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a1

1) Dijkstra's algorithm is an algorithm for finding the shortest paths between nodes in a weighted graph

2) a) a, f

Literation	S	N	L(a)	L(b)	L(c)	L(h)	L(i)	L(f)	L(j)	L(d)	L(g)	L(j)
0	{ }	{a,b,c,h,i,f,d,g,j}	0	∞	∞	∞	∞	∞	∞	∞	∞	∞
1	{a}	{b,c,h,i,f,d,g,j}	0	(3)	5	4	∞	∞	∞	∞	∞	∞
2	{a,b}	{c,h,i,f,d,g,j}	0	3	5	(4)	5	10	∞	∞	∞	∞
3	{a,b,h}	{c,i,f,d,g,j}	0	3	(5)	4	5	9	6	∞	∞	∞
4	{a,b,h,e}	{c,i,f,d,g,j}	0	3	5	4	(5)	9	6	∞	∞	∞
5	{a,b,h,e,c}	{f,i,d,g,j}	0	3	5	4	5	7	(6)	8	11	∞
6	{a,b,h,e,c,i}	{f,d,g,j}	0	3	5	4	5	(7)	6	8	11	12
7	{a,b,h,e,c,i,f}	{d,g,j}	0	3	5	4	5	7	6	8	11	12

shortest path : $a \rightarrow b \rightarrow c \rightarrow f$ which is 7

b) b, j

Literation	S	N	L(b)	L(c)	L(e)	L(f)	L(d)	L(g)	L(j)	L(i)	L(h)	L(z)
0	{ }	{b,c,e,f,d,g,j,i,h,z}	0	∞	∞	∞	∞	∞	∞	∞	∞	∞
1	{b}	{c,e,f,d,g,j,i,h,z}	0	(2)	5	7	∞	∞	∞	∞	∞	∞
2	{b,c}	{e,f,d,g,j,i,h,z}	0	2	5	(4)	5	8	∞	∞	∞	∞
3	{b,c,f}	{e,d,g,j,i,h,z}	0	2	(5)	4	5	8	7	8	9	∞
4	{b,c,f,e}	{d,g,j,i,h,z}	0	2	5	4	(5)	8	7	8	9	∞
5	{b,c,f,e,d}	{g,j,i,h,z}	0	2	5	4	5	8	(7)	8	9	7
6	{b,c,f,e,d,j}	{g,i,h,z}	0	2	5	4	5	8	7	8	9	7

shortest path : $b \rightarrow c \rightarrow f \rightarrow j$ which is 7

c) a, g

Literation	S	N	L(a)	L(b)	L(e)	L(h)	L(i)	L(f)	L(j)	L(d)	L(g)	L(j)	L(z)
0	{ }	{a,b,c,h,i,f,d,g,j,z}	0	∞	∞	∞	∞	∞	∞	∞	∞	∞	∞
1	{a}	{b,c,h,i,f,d,g,j,z}	0	(3)	5	4	∞	∞	∞	∞	∞	∞	∞
2	{a,b}	{c,h,i,f,d,g,j,z}	0	3	5	(4)	5	10	∞	∞	∞	∞	∞
3	{a,b,h}	{c,i,f,d,g,j,z}	0	3	(5)	4	5	10	6	∞	∞	∞	∞
5	{a,b,h,e}	{c,i,f,d,g,j,z}	0	3	5	4	(5)	9	6	∞	∞	∞	∞
6	{a,b,h,e,c}	{f,i,d,g,j,z}	0	3	5	4	5	7	(6)	8	11	∞	∞
7	{a,b,h,e,c,i}	{f,d,g,j,z}	0	3	5	4	5	7	6	(8)	11	12	∞
8	{a,b,h,e,c,i,d}	{f,g,j,z}	0	3	5	4	5	7	6	8	11	12	(10)
9	{a,b,h,e,c,i,d,z}	{f,g,j}	0	3	5	4	5	7	6	8	(11)	12	10
10	{a,b,h,e,c,i,d,z,g}	{f,j}	0	3	5	4	5	7	6	8	11	12	10

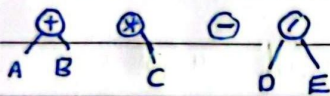
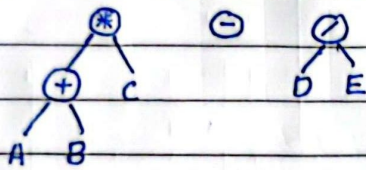
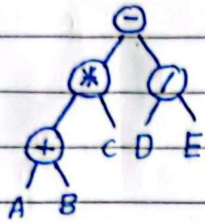
shortest path : $a \rightarrow b \rightarrow c \rightarrow g$ which is 11

Q2

1) a is balanced as every leaves are at level 2 or level 1 (maximum height = 2)

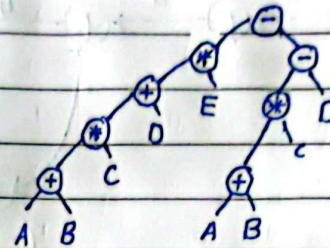
b is balanced as every leaves are at level 3 or level 2 (maximum height = 3)

2)

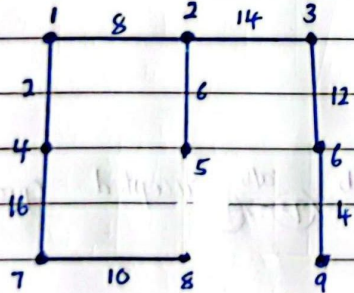


$$A \oplus B \otimes C \ominus D \oslash E$$
inorder traversal : $A + B * C - D / E$

3)

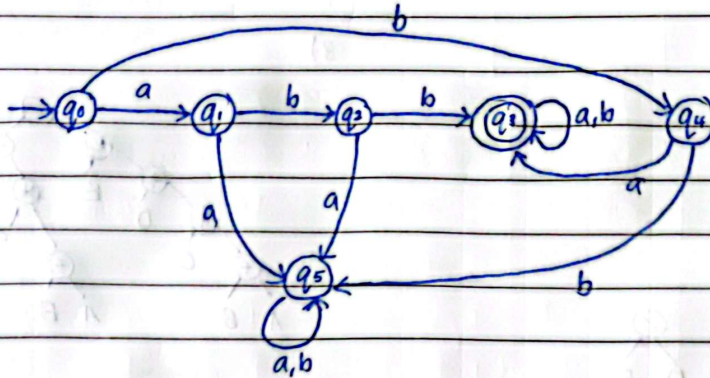
prefix form : $- * + * + A B C D E - * + A B C D$ postfix form : $AB + C * D + E * AB + C * D - -$

4)



$$\begin{aligned} \text{MST} &= 2 + 4 + 6 + 8 + 10 + 12 + 14 + 16 \\ &= 72 \end{aligned}$$

Q3

1) accept the strings over $\{a, b\}$, starting with either abb or ba Let $M = \{q_0, q_1, q_2, q_3, q_4, q_5\}$, $\{a, b\}$, $q_0, f_s, \{q_3\}$ 

Transition table :

	f_s	a	b
q_0	q_1	q_1	q_4
q_1	q_5	q_5	q_2
q_2	q_5	q_5	q_3
q_3	q_3	q_3	q_3
q_4	q_3	q_3	q_5
q_5	q_5	q_5	q_5

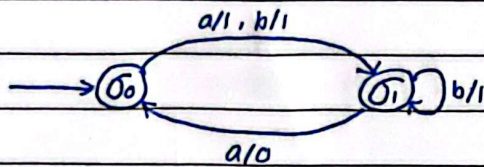
when starting from abb : $q_0 \xrightarrow{a} q_1 \xrightarrow{b} q_2 \xrightarrow{b} q_3$ accepted (proved)

when starting from ba : $q_0 \xrightarrow{b} q_4 \xrightarrow{a} q_3$ accepted (proved)

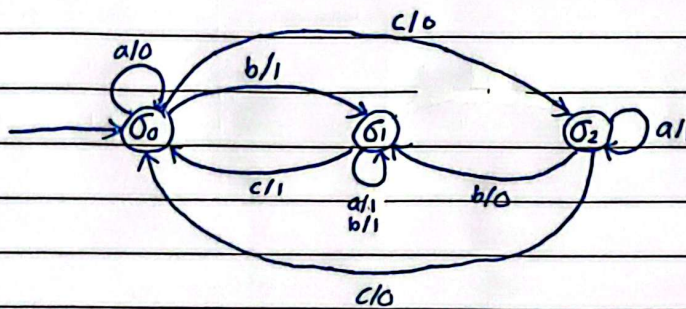
Q4

1) Finite-state machine (FSM) is a mathematical model of computation. Every state has an input and corresponding to the input and the state also has an output. It is a computational model that can be used to stimulate sequential logic.

2) a)



b)



3) $I = \{a, b\}$ $O = \{0, 1\}$ $S = \{q_0, q_1, q_2, q_3\}$ initial state = q_0

s \ I	f_s		f_o	
	a	b	a	b
q_0	q_1	q_2	0	0
q_1	q_0	q_2	1	0
q_2	q_3	q_0	0	1
q_3	q_1	q_3	0	0