

By definition, a PTAS with  $0 < \epsilon < 1$  generates a solution within a factor  $1 + \epsilon$  of the optimal value. Then we can prove that the rounding in the Bin Packing Problem does not lead to a PTAS by contradiction.

Suppose the rounding yields a result within  $(1 + \epsilon) * OPT$  for any instances. Then we construct a Bin Packing instance with  $2n$  items, each of which occupies  $s_i = 0.5$  space. The optimal solution is to have  $n$  bins, each packed with 2 items. Because the rounded value of the items are greater than 0.5, the approximation gives at least  $2n$  bins, which is twice the optimal value.  $1 + \epsilon \geq 2$  leads to  $\epsilon \geq 1$ , which contradicts the assumption that  $0 < \epsilon < 1$ .

(Discussed with Diqu Zhou)