# First Results from the Taiwan Axion Search Experiment with

Haloscope in the  $19.47-19.84 \,\mu\text{eV}$  Mass Range\*

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## Abstract

This paper presents the first results from the Taiwan Axion Search Experiment with Haloscope, a search for axions using a microwave cavity at frequencies between 4.707506 and 4.798145 GHz. Apart from the external signals, no candidates with a significance more than  $3.355\sigma$  were found. The experiment excludes models with the axion-two-photon coupling  $|g_{a\gamma\gamma}| \gtrsim 7.7 \times 10^{-14} \,\text{GeV}^{-1}$ , a factor of ten above the benchmark KSVZ model for the mass range  $19.47 < m_a < 19.84 \,\mu\text{eV}$ . For the first time, constraints on the  $|g_{a\gamma\gamma}|$  are placed in this mass region.

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#### 34 I. INTRODUCTION

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The axion is a hypothetical particle predicted as a consequence of a solution to the strong 35 CP problem [1–3], i.e. why the CP symmetry is conserved in the strong interactions when there is an explicit CP-violating term in the QCD Lagrangian. In other words, why is the electric dipole moment of the neutron so tiny:  $|d_n| < 1.8 \times 10^{-26} \ e \cdot \text{cm}$  [4, 5]? The solution proposed by Peccei and Quinn is to introduce a new global Peccei-Quinn  $U(1)_{PQ}$ 39 symmetry that is spontaneously broken; the axion is the pseudo Nambu-Goldstone boson of 40  $U(1)_{PQ}$  [1]. Axions are abundantly produced during the QCD phase transition in the early 41 universe and may constitute the dark matter (DM). In the post-inflationary PQ symmetry 42 breaking scenario, where the PQ symmetry is broken after inflation, current calculations 43 suggest a mass range of 1—100  $\mu$ eV for axions so that the cosmic axion density does not 44 exceed the observed cold DM density [6–18]. Therefore, axions are compelling because they 45 may explain at the same time puzzles that are on scales different by more than thirty orders 46 of magnitude. 47

Axions could be detected and studied via their two-photon interaction, the so-called "inverse Primakoff effect". For QCD axions, i.e. the axions proposed to solve the strong CP problem, the axion-two-photon coupling constant  $g_{a\gamma\gamma}$  is related to the mass of the axion  $m_a$ :

$$g_{a\gamma\gamma} = \left(\frac{g_{\gamma}\alpha}{\pi\Lambda^2}\right) m_a,\tag{1}$$

where  $g_{\gamma}$  is a dimensionless model-dependent parameter,  $\alpha$  is the fine-structure constant,  $\Lambda = 78$  MeV is a scale parameter that can be derived from the mass and the decay constant of the pion, and the ratio of the up to down quark masses. The numerical values of  $g_{\gamma}$ are -0.97 and 0.36 in the Kim-Shifman-Vainshtein-Zakharov (KSVZ) [19, 20] and the Dine-Fischler-Srednicki-Zhitnitsky (DFSZ) [21, 22] benchmark models, respectively.

The detectors with the best sensitivities to axions with a mass of  $\approx \mu eV$ , as first put forward by Sikivie [23, 24], are haloscopes consisting of a microwave cavity immersed in a strong

static magnetic field and operated at a cryogenic temperature. In the presence of an external magnetic field, the ambient oscillating axion field drives the cavity and they resonate when 61 the frequencies of the electromagnetic modes in the cavity match the microwave frequency 62 f, where f is set by the total energy of the axion:  $hf = E_a = m_a c^2 + \frac{1}{2} m_a v^2$ ; the signal 63 power is further delivered to the readout probe followed by a low-noise linear amplifier. The axion mass is unknown, therefore, the cavity resonator must allow the possibility to be tuned through a range of possible axion masses. The Axion Dark Matter experiment (ADMX), one of the flagship dark matter search experiments, had developed and improved the cavity design and readout electronics over the years. The results from the previous versions of ADMX and the Generation 2 ADMX (ADMX G2) excluded the KSVZ benchmark model within the mass range of  $1.9-4.2\,\mu\text{eV}$  and the DFSZ benchmark model for the mass ranges 70 of 2.66–3.31 and 3.9–4.1  $\mu$ eV, respectively [25–31]. One of the major goals of ADMX G2 is 71 to search for higher-mass axions in the range of  $4-40 \,\mu\text{eV}$  (1–10 GHz), similarly for the axion 72 experiments that were established during the last ten years. The Haloscope at Yale Sensitive 73 to Axion Cold dark matter (HAYSTAC) had performed searches first for the mass range 74 of 23.15–24  $\mu eV$  and later at around 17  $\mu eV$ ; they excluded axions with  $|g_{\gamma}| \ge 1.38 |g_{\gamma}|^{KSVZ}$ 75 for  $m_a=16.96-17.12$  and 17.14– $17.28\,\mu\text{eV}$ , respectively [32]. The Center for Axion and 76 Precision Physics Research (CAPP) constructed and ran simultaneously several experiments targeting at different frequencies; they have pushed the limits towards the KSVZ value within a narrow mass region of 10.7126–10.7186  $\mu$ eV [33]. The QUest for AXions- $a\gamma$  (QUAX- $a\gamma$ ) also pushed their limits close to the upper bound of the QCD axion-two-photon couplings for  $m_a \approx 43 \,\mu\text{eV}$  [34]. 81

This paper presents the first results and the analysis details of a search for axions for the mass range of 19.47–19.84  $\mu$ eV, from the Taiwan Axion Search Experiment with Haloscope (TASEH). The expected axion signal power and signal line shape, the noise power, and the signal-to-noise ratio are described in Secs. I A–I B. An overview of the TASEH experimental setup is presented in Sec. II. Section III gives a brief description of the calibration for the whole amplification chain while Sec. IV details the analysis procedure. Section V presents the analysis of the synthetic axion data and Sec. VI discusses the systematic uncertainties that may affect the limits on the  $|g_{a\gamma\gamma}|$ . The final results and the conclusion are presented in Sec. VII and Sec. VIII, respectively.

#### The expected axion signal power and signal line shape

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The signal power extracted from a microwave cavity on resonance is given by:

$$P_s = \left(g_\gamma^2 \frac{\alpha^2 \hbar^3 c^3 \rho_a}{\pi^2 \Lambda^4}\right) \times \left(\omega_c \frac{1}{\mu_0} B_0^2 V C_{mnl} Q_L \frac{\beta}{1+\beta}\right),\tag{2}$$

where  $\rho_a = 0.45 \text{ GeV/cm}^3$  is the local dark-matter density. The second set of parentheses 94 contains parameters related to the experimental setup: the angular resonant frequency of the 95 cavity  $\omega_c$ , the vacuum permeability  $\mu_0$ , the nominal strength of the external magnetic field  $B_0$ , the volume of the cavity V, and the loaded quality factor of the cavity  $Q_L = Q_0/(1+\beta)$ , 97 where  $Q_0$  is the unloaded, intrinsic quality factor of the cavity and  $\beta$  is the coupling coefficient which determines the amount of coupling of the signal to the receiver. The form factor  $C_{mnl}$ is the normalized overlap of the electric field  $\vec{E}$ , for a particular cavity resonant mode, with 100 the external magnetic field  $\vec{B}$ : 101

$$C_{mnl} = \frac{\left[\int \left(\vec{\boldsymbol{B}} \cdot \vec{\boldsymbol{E}}_{mnl}\right) d^3 \boldsymbol{x}\right]^2}{B_0^2 V \int E_{mnl}^2 d^3 \boldsymbol{x}}.$$
 (3)

Here, the magnetic field  $\vec{B}$  points mostly along the axial direction (z-axis) of the cavity. 103 The field strength has a small variation along the radial and axial directions and  $B_0$  is the nominal magnetic field strength. For cylindrical cavities, the largest form factor is from the  $TM_{010}$  mode. The expected signal power derived from the experimental parameters of 106 TASEH (see Table I) is  $P_s \simeq 1.5 \times 10^{-24}$  W for a KSVZ axion with a mass of 19.5  $\mu$ eV.

In the direct dark matter search experiments, several assumptions were made in order to derive a signal line shape. The density and the velocity distributions of DM are related to each other through the gravitational potential. The DM in the galactic halo is assumed to be virialized. The DM halo density distribution is assumed to be spherically symmetric and close to be isothermal, which results in a velocity distribution similar to the Maxwell-Boltzmann distribution. The distribution of the measured signal frequency can be further derived from the velocity distribution after a change of variables and set  $hf_a = m_a c^2$ . Previous experimental results typically adopt the following function for frequency  $f \geq f_a$ :

$$\mathcal{F}(f) = \frac{2}{\sqrt{\pi}} \sqrt{f - f_a} \left(\frac{3}{\alpha}\right)^{3/2} e^{\frac{-3(f - f_a)}{\alpha}},\tag{4}$$

where  $\alpha \equiv f_a \langle v^2 \rangle / c^2$ . For a Maxwell-Boltzmann velocity distribution, the variance  $\langle v^2 \rangle$  and 117 the most probable velocity (speed)  $v_p$  are related to each other:  $\langle v^2 \rangle = 3v_p^2/2 = (270 \text{ km/s})^2$ , 118

where  $v_p = 220 \text{ km/s}$  is the local circular velocity of DM in the galactic rest frame. Equa-119 tion (4) is modified if one considers that the relative velocity of the DM halo with respect 120 to the Earth is not the same as the DM velocity in the galactic rest frame [35]. The ve-121 locity distributions shall also be truncated so that the DM velocity is not larger than the 122 escape velocity of the Milky Way [36]. Several N-body simulations [37, 38] follow structure 123 formation from the initial DM density perturbations to the largest halo today and take into account the merger history of the Milky Way, rather than assuming that the Milky Way is 125 in a steady state; the simulated results suggest velocity distributions with more high-speed 126 particles relative to the Maxwellian case [39, 40]. However, these numerical simulations con-127 tain only DM particles; an inclusion of baryons may enhance the halo's central density due 128 to a condensation of gas towards the center of the halo via an adiabatic contraction [41, 42], 129 or may reduce the density due to the supernova outflows, etc [43, 44]. 130

In order to compare the results of TASEH with those of the former experiments, the 131 analysis presented in this paper assumes an axion signal line shape by including Eq. (4) in 132 the weights when merging the measured power from multiple frequency bins (see Sec. IV D). 133 Still given the caveats above and a lack of strong evidence for any particular choice of the 134 velocity distribution, the results without an assumption of signal line shape and the results 135 with a simple Gaussian weight are also presented for comparison. In addition, a signal 136 line width  $\Delta f_a = m_a \langle v^2 \rangle / h \simeq 5$  kHz, which is much smaller than the TASEH cavity line 137 width  $f_a/Q_L \simeq 250$  kHz, is assumed and five frequency bins are merged to perform the final analysis. For a signal line shape as described in Eq. (4), a 5-kHz bandwidth includes about 95% of the distribution. 140

#### B. The expected noise and the signal-to-noise ratio

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Several physics processes can contribute to the total noise and all of them can be seen as
Johnson thermal noise at some effective temperature, or the so-called system noise temperature  $T_{\text{sys}}$ . The total noise power in a bandwidth b is then:

$$P_n = k_B T_{\text{svs}} b,\tag{5}$$

where  $k_B$  is the Boltzmann constant. The system noise temperature  $T_{\rm sys}$  has three major components:

$$T_{\rm sys} = T_{\rm b} + T_{\rm qn} + T_{\rm a},\tag{6}$$

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$$T_{\rm qn} = \frac{1}{2} hf/k_B . \tag{7}$$

The three terms in Eq. (6) correspond to the effective temperatures of the following noise 151 sources: (i)  $T_{\rm b}$ , the blackbody radiation from the cavity at a physical temperature  $T_{\rm c}$ , (ii) 152  $T_{\rm qn}$ , the quantum noise associated with the zero-point fluctuation of the vacuum, and (iii)  $T_{\rm a}$ , the noise added by the receiver (mainly from the first-stage amplifier). Equation (6) implies that the noise spectrum has little dependence on the frequency (white spectrum) 155 for the narrow bandwidth considered in the experiment. However, apart from the flat 156 baseline as described by Eq. (6), the noise spectrum observed by TASEH has an additional 157 component with a Lorentzian shape due to the higher temperature at the cavity with respect 158 to the temperature in the dilution refrigerator. More details may be found in Sec. II and 159 Appendix A. The Lorentzian component will be removed from the measured spectrum and 160 only the baseline  $T_{\rm sys}$  will be used in the final analysis (Sec. IV). 161

Using the operation parameters of TASEH in Table I and the results from the calibration of readout electronics, the values of  $T_{\rm b}$ ,  $T_{\rm qn}$ , and  $T_{\rm a}$  are estimated to be about 0.07 K, 0.12 K, and 1.9 – 2.2 K, respectively. Therefore, the baseline value of  $T_{\rm sys}$  for TASEH is about 2.1–2.4 K, which gives a noise power of approximately  $(1.5-1.7)\times 10^{-19}$  W within the 5-kHz axion signal line-width, five orders of magnitude larger than the signal. Nevertheless, what matters in the analysis is the signal significance, or the so-called signal-to-noise ratio (SNR) using the standard terminology of axion experiments, i.e. the ratio of the signal power to the fluctuation in the averaged noise power spectrum  $\sigma_n$ .

According to Dicke's Radiometer Equation [45], the  $\sigma_n$  is given by:

$$\sigma_n = \frac{P_n}{\sqrt{N_{\text{avg}}}},$$

$$= \frac{P_n}{\sqrt{t\Delta f}},$$

$$= k_B T_{\text{sys}} \sqrt{\frac{\Delta f}{t}}$$
(8)

where  $N_{\text{avg}}$  is the number of noise power spectra used in the average; it is related to the amount of data integration time t and the bandwidth over which a single measurement is

made  $\Delta f$ . The SNR will therefore be:

SNR = 
$$\frac{P_s}{\sigma_n}$$
,
$$= \frac{P_s}{k_B T_{\text{sys}}} \sqrt{\frac{t}{\Delta f}},$$
(9)

Combining Eq. (2) and Eq. (9), one could see that the SNR is maximized by an experimental setup with a strong magnetic field, a large cavity volume, an efficient cavity resonant mode, a receiver with low system noise temperature, and a long integration time.

#### $_{12}$ II. EXPERIMENTAL SETUP

The detector of TASEH is located at the Department of Physics, National Central University, Taiwan and housed within a cryogen-free dilution refrigerator (DR) from BlueFors.

An 8-Tesla superconducting solenoid with a bore diameter of 76 mm and a length of 240 mm is integrated with the DR.

The data for the analysis presented in this paper were collected by TASEH from October 187 13, 2021 to November 15, 2021, and termed as the CD102 data, where CD stands for "cool 188 down". During the data taking, the cavity sat in the center of the magnet bore and was 189 connected via holders to the mixing flange of the DR at a temperature of  $T_{\rm mx} \approx 27$  mK. 190 The temperature of the cavity stayed at  $T_{\rm c} \simeq 155$  mK, higher with respect to the DR; it 191 is believed that the cavity had an accidental thermal contact with the radiation shield in 192 the DR. The cavity, made of oxygen-free high-conductivity (OFHC) copper, has an effective 193 volume of 0.234 L and is a two-cell cylinder split along the axial direction (z-axis). The 194 cylindrical cavity has an inner radius of 2.5 cm and a height of 12 cm. In order to maintain 195 a smooth surface, the cavity underwent the processes of annealing, polishing, and chemical 196 cleaning. The resonant frequency of the  $TM_{010}$  mode can be tuned over the range of 4.667– 197 4.959 GHz via the rotation of an off-axis OFHC copper tuning rod, from the position closer 198 to the cavity wall to the position closer to the cavity center (i.e. when the vector from 199 the rotation axis to the tuning rod is at an angle of 0° to 180°, with respect to the vector 200 from the cavity center to the rotation axis). The CD102 data cover the frequency range of 201 4.707506-4.798145 GHz. There were 839 resonant-frequency steps in total, with a frequency 202 difference of  $\Delta f_{\rm s}=95-115$  kHz between the steps. The value of  $\Delta f_{\rm s}$  was kept within 203 10% of 105 kHz rather than a fixed value, such that the rotation angle of the tuning rod 204

did not need to be fine-tuned and the operation time could be minimized; a 10% variation 205 of the  $\Delta f_{\rm s}$  is found to have no impact on the  $|g_{a\gamma\gamma}|$  limits. Each resonant-frequency step is 206 denoted as a "scan" and the data integration time was about 32-42 minutes. The integration 207 time was determined based on the target  $|g_{a\gamma\gamma}|$  limits and the experimental parameters in 208 Table I; the variation of the integration time aimed to remove the frequency-dependence in 209 the  $|g_{a\gamma\gamma}|$  limits caused by frequency dependence of the added noise  $T_a$ . The form factor  $C_{010}$ 210 as defined in Eq. (3) varies from 0.64 to 0.69 over the full frequency range. The intrinsic, 211 unloaded quality factor  $Q_0$  at the cryogenic temperature ( $T_c \simeq 155$  mK) is  $\simeq 60000$  at the 212 frequency of 4.74 GHz. 213

An output probe, made of a  $50-\Omega$  semi-rigid coaxial cable that was soldered to an SMA 214 (SubMiniature version A) connector, was inserted into the cavity and its depth was set for 215  $\beta \simeq 2$ . The signal from the output probe was directed to an impedance-matched ampli-216 fication chain. The first-stage amplifier was a low noise high-electron-mobility transistor 217 (HEMT) amplifier with an effective noise temperature of  $\approx 2$  K, mounted on the 4K flange. 218 The signal was further amplified at room temperature via a three-stage post-amplifier, and 219 down-converted and demodulated to in-phase (I) and quadrature (Q) components and dig-220 itized by an analog-to-digital converter with a sampling rate of 2 MHz. 221

A more detailed description of the TASEH detector, the operation of the data run, and the calibration of the gain and added noise temperature of the whole amplification chain can be found in Ref. [46]. See Table I for the benchmark experimental parameters that can be used to estimate the sensitivity of TASEH.

#### 226 III. CALIBRATION

The noise is one of the most important parameters for the axion searches. Therefore, 227 calibration for the amplification chain is a crucial part in the operation of TASEH. In 228 order to perform a calibration, the HEMT was connected to a heat source (a 50- $\Omega$  resistor) 229 instead of the cavity; various values of input currents were sent to the source to change 230 its temperature monitored by a thermometer. The power from the source was delivered 231 following the same transmission line as that in the axion data running. The output power 232 is fitted to a first-order polynomial, as a function of the source temperature, to extract the 233 gain and added noise for the amplification chain. More details of the procedure can be found 234

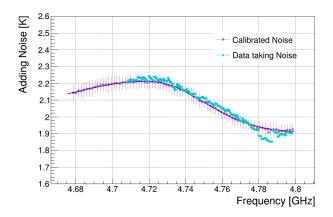
TABLE I. The benchmark experimental parameters for estimating the sensitivity of TASEH. The definitions of the parameters can be found in Sec. I. More details regarding the determination and the measurements of some of the parameters may be found in Ref. [46].

$f_{ m lo}$	4.707506 GHz
$f_{ m hi}$	4.798145 GHz
$N_{\rm step}$	839
$\Delta f_{\mathrm{s}}$	$95-115~\mathrm{kHz}$
$B_0$	8 Tesla
V	$0.234~\mathrm{L}$
$C_{010}$	0.64 - 0.69
$Q_0$	59000 - 65000
$\beta$	1.9 - 2.3
$T_{ m mx}$	$2728~\mathrm{mK}$
$T_{ m c}$	$155~\mathrm{mK}$
$T_{\rm a}$	1.9 - 2.2  K
$\Delta f_a$	5 kHz

235 in Ref. [46].

The calibration was carried out before, during, and after the data taking, which showed 236 that the performance of the system was stable over time. The average of the added noise 237  $T_{\rm a}$  over 19 measurements has the lowest value of 1.9 K at the frequency of 4.8 GHz and the 238 highest value of 2.2 K at 4.72 GHz, as presented in Fig. 1. The error bars are the RMS of  $T_{\rm a}$ 239 and the largest RMS is used to calculate the systematic uncertainty for the limits on  $|g_{a\gamma\gamma}|$ . 240 The light blue points in Fig. 1 are the noise from the axion data estimated by removing the 241 gain and subtracting the contribution from the cavity noise, assuming that the presence of a 242 narrow signal in the data would have no effect on the estimation. A good agreement between the results from the calibration and the ones estimated from the axion data is shown. The 244 biggest difference is 0.076 K in the frequency range during which the data were recorded 245 after an earthquake. The source of the difference is not understood, therefore, the difference 246

is quoted as a systematic uncertainty together with the RMS of the noise.



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FIG. 1. The average added noise obtained from the calibration (pink points) and the noise estimated from the axion data (light blue points) as a function of frequency. The error bars on the
pink points are the RMS of the  $T_a$ , as computed from the 19 measurements for each frequency in
the calibration. The blue curve is obtained after performing a fit to the pink points and is used to
estimate the  $T_a$  at each resonant frequency of the cavity.

#### 254 IV. ANALYSIS PROCEDURE

The goal of TASEH is to find the axion signal hidden in the noise. In order to achieve this, the analysis procedure includes the following steps:

- 1. Perform fast Fourier transform (FFT) on the IQ time series data to obtain the frequency-domain power spectrum.
- 259 2. Apply the Savitzky-Golay (SG) filter to remove the structure of the background in the frequency-domain power spectrum.
- 3. Combine all the spectra from different frequency scans with the weighting algorithm.
- 4. Merge bins in the combined spectrum to maximize the SNR.
- 5. Rescan the frequency regions with candidates and set limits on the axion-two-photon coupling  $|g_{a\gamma\gamma}|$  if no candidates were found.

The analysis is done by following the procedure similar to that adopted by the HAYSTAC experiment [47].

#### A. Fast Fourier transform

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The in-phase I(t) and quadrature Q(t) components of the time-domain data were sampled and saved in the TDMS (Technical Data Management Streaming) files - a binary format developed by National Instruments. The FFT is performed to convert the data into frequency-domain power spectrum in which the measured power is calculated using the following equation:

$$Power = \frac{|FFT(I + i \cdot Q)|^2}{N \cdot 2R},$$
(10)

where N is the number of data points (N=2000 in the TASEH CD102 data), and R is the input resistance of the signal analyzer (50  $\Omega$ ). The FFT is done for every one-millisecond subspectrum data. The integration time for each frequency scan was about 32-42 minutes, which resulted in 1920000 to 2520000 subspectra; an average over these subspectra gives the averaged frequency-domain power spectrum for each scan. The frequency span in the spectrum from each resonant-frequency scan is 1.6 MHz while the resolution is 1 kHz, giving 1600 frequency bins in each spectrum.

#### B. Remove the structure of the background

In the absence of the axion signal, the output data spectrum is simply the noise from 282 the cavity and the amplification chain. If axions are present in the cavity, the signal will be 283 buried in the noise because the signal power is very weak. Therefore, the structure of the 284 raw averaged output power spectrum, as shown in the upper panel of Fig. 2, is dominated 285 by the noise of the system and an explanation for the structure can be found in Appendix A. The Savitzky Golay (SG) filter [48], a digital filter that can smooth data without distorting the signal tendency, is applied to remove the structure of the background. The SG filter is performed on the averaged spectrum of each frequency scan by fitting adjacent points 289 of successive sub-sets of data with an  $n^{\text{th}}$ -order polynomial. The result depends on two 290 parameters: the number of data points used for fitting, the so-called window width, and the 291

order of the polynomial. If the window is too wide, the filter will not remove small structures, 292 and if it is too narrow, it may kill the signal. The window and the order were first chosen 293 during the data taking, by requiring the ratio of the raw data to the filter output consistent 294 with unity. After the data taking, they were optimized by injecting an axion signal on top 295 of the noise data and found that they were consistent with the original choice (see Sec. VI). The raw averaged power spectrum is divided by the output of the SG filter, then unity 297 is subtracted from the ratio to get the dimensionless normalized spectrum (lower panel of 298 Fig. 2). The value in each bin of the normalized spectrum is the deviation of the averaged 299 measured power from the SG-filter output (can be considered as the averaged noise power) 300 relative to the SG output. The symbol  $\delta$  and term "RDP" are used to denote the relative 301 deviation of power in the normalized spectrum and also in the spectra processed with rescal-302 ing, combining, and merging afterwards; the value can be zero, positive, or negative. In the 303 absence of the axion signal, the RDPs in the normalized spectrum are samples drawn from 304 a Gaussian distribution with a zero mean and a standard deviation of  $1/\sqrt{N_{\rm spectra}}$ , where 305  $N_{\rm spectra}$  is the number of subspectra used to compute the average (Sec. IV A). If the axion

During the data taking, the resonant frequency of the cavity was adjusted by the tuning bar so to scan a large range of frequencies and to reduce the uncertainty of the averaged noise power at the overlapped region. Therefore, the spectra of all the scans need to be combined to create one big spectrum. Before doing this, the normalized spectrum from each scan is rescaled and the rescaled spectrum, shown in Fig. 3, is computed with the following formula:

$$\delta_{ij}^{\text{res}} = R_{ij}\delta_{ij}^{\text{norm}},\tag{11}$$

and the standard deviation of each bin is: 315

signal exists, there will be a significant excess above zero.

$$\sigma_{ij}^{\text{res}} = R_{ij}\sigma_i^{\text{norm}},\tag{12}$$

where 317

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$$R_{ij} = \frac{k_B T_{\text{sys}} \Delta f_{\text{bin}}}{P_{ij}^{\text{KSVZ}} h_{ij}},\tag{13}$$

and 319

$$h_{ij} = \frac{1}{1 + 4Q_{Li}(f_{ij}/f_{ci} - 1)^2}. (14)$$

The  $\delta_{ij}^{\text{norm}}$  ( $\delta_{ij}^{\text{res}}$ ) and  $\sigma_i^{\text{norm}}$  ( $\sigma_{ij}^{\text{res}}$ ) are the RDP and the standard deviation of the  $j^{\text{th}}$  frequency 321 bin in the normalized (rescaled) spectrum from the  $i^{\rm th}$  resonant-frequency scan. The value

of  $\sigma_i^{\text{norm}}$  is derived from the spread of the RDPs over the 1600 frequency bins for the  $i^{\text{th}}$  scan. 323 The factor  $R_{ij}$  is the ratio of the system noise power to the expected signal power of the 324 KSVZ axion  $P_{ij}^{KSVZ}$ , with the Lorentzian cavity response  $h_{ij}$  taken into account. The system-325 noise temperature  $T_{\text{sys}}$  is calculated following Eq. (6), where the frequency dependence of 326 the added-noise temperature  $T_{\rm a}$  is obtained from the fitting function in Fig. 1. The  $\Delta f_{\rm bin}$ is the bin width of spectrum (1 kHz). The factor  $h_{ij}$  describes the Lorentzian response of the cavity, which depends on the loaded quality factor  $Q_{Li}$  and the difference between 329 the frequency  $f_{ij}$  in bin j and the resonant frequency  $f_{ci}$ . If a signal appears in a certain 330 frequency bin j, its expected power will vary depending on the bin position due to the 331 cavity's Lorentzian response. The rescaling will take into account this effect. The procedure 332 of the normalization and the rescaling also ensures that a KSVZ axion signal will have a 333 rescaled RDP  $\delta_{ij}^{\text{res}}$  that is approximately equal to unity. 334

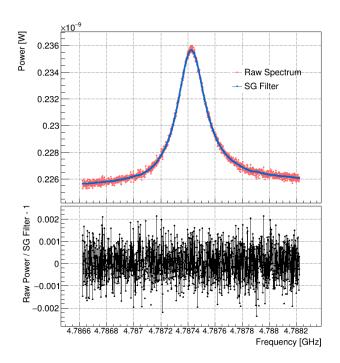


FIG. 2. Upper panel: The raw averaged power spectrum (red points) and the output of the SG filter (blue curve) of one scan. Lower panel: The normalized spectrum, derived by taking the ratio of the raw spectrum to the SG filter and subtracting unity from the ratio.

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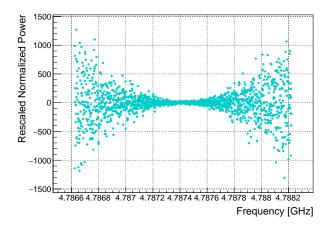


FIG. 3. The rescaled spectrum, obtained by multiplying the RDPs in the normalized spectrum with the ratio of the system noise power to the expected signal power of the KSVZ axion, with the Lorentzian response of the cavity taken into account.

#### C. Combine the spectra with the weighting algorithm

The purpose of the weighting algorithm is to add the spectra from different resonant-frequency scans, particularly for the frequency bins that appear in multiple spectra. Each spectrum was collected with a different cavity resonant frequency. Therefore, if a signal appears in a certain frequency bin j, due to the difference in the resonant frequency and the Lorentzian response, the expected signal power will be different in each spectrum i. The weighting algorithm is expected to take this into account with a weight calculated for each bin j of the rescaled spectrum i, as defined below:

$$w_{ijn} = \frac{\Gamma_{ijn}}{(\sigma_{ij}^{\text{res}})^2}. (15)$$

Note, the symbol  $\Gamma_{ijn} = 1$  if the  $j^{\text{th}}$  frequency bin in the  $i^{\text{th}}$  rescaled spectrum correspond to the same frequency in the  $n^{\text{th}}$  bin of the combined spectrum; otherwise,  $\Gamma_{ijn} = 0$ .

The RDP  $\delta_n^{\text{com}}$  and the standard deviation  $\sigma_n^{\text{com}}$  of the  $n^{\text{th}}$  bin in the combined spectrum are calculated using Eq. (16) and Eq. (17), respectively. The SNR<sub>n</sub><sup>com</sup> is the ratio of  $\delta_n^{\text{com}}$  to  $\sigma_n^{\text{com}}$  as given in Eq. (18). Figure 4 and Fig. 5 show the RDP, the standard deviation, and the SNR of the combined spectrum, respectively.

$$\delta_n^{\text{com}} = \frac{\sum_{i} \sum_{j} \left(\delta_{ij}^{\text{res}} \cdot w_{ijn}\right)}{\sum_{i} \sum_{j} w_{ijn}},\tag{16}$$

$$\sigma_n^{\text{com}} = \frac{\sqrt{\sum_i \sum_j (\sigma_{ij}^{\text{res}} \cdot w_{ijn})^2}}{\sum_i \sum_j w_{ijn}},$$
(17)

(18)

SNR<sub>n</sub><sup>com</sup> =  $\frac{\delta_n^{\text{com}}}{\sigma_n^{\text{com}}} = \frac{\sum_i \sum_j \left(\delta_{ij}^{res} \cdot w_{ijn}\right)}{\sqrt{\sum_i \sum_j \left(\sigma_{ij}^{res} \cdot w_{ijn}\right)^2}}.$ 

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For each bin n in the combined spectrum, there are  $m_n$  non-vanishing contributions to the sums above. The value of  $m_n$  ranges from 2 to 26; in general the leftmost bin or the bin with the smallest frequency (the rightmost bin or the bin with the highest frequency) in each scan has the minimum (maximum) number of  $m_n$ .

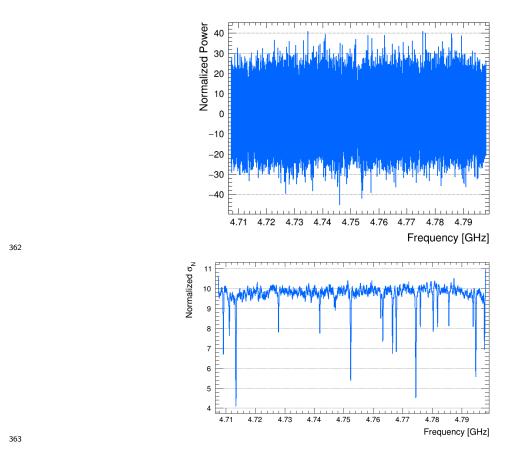


FIG. 4. The combined RDP  $\delta$  following Eq. (16) (upper) and the standard deviation  $\sigma$  derived from Eq. (17) (lower).

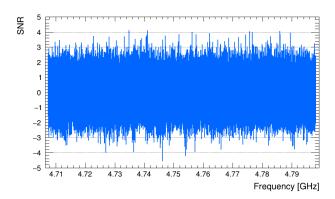


FIG. 5. The signal-to-noise ratio (SNR) calculated using Eq.(18) of the combined spectrum.

## D. Merge bins

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The expected axion bandwidth is about 5 kHz at the frequency of  $\approx 5$  GHz. In this paper, the interested frequency range is 4.707506– 4.798145 GHz and the bin width is 1 kHz. Therefore, in order to maximize the SNR, a running window of five consecutive bins in the combined spectrum are merged to construct a final spectrum. The purpose of using a running window is to avoid the signal power broken into different neighboring bins of the merged spectrum. Then the maximum likelihood weights, defined in Eq. (19) based on the Maxwellian line shape for axions [Eq. (4)], are used to build the merged spectrum:

$$w_{gk} = \frac{L_{gk}}{(\sigma_{g+k-1}^{\text{com}})^2},$$
 (19)

375 in which

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$$L_{gk} = \int_{f_a + \delta f_m + (k-1)\Delta f_{\text{bin}}}^{f_a + \delta f_m + k\Delta f_{\text{bin}}} \mathcal{F}(f) \, df. \tag{20}$$

Here, g = 1,..., N-M+1 is the index for the frequency bins in the final spectrum and M = 5 is the number of merged bins. The total number of bins in the combined (final merged) spectrum is N(N-M+1). The variable k is the index within the group of bins for merging and k = 1,..., M. The frequency  $f_a = m_a c^2/h$  is the axion frequency,  $\delta f_m$  is the misalignment between  $f_a$  and the lower boundary of the  $g^{th}$  bin in the combined spectrum. The function  $\mathcal{F}(f)$  has been defined in Eq. (4).

The RDP, the standard deviation, and the SNR of the merged spectrum are:

$$\delta_g^{\text{merged}} = M \frac{\sum_{k=1}^{M} \left( \delta_{g+k-1}^{\text{com}} \cdot w_{gk} \right)}{\sum_{k=1}^{M} w_{gk}}, \tag{21}$$

$$\sigma_g^{\text{merged}} = M \frac{\sqrt{\sum_{k=1}^{M} \left(\sigma_{g+k-1}^{\text{com}} \cdot w_{gk}\right)^2}}{\sum_{k=1}^{M} w_{gk}},$$
(22)

$$SNR_g^{\text{merged}} = \frac{\delta_g^{\text{merged}}}{\sigma_g^{\text{merged}}} = \frac{\sum_{k=1}^M \left(\delta_{g+k-1}^{\text{com}} \cdot w_{gk}\right)}{\sqrt{\sum_{k=1}^M \left(\sigma_{g+k-1}^{\text{com}} \cdot w_{gk}\right)^2}},$$
(23)

Without the multiplication factor M in Eqs. (21)– (22), the results of the two equations simply provide the weighted averages of RDP and standard deviation, respectively. Assuming that the axion signal leaves a fraction 1/M of its power in one frequency bin, adding the factor M converts the average into a summation of the values in the five bins and can recover the full size of the axion signal.

### E. Rescan and set limits on $|g_{a\gamma\gamma}|$

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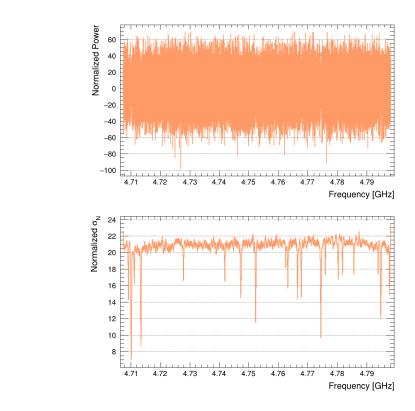
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Before the collection of the CD102 data, a  $5\sigma$  SNR target was chosen, which corresponds 393 to a candidate threshold of  $3.355\sigma$  at 95% confidence. After the merging as described in 394 Sec. IVD, if there were any potential signal with an SNR larger than 3.355, a rescan would 395 be proceeded to check if it were a real signal or a statistical fluctuation. The procedure of 396 the CD102 data taking was to perform a rescan after covering every 10 MHz; the rescan 397 was done by adjusting the tuning rod of the cavity so to match the resonant frequency to 398 the frequency of the candidate. In total, 22 candidates with an SNR greater than 3.355 399 were found. Among them, 17 candidates were from the fluctuations because they were gone 400 after a few rescans. The remaining five candidates, in the frequency ranges of 4.710170 – 401 4.710190 GHz and 4.747301 - 4.747380 GHz, reached an SNR greater than 4 after rescanning. The signals in the second frequency range were detected via a portable antenna outside the 403 DR and found to come from the instruments in the laboratory, while the signals in the first 404 frequency range were weaker but still present after turning off the external magnetic field. 405

Therefore, these five candidates are considered external signals and no limits are placed for the above two frequency ranges. More details can be found in the TASEH instrumentation paper [46]. Figure 6 and Fig. 7 show the RDP, the standard deviation, and the SNR of the merged spectrum after including data from both the original scans and the rescans, respectively.

Since no candidates were found after the rescan, an upper limit on the signal power  $P_s$  is derived by setting  $P_s$  equal to  $5\sigma_g^{\rm merged} \times P_g^{\rm KSVZ}$ , where the  $\sigma_g^{\rm merged}$  and  $P_g^{\rm KSVZ}$  are the standard deviation and the expected signal power for the KSVZ axion for a certain frequency bin g in the merged spectrum. Then, the 95% C.L. limits on the dimensionless parameter  $|g_{\gamma}|$  and the axion-two-photon coupling  $|g_{a\gamma\gamma}|$  could be derived according to Eq. (2) and Eq. (1). See Sec. VII for the final limits including the systematic uncertainties.



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FIG. 6. The merged RDP  $\delta$  following Eq. (21) (upper) and the standard deviation  $\sigma$  derived from Eq. (22) (lower). The results shown were obtained using data from both the original scans and the rescans.

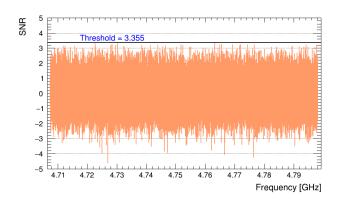


FIG. 7. The signal-to-noise ratio (SNR) calculated using Eq. (23) for the merged spectrum including data from both the original scans and the rescans. No candidate exceeds the threshold of  $3.355\sigma$ (solid-black horizontal line).

#### ANALYSIS OF THE SYNTHETIC AXION DATA 422

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After TASEH finished collecting the CD102 data on November 15, 2021, the synthetic 423 axion signals were injected into the cavity and read out via the same transmission line 424 and amplification chain. The procedure to generate axion-like signals is summarized in 425 Ref. [46]. Due to the uncertainties on the losses of readout electronics and transmission 426 lines, the synthetic axion signals were not used to perform an absolute calibration of the search sensitivity. Instead, a test with synthetic axion signals could be used to verify the 428 procedures of data acquisition and physics analysis. The signal-to-noise ratio (SNR) of the 429 frequency bin with maximum power from the synthetic axion signals, at 4.708970 GHz, was 430 set to  $\approx 3.35\sigma$ , corresponding to a power of  $\approx 6.03 \times 10^{-13}$  W in a 1-kHz frequency bin. 431

The same analysis procedure as described in Sec. IV was applied to the data with synthetic 432 axion signals. Figure 8 presents the individual raw power spectra in 24 frequency scans. 433 Before combining the 24 spectra vertically, the SNR of the maximum-power bin is measured 434 to be  $3.577\sigma$ ; the SNR is slightly higher than  $3.35\sigma$  due to a 5% difference in the noise 435 fluctuation between the measurements from the calibration and the measurements taken right before injecting axion-like signals. After the vertical combination of power spectra 437 and the merging of five frequency bins, the SNRs increase to  $4.74\sigma$  and  $6.12\sigma$ , respectively. 438 In addition to the injected synthetic axion signal, a candidate at 4.708006 GHz was found 439 after merging the spectra. Since it was not possible to perform a rescan later, the real axion 440

data from the two scans that had resonant frequencies close to the candidate frequency were added so to mimic the rescan; the candidate disappeared afterwards and is a statistical fluctuation. Figures 9– 10 present the spectra with the corresponding SNR, respectively, after combining the 24 spectra vertically and after merging five neighboring bins, including both the 24 scans of the synthetic axion data and the two scans of the real axion data. The analysis results of the synthetic axion signals prove that an power excess of more than  $5\sigma$ can be found at the expected frequencies via the standard analysis procedure.

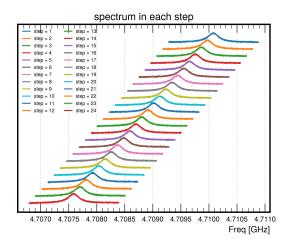


FIG. 8. The raw output power spectra, before applying the SG filter, from the 24 frequency steps
of the synthetic axion data. In order to show the spectra clearly, the spectra are shifted with
respect to each other with an arbitrary offset in the vertical scale.

#### 2 VI. SYSTEMATIC UNCERTAINTIES

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The systematic uncertainties on the  $|g_{a\gamma\gamma}|$  limits arise from the following sources:

- Uncertainty on the product  $Q_L\beta/(1+\beta)$  in Eq. (2): In order to extract the loaded quality factor  $Q_L$  and the coupling parameter  $\beta$ , a fitting of the measured results of the cavity scattering matrix was performed, which results in a relative uncertainty of 0.2% on this product.
- Uncertainty on the noise temperature  $T_a$  from the RMS of the measurements in the calibration:  $\Delta T_a/T_a = 2.3\%$  (see Sec. III and Fig. 1).

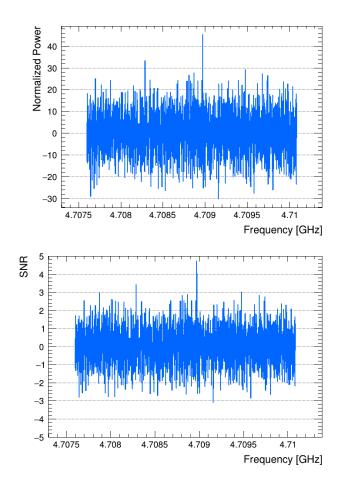


FIG. 9. The power (upper) and the signal-to-noise ratio (lower) after combining the spectra of the synthetic axion data with overlapping frequencies vertically. The procedure and the weights for combination are summarized in Sec. IV.

• Uncertainty on the noise temperature  $T_a$  from the largest difference between the value determined by the calibration and that from the axion data:  $\Delta T_a/T_a = 4\%$  (see Sec. III and Fig. 1).

• Uncertainty from the choice of the SG-filter parameters: i.e. the window width and the order of the polynomial in the SG filter. At the beginning of the data taking, a preliminary optimization was performed: a window width of 201 bins and a 4<sup>th</sup> order polynomial were used for the first analysis of the CD102 data (see Sec. IV). This choice was kept for the central results. Nevertheless, various methods of optimization were also explored. The goal of the optimization is to find a set of SG-filter parameters that only model the noise spectrum and do not remove a real signal. The methods include:

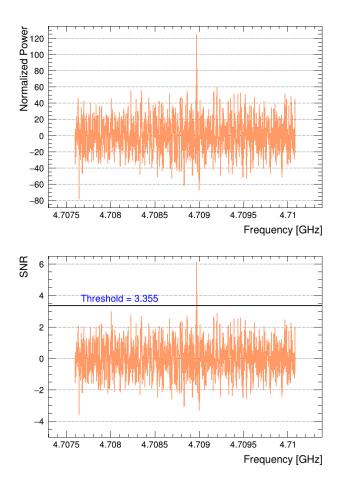


FIG. 10. The power (upper) and the signal-to-noise ratio (lower) after merging the power measured in five neighboring frequency bins of the synthetic axion data. The procedure and the weights for merging are summarized in Sec. IV.

- Minimize the difference between the two functions returned by the SG filter, when the SG filter is applied to: (i) the real data only, and (ii) the sum of the real data and a simulated axion signal.
- Minimize the difference between the function returned by the SG filter and the input noise function (including the Lorentzian distribution due to the cavity noise), when the SG filter is applied to a spectrum that includes the simulation of the axion signal and the simulation based on the input noise function. See Fig. 11 for a comparison of the simulated spectrum, input noise function, and the function returned by the SG filter when a 3<sup>rd</sup>-order polynomial and a window of 141 bins are chosen; the differences from all the frequency bins are summed

together when performing the optimization. Figure 12 shows the difference as a function of window widths when the order of polynomial is set to three, four, and six.

– Compare the mean  $\mu_{\text{noise}}$  and the width  $\sigma_{\text{noise}}$  of the measured power, assuming no signal is present in the data. See Fig. 13 for an example distribution of the measured power from the averaged spectrum of a single scan, when the cavity resonant frequency is 4.798147 GHz; a Gaussian fit is performed to extract  $\mu_{\text{noise}}$  and  $\sigma_{\text{noise}}$ . Given the nature of the thermal noise, the two variables are supposed to be related to each other if proper window width and order are chosen:

$$\sigma_{\text{noise}} = \frac{\mu_{\text{noise}}}{\sqrt{N_{\text{spectra}}}},$$

where  $N_{\text{spectra}}$  is the number of spectra for averaging and is related to the amount of integration time for each frequency step. In general,  $N_{\text{spectra}} = 1920000 - 2520000$ .

In addition, one could choose to optimize for each frequency step individually, optimize for a certain frequency step but apply the results to all data, or optimize by adding all the frequency steps together. Figure 14 shows that the deviations from the central results using different optimization approaches are in general within 1% and the maximum deviation of 1.8% on the  $|g_{a\gamma\gamma}|$  limit is used as a conservative estimate of the systematic uncertainty from the SG filter.

The first source of the systematic uncertainty has negligible effect on the limits of  $|g_{a\gamma\gamma}|$  while the latter three sources are studied and added in quadrature to obtain the total systematic uncertainty. The systematic uncertainties on the  $|g_{a\gamma\gamma}|$  limits are displayed together with the central results in Sec. VII. Overall the total relative systematic uncertainty is  $\approx 3.4\%$ .

#### 497 VII. RESULTS

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Figure 15 shows the limits on the axion-two-photon coupling  $|g_{a\gamma\gamma}|$  and the ratio of the limits on the dimensionless parameter  $|g_{\gamma}|$  with respect to the KSVZ benchmark value  $(|g_{KSVZ}| = 0.97)$ . The blue error band indicates the systematic uncertainties as discussed

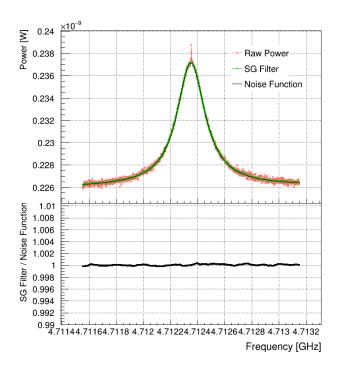


FIG. 11. Upper panel: The simulated spectrum, including the axion signal and the noise, is overlaid with the input noise function and the function returned by the SG filter. Lower panel: The ratio of the function returned by the SG filter to the input noise function.

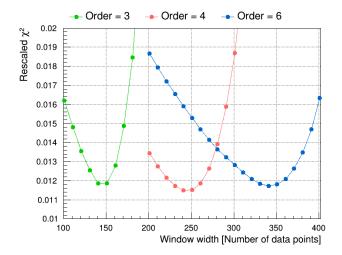


FIG. 12. The difference between the function returned by the SG filter and the input noise function, when various values of window widths and a 3<sup>rd</sup>, a 4<sup>th</sup>, or a 6<sup>th</sup>-order polynomial are applied in the SG filter. In this figure, the best choice is a 4<sup>th</sup>-order polynomial with a window width of 241 data points (bins).

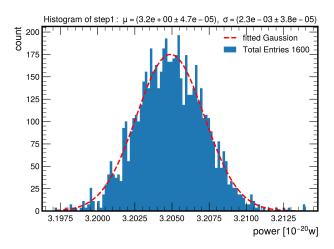


FIG. 13. An example of the distribution of the measured power, after removing the receiver gain and applying the SG filter, when the cavity resonant frequency is 4.798147 GHz. The distribution contains 1600 entries and each entry corresponds to the measured power in one frequency bin, averaged over 1920000 subspectra. The mean and the width returned by a Gaussian fit to the distribution are used to determine the best choice of SG parameters. The mean  $\mu_{\text{noise}} = 3.2 \times 10^{-20} \text{ W}$  in a 1-kHz frequency bin would imply a noise temperature of 2.3 K.

in Sec. VI. No limits are placed for the frequency ranges of 4.710170 - 4.710190 GHz and 4.747301 – 4.747380 GHz, which correspond to the external signal from the instruments in the laboratory during the collection of the CD102 data. The limits on  $|g_{a\gamma\gamma}|$  range from  $4.4 \times 10^{-14}$  to  $8.3 \times 10^{-14}$ , with an average value of  $7.7 \times 10^{-14}$ ; the lowest value comes from the frequency bins with additional eight times more data from the rescans, while the highest 505 value comes from the frequency bins near the boundaries of the spectrum. Figure 16 displays 506 the limits on  $|g_{a\gamma\gamma}|$  obtained by TASEH with those from the previous searches. The results of 507 TASEH exclude the models with the axion-two-photon coupling  $|g_{a\gamma\gamma}| \gtrsim 7.7 \times 10^{-14} \,\text{GeV}^{-1}$ , a 508 factor of ten above the benchmark KSVZ model for the mass range  $19.47 < m_a < 19.84 \,\mu\text{eV}$ 509 (corresponding to the frequency range of  $4.707506 < f_a < 4.798145$  GHz). 510

The central results shown in Figs. 15–16 were obtained assuming an axion signal line shape that follows Eq. (4). Both the analysis that merges bins without including a weight from the signal line shape  $[L_n = 1 \text{ in Eq. (19)}]$  and the one that assumes a simple Gaussian weight, with a mean at the center of the five frequency bins and a width  $\sigma$  giving half-maximum-weight when the frequency is 2.5 kHz away from the center, i.e.  $\sigma = 5 \text{ kHz} / 2\sqrt{2 \ln 2}$ ,

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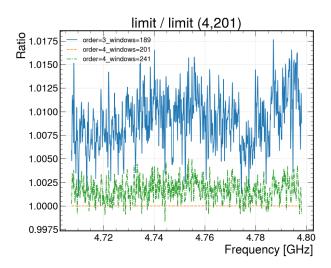


FIG. 14. The ratios of the limits on  $|g_{a\gamma\gamma}|$  due to the different choices of the window width and the order of polynomial in the SG filter, with respect to the central results (a window width of 201 bins and the 4<sup>th</sup>-order polynomial). The window width of 241 bins and the 4<sup>th</sup>-order polynomial were obtained from the optimization after injecting an axion signal on top of a simulated noise spectrum. The window width of 189 bins and the 3<sup>rd</sup>-order polynomial were obtained from the optimization after comparing the means and the widths of the measured power distributions.

produce limits that are 5-6% higher than the central results (see Fig. 17). 516

#### **CONCLUSION** VIII.

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This paper presents the first results of a search for axions for the mass range 19.47 < 518  $m_a < 19.84\,\mu\mathrm{eV}$ , using the CD102 data collected by the Taiwan Axion Search Experiment 519 with Haloscope from October 13, 2021 to November 15, 2021. Apart from the external 520 signals, no candidates with a significance more than  $3.355\sigma$  were found. The experiment 521 excludes models with the axion-two-photon coupling  $|g_{a\gamma\gamma}| \gtrsim 7.7 \times 10^{-14} \, \text{GeV}^{-1}$ , a factor of 522 ten above the benchmark KSVZ model. This is the first time that constraints on the  $|g_{a\gamma\gamma}|$ are placed in this mass region. The synthetic axion signals were injected after the collection of data and the successful results validate the data acquisition and the analysis procedure. 525 The target of TASEH is to search for axions for the mass range of  $16-40 \mu eV$ , correspond-526 ing to a frequency range of 3.9–9.7 GHz. In the coming years, several upgrades are expected, 527

including: the use of the Josephson parametric amplifier as the first-stage amplifier, the re-

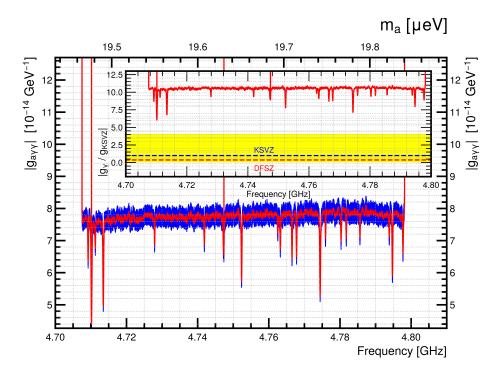


FIG. 15. The limits on  $|g_{a\gamma\gamma}|$  and the ratio of the limits on  $|g_{\gamma}|$  relative to  $|g_{KSVZ}| = 0.97$  (inset) for the frequency range of 4.707506–4.798145 GHz. The blue error band indicates the systematic uncertainties as discussed in Sec. VI. The yellow band in the inset shows the allowed region of  $|g_{\gamma}|$  vs.  $m_a$  from various QCD axion models, while the blue and red dashed lines are the values predicted by the KSVZ and DFSZ benchmark models, respectively

placement of the existing dilution refrigerator with a new one that has a magnetic field of 9 Tesla and a larger bore size, and the development of a new cavity with an effective volume reaching one liter. These upgrades will reduce the added noise by a factor of 10 and increase the magnetic field and the cavity volume by a factor of 1.125 and 5. With the improvements of the experimental setup and several years of data taking, TASEH is expected to probe the QCD axion photon band in the target mass range.

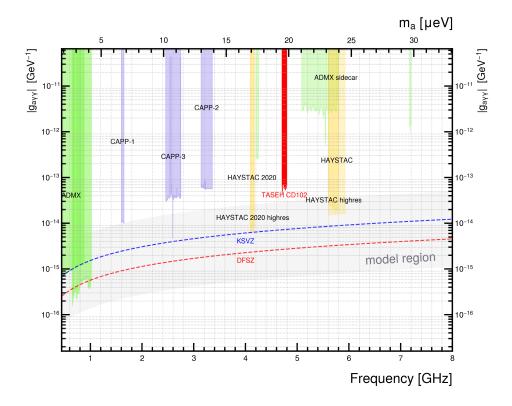


FIG. 16. The limits on the axion-two-photon coupling  $|g_{a\gamma\gamma}|$  for the frequency ranges of 0.4–8 GHz, from the CD102 data of TASEH and previous searches performed by the ADMX, CAPP, and HAYSTAC Collaborations. The gray band indicates the allowed region of  $|g_{a\gamma\gamma}|$  vs.  $m_a$  from various QCD axion models while the blue and red dashed lines are the values predicted by the KSVZ and DFSZ benchmark models, respectively.

#### ACKNOWLEDGMENTS

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#### Appendix A: The Derivation of the Noise Spectrum from the Cavity

The Hamiltonian of a single-mode cavity is

$$H = \hbar\omega_{\rm c}(C^{\dagger}C + \frac{1}{2}),\tag{A1}$$

where  $\omega_{\rm c}/2\pi$  is the cavity resonant frequency and C is the annihilation operator of the inner cavity field. The cavity field is coupled to the modes A of a transmission line with the rate  $\kappa_2$ . The cavity field is also coupled to the environment modes B with the rate  $\kappa_0$ . Based on the model of Fig. 18 and the input-output theory, the equation of motion for C is obtained:

$$\frac{dC}{dt} = -i\omega_{\rm c}C - \frac{\kappa_2 + \kappa_0}{2}C + \sqrt{\kappa_2}A_{\rm in} + \sqrt{\kappa_0}B_{\rm in}.$$
 (A2)

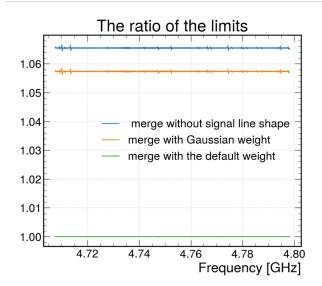


FIG. 17. The ratios of the limits on  $|g_{a\gamma\gamma}|$  from the merging without assuming a signal line shape (blue) and from the merging with a Gaussian weight (orange), with respect to the central results.

A boundary condition holds for the transmission modes:

$$A_{\text{out}} = \sqrt{\kappa_2 C - A_{\text{in}}}.$$
 (A3)

Considering working in a rotating frame of the signal frequency  $\omega$  near  $\omega_c$ , the equation of motion becomes:

$$-i\omega C + \frac{dC}{dt} = -i\omega_{\rm c}C - \frac{\kappa_2 + \kappa_0}{2}C + \sqrt{\kappa_2}A_{\rm in} + \sqrt{\kappa_0}B_{\rm in}.$$
 (A4)

The steady state solution for the cavity field is:

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$$C = \frac{\sqrt{\kappa_2 A_{\rm in} + \sqrt{\kappa_0 B_{\rm in}}}}{-i(\omega - \omega_c) + \frac{\kappa_2 + \kappa_0}{2}}.$$
 (A5)

By substituting Eq. (A5) into Eq. (A3), the reflected modes of the transmission line  $A_{\text{out}}$  are expressed in terms of the input modes of the transmission line  $A_{\text{in}}$  and the environment  $B_{\text{in}}$ :

$$A_{\text{out}} = \frac{i(\omega - \omega_{\text{c}}) + \frac{\kappa_{2} - \kappa_{0}}{2}}{-i(\omega - \omega_{\text{c}}) + \frac{\kappa_{2} + \kappa_{0}}{2}} A_{\text{in}} + \frac{\sqrt{\kappa_{2}\kappa_{0}}}{-i(\omega - \omega_{\text{c}}) + \frac{\kappa_{2} + \kappa_{0}}{2}} B_{\text{in}}$$

$$= \frac{-(\omega - \omega_{\text{c}})^{2} + \frac{\kappa_{2}^{2} - \kappa_{0}^{2}}{4} + i\kappa_{2}(\omega - \omega_{\text{c}})}{(\omega - \omega_{\text{c}})^{2} + (\frac{\kappa_{2} + \kappa_{0}}{2})^{2}} A_{\text{in}}$$

$$+ \frac{\sqrt{\kappa_{2}\kappa_{0}} \frac{\kappa_{2} + \kappa_{0}}{2} + i\sqrt{\kappa_{2}\kappa_{0}}(\omega - \omega_{\text{c}})}{(\omega - \omega_{\text{c}})^{2} + (\frac{\kappa_{2} + \kappa_{0}}{2})^{2}} B_{\text{in}}.$$
(A6)

Therefore, the autocorrelation of  $A_{\text{out}}$  is related to those of  $A_{\text{in}}$  and  $B_{\text{in}}$ :

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$$\langle A_{\text{out}}^{\dagger} A_{\text{out}} \rangle = \frac{\left[ (\omega - \omega_{\text{c}})^2 - \frac{\kappa_2^2 - \kappa_0^2}{4} \right]^2 + \kappa_2^2 (\omega - \omega_{\text{c}})^2}{\left[ (\omega - \omega_{\text{c}})^2 + (\frac{\kappa_2 + \kappa_0}{2})^2 \right]^2} \langle A_{\text{in}}^{\dagger} A_{\text{in}} \rangle + \frac{\kappa_2 \kappa_0 (\frac{\kappa_2 + \kappa_0}{2})^2 + \kappa_2 \kappa_0 (\omega - \omega_{\text{c}})^2}{\left[ (\omega - \omega_{\text{c}})^2 + (\frac{\kappa_2 + \kappa_0}{2})^2 \right]^2} \langle B_{\text{in}}^{\dagger} B_{\text{in}} \rangle.$$
(A7)

The spectrum from the cavity  $S(\omega)$  is found to be related to the spectrum of the readout transmission line  $S_{\rm rt}(\omega)$  and the spectrum of the cavity environment  $S_{\rm cav}(\omega)$ :

$$S(\omega) = \frac{[(\omega - \omega_{c})^{2} - \frac{\kappa_{2}^{2} - \kappa_{0}^{2}}{4}]^{2} + \kappa_{2}^{2}(\omega - \omega_{c})^{2}}{[(\omega - \omega_{c})^{2} + (\frac{\kappa_{2} + \kappa_{0}}{2})^{2}]^{2}} S_{\text{rt}}(\omega) + \frac{\kappa_{2}\kappa_{0}(\frac{\kappa_{2} + \kappa_{0}}{2})^{2} + \kappa_{2}\kappa_{0}(\omega - \omega_{c})^{2}}{[(\omega - \omega_{c})^{2} + (\frac{\kappa_{2} + \kappa_{0}}{2})^{2}]^{2}} S_{\text{cav}}(\omega).$$
(A8)

As the the readout transmission line and the cavity environment are both in thermal states, i.e.  $S_{\rm rt}(\omega) = [n_{\rm BE}(T_{\rm rt}) + 1/2] \hbar \omega$  and  $S_{\rm cav}(\omega) = [n_{\rm BE}(T_{\rm cav}) + 1/2] \hbar \omega$ , where  $n_{\rm BE}$  is the mean photon number given by the Bose-Einstein distribution,  $S(\omega)$  is white if  $T_{\rm cav} = T_{\rm rt}$ , and Lorentzian if  $T_{\rm cav} \gg T_{\rm rt}$ .

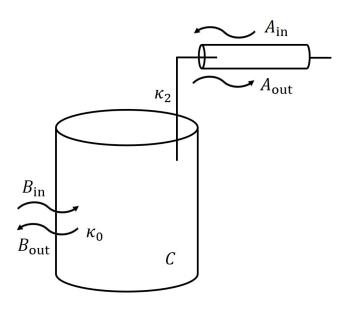


FIG. 18. A cavity is coupled to the modes of transmission line A with the rate  $\kappa_2$  and the modes of environment B with the rate  $\kappa_0$ .

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