





Scientific and Technical Computing

Hardware and Code Optimization

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UT Austin, 9/15/22 & 9/22/22



Our Computer: CPU, Cache, Memory, 'Connection'

CPU

1. Pipelined operation

System designed to get 1 opc

Memory

Data streams

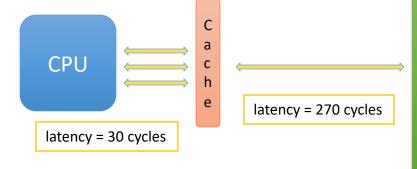
System designed to support 1 wpc (for one row)

Caches

- 1. Managed by run-time
- 2. Cache size (for stencil update)

System designed for 'enough' bandwidth to support 2 rows Size: at least 3×n words

Our computer has been somewhat 'hypothetical' so far We have designed the specs so that we get 'optimal' performance for a stencil update



But there is a problem with our cache



CPU

Pipelined operation

System designed to get 1 opc

Memory

Data streams

System designed to support 1 wpc (for one row)

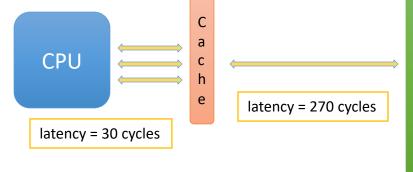
Caches

- Managed by run-time
- Cache size (for stencil update)

System designed for 'enough' bandwidth to support 2 rows

Size: at least 3×n words

Our computer has been somewhat 'hypothetical' so far We have designed the specs so that we get 'optimal' performance for a stencil update



Requirement: Size of the cache = $3 \times n$

n could be any number, any large number

Size of cache in hardware certainly not adjustable Also differences between chip generations



Outline

CPU & Memory, latency, bandwidth, wpc, opc ...

Data streaming, pipelining, caches (part 1)

Caches: software (short)

Caches (working principles)

There are at least 4 'working principles' that we will have to cover

TACC

My 'big' plan

Cover many hardware fundamentals as they guide code design

loosely in decreasing order of importance

For each hardware feature:

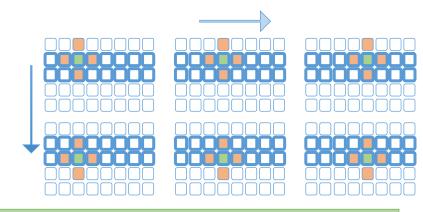
Add details as necessary to describe a simplified, yet functional 'working model'

Example:

n=500, cache size=300 words

At what iteration 'i' do we (approximately) start to replace data in the cache?

- 'i' is inner loop, left to right
- 'j' is outer loop, top to bottom



```
do j=1, n
do i=1, n
y(i,j) = 0.25 * (x(i-1,j) + x(i+1,j) + x(i,j-1) + x(i,j+1))
enddo
enddo
```



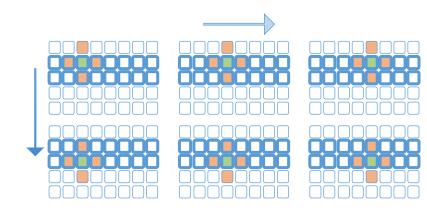
Example:

n=500, cache size=300 words

At what iteration 'i' do we (approximately) start to replace data in the cache? i~100

What do we do when we reach 'i=100'?

Hint: going further to the right is a 'dead end'



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do j=1, n
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y(i,j) = 0.25 * (x(i-1,j) + x(i+1,j) + x(i,j-1) + x(i,j+1))
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Example:

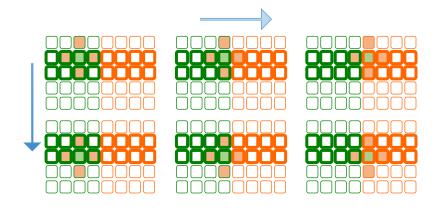
n=500, cache size=300 words

At what iteration 'i' do we (approximately) start to replace data in the cache? i~100

What do we do when we reach 'i=100'

- Hint: going further to the right is a 'dead end'
- Instead, we go one row down
- The green area first, then the orange area

How do we do this in code?



```
do j=1, n
  do i=1, n
    y(i,j) = 0.25 * (x(i-1,j) + x(i+1,j) + x(i,j-1) + x(i,j+1))
  enddo
enddo
```

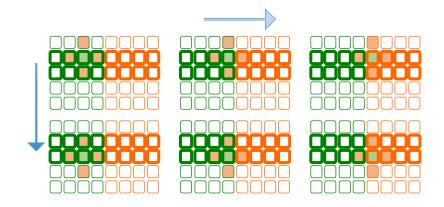


Example:

n=500, cache size=300 words

So how do we do this in code?

- What is the width of a stripe/block?
- How many stripes?
- How many loops in the code?



```
do j=1, n
  do i=1, n
    y(i,j) = 0.25 * (x(i-1,j) + x(i+1,j) + x(i,j-1) + x(i,j+1))
  enddo
enddo
```

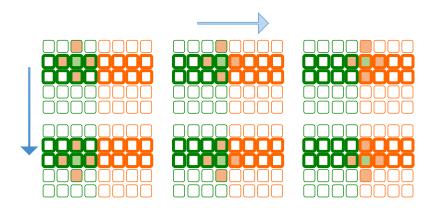


Example:

n=500, cache size=300 words

So how do we do this in code?

- What is the width of a stripe? 100
- How many stripes?
- How many loops in the code? 3 (up from 2)



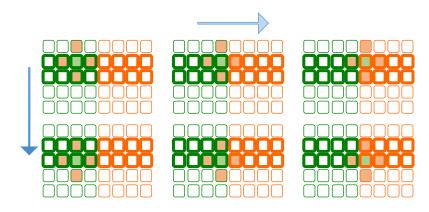
```
n = 500; ns = 100
do iout=1, ...
do j=1, n
   is = ...
   ie = ...
   do i=is, ie
      y(i,j) = 0.25 * (x(i-1,j) + x(i+1,j) + x(i,j-1) + x(i,j+1))
   enddo
enddo
enddo
enddo
```

Example:

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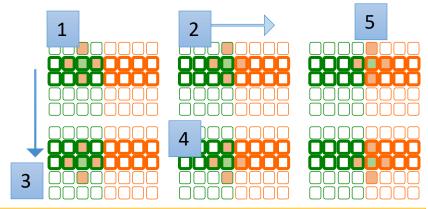
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  do j=1, n
    is = ...
    ie = ...
    do i=is, ie
        y(i,j) = 0.25 *
    enddo
enddo
enddo
```



We go fast left to right (**x**-direction)
We go slowly in **y**-direction
Hence left to right is the inner loop. Loop index is 'i'

The 'fast' loop, i.e. the inner loop 'exceeds' the size of the cache We split up the inner loop in 2 loops. Indexes 'i' and 'iout'

The loop 'j' that re-uses the data of the inner loop is in the middle



Re-use data before it is evicted

Breaking a loop into 2 (or more) parts

(There can be cache blocking for multiple loops)

Note:

In our example we have been overly optimistic
Width of the strip stretched to the max
Real application: other data is also stored in cache
(there are also other processes)

Let's fill in the blanks

```
n = 500; ns = 100
do iout=1, ...
  do j=1, n
    is = ...
  ie = ...
    do i=is, ie
        y(i,j) = 0.25 * (x(i-1,j) + x(i+1,j) + x(i,j-1) + x(i,j+1))
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enddo
```

Re-use data before it is evicted

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Be aware that for arbitrary pairs (n,ns) the code will be more complicated

Consider:

N=495; ns=100

TACC

```
n = 495; ns = 100
do iout=1, ...
  do j=1, n
    is = ...
    ie = ...
    do i=is, ie
        y(i,j) = 0.25 * (x(i-1,j) + x(i+1,j) + x(i,j-1) + x(i,j+1))
        enddo
    enddo
enddo
```

Re-use data before it is evicted

Breaking a loop into 2 (or more) parts

There can be cache blocking for multiple loops

1. Be aware that for arbitrary pairs (n,ns) the code will be more complicated

2. Cache size=300 → ns=100 ns is too large (by 2×) Why?



In our example we have been overly optimistic
Width of the strip stretched to the max
Real application: other data is also stored in cache
(there are also other processes)

In our example, why should the width of the strip (ns) be smaller than 50?

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n = 500; ns = 100
do iout=1, ...
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Re-use data before it is evicted

Breaking a loop into 2 (or more) parts

There can be cache blocking for multiple loops

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In our example, why should the width of the strip (ns) be smaller than 50?

Usually numerical tests (trials) are used to determine a suitable size for the cache blocking

Tests are repeated, if:

- Architecture changes (different machine)
- Implementation changes (more/less data in loop kernel)

```
n = 500; ns = 100
do iout=1, ...
do j=1, n
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Re-use data before it is evicted

Breaking a loop into 2 (or more) parts

There can be cache blocking for multiple loops

2. Cache size=300 → ns=100 ns is too large (by 2×) Why?

Everything moving between memory and CPU is cached:

Not just 'x' but also 'y'

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enddo
```



Limitations

Conflicting goals

- Purpose of cache: fast --- low latency/high bandwidth
- Organization of cache: FIFO (First In First Out) or LRU

Match or no-match?

How do we find a match?

How do we find an element to evict?

- 4 6 12 11
- 5 | 1 | 14 | 10
- 9 8 2 3
- 7 | 15 | 13 | 16

Problems to tackle

- Speed
- 2. FIFO
- 3. Storage efficiency

For illustration purposes
Cache is drawn as a 2d 'array'
You can imagine that the cache is
organized as a 1d array

Basic principle

The cache is small, therefore it can hold data only for a (very) limited time (time in cycles)

How long (# of cycles) and how often data is re-used depends on the code (implementation of the algorithm)

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- 4 6 12 11
 - 5 | 1 | 14 | 10
- 9 8 2 3
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Keep in this in mind when thinking about how a cache works:

- The cache stores where the data came from, i.e. the original address
- The cache stores the actual value

These numbers are the addresses, not the actual data Assume that in this example we encounter the addresses consecutive and in order.

Address '1', and its content, was stored first, and is the oldest Address '2', and its content', is the second oldest Address '16' was stored last

Problems to tackle

- 1. Speed
- 2. FIFO
- 3. Storage efficiency

Basic principle

The cache is small, therefore it can hold data only for a (very) limited time (time in cycles) How long (# of cycles) and how often data is re-used depends on the code (implementation of the algorithm)

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Problems to tackle

- 1. Speed
- 2. FIFO
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For illustration purposes
Cache is drawn as a 2d 'array'
You can imagine that the cache is
organized as a (long) 1d array

Example:

Loading element #3: This element is stored in the cache. How do we find element #3

Loading element #17: This is not a match; #17 loaded from memory and will replace oldest element in cache

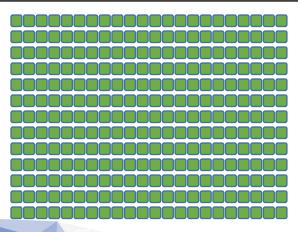
Limitations: The Cache can be quite large

Fully associative cache

- Data can be 'anywhere' in the cache
- Large number of checks to find elements in cache
- Bookkeeping of age for all elements

Conflicting goals

- Purpose of cache: fast --- low latency/high bandwidth
- Organization of cache: FIFO (First In- First Out) or LRU



Note:

For every cell in the cache the original address must be stored

Address = 1 word
Therefore, half the cache stores addresses
Half the cache stores data
... and then some ordering is needed

OK, for a cache holding 16 words we may be able to compare all addresses <u>and</u> also make FIFO work

Cache size may exceed 1Mw More that a million entries (1Mw = 4 or 8 Mb)

How can we devise a fast strategy?

Let's tackle 'fast access' first, and the add some FIFO and then storage efficiency



Example: Let's make our cache access fast

Let's make up some address space notation

- Address (main memory) has 6 digits
- Each digit holds a value between 1 and 4
- Example 142314

We encounter addresses in this order

141423

141424

141431

443311

141432

141433

121111

...

How can we map our addresses into the cache address space?

Our cache



Example: Let's make our cache fast

Let's make up some address space notation

- Address has 6 digits
- Each digit holds a value between 1 and 4

We encounter addresses in this order

What if I write it like this

1414 23

1414 24

1414 31

4433 11

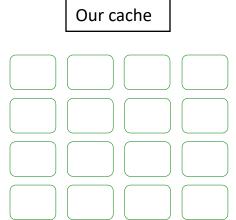
1414 32

1414 33

1211 11

...

How can we **map** our addresses into the cache address space?





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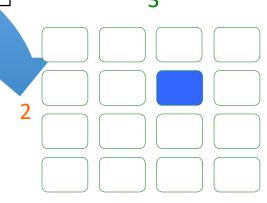
1414 32

1414 33

1211 11

...

How can we **map** our addresses into the cache address space?



Algorithm

CPU reads address

CPU checks if data is stored in cache

(How many storage locations have to be checked?)

- 1. If yes, read it from there
- 2. If no, read data from memory and store it also in cache



How does this implementation accelerate data access?

Cache with Direct Mapping

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- Address has 6 digital
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We enco r addresses in this order

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1414 23

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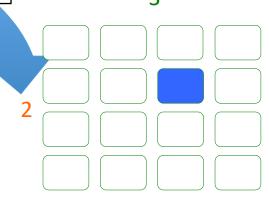
1414 32

1414 33

1211 11

. . .

How can we map our addresses into the cache address space?



<u>Direct Mapping</u> (many to one)

Every element in main memory can be stored In exactly one cache location

Problems

- 1. No FIFO --- Why?
- 2. Why do some access patterns render caching ineffective?



Cache with Direct Mapping: Problems

Conflicting goals

- Purpose of cache: fast --- low latency/high bandwidth
- Organization of cache: FIFO (First In- First Out) or LRU

Example: array with 16×16 elements Assume row major ordering Loop through the first column

How far are these elements apart in main memory addresses a(1,1), a(1,2), a(1,3)? or a[0,0], a[1,0], a[2,0] for column major ordering?





Cache with Direct Mapping: Problems

Conflicting goals

- Purpose of cache: fast --- low latency/high bandwidth
- Organization of cache: FIFO (First In- First Out) or LSR

```
Example: array with 16×16 elements

Assume row major ordering

Loop through the first column

How far are these elements apart in main memory addresses

a(1,1), a(1,2), a(1,3)?

a[0,0], a[1,0], a[2,0]?

Answer: The distance is 16
```



Example addresses are:

4422 22

4423 22

Where are these elements mapped in the cache?

4424 22

Cache with Direct Mapping: Problems

Conflicting goals

- Purpose of cache: fast --- low latency/high bandwidth
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```
Example: array with 16×16 elements
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How far are these elements apart in main memory addresses a(1,1), a(1,2), a(1,3) or a[0,0], a[1,0], a[2,0]? Answer: The distance is 16

Example addresses are:

4422 22

4423 22

4424 22

Where are these elements mapped in the cache? All to the same element Therefore, our cache has a reduced effective size (In our case just one element)







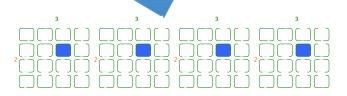
Cache Associativity

Let's make up some address space notation

- Address has 6 digits
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What if I it like this
1414 23
1414 24
1414 31
4433 11
1414 32
1414 33
1211 23
4433 23

Example: Cache with 4-way associativity



An element of data may be cached in 1 of 4 locations FIFO: replace the 'oldest' data element (out of the 4)

Advantages of Caches with Associativity

- 1. Ineffective mapping alleviated (somewhat)
- 2. Compare addresses only for few (4) locations
- 3. Eviction policy FIFO or LRU schedule
- 4. Keep 'age' for few (4) entries (In principle, 'random' eviction could work, too)



Cache: So far

What we have addressed so far

- Why caches?
- Cache blocking
- Address mapping
- Associativity
 - fully associative, set-associative, direct mapping

Remaining problem

For each 'cell' in the cache we store the

- data (that's what we are interested in)
- where the data came from (i.e. the address in main memory)

50% is useful (to us) 50% is book keeping

We can do better! But how?

Requirements

Know what is stored (full address)
Know how 'old' the data is (within associativity)

Finding data

Compare address with address in cache Two possibilities

- Match: load data from cache
- 2. No match: Load form memory, evict oldest data, store new data in place

Does this help us?

$$a(i) = b(i) + c(i)$$

```
loop with index i
  a(i) = b(i) + c(i)
end loop
```

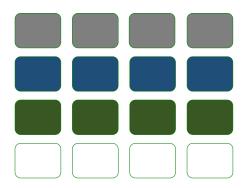
Can data streams help us reducing the overhead of book keeping?

Improved Cache Storage Efficiency

Let's make up some address space notation

- Address has 6 digits
- Each digit holds a lue between 1 and 4

Streams of data: a, b, c 1414 11 1414 12 1414 13 1414 14 3722 31 3722 32 3722 33 3722 34



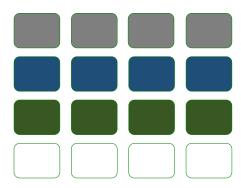
Consecutive (in memory) elements of a, b, and c are loaded Elements of a, b, and c are cached in consecutive locations

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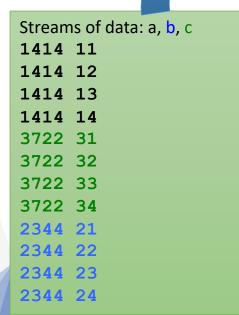
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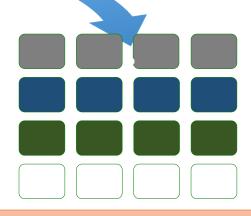
Let's take advantage and keep only track of consecutive tuples of 8/16 words (double/single precision), i.e. 512 bits

Cache Lines

Let's make up some address space notation

- Address has 6 digits
- Each digit holds a liue between 1 and 4





Complete cache lines are moved between memory, cache, and CPU 1 cache line: 512 bits (x86 architecture), or 8 words (dp), or 16 words (sp)

Book keeping is done per cache line (reduction by 7/8 or 15/16)

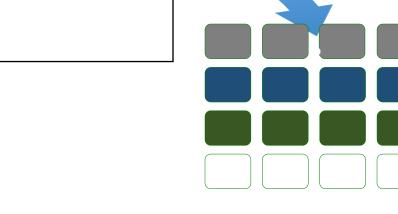
Assumption: It is likely that the code uses all elements rather than only 1 a(i) = b(i) + c(i): 3 streams each with consecutive data access

Is this always efficient? What would be a setup (addresses) were this works with limited efficiency?

Cache Lines

Let's make up some address space notation

- Address has 6 digits
- Each digit holds a lue between 1 and 4



Streams of data: a, b, c 1414 11 1414 12 1414 13 1414 14 3722 31

3722 32

3722 33

3722 34 2344 21

2344 22

2344 23

2344 24

Complete cache lines are moved between memory, cache, and CPU 1 cache line: 512 bits, or 8 words (dp), or 16 words (sp)

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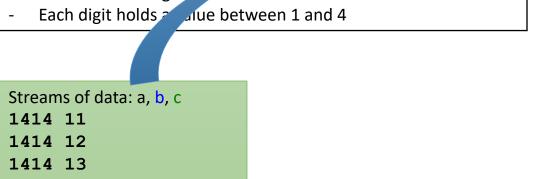
What will happen here?

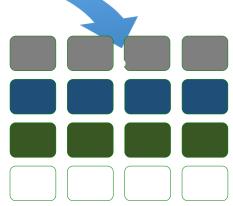
Loop with index i $a(2\times i) = b(2\times i) + c(2\times i)$

Cache Lines

Let's make up some address space notation

Address has 6 digits





Complete cache lines are moved between memory, cache, and CPU 1 cache line: 512 bits, or 8 words (dp), or 16 words (sp)

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What will happen here?

Loop with index i $a(2\times i) = b(2\times i) + c(2\times i)$

- Effective bandwidth reduced by 2×
- Effective cache size reduced by 2x

But wait ...

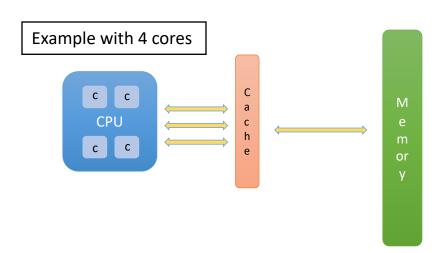
There is more!

about caches



Our Toy Computer with multi-core CPUs





Stampede2

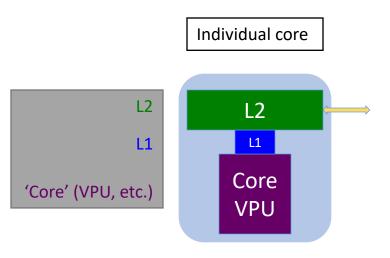
A socket/CPU has 24 cores
The total number of caches per socket is 49

How many caches are there

- Per core?
- Per CPU?



Our Toy Computer with multi-core CPUs



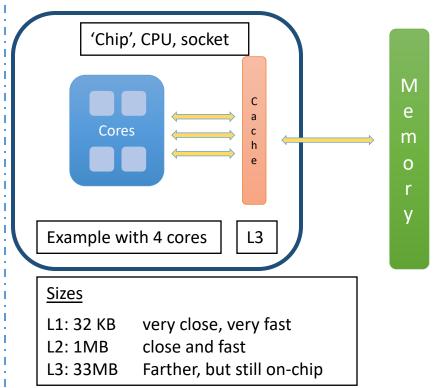
Stampede2

A socket/CPU has 24 cores
The total number of caches per CPU is 49

How many caches are there

- Per core? 2 (L1 and L2)
- Per CPU? 1 (L3)

Feel sorry for the 'bookkeeper' at least once!



Stampede2 nodes have 2 sockets
Total number of caches is 98



More bookkeeping

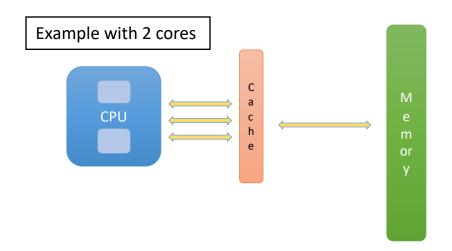
Bookkeeping: MOESI Protocol

For now, only consider reading data

$$... = b(i) + \underline{c(i)}$$

We start the loop, reading c(1) on core 0

- 1. Cache line for c(1:8) is in main memory
- 2. Cache line moves to L3
- Cache line moves to L2
- Cache line moves to L1
- 5. 'somehow' we perform the operation



So where do we read c(2) from?

For now, only consider reading data

$$\dots = b(i) + c(i)$$

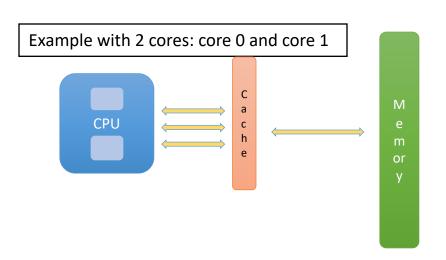
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So where do we read c(2) from?

We continue the loop, reading c(2)

- 1. There are now 4 copies of the cache line
- 2. We can read the data from any copy, <u>likely</u> reading from L1
- 3. 'somehow' we perform the operation



For now, only consider reading data

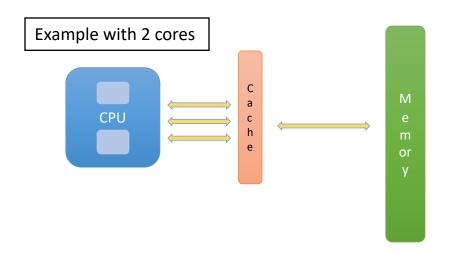
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We continue the loop, reading c(2)

- 1. There are now 4 copies of the cache line
- 2. We can read the data from any copy, likely reading from L1
- 3. 'somehow' we perform the operation



Process hops to <u>core 1</u> and we continue the loop, reading c(3)

- 1. There are now 4 copies of the cache line
- 2. 2 copies are far away, L1 and L2 of core 0
- 3. 1 copy is close: L3
- 4. 1 copy is far away (memory)
- 5. 'somehow' we perform the operation

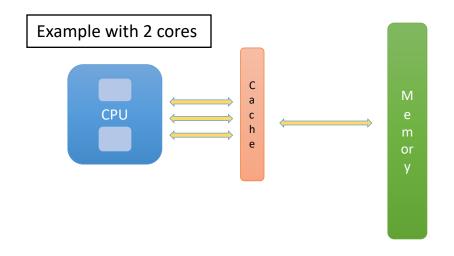
We can read from any copy (depending on availability and convenience)

For now, only consider writing data

a(i) = ...

We have to bring in cache line first (more later)

- 1. Cache line for a(1:8) is in main memory
- 2. Cache line moves to L3
- Cache line moves to L2
- 4. Cache line moves to L1
- 5. 'somehow' we perform the operation
- 6. a(1) is modified
- 7. Modified cache line moves back to L1



Process hops to <u>core 1</u> and we continue the loop, modifying a(2)

- 1. Again, there are now 4 copies of the cache line
- 2. Which one do we use?

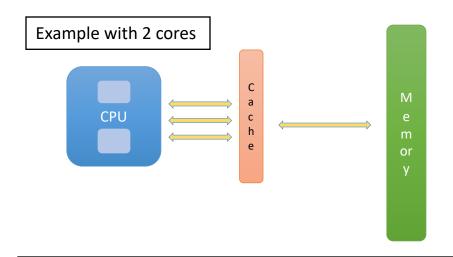


For now, only consider writing data

a(i) = ...

We have to bring in cache line first (more later)

- 1. Cache line for a(1:8) is in main memory
- 2. Cache line moves to L3
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- 4. Cache line moves to L1
- 5. 'somehow' we perform the operation
- 6. a(1) is modified
- 7. Cache line moves back to L1



Process hops to <u>core 1</u> and

we continue the loop, modifying a(2)

- 1. Again, there are now 4 copies of the cache line
- Which one do we use?
- 3. 3 of the 4 copies are invalid
- 4. Only the copy in L1 of core 0 is 'good to go'

A cache line can be in one of these states

Modified (M): Only one cache has a valid copy (which has been modified). All other copies are invalid

Owned (O): Multiple caches hold a copy, which may or may not be valid. Only one cache 'owns'

the cache line

• Exclusive (E): Only one cache holds an exclusive copy

• Shared (S): Multiple caches hold a copy of the cache line

<u>Invalid</u> (I): A copy of the cache line that is invalid

Writing

Before a process can modify data, it must own the cache line. Then the modification renders all other copies invalid

Reading

To read from a cache line, the status of the cache line has to be 'shared', or 'owned', or 'modified', but not 'invalid'!

Complexity: very large

49 caches per socket (per CPU)

2 sockets: lot's of traffic between sockets (cache snooping)

Cache coherency

MOESI protocol ensures cache coherency

Programmer not responsible for managing cache lines

Cornerstone of <u>any</u> shared-memory platform

Backbone of any thread-based parallel computing



Performance/programming implications from MO(E)SI

Parallel computing is not part of this class (see PCSE in the Spring)

Nevertheless, there is one implication that I'd like to discuss.

Imagine your code executes on 2 cores

- Two 'thingies' are executing. These 'thingies' are called threads (reference to OpenMP)
- A loop is split in two halves. Each thread is executing ½ of the loop → 2x speed-up (theoretically)

Which solution will work better? (having cache-coherency in mind)

```
Scenario 1: Loop split into 2

Thread 0

do i=1, n/2

a(i) = b(i) + c(i)

enddo

Thread 1

do i=n/2+1, n

a(i) = b(i) + c(i)

enddo
```

```
Scenario 2: Loops for odd and even elements

Thread 0 (odd)

do i=1, n, 2 do i=2, n, 2

a(i) = b(i) + c(i) a(i) = b(i) + c(i) enddo
```



```
General syntax: Do <start>, <end>, <increment> (default increment is +1)

Odd elements: do i=1, n, 2 (1, 3, 5, 7, ...)

Even elements: do i=2, n, 2 (2, 4, 6, 8, ...)
```

False Sharing of Cache Lines

Imagine your code executes on 2 cores

- Two 'thingies' are executing. These 'thingies' are called threads
- A loop is split in two halves. Each thread is executing $\frac{1}{2} \Rightarrow 2 \times$ speed-up (theoretically)

Which solution will work better? (having cache-coherency in mind)

```
Scenario 2: Loops for odd and even elements

Thread 0

do i=1, n, 2

a(i) = b(i) + c(i)

enddo

Thread 1

do i=2, n, 2

a(i) = b(i) + c(i)

enddo
```

Scenario 2: Two threads are writing to the same cache line (at potentially the same time) The cache lines are (potentially) bouncing around multiple times, negating any speed-up

This happens after one thread has modified a cache line (close to one core)

- Other copies are invalidated
- Before the other thread can write, the cache line has to be transferred
- Now both threads have a cache line available close by
- But once a thread is modifying its cache line, the other copy becomes 'invalid'



False Sharing of Cache Lines

Imagine your code executes on 2 cores

- Two 'thingies' are executing. These 'thingies' are called threads
- A loop is split in two halves. Each thread is executing $\frac{1}{2} \Rightarrow 2 \times$ speed-up (theoretically)

Which solution will work better? (having cache-coherency in mind)

```
Scenario 2: Loops for odd and even elements

Thread 0

do i=1, n, 2

a(i) = b(i) + c(i)

enddo

\frac{\text{Thread 1}}{\text{do i=2, n, 2}}

a(i) = b(i) + c(i)

enddo

enddo
```

Scenario 2: Two threads are writing to the same cache line (at potentially the same time) The cache lines are (potentially) bouncing around multiple times, negating any speed-up

This happens after one thread has modified a cache line (close to one core)

- Other copies are invalidated
- Before the other thread can write, the cache line has to be transferred
- Now both threads have a cache line available close by
- But once a thread is modifying its cache line, the other copy becomes 'invalid'

OK, why would anybody write code like this?

Here is a better example with a reduction

False Sharing of Cache Lines: Reduction Example

Task: Compute the sum of a vector using 2 threads

```
real, dimension(0:1) :: s ! Partial sums, 2 elements

\frac{\text{Thread 0}}{\text{s(0)} = 0.} \qquad \frac{\text{Thread 1}}{\text{s(1)} = 0.} \\
\text{do } i=1, \, n/2 \qquad \text{do } i=n/2+1, \, n \\
\text{s(0)} = \text{s(0)} + \text{a(i)} \qquad \text{s(1)} = \text{s(1)} + \text{a(i)} \\
\text{enddo} \qquad \text{enddo}

\text{sum} = \text{s(0)} + \text{s(1)} \qquad ! \text{ Global sum from partial sums}
```

Reduction:

- Decreasing/reducing complexity
- Calculating a result with a lower 'dimensionality' from higher 'dimensionality'

Examples

- sum of a vector (1-d → scalar)
- Sum of an array ('any'-d → scalar)

Problem: both threads update repeatedly data stored in the same cache line

So what would be a remedy?

Two threads are writing to the same cache line (at potentially the same time)

The cache lines are (potentially) bouncing around multiple times, wiping out any speed-up

This happens after one thread has modified a cache line (close to one core)

- Other copies are invalidated
- Before the other thread can write, the cache line has to be transferred
- Now both threads have a cache line available close by
- But once a thread is modifying its cache line, the other copy becomes 'invalid'

False Sharing of Cache Lines: Reduction Example

Task: Compute the sum of a vector using 2 threads

```
real, dimension(0:16) :: s ! Partial sums, 17 elements

\frac{\text{Thread 0}}{\text{s(0)}} = 0. \\
\text{do i=1, n/2} \\
\text{s(0)} = \text{s(0)} + \text{a(i)} \\
\text{enddo}

\frac{\text{Thread 1}}{\text{s(16)}} = 0. \\
\text{do i=n/2+1, n} \\
\text{s(0)} = \text{s(0)} + \text{a(i)} \\
\text{enddo}

\frac{\text{s(16)}}{\text{enddo}} = \text{s(16)} + \text{a(i)} \\
\text{enddo}

\frac{\text{s(16)}}{\text{enddo}} = \text{s(16)} + \text{a(i)} \\
\text{enddo}
```

Move your partial sums to <u>addresses</u> that are guaranteed <u>not</u> to be <u>on</u> the <u>same cache line</u>

Note that OpenMP provides other mechanisms to avoid 'false sharing' However, sometimes it is useful to intervene manually

Example: Stencil update

If you use multiple threads you may put the domain boundaries on top of a cache line boundary



Recap

Topics that we have addressed so far

Data streams

Pipelining

Caches

- Why?
- Cache blocking (software)
- Address mapping
- Eviction policy (FIFO, etc.)
- Associativity
 - fully associative, <u>set-associative</u>, direct mapping
- Storage efficiency (for addresses)
 - Cache lines
- Cache coherency (MOSI protocol)
- Shared-memory architecture
- False sharing

Overarching idea

Single transaction is limited in speed

Increasing concurrency is our goal

Memory transactions and (floating point) operations

One more hardware feature to cover (unrelated to caches)

And then we will start looking into 'writing fast code'

All these topics come with these questions:

- What is it?
- Why do we need it?
- How is it implemented?
- Is there a specific trick?
- How does this increase concurrency?