

CIRCULAR MOTION

- RELATION B/w $\vec{\omega}$ & \vec{v}

Distance $\Rightarrow S = R\theta$

Velocity $\Rightarrow v = R \frac{d\theta}{dt} \Rightarrow \boxed{v = R\omega}$

Velocity $\Rightarrow \boxed{\vec{v} = \vec{R} \times \vec{\omega}}$

- Uniform Circular motion

$a_t = 0$, $\alpha = 0$, $v \Rightarrow \text{Const}$

$a_r = \omega^2 R$, $|a_r| \Rightarrow \text{Const}$

Time period = $\frac{2\pi}{\omega}$

- Banking of the roads

$v = \sqrt{gR \tan \theta}$ (no friction)

$v_{\max} = \sqrt{\frac{gR(\mu + \tan \theta)}{(1 - \mu \tan \theta)}}$ (friction)

- Acceleration (a)

$a = \alpha R (\hat{e}_t) + \omega^2 R (-\hat{e}_r)$

$|\vec{a}_t| = \alpha R$ $|\vec{a}_r| = \omega^2 R = \frac{v^2}{R}$



॥ अहम ब्रह्मास्मी ॥

- Radius of Curvature

$y = f(x) \rightarrow \text{eq}^n \text{ of path}$

$R_{oc} = \frac{[1 + (y')^2]^{3/2}}{y''}$

- Forces (dynamics)

$F_r = \frac{mv^2}{R} = m\omega^2 R$
(centripetal)

- Rotor

$\omega > \sqrt{\frac{g}{\mu R}}$

- Death well

$v > \sqrt{\frac{gR}{\mu}}$

$v_{\min} = \sqrt{\frac{gR}{\mu}}$