

**First Results from the Taiwan Axion Search Experiment with  
Haloscope in the 19.47–19.84  $\mu\text{eV}$  Mass Range\***

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# Abstract

This paper presents the first results from the Taiwan Axion Search Experiment with Haloscope, a search for axions using a microwave cavity at frequencies between 4.707506 and 4.798145 GHz. Apart from the external signals, no candidates with a significance more than  $3.355\sigma$  were found. The experiment excludes models with the axion-two-photon coupling  $|g_{a\gamma\gamma}| \gtrsim 7.7 \times 10^{-14} \text{ GeV}^{-1}$ , a factor of ten above the benchmark KSVZ model for the mass range  $19.47 < m_a < 19.84 \mu\text{eV}$ . For the first time, constraints on the  $|g_{a\gamma\gamma}|$  are placed in this mass region.

## CONTENTS

I. Introduction	3
A. The expected axion signal power and signal line shape	5
B. The expected noise and the signal-to-noise ratio	6
II. Experimental Setup	8
III. Calibration	9
IV. Analysis Procedure	11
A. Fast Fourier transform	12
B. Remove the structure of the background	12
C. Combine the spectra with the weighting algorithm	14
D. Merge bins	16
E. Rescan and set limits on $ g_{a\gamma\gamma} $	19
V. Analysis of the Synthetic Axion Data	19
VI. Systematic Uncertainties	21
VII. Results	25
VIII. Conclusion	28

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\* A footnote to the article title

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31	Acknowledgments	30
32	A. The Derivation of the Noise Spectrum from the Cavity	30
33	References	31

## 34 I. INTRODUCTION

35 The axion is a hypothetical particle predicted as a consequence of a solution to the strong  
36 CP problem [1–3], i.e. why the CP symmetry is conserved in the strong interactions when  
37 there is an explicit CP-violating term in the QCD Lagrangian. In other words, why is  
38 the electric dipole moment of the neutron so tiny:  $|d_n| < 1.8 \times 10^{-26} e \cdot \text{cm}$  [4, 5]? The  
39 solution proposed by Peccei and Quinn is to introduce a new global Peccei-Quinn  $U(1)_{\text{PQ}}$   
40 symmetry that is spontaneously broken; the axion is the pseudo Nambu-Goldstone boson of  
41  $U(1)_{\text{PQ}}$  [1]. Axions are abundantly produced during the QCD phase transition in the early  
42 universe and may constitute the dark matter (DM). In the post-inflationary PQ symmetry  
43 breaking scenario, where the PQ symmetry is broken after inflation, current calculations  
44 suggest a mass range of 1–100  $\mu\text{eV}$  for axions so that the cosmic axion density does not  
45 exceed the observed cold DM density [6–18]. Therefore, axions are compelling because they  
46 may explain at the same time puzzles that are on scales different by more than thirty orders  
47 of magnitude.

48 Axions could be detected and studied via their two-photon interaction, the so-called  
49 “inverse Primakoff effect”. For QCD axions, i.e. the axions proposed to solve the strong CP  
50 problem, the axion-two-photon coupling constant  $g_{a\gamma\gamma}$  is related to the mass of the axion  
51  $m_a$ :

$$52 \quad g_{a\gamma\gamma} = \left( \frac{g_\gamma \alpha}{\pi \Lambda^2} \right) m_a, \quad (1)$$

53 where  $g_\gamma$  is a dimensionless model-dependent parameter,  $\alpha$  is the fine-structure constant,  
54  $\Lambda = 78 \text{ MeV}$  is a scale parameter that can be derived from the mass and the decay constant  
55 of the pion, and the ratio of the up to down quark masses. The numerical values of  $g_\gamma$   
56 are -0.97 and 0.36 in the Kim-Shifman-Vainshtein-Zakharov (KSVZ) [19, 20] and the Dine-  
57 Fischler-Srednicki-Zhitnitsky (DFSZ) [21, 22] benchmark models, respectively.

58 The detectors with the best sensitivities to axions with a mass of  $\approx \mu\text{eV}$ , as first put for-  
59 ward by Sikivie [23, 24], are haloscopes consisting of a microwave cavity immersed in a strong

static magnetic field and operated at a cryogenic temperature. In the presence of an external magnetic field, the ambient oscillating axion field drives the cavity and they resonate when the frequencies of the electromagnetic modes in the cavity match the microwave frequency  $f$ , where  $f$  is set by the total energy of the axion:  $hf = E_a = m_a c^2 + \frac{1}{2}m_a v^2$ ; the signal power is further delivered to the readout probe followed by a low-noise linear amplifier. The axion mass is unknown, therefore, the cavity resonator must allow the possibility to be tuned through a range of possible axion masses. The Axion Dark Matter eXperiment (ADMX), one of the flagship dark matter search experiments, had developed and improved the cavity design and readout electronics over the years. The results from the previous versions of ADMX and the Generation 2 ADMX (ADMX G2) excluded the KSVZ benchmark model within the mass range of  $1.9\text{--}4.2\text{ }\mu\text{eV}$  and the DFSZ benchmark model for the mass ranges of  $2.66\text{--}3.31$  and  $3.9\text{--}4.1\text{ }\mu\text{eV}$ , respectively [25–31]. One of the major goals of ADMX G2 is to search for higher-mass axions in the range of  $4\text{--}40\text{ }\mu\text{eV}$  ( $1\text{--}10\text{ GHz}$ ), similarly for the axion experiments that were established during the last ten years. The Haloscope at Yale Sensitive to Axion Cold dark matter (HAYSTAC) had performed searches first for the mass range of  $23.15\text{--}24\text{ }\mu\text{eV}$  and later at around  $17\text{ }\mu\text{eV}$ ; they excluded axions with  $|g_\gamma| \geq 1.38 |g_\gamma|^{\text{KSVZ}}$  for  $m_a = 16.96 - 17.12$  and  $17.14\text{--}17.28\text{ }\mu\text{eV}$ , respectively [32]. The Center for Axion and Precision Physics Research (CAPP) constructed and ran simultaneously several experiments targeting at different frequencies; they have pushed the limits towards the KSVZ value within a narrow mass region of  $10.7126\text{--}10.7186\text{ }\mu\text{eV}$  [33]. The QUest for AXions- $a\gamma$  (QUAX- $a\gamma$ ) also pushed their limits close to the upper bound of the QCD axion-two-photon couplings for  $m_a \approx 43\text{ }\mu\text{eV}$  [34].

This paper presents the first results and the analysis details of a search for axions for the mass range of  $19.47\text{--}19.84\text{ }\mu\text{eV}$ , from the Taiwan Axion Search Experiment with Haloscope (TASEH). The expected axion signal power and signal line shape, the noise power, and the signal-to-noise ratio are described in Secs. I A–I B. An overview of the TASEH experimental setup is presented in Sec. II. Section III gives a brief description of the calibration for the whole amplification chain while Sec. IV details the analysis procedure. Section V presents the analysis of the synthetic axion data and Sec. VI discusses the systematic uncertainties that may affect the limits on the  $|g_{a\gamma\gamma}|$ . The final results and the conclusion are presented in Sec. VII and Sec. VIII, respectively.

## A. The expected axion signal power and signal line shape

The signal power extracted from a microwave cavity on resonance is given by:

$$P_s = \left( g_\gamma^2 \frac{\alpha^2 \hbar^3 c^3 \rho_a}{\pi^2 \Lambda^4} \right) \times \left( \omega_c \frac{1}{\mu_0} B_0^2 V C_{mnl} Q_L \frac{\beta}{1 + \beta} \right), \quad (2)$$

where  $\rho_a = 0.45 \text{ GeV/cm}^3$  is the local dark-matter density. The second set of parentheses contains parameters related to the experimental setup: the angular resonant frequency of the cavity  $\omega_c$ , the vacuum permeability  $\mu_0$ , the nominal strength of the external magnetic field  $B_0$ , the volume of the cavity  $V$ , and the loaded quality factor of the cavity  $Q_L = Q_0/(1 + \beta)$ , where  $Q_0$  is the unloaded, intrinsic quality factor of the cavity and  $\beta$  is the coupling coefficient which determines the amount of coupling of the signal to the receiver. The form factor  $C_{mnl}$  is the normalized overlap of the electric field  $\vec{E}$ , for a particular cavity resonant mode, with the external magnetic field  $\vec{B}$ :

$$C_{mnl} = \frac{\left[ \int (\vec{B} \cdot \vec{E}_{mnl}) d^3 \mathbf{x} \right]^2}{B_0^2 V \int E_{mnl}^2 d^3 \mathbf{x}}. \quad (3)$$

Here, the magnetic field  $\vec{B}$  points mostly along the axial direction ( $z$ -axis) of the cavity. The field strength has a small variation along the radial and axial directions and  $B_0$  is the nominal magnetic field strength. For cylindrical cavities, the largest form factor is from the  $\text{TM}_{010}$  mode. The expected signal power derived from the experimental parameters of TASEH (see Table I) is  $P_s \simeq 1.5 \times 10^{-24} \text{ W}$  for a KSVZ axion with a mass of  $19.5 \mu\text{eV}$ .

In the direct dark matter search experiments, several assumptions are made in order to derive a signal line shape. The density and the velocity distributions of DM are related to each other through the gravitational potential. The DM in the galactic halo is assumed to be virialized. The DM halo density distribution is assumed to be spherically symmetric and close to be isothermal, which results in a velocity distribution similar to the Maxwell-Boltzmann distribution. The distribution of the measured signal frequency can be further derived from the velocity distribution after a change of variables and set  $\hbar f_a = m_a c^2$ . Previous experimental results typically adopt the following function for frequency  $f \geq f_a$ :

$$\mathcal{F}(f) = \frac{2}{\sqrt{\pi}} \sqrt{f - f_a} \left( \frac{3}{\alpha} \right)^{3/2} e^{\frac{-3(f-f_a)}{\alpha}}, \quad (4)$$

where  $\alpha \equiv f_a \langle v^2 \rangle / c^2$ . For a Maxwell-Boltzmann velocity distribution, the variance  $\langle v^2 \rangle$  and the most probable velocity (speed)  $v_p$  are related to each other:  $\langle v^2 \rangle = 3v_p^2/2 = (270 \text{ km/s})^2$ ,

119 where  $v_p = 220$  km/s is the local circular velocity of DM in the galactic rest frame. Equa-  
 120 tion (4) is modified if one considers that the relative velocity of the DM halo with respect  
 121 to the Earth is not the same as the DM velocity in the galactic rest frame [35]. The ve-  
 122 locity distributions shall also be truncated so that the DM velocity is not larger than the  
 123 escape velocity of the Milky Way [36]. Several N-body simulations [37, 38] follow structure  
 124 formation from the initial DM density perturbations to the largest halo today and take into  
 125 account the merger history of the Milky Way, rather than assuming that the Milky Way is  
 126 in a steady state; the simulated results suggest velocity distributions with more high-speed  
 127 particles relative to the Maxwellian case [39, 40]. However, these numerical simulations con-  
 128 tain only DM particles; an inclusion of baryons may enhance the halo's central density due  
 129 to a condensation of gas towards the center of the halo via an adiabatic contraction [41, 42],  
 130 or may reduce the density due to the supernova outflows, etc [43, 44].

131 In order to compare the results of TASEH with those of the former experiments, the  
 132 analysis presented in this paper assumes an axion signal line shape by including Eq. (4) in  
 133 the weights when merging the measured power from multiple frequency bins (see Sec. IV D).  
 134 Still given the caveats above and a lack of strong evidence for any particular choice of the  
 135 velocity distribution, the results without an assumption of signal line shape and the results  
 136 with a simple Gaussian weight are also presented for comparison. In addition, a signal  
 137 line width  $\Delta f_a = m_a \langle v^2 \rangle / h \simeq 5$  kHz, which is much smaller than the TASEH cavity line  
 138 width  $f_a / Q_L \simeq 250$  kHz, is assumed and five frequency bins are merged to perform the final  
 139 analysis. For a signal line shape as described in Eq. (4), a 5-kHz bandwidth includes about  
 140 95% of the distribution.

## 141 **B. The expected noise and the signal-to-noise ratio**

142 Several physics processes can contribute to the total noise and all of them can be seen as  
 143 Johnson thermal noise at some effective temperature, or the so-called system noise temper-  
 144 ature  $T_{\text{sys}}$ . The total noise power in a bandwidth  $b$  is then:

$$145 \quad P_n = k_B T_{\text{sys}} b, \tag{5}$$

where  $k_B$  is the Boltzmann constant. The system noise temperature  $T_{\text{sys}}$  has three major components:

$$T_{\text{sys}} = T_{\text{b}} + T_{\text{qn}} + T_{\text{a}}, \quad (6)$$

where

$$T_{\text{qn}} = \frac{1}{2} hf/k_B. \quad (7)$$

The three terms in Eq. (6) correspond to the effective temperatures of the following noise sources: (i)  $T_{\text{b}}$ , the blackbody radiation from the cavity at a physical temperature  $T_{\text{c}}$ , (ii)  $T_{\text{qn}}$ , the quantum noise associated with the zero-point fluctuation of the vacuum, and (iii)  $T_{\text{a}}$ , the noise added by the receiver (mainly from the first-stage amplifier). Equation (6) implies that the noise spectrum has little dependence on the frequency (white spectrum) for the narrow bandwidth considered in the experiment. However, apart from the flat baseline as described by Eq. (6), the noise spectrum observed by TASEH has an additional component with a Lorentzian shape due to the higher temperature at the cavity with respect to the temperature in the dilution refrigerator. More details may be found in Sec. II and Appendix A. The Lorentzian component will be removed from the measured spectrum and only the baseline  $T_{\text{sys}}$  will be used in the final analysis (Sec. IV).

Using the operation parameters of TASEH in Table I and the results from the calibration of readout electronics, the values of  $T_{\text{b}}$ ,  $T_{\text{qn}}$ , and  $T_{\text{a}}$  are estimated to be about 0.07 K, 0.12 K, and 1.9 – 2.2 K, respectively. Therefore, the baseline value of  $T_{\text{sys}}$  for TASEH is about 2.1–2.4 K, which gives a noise power of approximately  $(1.5 - 1.7) \times 10^{-19}$  W within the 5-kHz axion signal line-width, five orders of magnitude larger than the signal. Nevertheless, what matters in the analysis is the signal significance, or the so-called signal-to-noise ratio (SNR) using the standard terminology of axion experiments, i.e. the ratio of the signal power to the fluctuation in the averaged noise power spectrum  $\sigma_n$ .

According to Dicke’s Radiometer Equation [45], the  $\sigma_n$  is given by:

$$\begin{aligned} \sigma_n &= \frac{P_n}{\sqrt{N_{\text{avg}}}}, \\ &= \frac{P_n}{\sqrt{t\Delta f}}, \\ &= k_B T_{\text{sys}} \sqrt{\frac{\Delta f}{t}} \end{aligned} \quad (8)$$

where  $N_{\text{avg}}$  is the number of noise power spectra used in the average; it is related to the amount of data integration time  $t$  and the bandwidth over which a single measurement is

made  $\Delta f$ . The SNR will therefore be:

$$\begin{aligned} \text{SNR} &= \frac{P_s}{\sigma_n}, \\ &= \frac{P_s}{k_B T_{\text{sys}}} \sqrt{\frac{t}{\Delta f}}, \end{aligned} \quad (9)$$

Combining Eq. (2) and Eq. (9), one could see that the SNR is maximized by an experimental setup with a strong magnetic field, a large cavity volume, an efficient cavity resonant mode, a receiver with low system noise temperature, and a long integration time.

## II. EXPERIMENTAL SETUP

The detector of TASEH is located at the Department of Physics, National Central University, Taiwan and housed within a cryogen-free dilution refrigerator (DR) from BlueFors. An 8-Tesla superconducting solenoid with a bore diameter of 76 mm and a length of 240 mm is integrated with the DR.

The data for the analysis presented in this paper were collected by TASEH from October 13, 2021 to November 15, 2021, and termed as the CD102 data, where CD stands for “cool down”. During the data taking, the cavity sat in the center of the magnet bore and was connected via holders to the mixing flange of the DR at a temperature of  $T_{\text{mx}} \approx 27$  mK. The temperature of the cavity stayed at  $T_c \simeq 155$  mK, higher with respect to the DR; it is believed that the cavity had an accidental thermal contact with the radiation shield in the DR. The cavity, made of oxygen-free high-conductivity (OFHC) copper, has an effective volume of 0.234 L and is a two-cell cylinder split along the axial direction ( $z$ -axis). The cylindrical cavity has an inner radius of 2.5 cm and a height of 12 cm. In order to maintain a smooth surface, the cavity underwent the processes of annealing, polishing, and chemical cleaning. The resonant frequency of the  $\text{TM}_{010}$  mode can be tuned over the range of 4.667–4.959 GHz via the rotation of an off-axis OFHC copper tuning rod, from the position closer to the cavity wall to the position closer to the cavity center (i.e. when the vector from the rotation axis to the tuning rod is at an angle of  $0^\circ$  to  $180^\circ$ , with respect to the vector from the cavity center to the rotation axis). The CD102 data cover the frequency range of 4.707506–4.798145 GHz. There were 839 resonant-frequency steps in total, with a frequency difference of  $\Delta f_s = 95 - 115$  kHz between the steps. The value of  $\Delta f_s$  was kept within 10% of 105 kHz rather than a fixed value, such that the rotation angle of the tuning rod



205 did not need to be fine-tuned and the operation time could be minimized; a 10% variation  
 206 of the  $\Delta f_s$  is found to have no impact on the  $|g_{a\gamma\gamma}|$  limits. Each resonant-frequency step is  
 207 denoted as a “scan” and the data integration time was about 32-42 minutes. The integration  
 208 time was determined based on the target  $|g_{a\gamma\gamma}|$  limits and the experimental parameters in  
 209 Table I; the variation of the integration time aimed to remove the frequency-dependence in  
 210 the  $|g_{a\gamma\gamma}|$  limits caused by frequency dependence of the added noise  $T_a$ . The form factor  $C_{010}$   
 211 as defined in Eq. (3) varies from 0.64 to 0.69 over the full frequency range. The intrinsic,  
 212 unloaded quality factor  $Q_0$  at the cryogenic temperature ( $T_c \simeq 155$  mK) is  $\simeq 60000$  at the  
 213 frequency of 4.74 GHz.

214 An output probe, made of a 50- $\Omega$  semi-rigid coaxial cable that was soldered to an SMA  
 215 (SubMiniature version A) connector, was inserted into the cavity and its depth was set for  
 216  $\beta \simeq 2$ . The signal from the output probe was directed to an impedance-matched ampli-  
 217 fication chain. The first-stage amplifier was a low noise high-electron-mobility transistor  
 218 (HEMT) amplifier with an effective noise temperature of  $\approx 2$  K, mounted on the 4K flange.  
 219 The signal was further amplified at room temperature via a three-stage post-amplifier, and  
 220 down-converted and demodulated to in-phase (I) and quadrature (Q) components and dig-  
 221 itized by an analog-to-digital converter with a sampling rate of 2 MHz.

222 A more detailed description of the TASEH detector, the operation of the data run, and  
 223 the calibration of the gain and added noise temperature of the whole amplification chain  
 224 can be found in Ref. [46]. See Table I for the benchmark experimental parameters that can  
 225 be used to estimate the sensitivity of TASEH.

### 226 **III. CALIBRATION**

227 The noise is one of the most important parameters for the axion searches. Therefore,  
 228 calibration for the amplification chain is a crucial part in the operation of TASEH. In  
 229 order to perform a calibration, the HEMT was connected to a heat source (a 50- $\Omega$  resistor)  
 230 instead of the cavity; various values of input currents were sent to the source to change  
 231 its temperature monitored by a thermometer. The power from the source was delivered  
 232 following the same transmission line as that in the axion data running. The output power  
 233 is fitted to a first-order polynomial, as a function of the source temperature, to extract the  
 234 gain and added noise for the amplification chain. More details of the procedure can be found

TABLE I. The benchmark experimental parameters for estimating the sensitivity of TASEH. The definitions of the parameters can be found in Sec. I. More details regarding the determination and the measurements of some of the parameters may be found in Ref. [46].

$f_{\text{lo}}$	4.707506 GHz
$f_{\text{hi}}$	4.798145 GHz
$N_{\text{step}}$	839
$\Delta f_{\text{s}}$	95 – 115 kHz
$B_0$	8 Tesla
$V$	0.234 L
$C_{010}$	0.64 – 0.69
$Q_0$	59000 – 65000
$\beta$	1.9 – 2.3
$T_{\text{mx}}$	27–28 mK
$T_{\text{c}}$	155 mK
$T_{\text{a}}$	1.9 – 2.2 K
$\Delta f_a$	5 kHz

in Ref. [46].

The calibration was carried out before, during, and after the data taking, which showed that the performance of the system was stable over time. The average of the added noise  $T_{\text{a}}$  over 19 measurements has the lowest value of 1.9 K at the frequency of 4.8 GHz and the highest value of 2.2 K at 4.72 GHz, as presented in Fig. 1. The error bars are the RMS of  $T_{\text{a}}$  and the largest RMS is used to calculate the systematic uncertainty for the limits on  $|g_{a\gamma\gamma}|$ . The light blue points in Fig. 1 are the noise from the axion data estimated by removing the gain and subtracting the contribution from the cavity noise, assuming that the presence of a narrow signal in the data would have no effect on the estimation. A good agreement between the results from the calibration and the ones estimated from the axion data is shown. The biggest difference is 0.076 K in the frequency range during which the data were recorded after an earthquake. The source of the difference is not understood, therefore, the difference

is quoted as a systematic uncertainty together with the RMS of the noise.

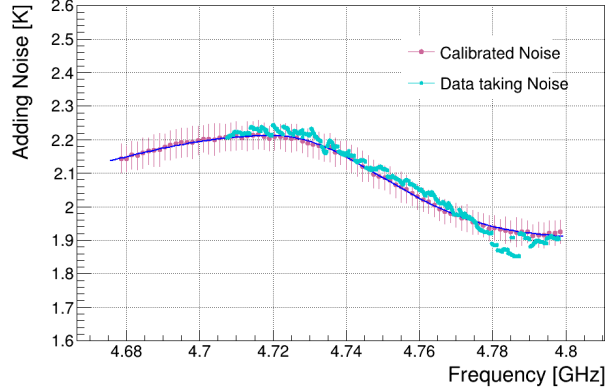


FIG. 1. The average added noise obtained from the calibration (pink points) and the noise estimated from the axion data (light blue points) as a function of frequency. The error bars on the pink points are the RMS of the  $T_a$ , as computed from the 19 measurements for each frequency in the calibration. The blue curve is obtained after performing a fit to the pink points and is used to estimate the  $T_a$  at each resonant frequency of the cavity.

#### IV. ANALYSIS PROCEDURE

The goal of TASEH is to find the axion signal hidden in the noise. In order to achieve this, the analysis procedure includes the following steps:

1. Perform fast Fourier transform (FFT) on the IQ time series data to obtain the frequency-domain power spectrum.
2. Apply the Savitzky-Golay (SG) filter to remove the structure of the background in the frequency-domain power spectrum.
3. Combine all the spectra from different frequency scans with the weighting algorithm.
4. Merge bins in the combined spectrum to maximize the SNR.
5. Rescan the frequency regions with candidates and set limits on the axion-two-photon coupling  $|g_{a\gamma\gamma}|$  if no candidates were found.

The analysis follows the procedure similar to that developed by the HAYSTAC experiment [47]. The important points and formulas for each step are highlighted below as a reminder for the convenience of readers. Note there are a few small differences between the HAYSTAC analysis and the one presented here. In this paper, the uncertainties are considered to be uncorrelated between different frequency bins while Ref. [47] takes into account the correlation. The frequency-domain spectra processed by each intermediate step are shown. The central results of the  $|g_{a\gamma\gamma}|$  limits assume the signal line shape described by Eq. (4) as in Ref. [47], and in addition the limits without an assumption of signal line shape (flat signal distribution) and the limits assuming a simple Gaussian shape are shown for comparison in Sec. VII.

### A. Fast Fourier transform

The in-phase  $I(t)$  and quadrature  $Q(t)$  components of the time-domain data were sampled and saved in the TDMS (Technical Data Management Streaming) files - a binary format developed by National Instruments. The FFT is performed to convert the data into frequency-domain power spectrum in which the measured power is calculated using the following equation:

$$\text{Power} = \frac{|\text{FFT}(I + i \cdot Q)|^2}{N \cdot 2R}, \quad (10)$$

where  $N$  is the number of data points ( $N = 2000$  in the TASEH CD102 data), and  $R$  is the input resistance of the signal analyzer ( $50 \Omega$ ). The FFT is done for every one-millisecond subspectrum data. The integration time for each frequency scan was about 32-42 minutes, which resulted in 1920000 to 2520000 subspectra; an average over these subspectra gives the averaged frequency-domain power spectrum for each scan. The frequency span in the spectrum from each resonant-frequency scan is 1.6 MHz while the resolution is 1 kHz, giving 1600 frequency bins in each spectrum.

### B. Remove the structure of the background

In the absence of the axion signal, the output data spectrum is simply the noise from the cavity and the amplification chain. If axions are present in the cavity, the signal will be

buried in the noise because the signal power is very weak. Therefore, the structure of the raw averaged output power spectrum, as shown in the upper panel of Fig. 2, is dominated by the noise of the system and an explanation for the structure can be found in Appendix A. The SG filter [48], a digital filter that can smooth data without distorting the signal tendency, is applied to remove the structure of the background. The SG filter is performed on the averaged spectrum of each frequency scan by fitting adjacent points of successive sub-sets of data with an  $n^{\text{th}}$ -order polynomial. The result depends on two parameters: the number of data points used for fitting, the so-called window width, and the order of the polynomial. If the window is too wide, the filter will not remove small structures, and if it is too narrow, it may kill the signal. The window and the order were first chosen during the data taking, by requiring the ratio of the raw data to the filter output consistent with unity. After the data taking, they were optimized by injecting an axion signal on top of the noise data and found that they were consistent with the original choice (see Sec. VI).

The raw averaged power spectrum is divided by the output of the SG filter, then unity is subtracted from the ratio to get the dimensionless normalized spectrum (lower panel of Fig. 2). The value in each bin of the normalized spectrum is the deviation of the averaged measured power from the SG-filter output (can be considered as the averaged noise power) relative to the SG output. The symbol  $\delta$  and term “RDP” are used to denote the relative deviation of power in the normalized spectrum and also in the spectra processed with rescaling, combining, and merging afterwards; the value can be zero, positive, or negative. In the absence of the axion signal, the RDPs in the normalized spectrum are samples drawn from a Gaussian distribution with a zero mean and a standard deviation of  $1/\sqrt{N_{\text{spectra}}}$ , where  $N_{\text{spectra}}$  is the number of subspectra used to compute the average (Sec. IV A). If the axion signal exists, there will be a significant excess above zero.

During the data taking, the resonant frequency of the cavity was adjusted by the tuning bar so to scan a large range of frequencies and to reduce the uncertainty of the averaged noise power at the overlapped region. Therefore, the spectra of all the scans need to be combined to create one big spectrum. Before doing this, the normalized spectrum from each scan is rescaled and the rescaled spectrum, shown in Fig. 3, is computed with the following formula:

$$\delta_{ij}^{\text{res}} = R_{ij} \delta_{ij}^{\text{norm}}, \quad (11)$$

and the standard deviation of each bin is:

$$\sigma_{ij}^{\text{res}} = R_{ij} \sigma_i^{\text{norm}}, \quad (12)$$

where

$$R_{ij} = \frac{k_B T_{\text{sys}} \Delta f_{\text{bin}}}{P_{ij}^{\text{KSVZ}} h_{ij}}, \quad (13)$$

and

$$h_{ij} = \frac{1}{1 + 4Q_{Li}^2 (f_{ij}/f_{ci} - 1)^2}. \quad (14)$$

The  $\delta_{ij}^{\text{norm}}$  ( $\delta_{ij}^{\text{res}}$ ) and  $\sigma_i^{\text{norm}}$  ( $\sigma_{ij}^{\text{res}}$ ) are the RDP and the standard deviation of the  $j^{\text{th}}$  frequency bin in the normalized (rescaled) spectrum from the  $i^{\text{th}}$  resonant-frequency scan. The value of  $\sigma_i^{\text{norm}}$  is derived from the spread of the RDPs over the 1600 frequency bins for the  $i^{\text{th}}$  scan. The factor  $R_{ij}$  is the ratio of the system noise power to the expected signal power of the KSVZ axion  $P_{ij}^{\text{KSVZ}}$ , with the Lorentzian cavity response  $h_{ij}$  taken into account. The system-noise temperature  $T_{\text{sys}}$  is calculated following Eq. (6), where the frequency dependence of the added-noise temperature  $T_a$  is obtained from the fitting function in Fig. 1. The  $\Delta f_{\text{bin}}$  is the bin width of spectrum (1 kHz). The factor  $h_{ij}$  describes the Lorentzian response of the cavity, which depends on the loaded quality factor  $Q_{Li}$  and the difference between the frequency  $f_{ij}$  in bin  $j$  and the resonant frequency  $f_{ci}$ . If a signal appears in a certain frequency bin  $j$ , its expected power will vary depending on the bin position due to the cavity's Lorentzian response. The rescaling will take into account this effect. The procedure of the normalization and the rescaling also ensures that a KSVZ axion signal will have a rescaled RDP  $\delta_{ij}^{\text{res}}$  that is approximately equal to unity.

### C. Combine the spectra with the weighting algorithm

The purpose of the weighting algorithm is to add the spectra from different resonant-frequency scans, particularly for the frequency bins that appear in multiple spectra. Each spectrum was collected with a different cavity resonant frequency. Therefore, if a signal appears in a certain frequency bin  $j$ , due to the difference in the resonant frequency and the Lorentzian response, the expected signal power will be different in each spectrum  $i$ . The weighting algorithm is expected to take this into account with a weight calculated for each

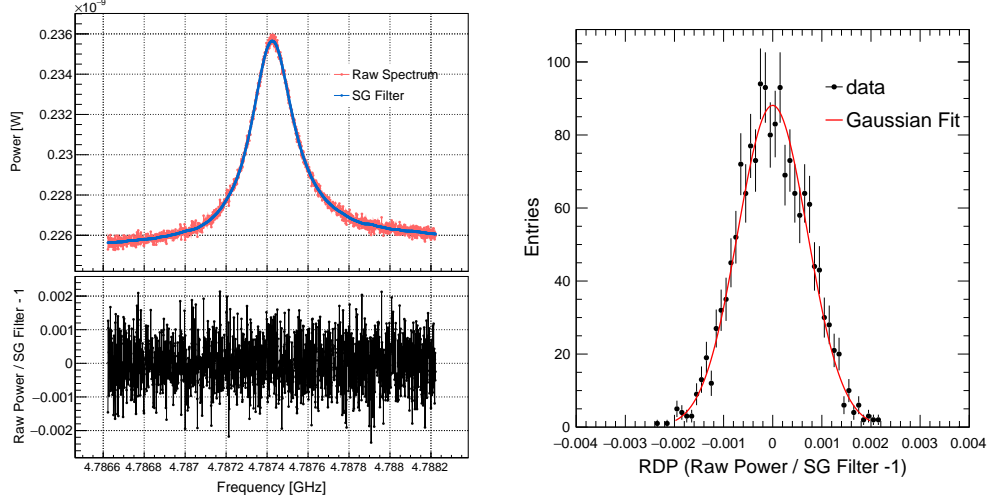


FIG. 2. Upper left panel: The raw averaged power spectrum (red points) and the output of the SG filter (blue curve) of one scan. Lower left panel: The normalized spectrum, derived by taking the ratio of the raw spectrum to the SG filter and subtracting unity from the ratio. Right plot: Histogram of the normalized spectrum with Gaussian fit.

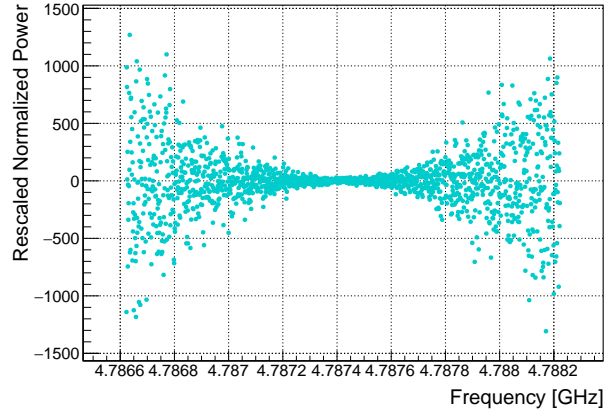


FIG. 3. The rescaled spectrum, obtained by multiplying the RDPs in the normalized spectrum with the ratio of the system noise power to the expected signal power of the KSVZ axion, with the Lorentzian response of the cavity taken into account.

350 bin  $j$  of the rescaled spectrum  $i$ , as defined below:

$$351 \quad w_{ijn} = \frac{\Gamma_{ijn}}{(\sigma_{ij}^{\text{res}})^2}. \quad (15)$$

352 Note, the symbol  $\Gamma_{ijn} = 1$  if the  $j^{\text{th}}$  frequency bin in the  $i^{\text{th}}$  rescaled spectrum correspond  
 353 to the same frequency in the  $n^{\text{th}}$  bin of the combined spectrum; otherwise,  $\Gamma_{ijn} = 0$ .

The RDP  $\delta_n^{\text{com}}$  and the standard deviation  $\sigma_n^{\text{com}}$  of the  $n^{\text{th}}$  bin in the combined spectrum are calculated using Eq. (16) and Eq. (17), respectively. The  $\text{SNR}_n^{\text{com}}$  is the ratio of  $\delta_n^{\text{com}}$  to  $\sigma_n^{\text{com}}$  as given in Eq. (18). Figure 4 and Fig. 5 show the RDP, the standard deviation, and the SNR of the combined spectrum, respectively.

$$\delta_n^{\text{com}} = \frac{\sum_i \sum_j (\delta_{ij}^{\text{res}} \cdot w_{ijn})}{\sum_i \sum_j w_{ijn}}, \quad (16)$$

$$\sigma_n^{\text{com}} = \frac{\sqrt{\sum_i \sum_j (\sigma_{ij}^{\text{res}} \cdot w_{ijn})^2}}{\sum_i \sum_j w_{ijn}}, \quad (17)$$

$$\text{SNR}_n^{\text{com}} = \frac{\delta_n^{\text{com}}}{\sigma_n^{\text{com}}} = \frac{\sum_i \sum_j (\delta_{ij}^{\text{res}} \cdot w_{ijn})}{\sqrt{\sum_i \sum_j (\sigma_{ij}^{\text{res}} \cdot w_{ijn})^2}}. \quad (18)$$

For each bin  $n$  in the combined spectrum, there are  $m_n$  non-vanishing contributions to the sums above. The value of  $m_n$  ranges from 2 to 26; in general the leftmost bin or the bin with the smallest frequency (the rightmost bin or the bin with the highest frequency) in each scan has the minimum (maximum) number of  $m_n$ .

#### D. Merge bins

The expected axion bandwidth is about 5 kHz at the frequency of  $\approx 5$  GHz. In this paper, the interested frequency range is 4.707506–4.798145 GHz and the bin width is 1 kHz. Therefore, in order to maximize the SNR, a running window of five consecutive bins in the combined spectrum is applied and the five bins within each window are merged to construct a final spectrum. The purpose of using a running window is to avoid the signal power broken into different neighboring bins of the merged spectrum. Due to the nonuniform distribution of the axion signal [Eq. (4)], the contributing bins need to be rescaled to have the same RDP, of which the standard deviation is used to define the maximum likelihood (ML) weight for merging. The rescaling is performed by dividing the  $\delta_{g+k-1}^{\text{com}}$  and  $\sigma_{g+k-1}^{\text{com}}$  in the combined



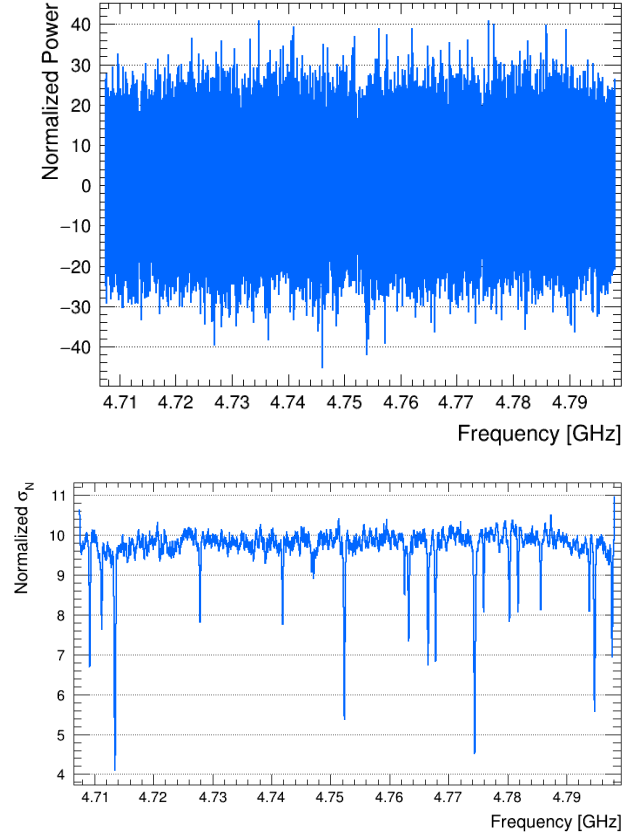


FIG. 4. The combined RDP  $\delta$  following Eq. (16) (upper) and the standard deviation  $\sigma$  derived from Eq. (17) (lower).

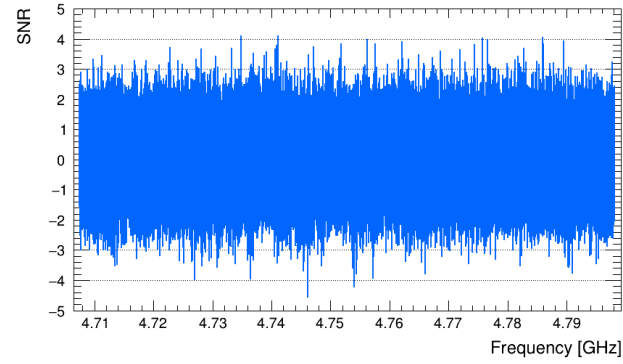


FIG. 5. The signal-to-noise ratio (SNR) calculated using Eq.(18) of the combined spectrum.

spectrum by an integral of the signal line shape  $L_k$  [Eq. (20)]:

$$\begin{aligned}\delta_{g+k-1}^{\text{rs}} &= \frac{\delta_{g+k-1}^{\text{com}}}{L_k}, \\ \sigma_{g+k-1}^{\text{rs}} &= \frac{\sigma_{g+k-1}^{\text{com}}}{L_k}.\end{aligned}\tag{19}$$

Here, the  $\delta_{g+k-1}^{\text{rs}}$  and  $\sigma_{g+k-1}^{\text{rs}}$  are the rescaled RDP and standard deviation that will be used later for merging. The variable  $g = 1, \dots, N - M + 1$  is the index for the frequency bins in the final spectrum and  $k = 1, \dots, M$ , in which  $M = 5$  is the number of merged bin in this analysis. The numbers  $N$  and  $N - M + 1$  are the total numbers of bins in the combined and final spectrum, respectively. The integral  $L_k$  is defined as:

$$L_k = \int_{f_a + \delta f_m + (k-1)\Delta f_{\text{bin}}}^{f_a + \delta f_m + k\Delta f_{\text{bin}}} \mathcal{F}(f) df,\tag{20}$$

where the frequency  $f_a = m_a c^2 / h$  is the axion frequency,  $\delta f_m$  is the misalignment between  $f_a$  and the lower boundary of the  $g^{\text{th}}$  bin in the combined spectrum. The function  $\mathcal{F}(f)$  has been defined in Eq. (4). The misalignment effect as mentioned in the HAYSTAC paper [47] has been studied and the results of the  $|g_{a\gamma\gamma}|$  limits are found to be insensitive to this effect.

The ML weight is defined as:

$$w_{gk} = \frac{1}{(\sigma_{g+k-1}^{\text{rs}})^2} = \frac{L_k^2}{(\sigma_{g+k-1}^{\text{com}})^2},\tag{21}$$

The RDP, the standard deviation, and the SNR of the merged spectrum are:

$$\delta_g^{\text{merged}} = \frac{\sum_{k=1}^M (\delta_{g+k-1}^{\text{rs}} \cdot w_{gk})}{\sum_{k=1}^M w_{gk}} = \frac{\sum_{k=1}^M \frac{\delta_{g+k-1}^{\text{com}}}{L_k} \cdot \left(\frac{L_k}{\sigma_{g+k-1}^{\text{com}}}\right)^2}{\sum_{k=1}^M \left(\frac{L_k}{\sigma_{g+k-1}^{\text{com}}}\right)^2},\tag{22}$$

$$\begin{aligned}\sigma_g^{\text{merged}} &= \frac{\sqrt{\sum_{k=1}^M (\sigma_{g+k-1}^{\text{rs}} \cdot w_{gk})^2}}{\sum_{k=1}^M w_{gk}} = \frac{\sqrt{\sum_{k=1}^M \left(\frac{L_k}{\sigma_{g+k-1}^{\text{com}}}\right)^2}}{\sum_{k=1}^M \left(\frac{L_k}{\sigma_{g+k-1}^{\text{com}}}\right)^2} \\ &= \frac{1}{\sqrt{\sum_{k=1}^M \left(\frac{L_k}{\sigma_{g+k-1}^{\text{com}}}\right)^2}}\end{aligned}\tag{23}$$

$$\text{SNR}_g^{\text{merged}} = \frac{\delta_g^{\text{merged}}}{\sigma_g^{\text{merged}}} = \frac{\sum_{k=1}^M \frac{\delta_{g+k-1}^{\text{com}}}{L_k} \cdot \left(\frac{L_k}{\sigma_{g+k-1}^{\text{com}}}\right)^2}{\sqrt{\sum_{k=1}^M \left(\frac{L_k}{\sigma_{g+k-1}^{\text{com}}}\right)^2}}\tag{24}$$

### 396 E. Rescan and set limits on $|g_{a\gamma\gamma}|$

397 Before the collection of the CD102 data, a  $5\sigma$  SNR target was chosen, which corresponds  
 398 to a candidate threshold of  $3.355\sigma$  at 95% confidence. After the merging as described in  
 399 Sec. IV D, if there were any potential signal with an SNR larger than 3.355, a rescan would  
 400 be proceeded to check if it were a real signal or a statistical fluctuation. The procedure of  
 401 the CD102 data taking was to perform a rescan after covering every 10 MHz; the rescan  
 402 was done by adjusting the tuning rod of the cavity so to match the resonant frequency to  
 403 the frequency of the candidate. In total, 22 candidates with an SNR greater than 3.355  
 404 were found. Among them, 17 candidates were from the fluctuations because they were gone  
 405 after a few rescans. The remaining five candidates, in the frequency ranges of 4.710170 –  
 406 4.710190 GHz and 4.747301 – 4.747380 GHz, reached an SNR greater than 4 after rescanning.  
 407 The signals in the second frequency range were detected via a portable antenna outside the  
 408 DR and found to come from the instruments in the laboratory, while the signals in the first  
 409 frequency range were weaker but still present after turning off the external magnetic field.  
 410 Therefore, these five candidates are considered external signals and no limits are placed for  
 411 the above two frequency ranges. More details can be found in the TASEH instrumentation  
 412 paper [46]. Figure 6 and Fig. 7 show the RDP, the standard deviation, and the SNR of  
 413 the merged spectrum after including data from both the original scans and the rescans,  
 414 respectively.

415 Since no candidates were found after the rescan, an upper limit on the signal power  $P_s$  is  
 416 derived by setting  $P_s$  equal to  $5\sigma_g^{\text{merged}} \times P_g^{\text{KSVZ}}$ , where the  $\sigma_g^{\text{merged}}$  and  $P_g^{\text{KSVZ}}$  are the standard  
 417 deviation and the expected signal power for the KSVZ axion for a certain frequency bin  $g$  in  
 418 the merged spectrum. Then, the 95% C.L. limits on the dimensionless parameter  $|g_\gamma|$  and  
 419 the axion-two-photon coupling  $|g_{a\gamma\gamma}|$  could be derived according to Eq. (2) and Eq. (1). See  
 420 Sec. VII for the final limits including the systematic uncertainties.

## 421 V. ANALYSIS OF THE SYNTHETIC AXION DATA

422 After TASEH finished collecting the CD102 data on November 15, 2021, the synthetic  
 423 axion signals were injected into the cavity and read out via the same transmission line and  
 424 amplification chain. The procedure to generate axion-like signals is summarized in Ref. [46].

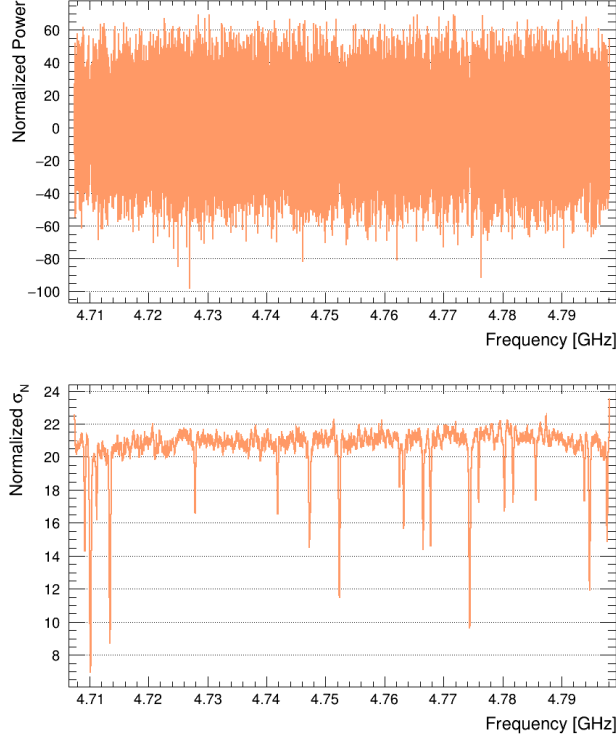


FIG. 6. The merged RDP  $\delta$  following Eq. (22) (upper) and the standard deviation  $\sigma$  derived from Eq. (23) (lower). The results shown are obtained using data from both the original scans and the rescans.

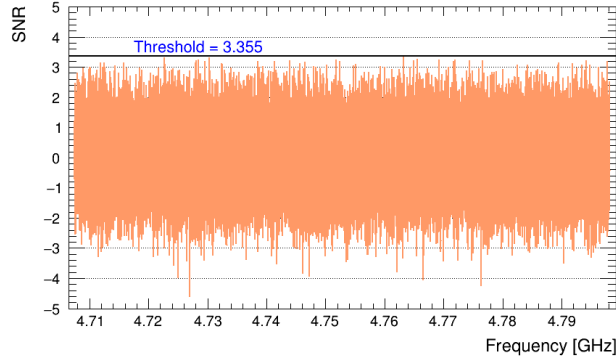


FIG. 7. The signal-to-noise ratio (SNR) calculated using Eq. (24) for the merged spectrum including data from both the original scans and the rescans. No candidate exceeds the threshold of  $3.355\sigma$  (solid-black horizontal line).

Due to the uncertainties on the losses of signal transmission lines, the synthetic axion signals are not used to perform an absolute calibration of the search sensitivity. Instead, a test

with synthetic axion signals could be used to verify the procedures of data acquisition and physics analysis. The SNR of the frequency bin with maximum power from the synthetic axion signals, at 4.708970 GHz, was set to  $\approx 3.35$ .

The same analysis procedure as described in Sec. IV is applied to the data with synthetic axion signals. Figure 8 presents the individual raw power spectra in the 24 frequency scans. Before combining the 24 spectra, the SNR of the maximum-power bin is measured to be 3.577; the SNR is slightly higher than 3.35 due to a 5% difference in the noise fluctuation between the measurements from the calibration and the measurements taken right before injecting axion-like signals. After the combination of the spectra and the merging of five frequency bins, the SNRs increase to 4.74 and 6.12, respectively. In addition to the injected synthetic axion signal, a candidate at 4.708006 GHz is found after merging the spectra. Since it is not possible to perform a rescan, the real axion data from the two scans that had resonant frequencies close to the candidate frequency are added so to mimic the rescan; the candidate is found to be a statistical fluctuation. Figures 9–10 present the RDP spectra with the corresponding SNR, respectively, after combining the spectra that share the same frequency bins and after merging five neighboring bins; the 24 scans of the synthetic axion data and the two scans of the real axion data are included and processed together. The analysis results of the synthetic axion signals prove that an power excess of more than  $5\sigma$  can be found at the expected frequencies via the standard analysis procedure.

## VI. SYSTEMATIC UNCERTAINTIES

The systematic uncertainties on the  $|g_{a\gamma\gamma}|$  limits arise from the following sources:

- Uncertainty on the product  $Q_L\beta/(1+\beta)$  in Eq. (2): In order to extract the loaded quality factor  $Q_L$  and the coupling coefficient  $\beta$ , a fitting of the measured results of the cavity scattering matrix was performed, which results in a relative uncertainty of 0.2% on this product.
- Uncertainty on the noise temperature  $T_a$  from the RMS of the measurements in the calibration:  $\Delta T_a/T_a = 2.3\%$  (see Sec. III and Fig. 1).
- Uncertainty on the noise temperature  $T_a$  from the largest difference between the value determined by the calibration and that from the axion data:  $\Delta T_a/T_a = 4\%$  (see

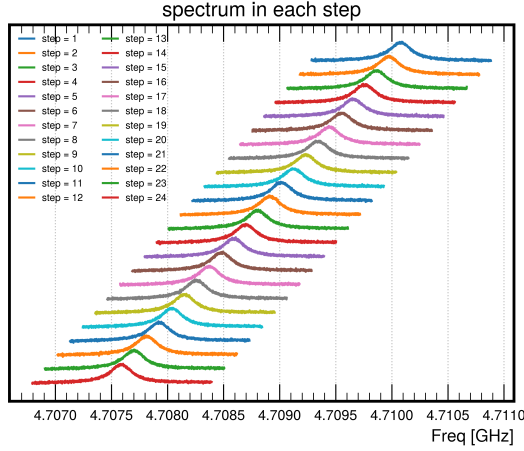


FIG. 8. The raw output power spectra, before applying the SG filter, from the 24 frequency steps of the synthetic axion data. In order to show the spectra clearly, the spectra are shifted with respect to each other with an arbitrary offset in the vertical scale.

Sec. III and Fig. 1).

- Uncertainty from the choice of the SG-filter parameters: i.e. the window width and the order of the polynomial in the SG filter. At the beginning of the data taking, a preliminary optimization was performed: a window width of 201 bins and a 4<sup>th</sup> order polynomial were used for the first analysis of the CD102 data (see Sec. IV). This choice is kept for the central results. Nevertheless, various methods of optimization are also explored. The goal of the optimization is to find a set of SG-filter parameters that only model the noise spectrum and do not remove a real signal. The methods include:
  - Minimize the difference between the two functions returned by the SG filter, when the SG filter is applied to: (i) the real data only, and (ii) the sum of the real data and a simulated axion signal.
  - Minimize the difference between the function returned by the SG filter and the input noise function (including the Lorentzian distribution due to the cavity noise), when the SG filter is applied to a spectrum that includes the simulation of the axion signal and the simulation based on the input noise function. See Fig. 11 for a comparison of the simulated spectrum, input noise function, and the function returned by the SG filter when a 3<sup>rd</sup>-order polynomial and a window

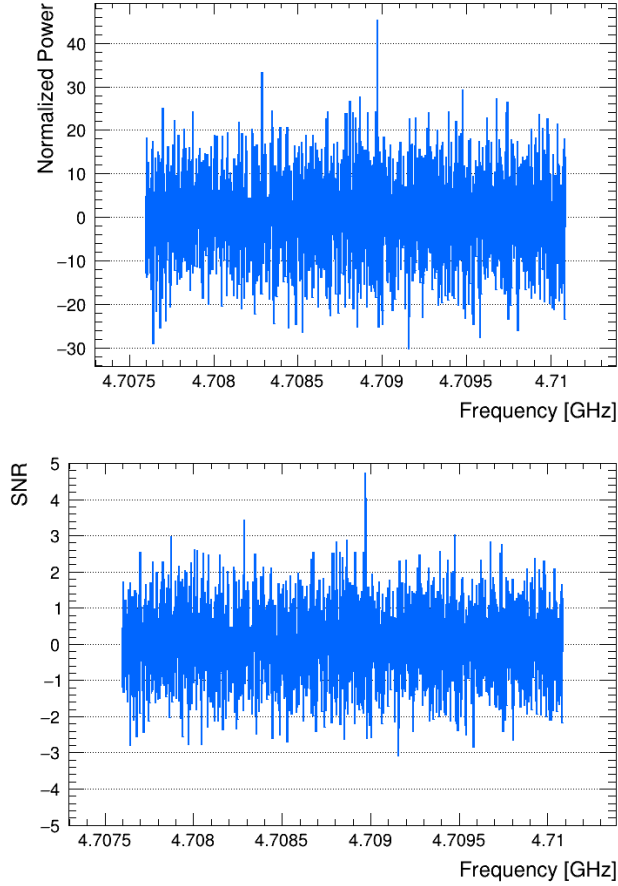


FIG. 9. The RDP (upper) and the signal-to-noise ratio (lower) after combining the spectra of the synthetic axion data with overlapping frequencies from different scans. The procedure and the weights for combination are summarized in Sec. IV C.

of 141 bins are chosen; the differences from all the frequency bins are summed together when performing the optimization. Figure 12 shows the difference as a function of window widths when the order of polynomial is set to three, four, and six.

- Compare the mean  $\mu_{\text{noise}}$  and the width  $\sigma_{\text{noise}}$  of the measured power, assuming that no signal is present in the data. See Fig. 13 for an example distribution of the measured power from the averaged spectrum of a single scan; a Gaussian fit is performed to extract  $\mu_{\text{noise}}$  and  $\sigma_{\text{noise}}$ . Given the nature of the thermal noise, the two variables are supposed to be related to each other if proper window width

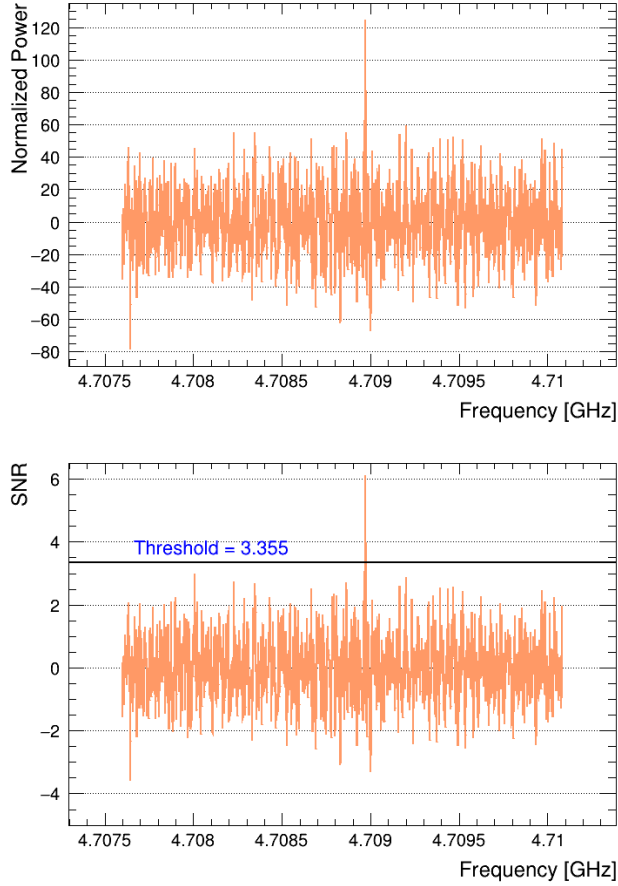


FIG. 10. The RDP (upper) and the signal-to-noise ratio (lower) after merging the RDP measured in five neighboring frequency bins of the synthetic axion data. The procedure and the weights for merging are summarized in Sec. IV D.

and order are chosen:

$$\sigma_{\text{noise}} = \frac{\mu_{\text{noise}}}{\sqrt{N_{\text{spectra}}}},$$

where  $N_{\text{spectra}}$  is the number of spectra for averaging and is related to the amount of integration time for each frequency step. In general,  $N_{\text{spectra}} = 1920000 - 2520000$ .

In addition, one could choose to optimize for each frequency step individually, optimize for a certain frequency step but apply the results to all data, or optimize by adding all the frequency steps together. Figure 14 shows that the deviations from the central results using different optimization approaches are in general within 1% and the maximum deviation of 1.8% on the  $|g_{a\gamma\gamma}|$  limit is used as a conservative estimate



of the systematic uncertainty from the SG filter.

The first source of the systematic uncertainty has negligible effect on the limits of  $|g_{a\gamma\gamma}|$  while the latter three sources are studied and added in quadrature to obtain the total systematic uncertainty. The systematic uncertainties on the  $|g_{a\gamma\gamma}|$  limits are displayed together with the central results in Sec. VII. Overall the total relative systematic uncertainty is  $\approx 3.4\%$ .

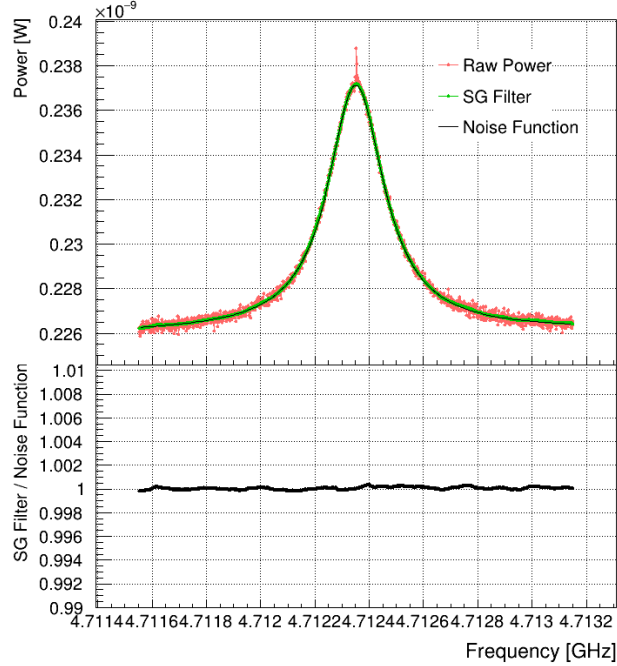


FIG. 11. Upper panel: The simulated spectrum, including the axion signal and the noise, is overlaid with the input noise function and the function returned by the SG filter. Lower panel: The ratio of the function returned by the SG filter to the input noise function.

## VII. RESULTS

Figure 15 shows the limits on the axion-two-photon coupling  $|g_{a\gamma\gamma}|$  and the ratio of the limits on the dimensionless parameter  $|g_\gamma|$  with respect to the KSVZ benchmark value ( $|g_{\text{KSVZ}}| = 0.97$ ). The blue error band indicates the systematic uncertainties as discussed in Sec. VI. No limits are placed for the frequency ranges of 4.710170 – 4.710190 GHz and 4.747301 – 4.747380 GHz, which correspond to the external signals during the collection of the CD102 data. The limits on  $|g_{a\gamma\gamma}|$  range from  $4.4 \times 10^{-14}$  to  $8.3 \times 10^{-14}$ , with an

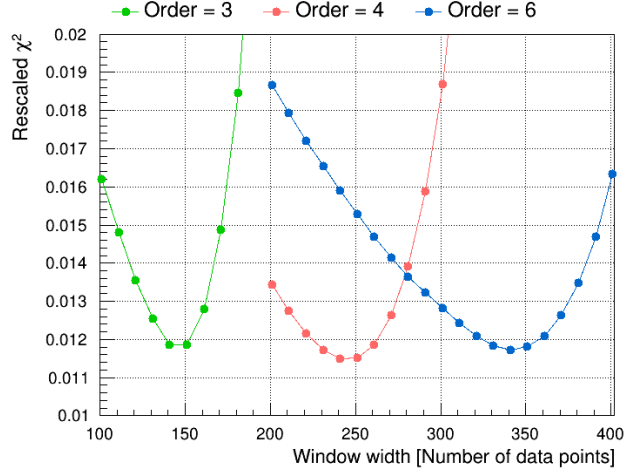


FIG. 12. The difference between the function returned by the SG filter and the input noise function, when various values of window widths and a 3<sup>rd</sup>, a 4<sup>th</sup>, or a 6<sup>th</sup>-order polynomial are applied in the SG filter. In this figure, the best choice is a 4<sup>th</sup>-order polynomial with a window width of 241 data points (bins).

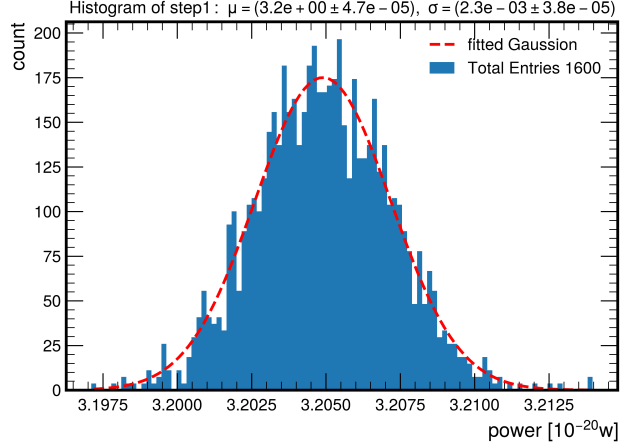


FIG. 13. An example of the distribution of the measured power, after removing the receiver gain and applying the SG filter, when the cavity resonant frequency is 4.798147 GHz. The distribution contains 1600 entries and each entry corresponds to the measured power in one frequency bin, averaged over 1920000 subspectra. The mean and the width returned by a Gaussian fit to the distribution are used to determine the best choice of SG parameters. The mean  $\mu_{\text{noise}} = 3.2 \times 10^{-20}$  W in a 1-kHz frequency bin would imply a noise temperature of 2.3 K.

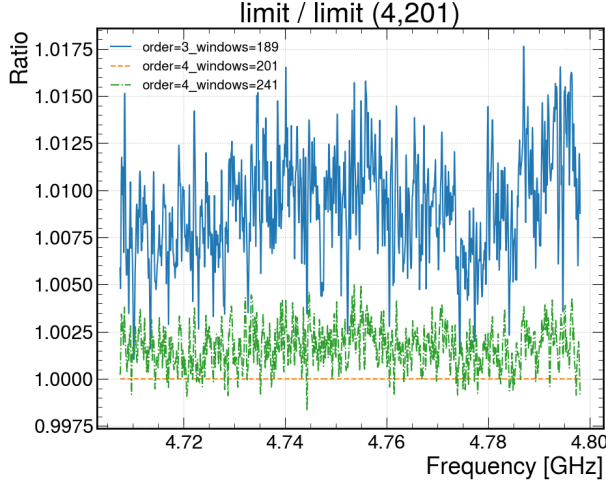


FIG. 14. The ratios of the limits on  $|g_{a\gamma\gamma}|$  due to the different choices of the window width and the order of polynomial in the SG filter, with respect to the central results (a window width of 201 bins and the 4<sup>th</sup>-order polynomial). The window width of 241 bins and the 4<sup>th</sup>-order polynomial are obtained from the optimization after injecting an axion signal on top of a simulated noise spectrum. The window width of 189 bins and the 3<sup>rd</sup>-order polynomial are obtained from the optimization after comparing the means and the widths of the measured power distributions.

average value of  $7.7 \times 10^{-14}$ ; the lowest value comes from the frequency bins with additional eight times more data from the rescans, while the highest value comes from the frequency bins near the boundaries of the spectrum. Figure 16 displays the  $|g_{a\gamma\gamma}|$  limits obtained by TASEH together with those from the previous searches. The results of TASEH exclude the models with the axion-two-photon coupling  $|g_{a\gamma\gamma}| \gtrsim 7.7 \times 10^{-14} \text{ GeV}^{-1}$ , a factor of ten above the benchmark KSVZ model for the mass range  $19.47 < m_a < 19.84 \mu\text{eV}$  (corresponding to the frequency range of  $4.707506 < f_a < 4.798145 \text{ GHz}$ ).

The central results shown in Figs. 15–16 are obtained assuming an axion signal line shape that follows Eq. (4). Both the analysis that merges bins without including a weight from the signal line shape [ $L_k = 1/5$  in Eq. (21)] and the one that assumes a simple Gaussian weight, with a mean at the center of the five frequency bins and a width  $\sigma$  giving half-maximum-weight when the frequency is 2.5 kHz away from the center, i.e.  $\sigma = 5 \text{ kHz} / 2\sqrt{2\ln 2}$ , produce limits that are 5-6% higher than the central results (see Fig. 17).

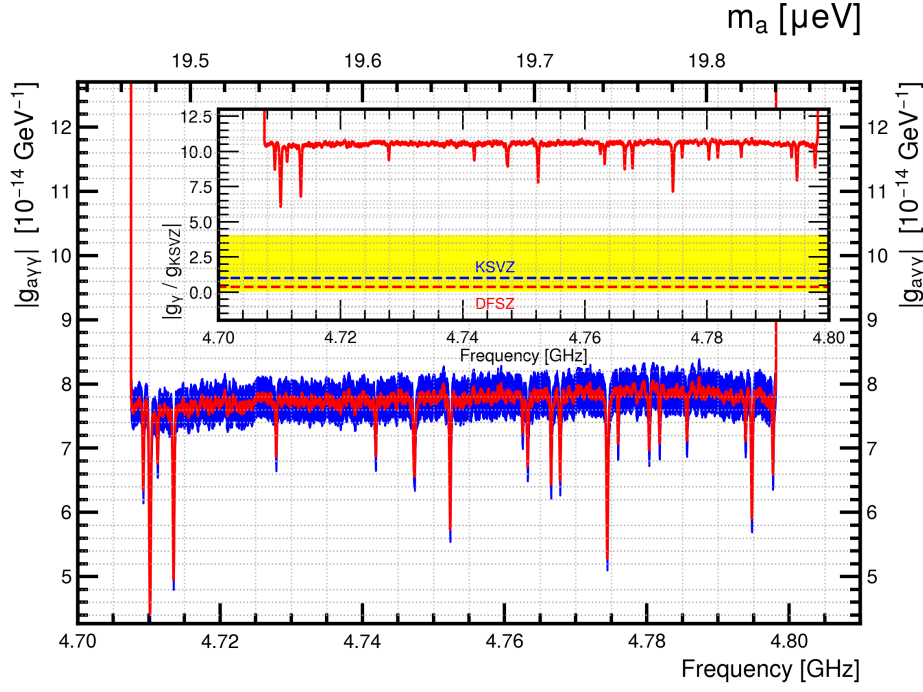


FIG. 15. The limits on  $|g_{a\gamma\gamma}|$  and the ratio of the limits on  $|g_\gamma|$  relative to  $|g_{\text{KSVZ}}| = 0.97$  (inset) for the frequency range of 4.707506–4.798145 GHz. The blue error band indicates the systematic uncertainties as discussed in Sec. VI. The yellow band in the inset shows the allowed region of  $|g_\gamma|$  vs.  $m_a$  from various QCD axion models, while the blue and red dashed lines are the values predicted by the KSVZ and DFSZ benchmark models, respectively

## VIII. CONCLUSION

This paper presents the first results of a search for axions for the mass range  $19.47 < m_a < 19.84 \mu\text{eV}$ , using the CD102 data collected by the Taiwan Axion Search Experiment with Haloscope from October 13, 2021 to November 15, 2021. Apart from the external signals, no candidates with a significance more than  $3.355\sigma$  were found. The experiment excludes models with the axion-two-photon coupling  $|g_{a\gamma\gamma}| \gtrsim 7.7 \times 10^{-14} \text{ GeV}^{-1}$ , a factor of ten above the benchmark KSVZ model. This is the first time that constraints on the  $|g_{a\gamma\gamma}|$  are placed in this mass region. The synthetic axion signals were injected after the collection of data and the successful results validate the data acquisition and the analysis procedure.

The target of TASEH is to search for axions for the mass range of  $16\text{--}40 \mu\text{eV}$ , corresponding to a frequency range of  $3.9\text{--}9.7$  GHz. In the coming years, several upgrades are

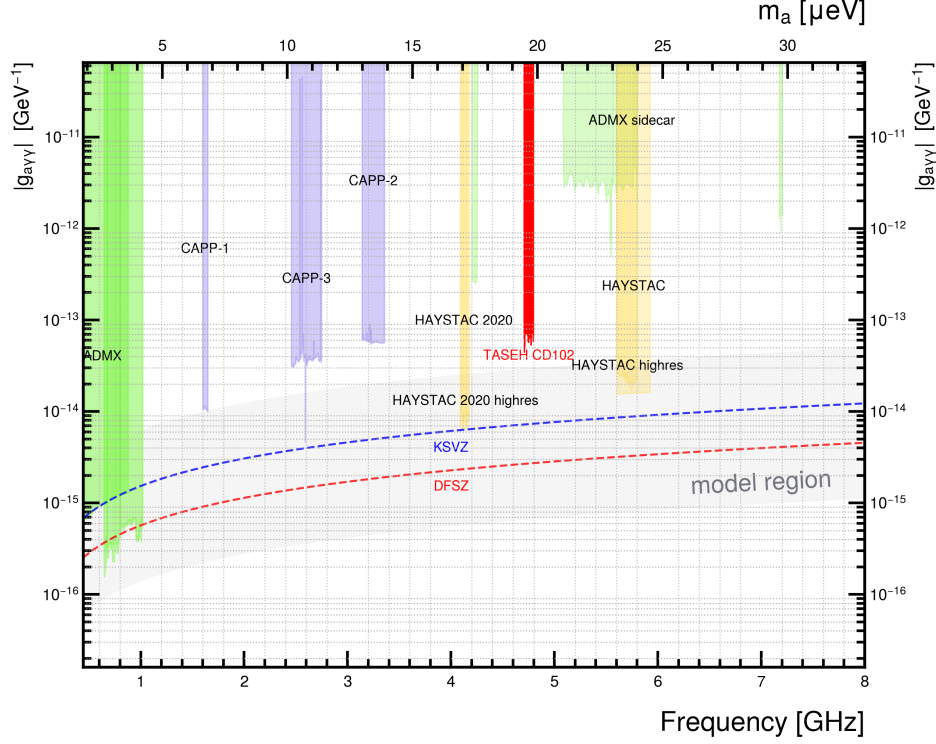


FIG. 16. The limits on the axion-two-photon coupling  $|g_{a\gamma\gamma}|$  for the frequency ranges of 0.4–8 GHz, from the CD102 data of TASEH and previous searches performed by the ADMX, CAPP, and HAYSTAC Collaborations. The gray band indicates the allowed region of  $|g_{a\gamma\gamma}|$  vs.  $m_a$  from various QCD axion models while the blue and red dashed lines are the values predicted by the KSVZ and DFSZ benchmark models, respectively.

expected, including: the use of the Josephson parametric amplifier as the first-stage amplifier, the replacement of the existing dilution refrigerator with a new one that has a magnetic field of 9 Tesla and a larger bore size, and the development of a new cavity with an effective volume reaching one liter. These upgrades will reduce the added noise by a factor of 10 and increase the magnetic field and the cavity volume by a factor of 1.125 and 5, respectively. With the improvements of the experimental setup and several years of data taking, TASEH is expected to probe the QCD axion photon band in the target mass range.

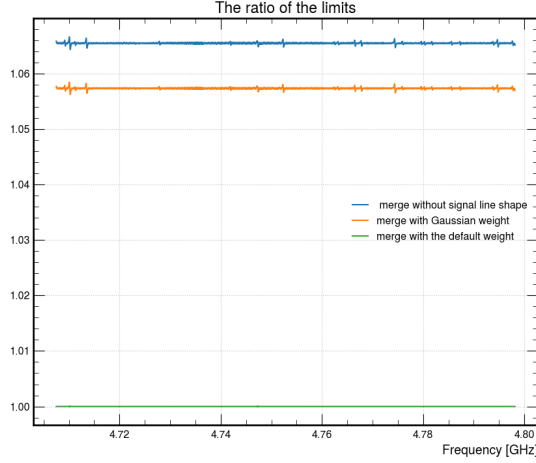


FIG. 17. The ratios of the limits on  $|g_{a\gamma\gamma}|$  from the merging without assuming a signal line shape (blue) and from the merging with a Gaussian weight (orange), with respect to the central results.

## ACKNOWLEDGMENTS

## Appendix A: The Derivation of the Noise Spectrum from the Cavity

The Hamiltonian of a single-mode cavity is

$$H = \hbar\omega_c(C^\dagger C + \frac{1}{2}), \quad (\text{A1})$$

where  $\omega_c/2\pi$  is the cavity resonant frequency and  $C$  is the annihilation operator of the inner cavity field. The cavity field is coupled to the modes  $A$  of a transmission line with the rate  $\kappa_2$ . The cavity field is also coupled to the environment modes  $B$  with the rate  $\kappa_0$ . Based on the model of Fig. 18 and the input-output theory, the equation of motion for  $C$  is obtained:

$$\frac{dC}{dt} = -i\omega_c C - \frac{\kappa_2 + \kappa_0}{2}C + \sqrt{\kappa_2}A_{\text{in}} + \sqrt{\kappa_0}B_{\text{in}}. \quad (\text{A2})$$

A boundary condition holds for the transmission modes:

$$A_{\text{out}} = \sqrt{\kappa_2}C - A_{\text{in}}. \quad (\text{A3})$$

Considering working in a rotating frame of the signal frequency  $\omega$  near  $\omega_c$ , the equation of motion becomes:

$$-i\omega C + \frac{dC}{dt} = -i\omega_c C - \frac{\kappa_2 + \kappa_0}{2}C + \sqrt{\kappa_2}A_{\text{in}} + \sqrt{\kappa_0}B_{\text{in}}. \quad (\text{A4})$$

The steady state solution for the cavity field is:

$$C = \frac{\sqrt{\kappa_2}A_{\text{in}} + \sqrt{\kappa_0}B_{\text{in}}}{-i(\omega - \omega_c) + \frac{\kappa_2 + \kappa_0}{2}}. \quad (\text{A5})$$

By substituting Eq. (A5) into Eq. (A3), the reflected modes of the transmission line  $A_{\text{out}}$  are expressed in terms of the input modes of the transmission line  $A_{\text{in}}$  and the environment  $B_{\text{in}}$ :

$$\begin{aligned} A_{\text{out}} &= \frac{i(\omega - \omega_c) + \frac{\kappa_2 - \kappa_0}{2}}{-i(\omega - \omega_c) + \frac{\kappa_2 + \kappa_0}{2}} A_{\text{in}} + \frac{\sqrt{\kappa_2 \kappa_0}}{-i(\omega - \omega_c) + \frac{\kappa_2 + \kappa_0}{2}} B_{\text{in}} \\ &= \frac{-(\omega - \omega_c)^2 + \frac{\kappa_2^2 - \kappa_0^2}{4} + i\kappa_2(\omega - \omega_c)}{(\omega - \omega_c)^2 + (\frac{\kappa_2 + \kappa_0}{2})^2} A_{\text{in}} \\ &\quad + \frac{\sqrt{\kappa_2 \kappa_0} \frac{\kappa_2 + \kappa_0}{2} + i\sqrt{\kappa_2 \kappa_0}(\omega - \omega_c)}{(\omega - \omega_c)^2 + (\frac{\kappa_2 + \kappa_0}{2})^2} B_{\text{in}}. \end{aligned} \quad (\text{A6})$$

Therefore, the autocorrelation of  $A_{\text{out}}$  is related to those of  $A_{\text{in}}$  and  $B_{\text{in}}$ :

$$\begin{aligned} \langle A_{\text{out}}^\dagger A_{\text{out}} \rangle &= \frac{[(\omega - \omega_c)^2 - \frac{\kappa_2^2 - \kappa_0^2}{4}]^2 + \kappa_2^2(\omega - \omega_c)^2}{[(\omega - \omega_c)^2 + (\frac{\kappa_2 + \kappa_0}{2})^2]^2} \langle A_{\text{in}}^\dagger A_{\text{in}} \rangle \\ &\quad + \frac{\kappa_2 \kappa_0 (\frac{\kappa_2 + \kappa_0}{2})^2 + \kappa_2 \kappa_0 (\omega - \omega_c)^2}{[(\omega - \omega_c)^2 + (\frac{\kappa_2 + \kappa_0}{2})^2]^2} \langle B_{\text{in}}^\dagger B_{\text{in}} \rangle. \end{aligned} \quad (\text{A7})$$

The spectrum from the cavity  $S(\omega)$  is found to be related to the spectrum of the readout transmission line  $S_{\text{rt}}(\omega)$  and the spectrum of the cavity environment  $S_{\text{cav}}(\omega)$ :

$$\begin{aligned} S(\omega) &= \frac{[(\omega - \omega_c)^2 - \frac{\kappa_2^2 - \kappa_0^2}{4}]^2 + \kappa_2^2(\omega - \omega_c)^2}{[(\omega - \omega_c)^2 + (\frac{\kappa_2 + \kappa_0}{2})^2]^2} S_{\text{rt}}(\omega) \\ &\quad + \frac{\kappa_2 \kappa_0 (\frac{\kappa_2 + \kappa_0}{2})^2 + \kappa_2 \kappa_0 (\omega - \omega_c)^2}{[(\omega - \omega_c)^2 + (\frac{\kappa_2 + \kappa_0}{2})^2]^2} S_{\text{cav}}(\omega). \end{aligned} \quad (\text{A8})$$

As the the readout transmission line and the cavity environment are both in thermal states, i.e.  $S_{\text{rt}}(\omega) = [n_{\text{BE}}(T_{\text{rt}}) + 1/2] \hbar \omega$  and  $S_{\text{cav}}(\omega) = [n_{\text{BE}}(T_{\text{cav}}) + 1/2] \hbar \omega$ , where  $n_{\text{BE}}$  is the mean photon number given by the Bose-Einstein distribution,  $S(\omega)$  is white if  $T_{\text{cav}} = T_{\text{rt}}$ , and Lorentzian if  $T_{\text{cav}} \gg T_{\text{rt}}$ .

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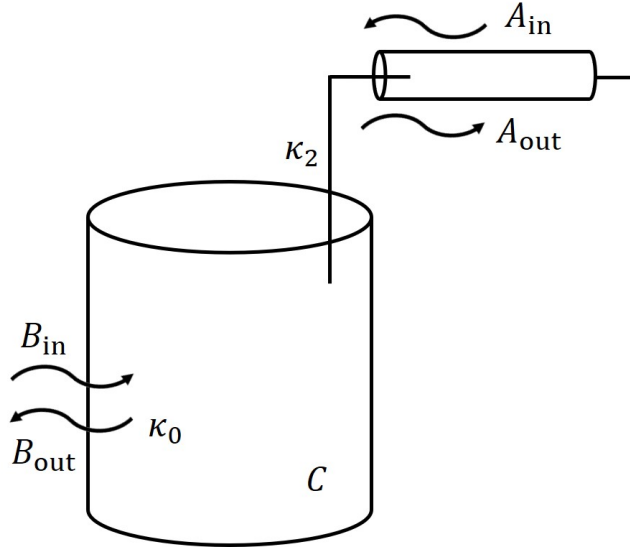


FIG. 18. A cavity is coupled to the modes of transmission line  $A$  with the rate  $\kappa_2$  and the modes of environment  $B$  with the rate  $\kappa_0$ .

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