result no result a1 b2 a1

a1

c1 time

b1

read

Moving assembly line: The workers are stationary, the cars (data)

cycle 2

c2

cycle 1

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We have just discovered <u>another</u> important hardware features in a CPU: Pipelining

- Pipelining
 - Single operation (add) takes more than a cycle
 - Pipelining (moving assembly line) allows to calculate one result per cycle once the pipeline is filled
- Questions for later
 - How do we or the CPU 'organize' pipelining?
 - How does this look in code?

There are 2 fundamental bottlenecks

- 1. The data supply to the CPU
- 2. The actual operations

There are 3 major technologies in a CPU

(we can argue about the exact number)

- 1. Data streams (R=1/100)
- 2. Pipelining (R=1/300 data supply even more important)
- 'Improving data movement'



Recap 'Data Streams'

<u>Bandwidth</u> is the amount of data transferred per unit of time Most convenient units for now based on words and cycles

Bandwidth & Latency

So far we have talked about data streams and how to improve bandwidth

Recap 'Data streams'

- 300 cycles to move data between main memory to the CPU
- This is the latency (300 cycles to get the first data)

Assume **no streams** for the example: a = b + c

I'm making this unit up wpc: word per cycle

- Average bandwidth = 1 'word' per 200 cycles (0.005 wpc)
 - 'a', 'b', and 'c' are 4-byte or 8-byte words
- Let's pause here: Why exactly is the average bandwidth 1 word per 200 cycles?
- Let's discuss ...



<u>Data latency</u> is the time it takes for the first data to arrive Most convenient unit is <u>cycles</u>

wpc: our unit

round-trip: 600 cycles

Recap 'Data Streams'

So far we have talked about data streams and how to improve bandwidth

Recap 'Data streams'

• 300 cycles to move data between main memory to the CPU

Assume no streams for the example: a = b + c

- Average bandwidth = 1 'word' per 200 cycles (0.005 wpc)
 - 'a', 'b', and 'c' are 4-byte or 8-byte words
- Moving 'b' and 'c' from memory to CPU: 2 words per 300 cycles
- Moving 'a' from CPU to memory: 1 word per 300 cycles
- Average: 3 words per 600 cycles = 0.005 wpc

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Recap 'Data Streams'

Same example, but now with streams and with pipelining: a = b + c

- Bandwidth = 3 wpc
- Again let's pause here: Why exactly is the bandwidth 3 words per cycle?

Recap 'Data Streams'

<u>Bandwidth</u> is the amount of data transferred per unit of time
Most convenient units for now: words and cycles

Same example, but now with streams and with pipelining: a = b + c

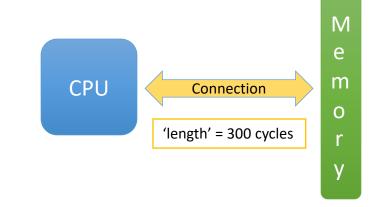
- Bandwidth = 3 wpc
- Every cycle one element of 'b' and 'c' are received, respectively
- Every cycle one element of 'a' is sent back
- In total, 3 words are received and sent every cycle
- Pipelining: one 'add' operation per cycle



Our first Computer: a(i) = b(i) + c(i)

Let's 'build' a computer and look at the requirements to achieve full performance

- CPU
 - Compute requirements: ...
 - Data movement: ...
- Memory
 - Data movement: ...
- Connection
 - Data movement: ...



Performance goal: 1 operation (add) per cycle (we are going to ignore the ramp-up and ramp-down phase for now)



Our first Computer: a(i) = b(i) + c(i)

Let's 'build' a computer and look at the requirements to achieve full performance

CPU

Compute requirements: pipelined, 1 opc

Data movement: 3 wpc

Memory

Data movement: 3 wpc

Connection

3 wpc and a total of 900 words 'en route' Data movement:

Performance goal: 1 operation per cycle (we are going to ignore the ramp-up and ramp-down phase for now)

But I'm starting to wonder how long these phases may be ...

CPU



m

0

Connection

'distance' = 300 cycles

Our <u>first</u> computer and our <u>first</u> source code

```
'Code kernel'
n = 10000
do i=1, n
a(i) = b(i) + c(i)
enddo
```

Pretty simple code

- Data streams between memory and CPU
- CPU executes the 'add' operation

```
'Full code'
program add
real,dimension(:),allocatable :: a,b,c
n = 10000
allocate (a(n),b(n),c(n))
do i=1, n
  a(i) = b(i) + c(i)
enddo
end program
Hints
- \real'
             = \float'
- 'allocate' = 'malloc'
- arrays count from 1, unless noted
                           otherwise
             = \for'
- \do'
```

Technically, the average performance depends on the value of 'n', but we'll make it easy

- 1. Large 'n': bandwidth = 3 wpc → performance 1 opc (operation per cycle)
- 2. Small 'n': bandwidth and performance limited (down to fractions of a percent)



Recap: class period 1

Things we have discussed:

- Primary components of a computer
- Clock tick, clock frequency and its limitations
- Units: word, wpc, opc
- Data streams
- Memory latency & bandwidth
- Pipelining



Let's beef-up our computer ... (just adding numbers is a bit dull)

We include 'mult' in our instruction set: multiply 2 numbers: $a = b \times c$

- 'add' 3 cycles, pipelined
- 'mult' 5 cycles, pipelined

3 and 5 cycles are realistic numbers or today's x86 hardware

We'll worry about the details later

Now we can implement a stencil update and can discover the next major hardware feature



Does anybody know: What is a stencil update? Where is a stencil update being used?

Very simple case in 2d ('x' and 'y' are 2d arrays)

For every position (i,j) an array element of 'y' is calculated as the average of its neighbors in the array 'x'

Each element:
$$y_{i,j} = 0.25 * (x_{i-1,j} + x_{i+1,j} + x_{i,j-1} + x_{i,j+1})$$

 $y = 0.25 * ('N' + 'S' + 'W' + 'E')$

Most simple implementation in 2d

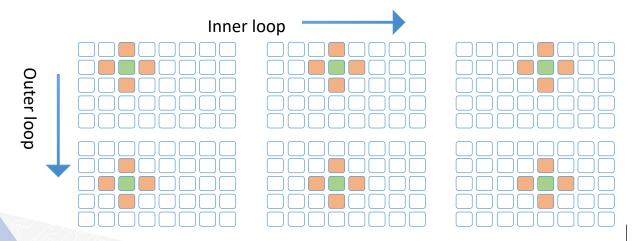
- Square arrays of identical size
- Only inner points are updated
- A little bit of space wasted, but no 'if' statements for the boundary

Let's discuss performance in terms of bandwidth

How much bandwidth (provided by the CPU-to-Memory connection) is needed for optimal/maximum performance?

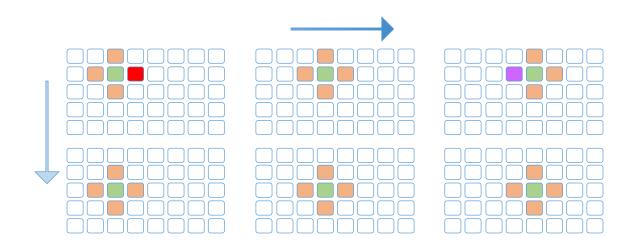
4 words input, 1 word output → 5 wpc

Can we lower the bandwidth requirement for the CPU-to-Memory connection?





Can we lower the bandwidth requirement?

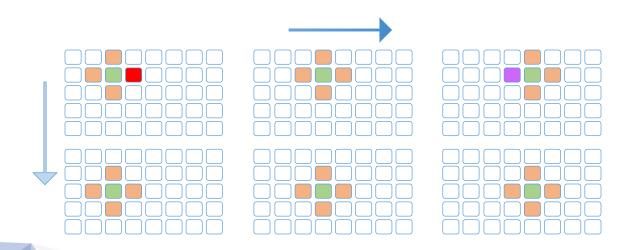




Can we lower the bandwidth requirement?

The element that we have loaded here is also loaded over here

If we go in <u>x-direction</u> first, this is just 2 loop iterations (inner loop) later

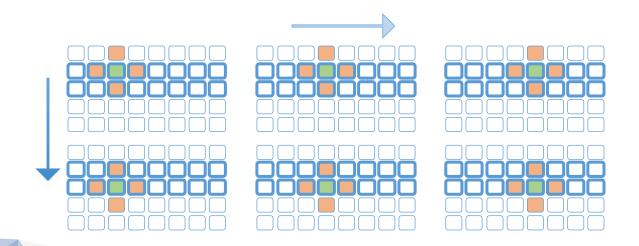




Can we lower the bandwidth requirement?

Similarly, two rows have been loaded in the previous y-loop

Can we use this to our advantage?



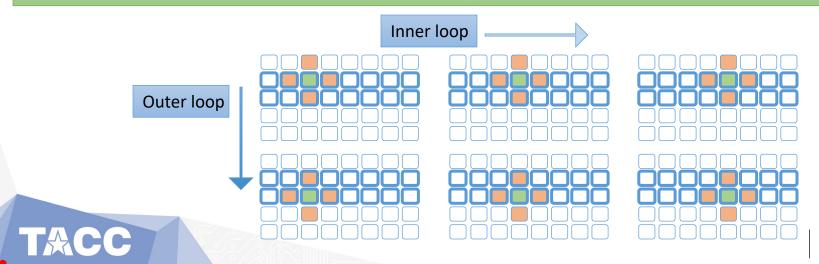


Can we lower the bandwidth requirement?

Two rows have been loaded in the previous y-loop

Can we use this to our advantage?

What if we could store two rows in a special buffer that provides higher bandwidth?

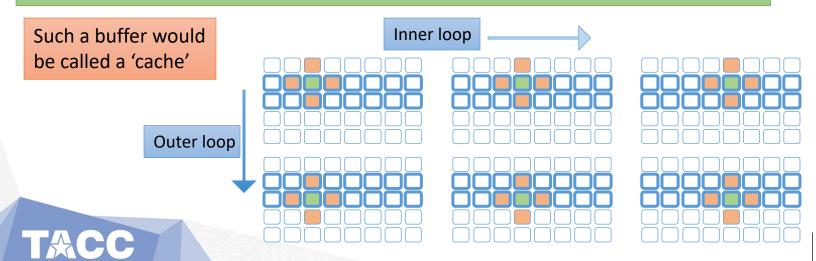


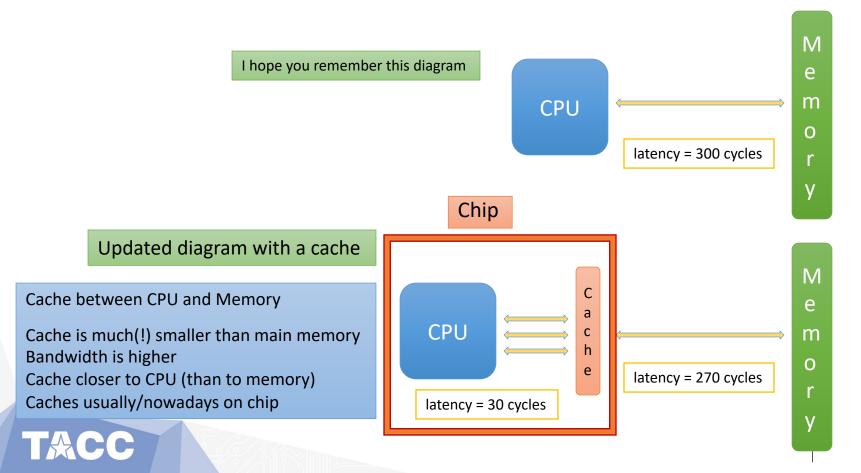
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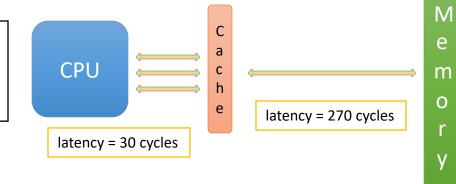
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Some questions to ponder:

- 1. How big should the cache be for our specific example?
 - Answer in terms of 'n'
- 2. How does the cache provide 3× higher bandwidth?



```
'Code kernel'
n = 10000
m = n+1
allocate (x(0:m,0:m),y(0:m,0:m))
do j=1, n
    do i=1, n
        y(i,j) = 0.25 * (x(i-1,j) + ...
    enddo
enddo
```



Some questions to ponder:

How big should the cache be for our specific example?

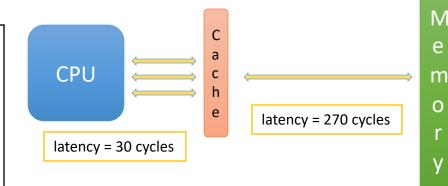
At least 2×n words

How does the cache provide 3× higher bandwidth?

Much closer

3× as many wires

•••



There is a deeper question here as well

How does the cache put '3x' more data onto the connection?

Note that the main memory is fast enough to feed '1×' data (the capabilities of the memory and the connection match)

```
'Code kernel'

n = 10000

m = n+1

allocate (x(0:m,0:m),y(0:m,0:m))

do j=1, n

do i=1, n

y(i,j) = 0.25 * (x(i-1,j) + ...

enddo

enddo
```



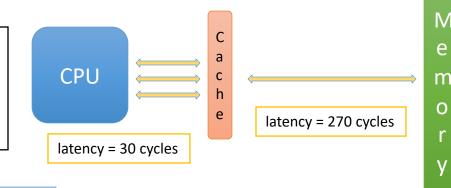
Some questions to ponder:

How big should the cache be for our specific example?

At least 2xn words

How does the cache provide 3× higher bandwidth?

More closely located, 3× as many wires, different hardware



There is a deeper question here as well

How does the cache put 3× more data onto the connection?

Assume that the main memory is fast enough to feed 1× data

Caches use a different storage technology

Main memory: DRAM --- Dynamic Random-Access Memory

Cache: SRAM --- Static Random-Access Memory

More later (maybe)

Random-access means that you can access data in any order

A different method would be a stack (of cards)
You can only add (write) to the top of the stack
You can only take (read) from the top of the stack

An additional fact about caches

- Caches are managed by the run-time
- User (user code) has no control over it

If a 'cache' were user-controlled, then it would (typically) have a different name

Such user-controlled 'caches' are sometimes part of non-x86 architectures

This leaves us with a big question

What strategy can we devise to make the cache most useful and 'automatic'?

The problem:

The cache is much(!) smaller (at least 1000×) then the memory

What do we do when the cache has filled up?



An additional fact about caches

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- Users (user code) has no control over it

This leaves us with a big question

What strategy can we devise to make the cache most useful and 'automatic'?

The problem:

The cache is much(!) smaller (at least 1000×) then the memory

What do we do when the cache has filled up?

One solution: **FIFO**, **First-in first-out**

When the cache is full and new data is entered, then the oldest data is evicted

In contrast: A stack is a LIFO, last-in first-out

Can you explain why?



Let's return to a slide we have discussed before

Some questions to ponder:

3. How is the cache managed?

Oldest data is evicted (FIFO)

Cache is managed by the run-time

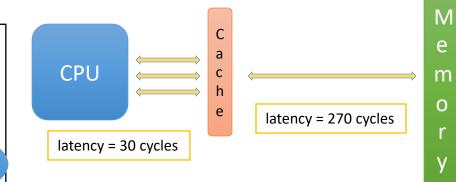
1. How big should the cache be for our specific example?

At least 2xn words

2. How does the cache provide 3× higher bandwidth?

Closer, 3× as many wires, different hardware

I added this **new** information to the slide



It seems to me that we must revise one of the statements above.

Which one, and why?



Reminder: Which rows are being re-used?

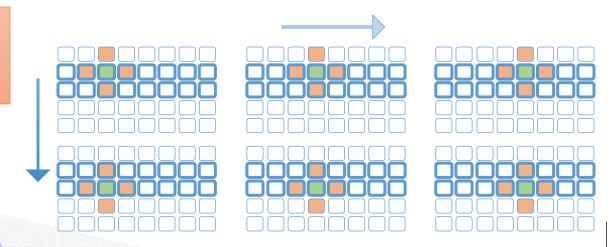
Can we lower the bandwidth requirement?

Similarly, two rows have been loaded in the previous y-loop

Can we use this to our advantage?

What if we could store two rows in a special buffer that provides higher bandwidth?

Such a buffer would be called a 'cache'





Let's revisit this slide

Some questions to ponder:

1. How big should the cache be for our specific example?

At least 3×n words

2. How does the cache provide 3× higher bandwidth? Closer, 3× as many wires, different hardware

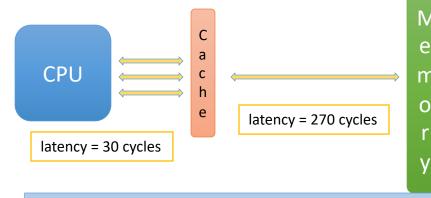
3. How is the cache managed?

Cache is managed by the run-time

Oldest data is evicted (FIFO)

It seems to me that we have to revise one of the statements above.

Which one, and why? Number of rows stored



The first re-use of cached data may happen when we start the second pass

During the second pass we evict data from the cache

The oldest elements are the first (leftmost) elements of the first 3 rows

In a user-managed setup we could just evict elements from the very first row

However, the cache will evict old elements from all rows. Hence we have to have room to store at least 3×n words, not just 2×n



Summary Part 1

Keep in mind that we have mostly discussed concepts

Many relevant details of the 3 major hardware features are still missing We have not discussed the ramifications for code design

Particularly our discussion of caches is very much incomplete!

(and we will continue with caches in the next section)

Main bottlenecks

Transfer the data between memory and CPU

Actual computation

Major technologies to increase concurrency

Streaming of data between memory and CPU to <u>hide memory latency</u> and <u>increase memory bandwidth</u>

Pipelining computation (add/mult) to increase compute throughput

Caches to re-use data in order to decrease pressure on the Memory-to-CPU connection and to also to <u>hide memory latency</u> and to <u>increase memory bandwidth</u>

Concurrency

A single action (flops, memory operation, etc.) can only be so fast

Clock speed, power consumption, speed of light

Increasing the 'concurrency' is the best (maybe only) way to increase performance substantially