

# Linear Regression

9/15/2021

### Lesson Plan

- Linear Regression with One Feature
- Cost Function
- Gradient Descent
- Linear Regression with Multiple Features

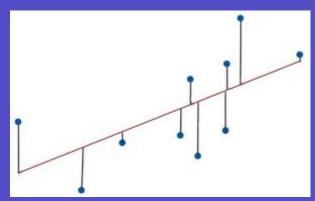
# Linear Regression with One Feature

Fuel Consumption	CO2 Emissions	
6.7	196	
7.7	221	
5.8	136	
9.1	255	
8.7	244	

- Hypothesis:  $h_{\theta}(x) = \theta_0 + \theta_1 x$
- How should one choose  $\theta_0$  and  $\theta_1$ ?

#### **Cost Function**

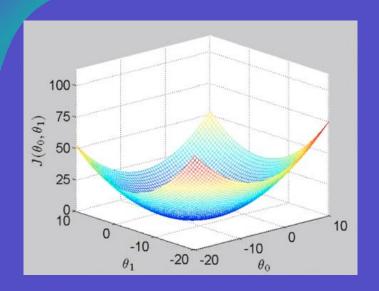
- Ordinary Least Squares Regression
  - Uses the mean squared error cost function



$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

Goal: minimize the cost function

### **Gradient Descent**



$$\theta_j = \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta)$$

- a: learning rate
- Low *a* → slow convergence
- High  $a \rightarrow$  may cause divergence

## Linear Regression with Multiple Features

Engine Size	Cylinders	City Fuel Consumption	Highway Fuel Consumption	CO2 Emissions
2	4	9.9	6.7	196
2.4	4	11.2	7.7	221
1.5	4	6	5.8	136
3.5	6	12.7	9.1	255
3.5	6	12.1	8.7	244

- Hypothesis:  $h_{\theta}(x) = \theta_0 + \theta_1 x_1 + \cdots + \theta_n x_n$
- Same cost function & gradient descent as single feature linear regression



Word of the Day: Hypothesis

Check In:

https://forms.gle/MXg4oTtn5ciZez3n8