

CPE381 #3

GEOMETRIC SERIES

$$a + a \cdot r + ar^2 + \dots + ar^{n-1} = \sum_{k=0}^{n-1} ar^k = a \cdot \frac{1-r^n}{1-r}$$

$$\sum_{n=0}^{\infty} 0.5^n = \frac{1-0.5^{\infty}}{1-0.5} = \frac{1-(\frac{1}{2})^{\infty}}{1-\frac{1}{2}} = \frac{1-\frac{1}{2^{\infty}}}{1-\frac{1}{2}} = \frac{1-\frac{1}{\infty}}{1-\frac{1}{2}} = 2$$

$(\frac{1}{2})^{\infty} = \frac{1}{2^{\infty}} = \frac{1}{\infty} \rightarrow 0$

ARITHMETIC SERIES

$$a_n = a_1 + (n-1) \cdot d$$

$$\sum_{i=1}^n a_i = n \cdot \frac{a_1 + a_n}{2}$$

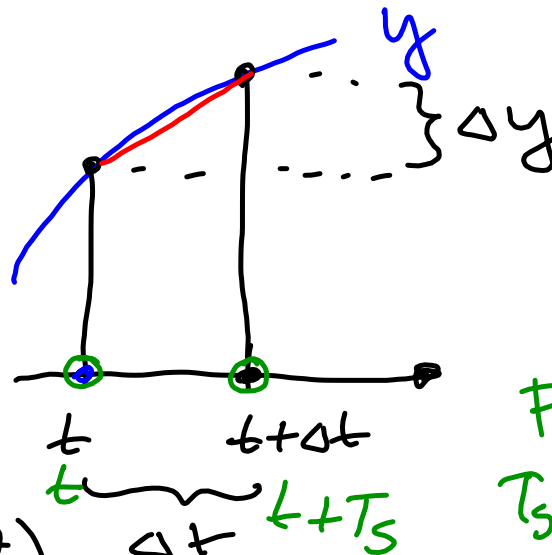
$$\Rightarrow 2, 5, 8, 11, 14$$

$$d=3$$

$$a_1=2$$

$$n=5$$

$$5 \cdot \frac{2+14}{2} = 5 \cdot 8 = 40$$

DIFFERENTIAL

$$y' = \lim_{\Delta t \rightarrow 0} \left(\frac{\Delta y}{\Delta t} \right)$$

$$\Delta t = T_s$$

$$F_s = 20 \text{ Hz}$$

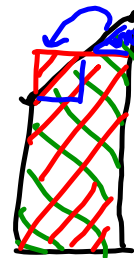
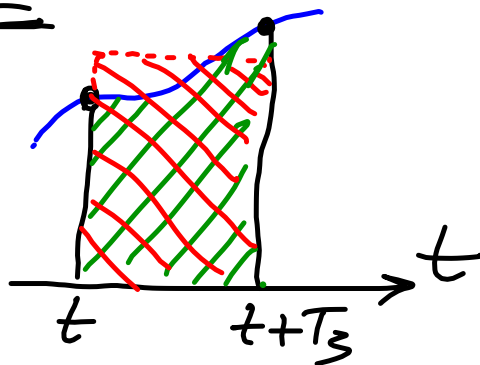
$$T_s = \frac{1}{F_s} = \frac{1}{20 \text{ Hz}} = 50 \text{ ms}$$

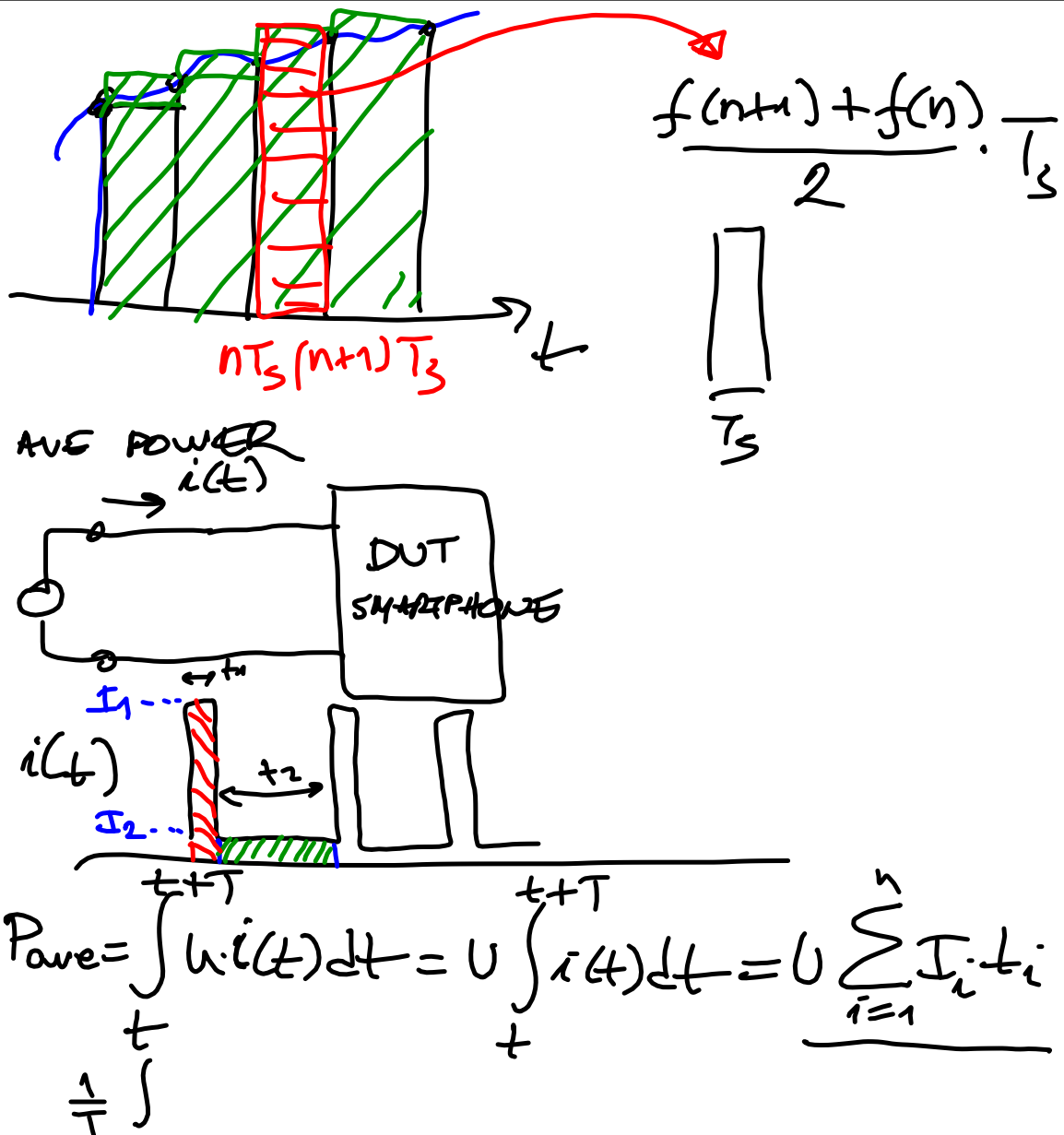
$$y' \approx \frac{y(t + T_s) - y(t)}{T_s}$$

$$\frac{1}{\text{Hz}} = \frac{1}{\frac{1}{\text{s}}} = \text{s}$$

INTEGRAL

$$\frac{\int_{t_1}^{t_2} y(t) dt}{t_2 - t_1} =$$

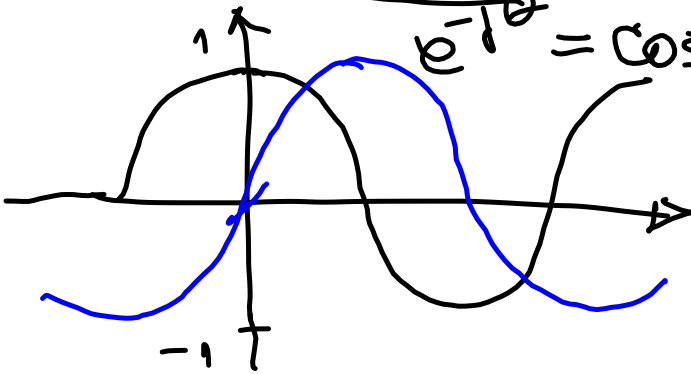




$$e^{j\theta} = \cos \theta + j \sin \theta$$

$$e^{-j\theta} = e^{j(-\theta)} = \cos(-\theta) + j \sin(-\theta)$$

$$e^{-j\theta} = \cos \theta - j \sin \theta$$



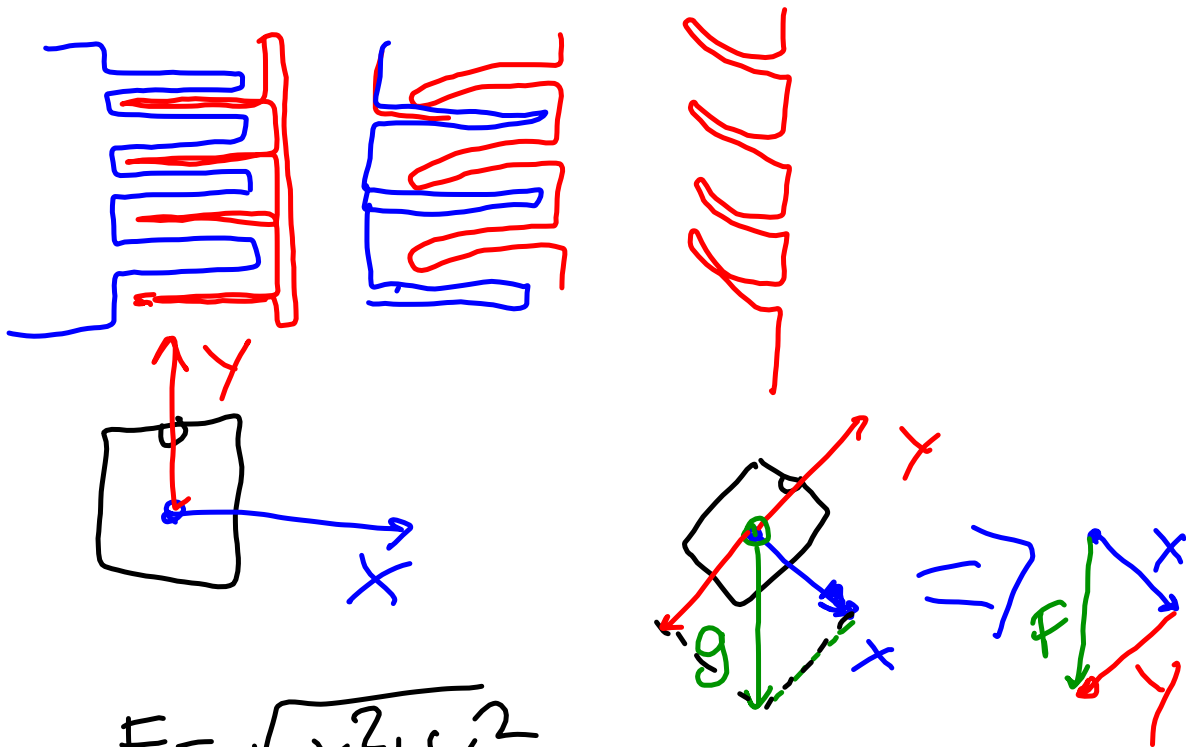
$$1 \quad e^{j\theta} = \cos \theta + j \sin \theta$$

$$2 \quad e^{-j\theta} = \cos \theta - j \sin \theta$$

$$+ \quad e^{j\theta} + e^{-j\theta} = 2 \cdot \cos \theta \Rightarrow \cos \theta = \frac{e^{j\theta} + e^{-j\theta}}{2}$$

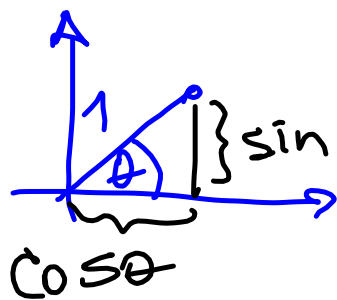
$$- \quad e^{j\theta} - e^{-j\theta} = 2j \sin \theta$$

$$\sin \theta = \frac{e^{j\theta} - e^{-j\theta}}{2j}$$



$$F = \sqrt{x^2 + y^2}$$

COMPLEX $z = \underbrace{x}_{\text{Real}} + j \underbrace{y}_{\text{Im}} = |z| e^{j\theta}$



$$1 \cdot e^{j\theta} = \cos \theta + j \sin \theta$$

$$\theta = \arctan\left(\frac{y}{x}\right)$$