

SHRI RAMDEOBABA COLLEGE OF ENGINEERING AND MANAGEMENT**NAME:TINA BORUNDIA****BATCH:C3****ROLL NO:65****EXPERIMENT NO:5****Experiment 5:Differential Calculus and its Application****Aim:to learn calculus with sagemath****1. LIMITS**PROBLEM:Find the limit of $\lim_{x \rightarrow 0} x/|x|$

```
In [2]: f(x)=x/abs(x)  
show(f(x))
```

$$\frac{x}{|x|}$$

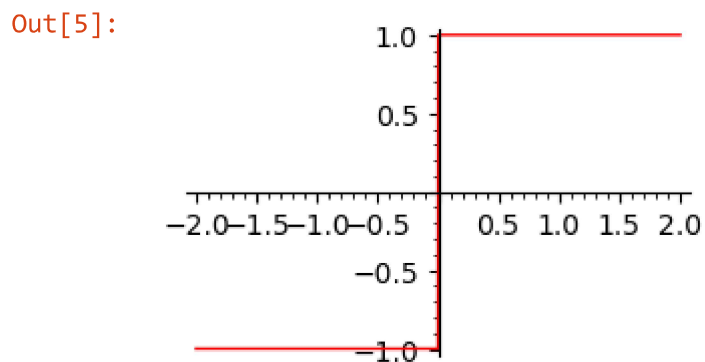
```
In [4]: limit(f(x),x=0)
```

```
Out[4]: und
```

```
In [5]: limit(f(x),x=0,dir='+')
```

```
Out[5]: 1
```

```
In [5]: f.plot(-2,2,figsize=3,color='red')
```

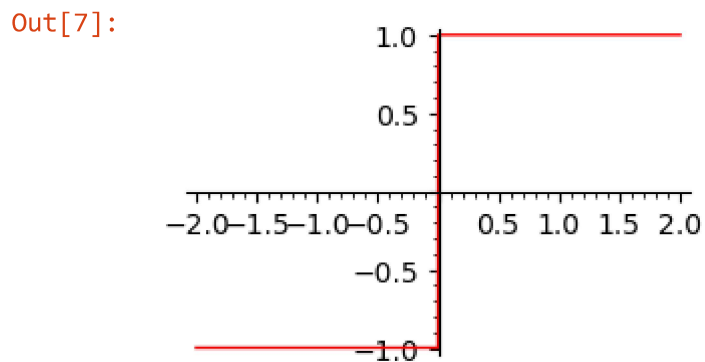


PROBLEM: Find the limit of $\lim_{x \rightarrow 2} (x^2 - 4)/(x - 2)$

```
In [6]: limit((x^2-4)/(x-2),x=2)
```

Out[6]: 4

```
In [7]:
```



PROBLEM: Evaluate $\lim_{x \rightarrow \infty} x^a$ for various values of a

```
In [7]: var('a')
        assume(a>0)
```

```
In [18]: limit(x^a,x=infinity)
```

Out[18]: +Infinity

```
In [21]: forget() #Assumption for 'a' are delete
```

```
In [ ]: assume(a<0)
```

```
In [8]: limit(x^a,x=infinity)
```

Out[8]: +Infinity

2.Derivative

In [1]: `f(x)=x^4`
`show(f(x))`

$$x^4$$

In [2]: `show(f(x).diff())`

$$4x^3$$

In [3]: `show(diff(f(x)))`

$$4x^3$$

In [4]: `show(diff(f(x),x))`

$$4x^3$$

In [5]: `show(diff(f(x),2))` *#double derivative*

$$12x^2$$

In [6]: `show(f(x).diff(2))`

$$12x^2$$

In [7]: `diff(f(x))(x=4)`

Out[7]: 256

In [8]: `show(diff(f(x),3))` *#triple derivative*

$$24x$$

In [9]: `diff(x^4,x,4)` *#four times derivative*

Out[9]: 24

In [10]: `show(diff(f(x),x,x,x))` *#triple derivative*

$$24x$$

In [11]: `var('x,y')`
`f(x,y)=x^3*y+(sin(y))*(cos(x))^2`
`show(f(x,y))`

$$x^3y + \cos(x)^2 \sin(y)$$

In [12]: `show(diff(f,x),x)` *#partially with resp to x*

$$(x, y) \mapsto 3x^2y - 2\cos(x)\sin(x)\sin(y)x$$

In [13]: `show(diff(f,x),y)` *#partially with resp to y*

$$(x, y) \mapsto 3x^2y - 2\cos(x)\sin(x)\sin(y)y$$

In [14]: `show(diff(f,x),x,y)` *#partially with resp to x then wrt y*

$$(x, y) \mapsto 3x^2y - 2\cos(x)\sin(x)\sin(y)xy$$

In [15]: `show(diff(f,x),y,x)` *#partially with resp to y then wrt x*

$$(x, y) \mapsto 3x^2y - 2\cos(x)\sin(x)\sin(y)yx$$

In [16]: `show(diff(f,x),y,y)` *##partially with resp to y twice*

$$(x, y) \mapsto 3x^2y - 2\cos(x)\sin(x)\sin(y)yy$$

In [17]: `show(diff(f,x),x,3,y,2)`

$$(x, y) \mapsto 3x^2y - 2\cos(x)\sin(x)\sin(y)x^3y^2$$

In [18]: `show(diff(f,x)(x=1,y=-1))`

$$2\cos(1)\sin(1)^2 - 3$$

In [19]: `show(diff(f,x,2,y,3)(x=1,y=-1))`

$$2\cos(1)^3 - 2\cos(1)\sin(1)^2$$

In [20]: `show(diff(f,x,5))` *#partially with resp to x ---5 times*

$$(x, y) \mapsto -32\cos(x)\sin(x)\sin(y)$$

In []: `=x^3` *#g for continous differential function*
`for i in range(0,3)`
`show(g.diff(i))`

Implicit Derivative

find the slope formula for the folium of Descartes implicitly defined by $X^3+y^3=6xy$. (Find dy/dx)

In [26]: `var('x,y')`
`f(x,y)= (x^3)+(y^3)-6*x*y`

```
In [27]: x=var('x')
y=var('y')
f(x,y)=x^3+y^3-6*x*y
y=function('y')(x)      # y is function of x
a=diff(f(x,y))
show(a)
```

$$3y(x)^2 \frac{\partial}{\partial x} y(x) + 3x^2 - 6x \frac{\partial}{\partial x} y(x) - 6y(x)$$

```
In [28]: solve(a,diff(y))
show(solve(a,diff(y)))
```

$$\left[\frac{\partial}{\partial x} y(x) = -\frac{x^2 - 2y(x)}{y(x)^2 - 2x} \right]$$

```
In [29]: g(x,y)=x^3+y^3-6*x*y
show(-diff(g,x)/diff(g,y))
```

$$(x, y) \mapsto -\frac{x^2 - 2y}{y^2 - 2x}$$

Local maxima and minimum

```
In [30]: var('f')
```

```
Out[30]: f
```

```
In [31]: f(x)=exp(-x/2)+exp(-2*x^2)
show(f(x))
```

$$e^{(-2x^2)} + e^{(-\frac{1}{2}x)}$$

```
In [ ]: plot(f(x),-2,2,figsize=3)
```

```
In [ ]: f.find_local_maximum(-1,0.5)
```

```
In [ ]: f.find_local_minimum(-2,4)
```

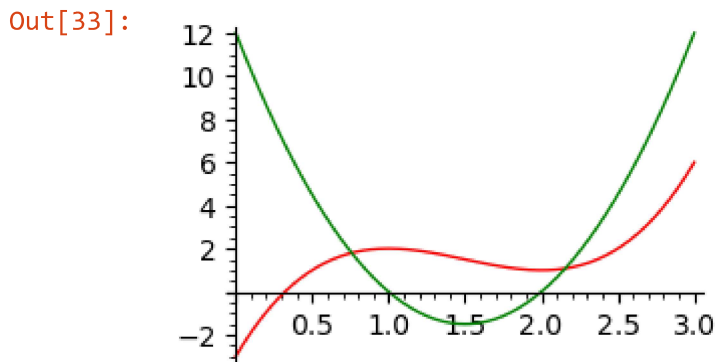
```
In [ ]: var('x,y')
f(x)=2*x^3-9*x^2+12*x-3
p1=plot(f,0,3,figsize=3,color='red')
show(p1)
```

find intervals on which f is increasing or decreasing

```
In [ ]: g(x)=f.diff()
show(g(x))
```

```
In [ ]: p2=plot(g,0,3,figsize=3,color='green')
show(p2)
```

```
In [33]: p1+p2
```



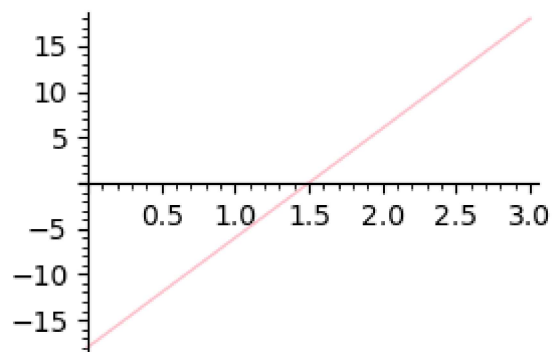
```
In [34]: solve(g(x),x)
```

Out[34]: [x == 1, x == 2]

```
In [35]: c=1
d=2
```

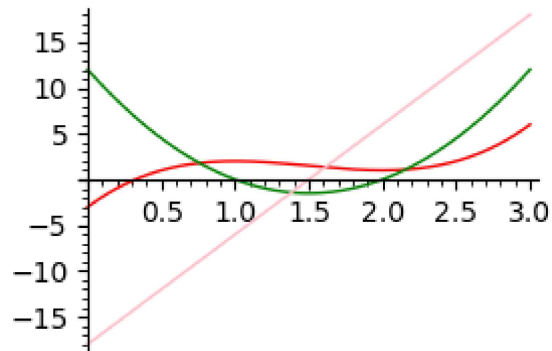
Therefor fun is increasing in the interval(0,1) and (2,3) as derivative is positive in these intervals. Function is decreasing in these intervals. Function is decreasing in the interval (1,2) as derivative is negative in this interval.

```
In [43]: h(x)=f.diff(2)
p3=plot(h,0,3,figsize=3,color='pink')
show(p3)
```



In [44]: `p1+p2+p3`

Out[44]:

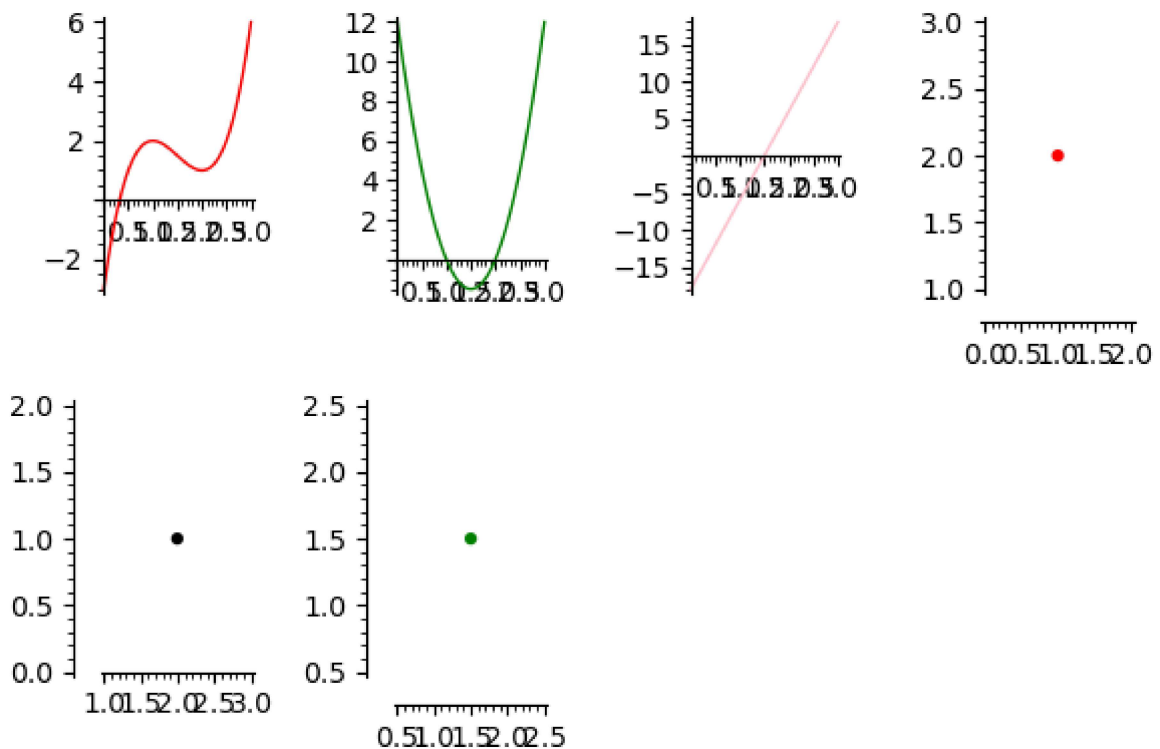


In [45]: `solve(h(x),x)`

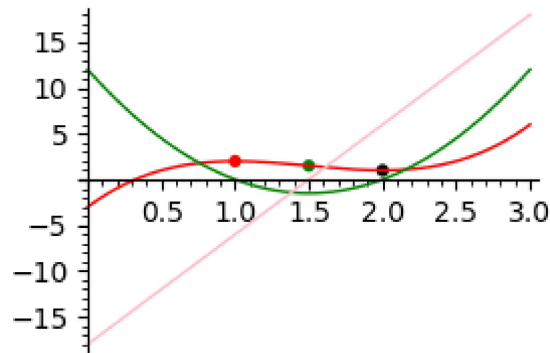
Out[45]: `[x == (3/2)]`

In [46]: `e=3/2`

In [48]: `p4=point((c,f(c)),color='red',size=20)`
`p5=point((d,f(d)),color='black',size=20)`
`p6=point((e,f(e)),color='green',size=20)`
`show(p1,p2,p3,p4,p5,p6)`



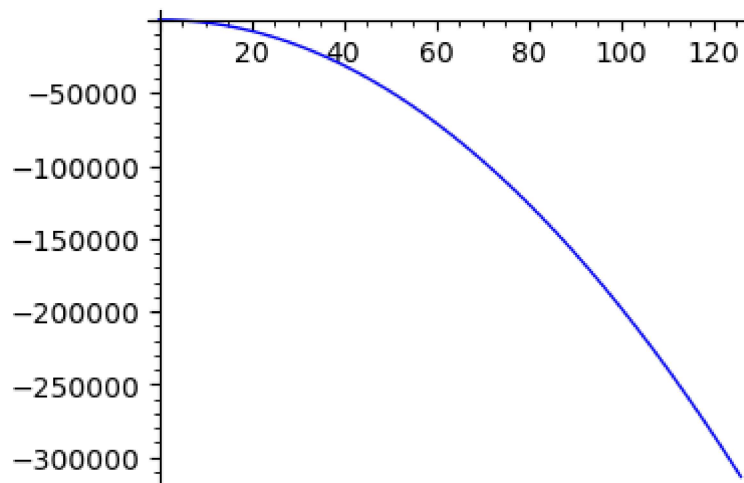
In [49]: `show(p1+p2+p3+p4+p5+p6)`



The hubble space telescope was developed was deployed on April 24, 1990 by the space shuttle discovery . A model for the velocity of the shuttle during this mission ,from liftoff at $t=0$ until he solid rocket boosters were jettisoned at $t=126$ sec, is given by $v(t)=0.001302t^3-20.09029t^2+23.61t-3.083$ Using this model ,estimate the absolute maximum and minimum values of the acceleration of the shuttle between liftoff and thw jettisoning of the booster.

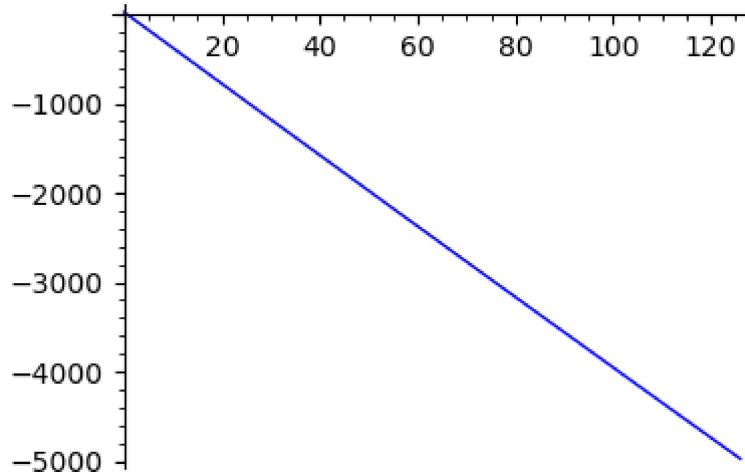
In [50]: `var('t')
v(t)=0.001302*t^3-20.09029*t^2+23.61*t-3.083
plot(v,0,126,figsize=4)`

Out[50]:




```
In [51]: a=v.diff()
a.plot(0,126,figsize=4)
```

Out[51]:



```
In [52]: a.find_local_minimum(0,126)
```

Out[52]: (-4977.131349515218, 125.9999980996971)

```
In [53]: a.find_local_maximum(0,126)
```

Out[53]: (23.609999727268548, 6.787643476263135e-09)

EXERCISE 3.35

QUE 1

```
In [1]: f(x)=(x^4)*e^(-x)
show(f(x))
```

$$x^4 e^{-x}$$

```
In [2]: f.find_local_maximum(-1,1)
```

Out[2]: (2.7182813252461533, -0.9999999629756616)

QUE 2

```
In [9]: # Let consider value of A and B be 1 and L be 10
```

```
In [7]: var('p,v')
p=v^3+(1/v)
d=diff(p,v)
show(d)
p=v^3+(100/v)
```

$$3v^2 - \frac{1}{v^2}$$

```
In [5]: p.find_local_minimum(-1,1)
```

```
Out[5]: (-59907451853.14301, -1.6692414200013008e-09)
```

CONCLUSION:

In this practical, I learned the to perform various differencial calculus operations such as finding limits and derivatives , maximum and minimum , derivatives of implicit functions and also the partial derivative value of a function ,using sageMath.

```
In [ ]:
```