

PART (A): PHYSICS

Answer Key & Solution

1. (A or C or D)
$$\Delta V = \vec{v}_F - \vec{v}_L = 10\sqrt{2}\hat{i} - 10\sqrt{2}\hat{j}$$
$$= 10\sqrt{2}\left(\hat{i} - \hat{j}\right)$$

2. (B)

$$W.D = \vec{F} \cdot \vec{d}$$

$$= (\vec{F_1} + \vec{F_2}) \cdot \vec{d}$$

$$= \left[(2\hat{i} - 5\hat{j} + 6\hat{k}) + (-\hat{i} + 2\hat{j} - \hat{k}) \right] \cdot (2\hat{i} + 4\hat{j} - \hat{k})$$

$$= -15 \text{ units.}$$

3. (C)
$$T = 2\pi \sqrt{\frac{L}{g}}$$

$$\frac{\Delta T}{T} = \frac{1}{2} \frac{\Delta L}{L} + \frac{1}{2} \frac{\Delta g}{g}$$

$$= \frac{1}{2} \times 2 + \frac{1}{2} \times 4 = 3\%$$

6. (A)

$$mg - T = ma_{C}$$

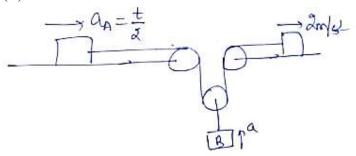
$$3T = ma_{A}$$

$$4T = ma_{B}$$

$$3a_{A} + 4a_{B} = a_{C} \implies a_{B} = \frac{2g}{13}$$



7. (C)



$$-a_A - a - a + a_C = 0$$

$$2a = 2 - \frac{t}{2}$$

$$a = 1 - \frac{t}{4}$$

$$\frac{dv}{dt} = 1 - \frac{t}{4}$$

$$\int_{0}^{v} dv = \int_{0}^{t} \left(1 - \frac{t}{4}\right) dt$$

$$v = t - \frac{t^2}{8} = 0$$

$$t = 8 \sec$$

$$v_x = 3 \,\mathrm{m/sec}$$

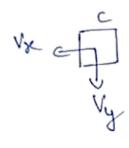
Applying constraint

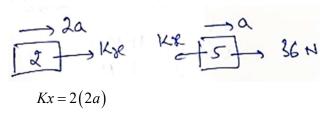
$$-3 - 3 + 1 + 1 + V_y = 0$$

$$V_v = 4 \,\mathrm{m/sec}$$

$$\left|V_C\right| = \sqrt{4^2 + 3^2}$$

$$= 5 \,\mathrm{m/sec}$$







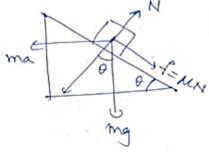
$$36 = 9a \implies a = \frac{36}{9} = 4 \text{ m/s}^2$$

$$Kx = 4 \times 4 = 16 \text{ m}$$

$$\Rightarrow x = 0.16 \,\mathrm{m}$$

$$=16 \,\mathrm{cm}$$

10. (B)



$$N = mg\cos 45 + ma\sin 45$$

$$f + mg\sin 45 = ma\cos 45$$

$$a = g\left(\frac{1+\mu}{1-\mu}\right)$$

11. **(B)**

Solved example in HCV.

$$2T = (100 + 50) a_x$$

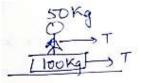
$$2\times100=150\times a$$

$$a = \frac{4}{3} \,\mathrm{m/s^2}$$

For man

$$T - f = 50a$$

$$f = \frac{100}{3}$$
N





When
$$x = R$$
 $y =$

$$0 = 12R - \frac{3}{4}R^2 \implies R = 16 \,\mathrm{m}$$



$$u_r = v_r = 6 \,\mathrm{m/sec}$$

$$v_y^2 - u_y^2 = 2(-g)h \implies u_y = 2\sqrt{3} \text{ m/sec}$$

$$\tan \theta = \frac{u_y}{u_x} = \frac{2\sqrt{3}}{6} = \frac{1}{\sqrt{3}}$$

$$\theta = 30^{\circ}$$

$$v_y^2 = u_y^2 + 2a_y S_y$$

$$(3u)^2 = u^2 + 2(-g)(-H)$$

$$H = \frac{4u^2}{g}$$

From
$$t = 0$$
 to $t = 24$

Area =
$$70 = x_2 - x_1 = x_2 - (-16)$$

$$x_2 = 54 \,\mathrm{m}$$

From
$$t = 0$$
 to $t = 18$ and $t = 0$ to $t = 30$

Area =
$$52 = x_2 - (-16)$$

$$x_2 = 36 \,\mathrm{m}$$

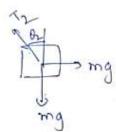
$$6 mg - 8T = 6 ma_2$$

$$T - mg = ma_1$$

$$a_1 = 8a_2 \implies a_2 = -g/35$$

$$a_1 = -8g/35$$
 and $V_1 = 8V_2$

18. (B, C, D)



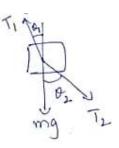
$$T_2\sin\theta_2=mg$$

$$T_2\cos\theta_2=mg$$

$$\tan \theta_2 = 1 \Longrightarrow \theta_2 = 45^{\circ}$$



For B



$$T_1 \sin \theta_1 = T_2 \sin \theta_2$$

$$T_2 \cos \theta_2 + mg = T_1 \cos \theta_1$$

$$\tan \theta_1 = \frac{1}{2}$$

&
$$T_2 = \sqrt{5} mg$$

$$M, B)$$

$$m_{B} > m_{A}$$

$$m_{B}g \sin \theta = f + \mathcal{I}'$$

$$-m_{A}g \sin \theta \pm f = -\mathcal{I}'$$

$$m_{B}g \sin \theta = f + \mathcal{I}'$$

$$(m_B - m_A)g\sin\theta = 2F$$

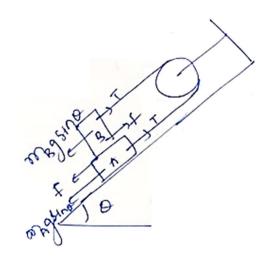
$$F = \frac{\left(m_B - m_A\right)g\sin\theta}{2}$$

And make sure $f < f_L$

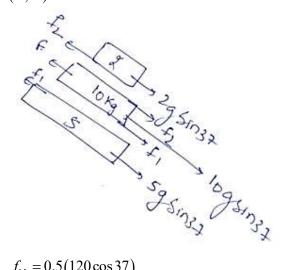
$$\frac{\left(m_{B}-m_{A}\right)\cancel{g}\sin\theta}{2}\leq\mu m_{B}\cancel{g}\cos\theta$$

$$\mu \ge \frac{\left(m_B - m_A\right) \cancel{g} \tan \theta}{2m_B}$$

If
$$m_A = m_B \implies f = 0$$



20.



$$f_{1L} = 0.5(120\cos 37)$$

 $=48 \, \text{N}$

Friction between 5 & 10 kg



Block will be 30 N (static)

$$f_1 = 30 \,\mathrm{N}$$

$$f_{2L} = 0.8 \times 20 \cos 37 = 12.8 \,\mathrm{N}$$

$$f_2 = 12 \,\mathrm{N}$$

$$F - f_1 - f_2 - 60 = 0$$

$$F = 102 \,\mathrm{N}$$