



# **Lecture Qt014**

## **Graphics I**

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# Outline

- QPainter and QPixmap Classes
- Aliasing
- Graphics Examples
- Key Points

# QPainter Class

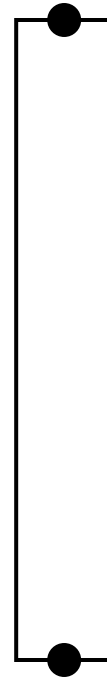
- Basics of 2-D graphics in Qt
- Enables drawing of
  - Geometric shapes
    - Points, Lines, Rectangles, Polygons, Ellipses, Arcs, Chords, Curves
  - Text, Images, Pixmaps
- Transformations
  - Translation, rotations, scaling, etc.

# QPainter Class

- Methods include
  - drawPoint()
  - drawLine()
  - drawRect()
  - drawPolygon()
  - drawEllipse()
  - drawText()
  - drawPixmap()

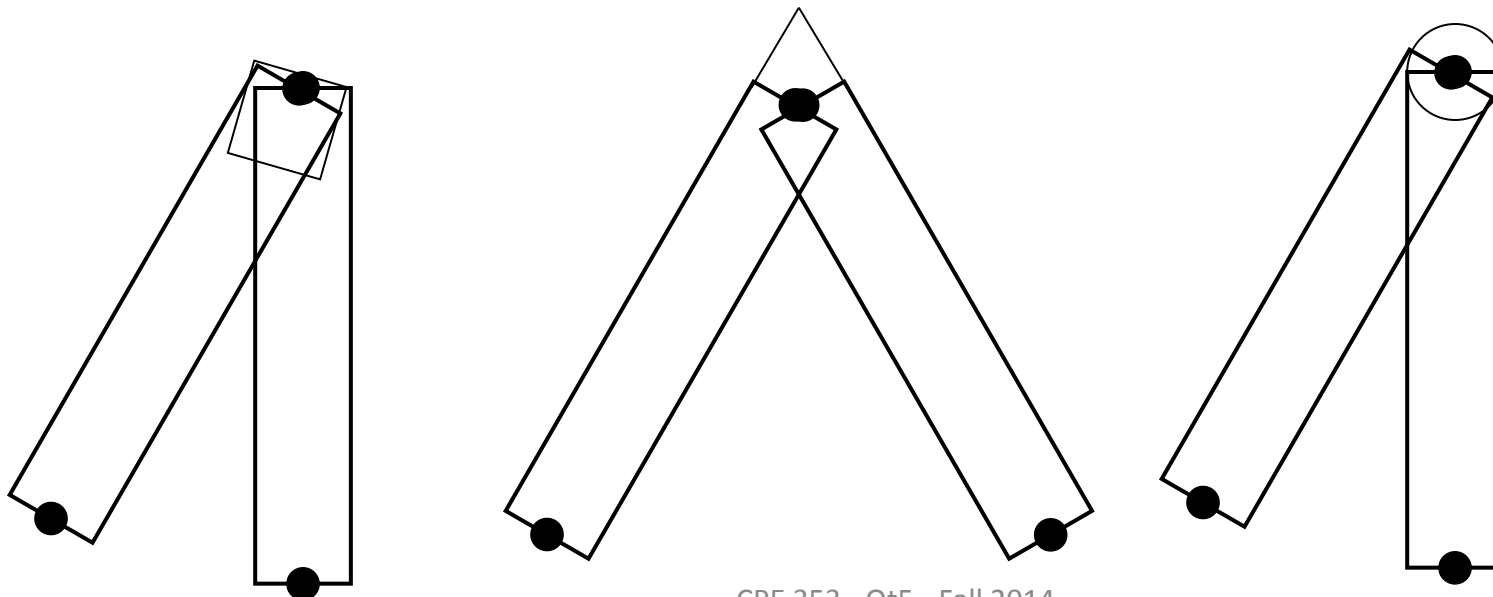
# QPainter Class

- Three key parameters to consider
  - **Pen** (QPen)
    - Color
      - Specified by `setColor(someColor)`
      - More on color
    - Width
      - Specified in pixels by `setWidth(someInt)` or `setWidthF(someReal)`
      - Retrieved as int by `width()` or real by `widthF()`
    - Line Style
      - Specified by `setStyle(someStyle)` using enumerated type `Qt::PenStyle` which includes values `Qt::SolidLine`, `Qt::DashLine`, `Qt::DotLine`, `Qt::DashDotLine`, etc.



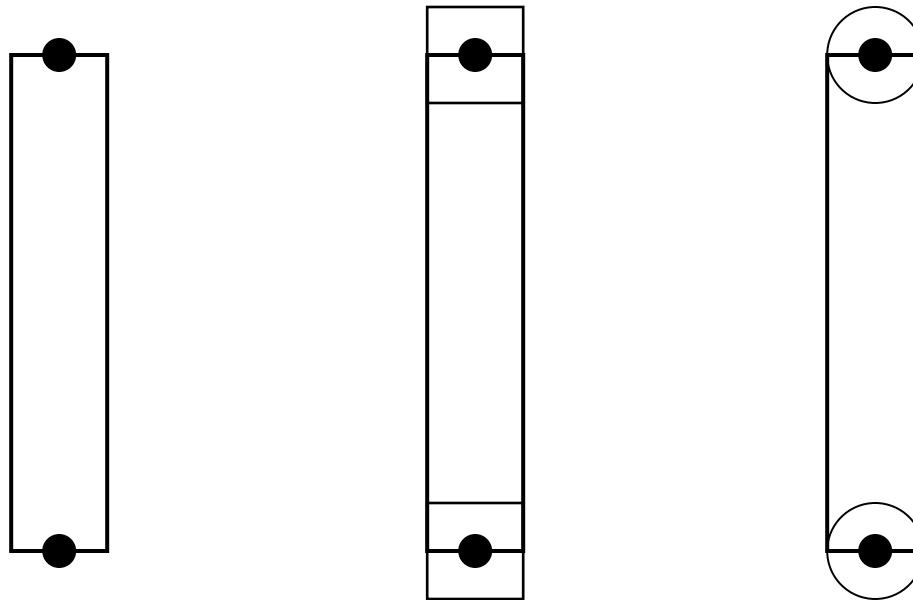
# QPainter Class

- Three key parameters to consider
  - **Pen** (QPen) continued
    - Join Style
      - Specified by `setJoinStyle(...)`
      - Beveled, Mitered, or Rounded line joints (`Qt::PenJoinStyle`)



# QPainter Class

- Three key parameters to consider
  - **Pen** (QPen) continued
    - Cap Style
      - Specified by `setCapStyle(...)`
      - Flat, Square, or Rounded endcaps (`Qt::PenCapStyle`)



# QPainter Class

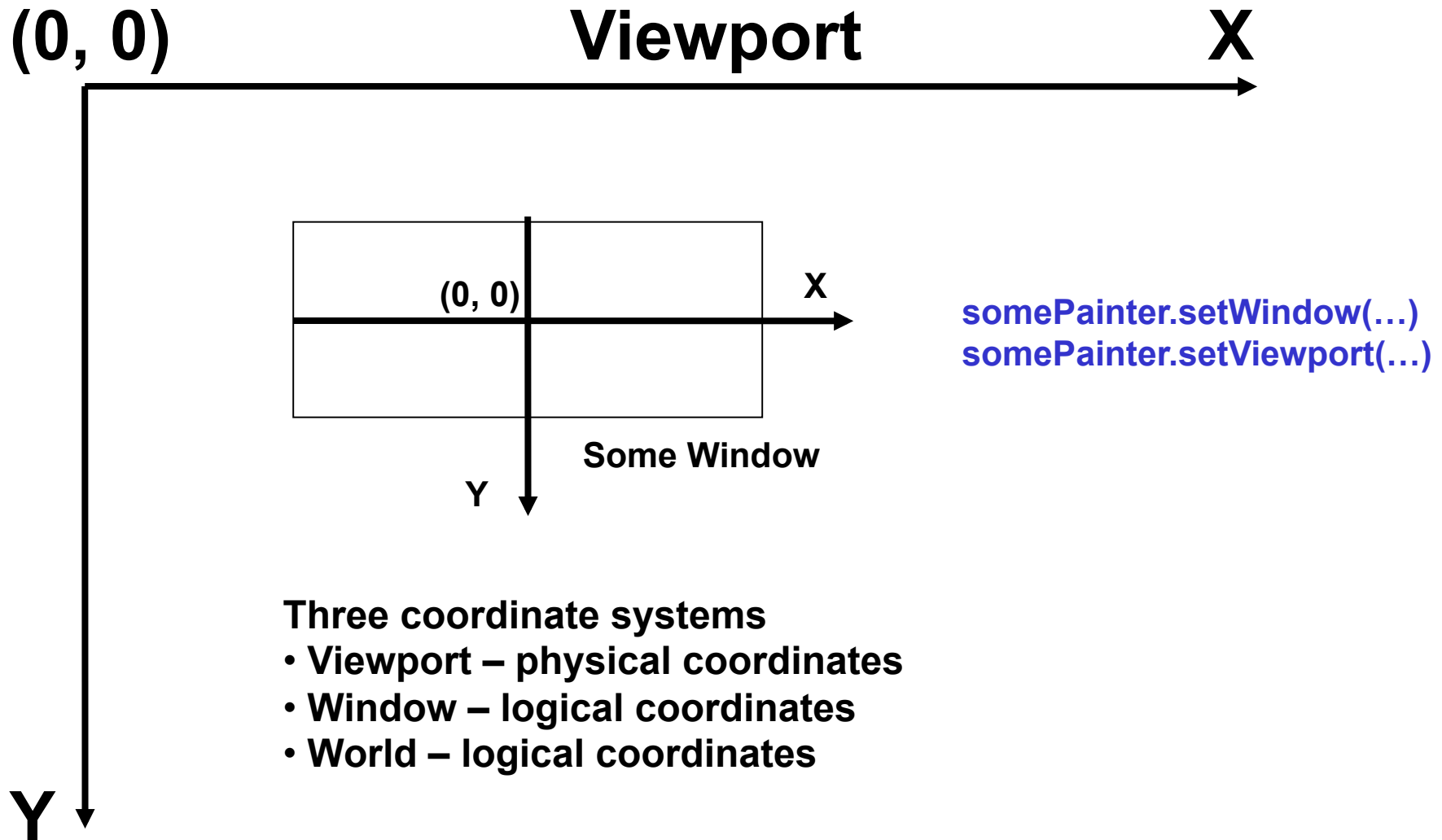
- Three key parameters to consider (continued)
  - **Brush** (QBrush)
    - Specified by `setBrush(...)`
    - Enumerated type `Qt::BrushStyle`
      - `Qt::SolidPattern`, `Qt::LinearGradientPattern`, `Qt::DiagCrossPattern`, etc



# QPainter Class

- Three key parameters to consider (continued)
  - **Font** (QFont)
    - Specified `setFont(...)`
    - Can select font name, point size, bold/italics/underline, etc.

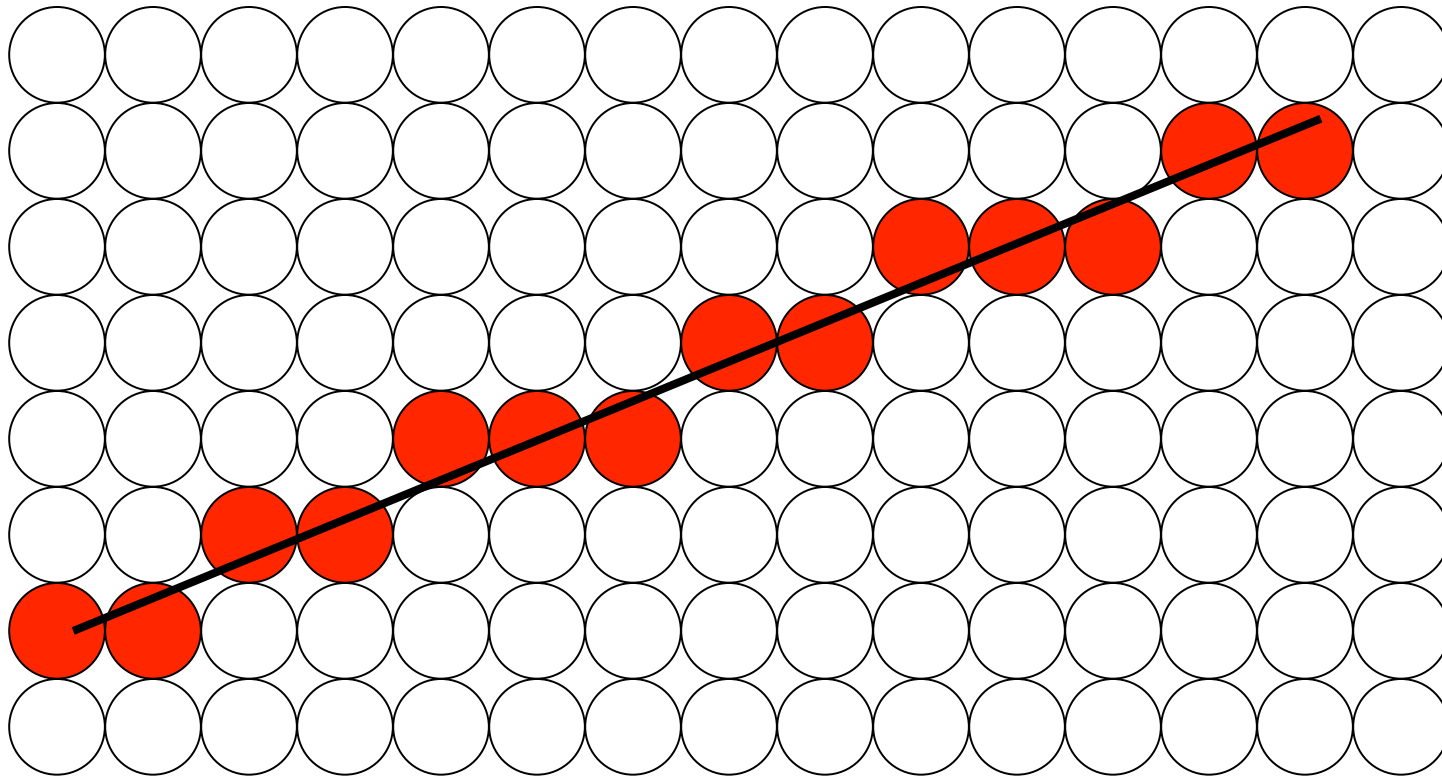
# QPainter Class



# QPixmap Class

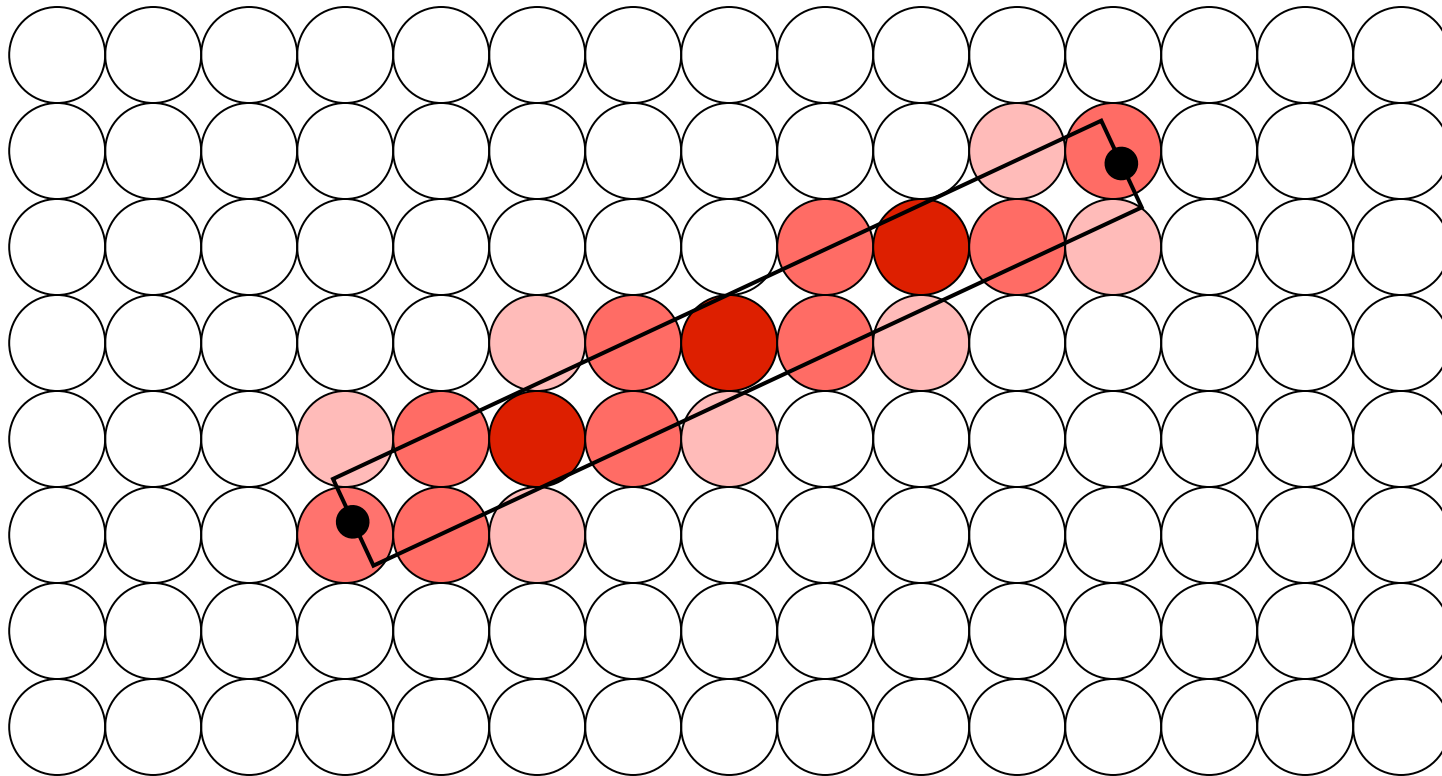
- One of four Qt classes used for images
- Optimized for on-screen image display
- Other classes include
  - **QImage**
    - Optimized for loading and saving of image data
  - **QPicture**
    - Recording & playback of **QPainter** commands

# Aliasing



Aliasing occurs when trying to use discrete sampling to render a continuous shape

# Aliasing



Many anti-aliasing strategies

-- here pixel intensity is proportional to amount of line overlap area

Suggestion – use built-in Qt anti-aliasing

# Graphics Example 01

- Goals
  - Create a rectangle object
  - Use it to draw an array of rectangles
  - Explore various pen options
    - Colors
    - Line Widths
    - Cap styles
    - Join styles
    - Lines styles
    - Brush styles

# Graphics Example 01

```
//
// Graphics Example 01
//
#include <QApplication>
#include <QPainter>
#include <QPixmap>
#include <QPen>
#include <QBrush>
#include <QRect>
#include <QLabel>

int main(int argc, char* argv[])
{
    QApplication myApp(argc, argv);           // Need application for event loop

    QPixmap myMap(400, 300);                  // Establish 400 X 300 pixel pixmap

    QPainter p(&myMap);
    p.setRenderHint(QPainter::Antialiasing, true); // Enable antialiasing

    // Draw frame just within perimeter
    p.setPen(QPen(Qt::black, 2, Qt::SolidLine, Qt::SquareCap));
    p.drawRect(10, 10, 380, 280);             // At (10, 10) with width=380, height=280

    // Vary Cap Style
    p.setPen(QPen(Qt::blue, 10, Qt::SolidLine, Qt::SquareCap));
    QRect rect1(25, 25, 50, 30);              // At (25, 25) with width=50, height=30
    p.drawRect(rect1);

    p.setPen(QPen(Qt::red, 10, Qt::SolidLine, Qt::RoundCap));
    rect1.translate(100, 0);                   // dx = 100, dy = 0
    p.drawRect(rect1);

    p.setPen(QPen(Qt::green, 10, Qt::SolidLine, Qt::FlatCap));
    rect1.translate(100, 0);                   // dx = 100, dy = 0
    p.drawRect(rect1);
```

# Graphics Example 01

```
// Graphics Example 01 - continued
```

```
// Vary Join Style
```

```
p.setPen(QPen(Qt::blue, 10, Qt::SolidLine, Qt::FlatCap, Qt::MiterJoin));  
rect1.translate(-200, 75); // dx = -200, dy = 75  
p.drawRect(rect1);
```

```
p.setPen(QPen(Qt::red, 10, Qt::SolidLine, Qt::FlatCap, Qt::BevelJoin));  
rect1.translate(100, 0);  
p.drawRect(rect1);
```

```
p.setPen(QPen(Qt::green, 10, Qt::SolidLine, Qt::FlatCap, Qt::RoundJoin));  
rect1.translate(100, 0);  
p.drawRect(rect1);
```

```
// Vary Line Style
```

```
p.setPen(QPen(Qt::blue, 2, Qt::DashLine, Qt::SquareCap));  
rect1.translate(-200, 75);  
p.drawRect(rect1);
```

```
p.setPen(QPen(Qt::red, 2, Qt::DotLine, Qt::RoundCap));  
rect1.translate(100, 0);  
p.drawRect(rect1);
```

```
p.setPen(QPen(Qt::green, 2, Qt::DashDotLine, Qt::FlatCap));  
rect1.translate(100, 0);  
p.drawRect(rect1);
```



# Graphics Example 01

```
// Graphics Example 01 - continued
```

```
// Vary Brush Style
p.setPen(QPen(Qt::blue, 2, Qt::SolidLine, Qt::SquareCap));
p.setBrush(QBrush(Qt::blue, Qt::SolidPattern));
rect1.translate(-200, 75);
p.drawRect(rect1);

p.setPen(QPen(Qt::red, 2, Qt::SolidLine, Qt::RoundCap));
p.setBrush(QBrush(Qt::red, Qt::DiagCrossPattern));
rect1.translate(100, 0);
p.drawRect(rect1);

p.setPen(QPen(Qt::green, 2, Qt::SolidLine, Qt::FlatCap));
p.setBrush(QBrush(Qt::green, Qt::VerPattern));
rect1.translate(100, 0);
p.drawRect(rect1);

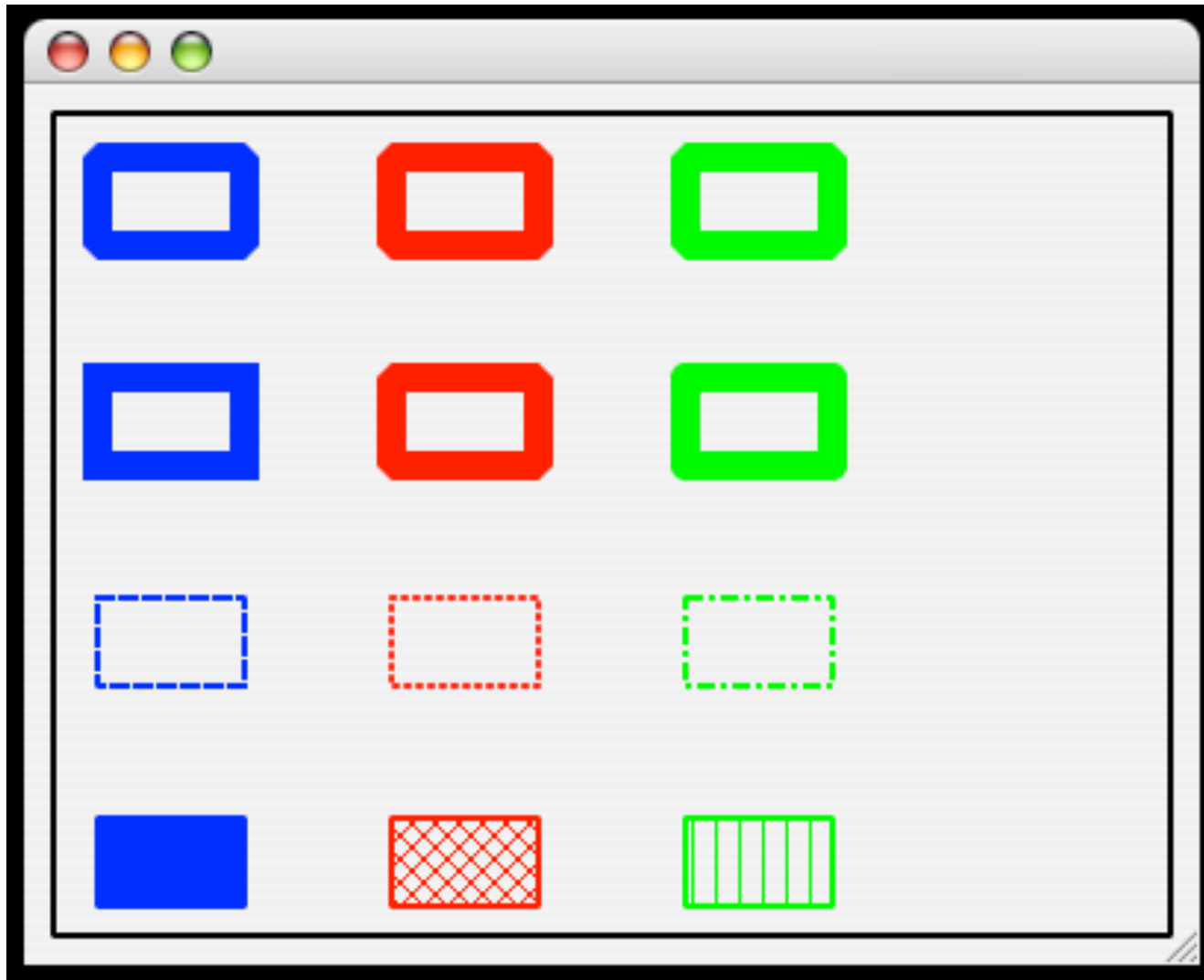
QLabel myLabel;
myLabel.setPixmap(myMap);
myLabel.show();

return myApp.exec();
} // End main()

// Allocate a Gui widget
// Associate pixmap with Gui widget
// Make widget visible

// Initiate event loop
```

# Graphics Example 01



# Graphics Example 02

- Goals
  - Draw crosshairs using an ellipse, four points, and two lines
  - Add text to pixmap
  - Draw four arcs

# Graphics Example 02

```
//  
// Graphics Example 2  
//  
#include <QApplication>  
#include <QPainter>  
#include <QPixmap>  
#include <QPen>  
#include <QBrush>  
#include <QRect>  
#include <QPoint>  
#include <QLine>  
#include <QFont>  
#include <QLabel>  
  
int main(int argc, char* argv[])  
{  
    QApplication myApp(argc, argv);           // Need application for event loop  
  
    QPixmap myMap(400, 300);                  // Establish pixmap  
    myMap.fill(Qt::black);  
  
    QPainter p(&myMap);  
    p.setRenderHint(QPainter::Antialiasing, true); // Enable antialiasing
```

# Graphics Example 02

```
// Graphics Example 2 -- continued

// Draw four points and two crosshair lines
p.setPen(QPen(Qt::red, 10, Qt::SolidLine, Qt::FlatCap));
QPoint p1(200, 25);
QPoint p2(200, 275);
QPoint p3(50, 150);
QPoint p4(350, 150);
p.drawPoint(p1);
p.drawPoint(p2);
p.drawPoint(p3);
p.drawPoint(p4);
p.setPen(QPen(Qt::white, 5, Qt::SolidLine, Qt::FlatCap));
QLine line1(p1, p2);
QLine line2(p3, p4);
p.drawLine(line1);
p.drawLine(line2);

// Define Bounding Rectangle, set pen, and draw ellipse
p.setPen(QPen(Qt::blue, 5, Qt::SolidLine, Qt::SquareCap));
QRect rect1(125, 75, 150, 150);
p.drawEllipse(rect1);

// Write text
p.setPen(Qt::red);
QPoint tp(300, 175);
p.drawText(tp, "Fire");
```

# Graphics Example 02

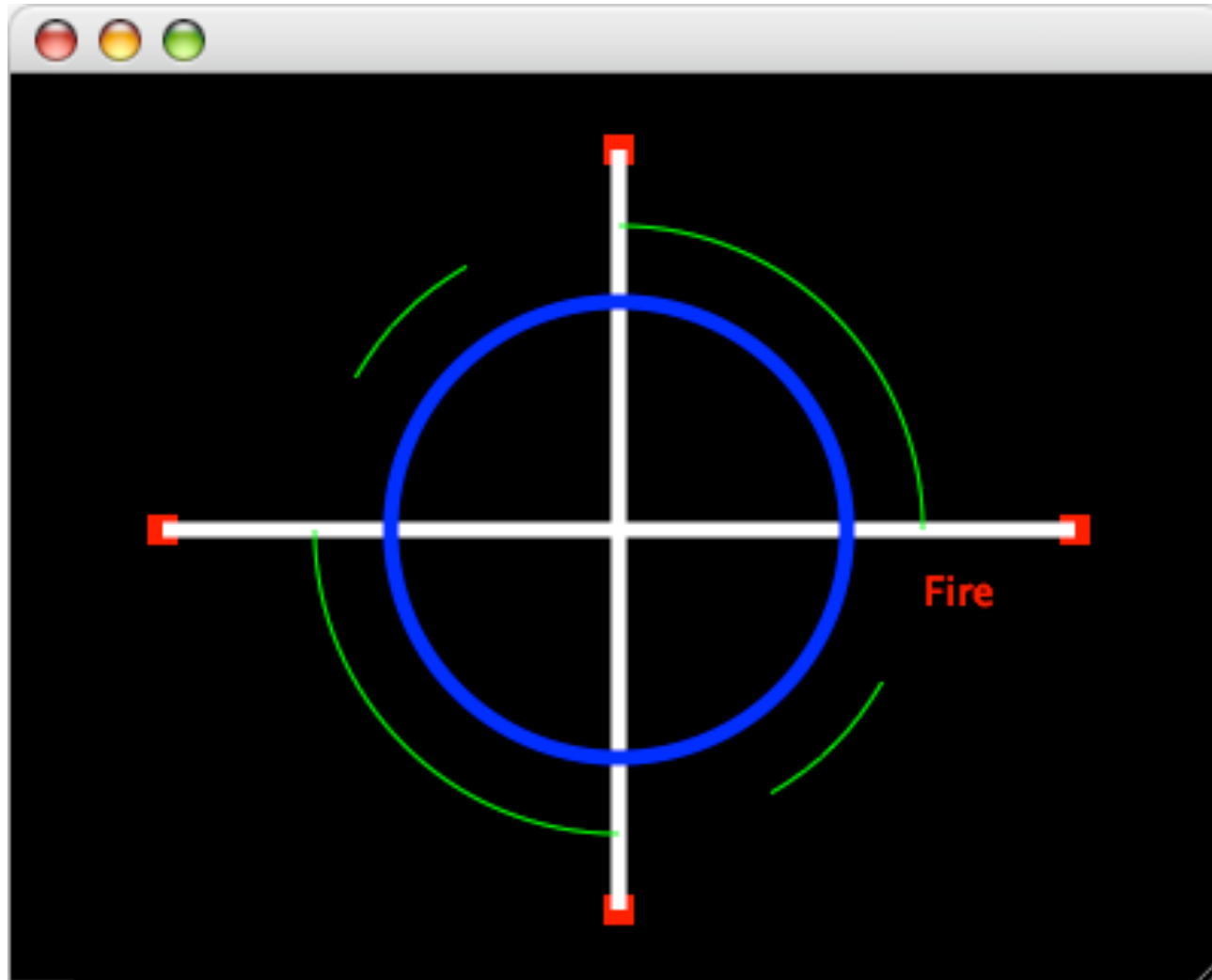
```
// Graphics Example 2 -- continued
```

```
// Draw arcs --- angles are 1/16 of a degree, hence the scale factor
p.setPen(Qt::green);
p.drawArc(QRect(100, 50, 200, 200), 00*16, 90*16);           // Rectangle defines ellipse
p.drawArc(QRect(100, 50, 200, 200), 180*16, 90*16);          // Arc needs start angle, span angle
p.drawArc(QRect(100, 50, 200, 200), 120*16, 30*16);
p.drawArc(QRect(100, 50, 200, 200), 300*16, 30*16);

QLabel myLabel;                                              // Allocate a Gui widget
myLabel.setPixmap(myMap);                                    // Associate pixmap with Gui widget
myLabel.show();                                              // Make widget visible

return myApp.exec();                                         // Initiate event loop
} // End main()
```

# Graphics Example 02



# Graphics Example 03

- Goals
  - Draw an arrow using a polygon
  - Translate and redraw arrow



# Graphics Example 03

```
//
// Graphics Example 3
//
#include <QApplication>
#include <QPainter>
#include <QPixmap>
#include <QPen>
#include <QBrush>
#include <QRect>
#include <QPoint>
#include <QLabel>

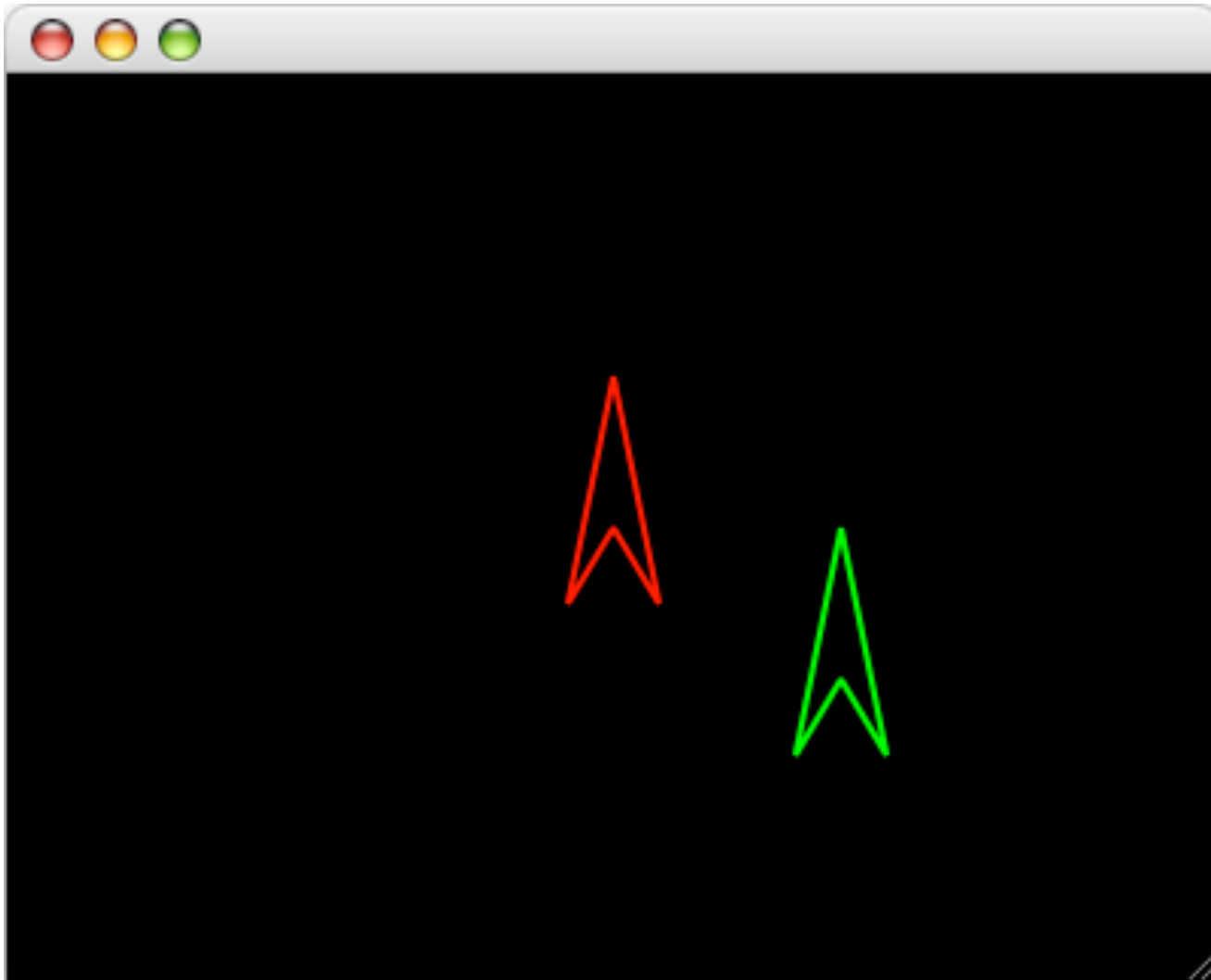
int main(int argc, char* argv[])
{
    QApplication myApp(argc, argv);           // Need application for event loop
    QPixmap myMap(400, 300);                  // Establish pixmap
    myMap.fill(Qt::black);
    QPainter p(&myMap);
    p.setRenderHint(QPainter::Antialiasing, true); // Enables antialiasing

    // Draw red arrow polygon
    p.setPen(QPen(Qt::red, 2, Qt::SolidLine, Qt::FlatCap));
    p.setBrush(QBrush(Qt::SolidPattern));
    QPoint points[4] = {QPoint(200, 100), QPoint(215, 175), QPoint(200, 150), QPoint(185, 175)};
    p.drawPolygon(points, 4);

    // Apply translation and redraw as green polygon
    p.translate(75, 50);                      // Translate dx = 75, dy = 50
    p.setPen(QPen(Qt::green, 2, Qt::SolidLine, Qt::FlatCap));
    p.drawPolygon(points, 4);

    QLabel myLabel;                          // Allocate a Gui widget
    myLabel.setPixmap(myMap);                 // Associate pixmap with Gui widget
    myLabel.show();                          // Make widget visible
    return myApp.exec();                     // Initiate event loop
} // End main()
```

# Graphics Example 03 - 2



# Graphics Example 04

- Goals
  - Draw an arrow using a polygon
  - Rotate by 30 degrees
  - Redraw arrow

# Graphics Example 04

```
//
// Graphics Example 4
//
#include <QApplication>
#include <QPainter>
#include <QPixmap>
#include <QPen>
#include <QBrush>
#include <QRect>
#include <QPoint>
#include <QLabel>

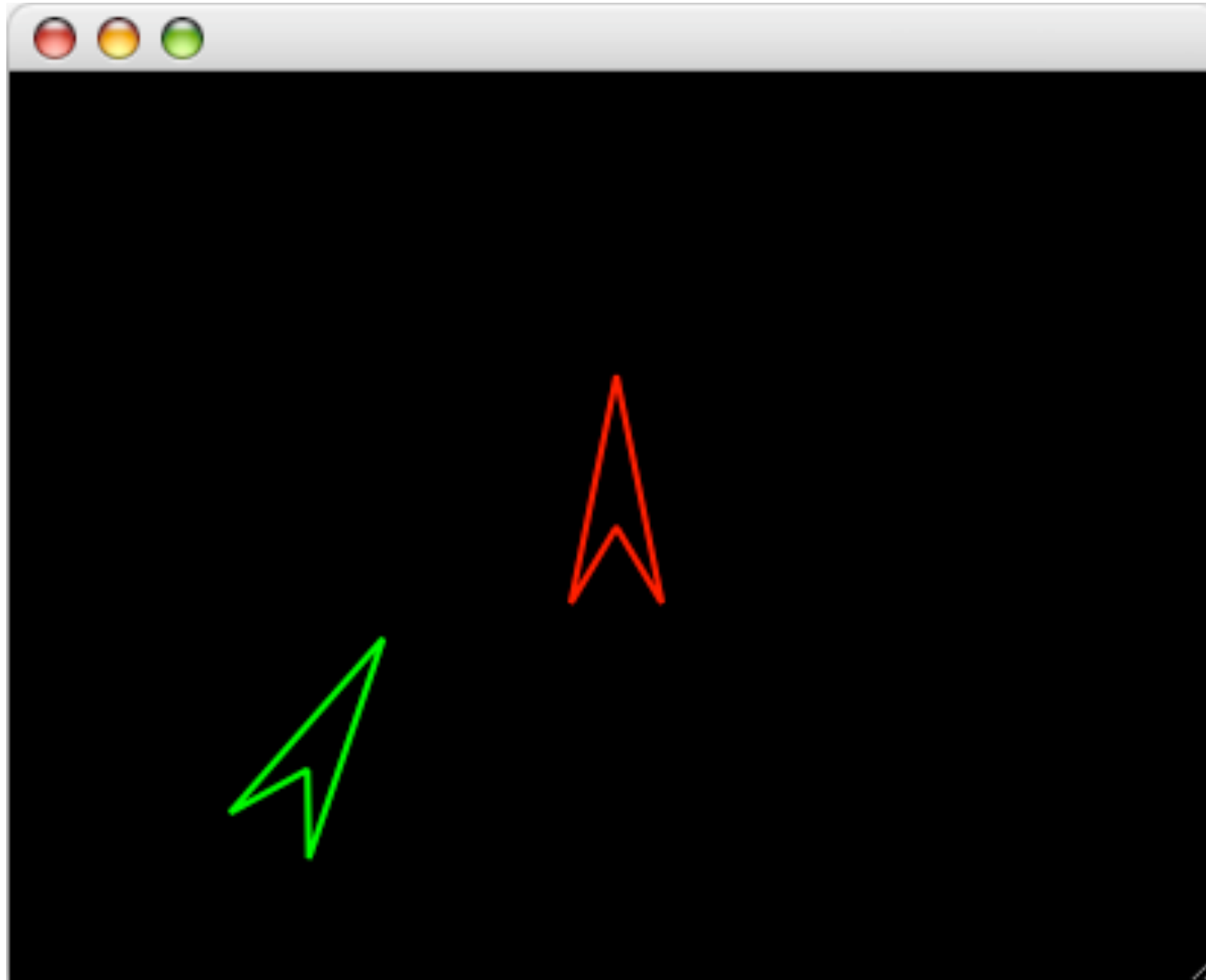
int main(int argc, char* argv[])
{
    QApplication myApp(argc, argv);           // Need application for event loop
    QPixmap myMap(400, 300);                  // Establish pixmap
    myMap.fill(Qt::black);
    QPainter p(&myMap);
    p.setRenderHint(QPainter::Antialiasing, true); // Enable antialiasing

    // Draw red arrow polygon
    p.setPen(QPen(Qt::red, 2, Qt::SolidLine, Qt::FlatCap));
    p.setBrush(QBrush(Qt::SolidPattern));
    QPoint points[4] = {QPoint(200, 100), QPoint(215, 175), QPoint(200, 150), QPoint(185, 175)};
    p.drawPolygon(points, 4);

    // Apply rotation and redraw as green polygon
    p.rotate(30);                             // Rotate 30 degrees
    p.setPen(QPen(Qt::green, 2, Qt::SolidLine, Qt::FlatCap));
    p.drawPolygon(points, 4);

    QLabel myLabel;                           // Allocate a Gui widget
    myLabel.setPixmap(myMap);                  // Associate pixmap with Gui widget
    myLabel.show();                           // Make widget visible
    return myApp.exec();                      // Initiate event loop
} // End main()
```

# Graphics Example 04



# Graphics Example 05

- Goals
  - Draw an arrow using a polygon
  - Scale coordinates by factor of 50%
  - Redraw arrow

# Graphics Example 05

```
//
// Graphics Example 5
//
#include <QApplication>
#include <QPainter>
#include <QPixmap>
#include <QPen>
#include <QBrush>
#include <QRect>
#include <QPoint>
#include <QLabel>

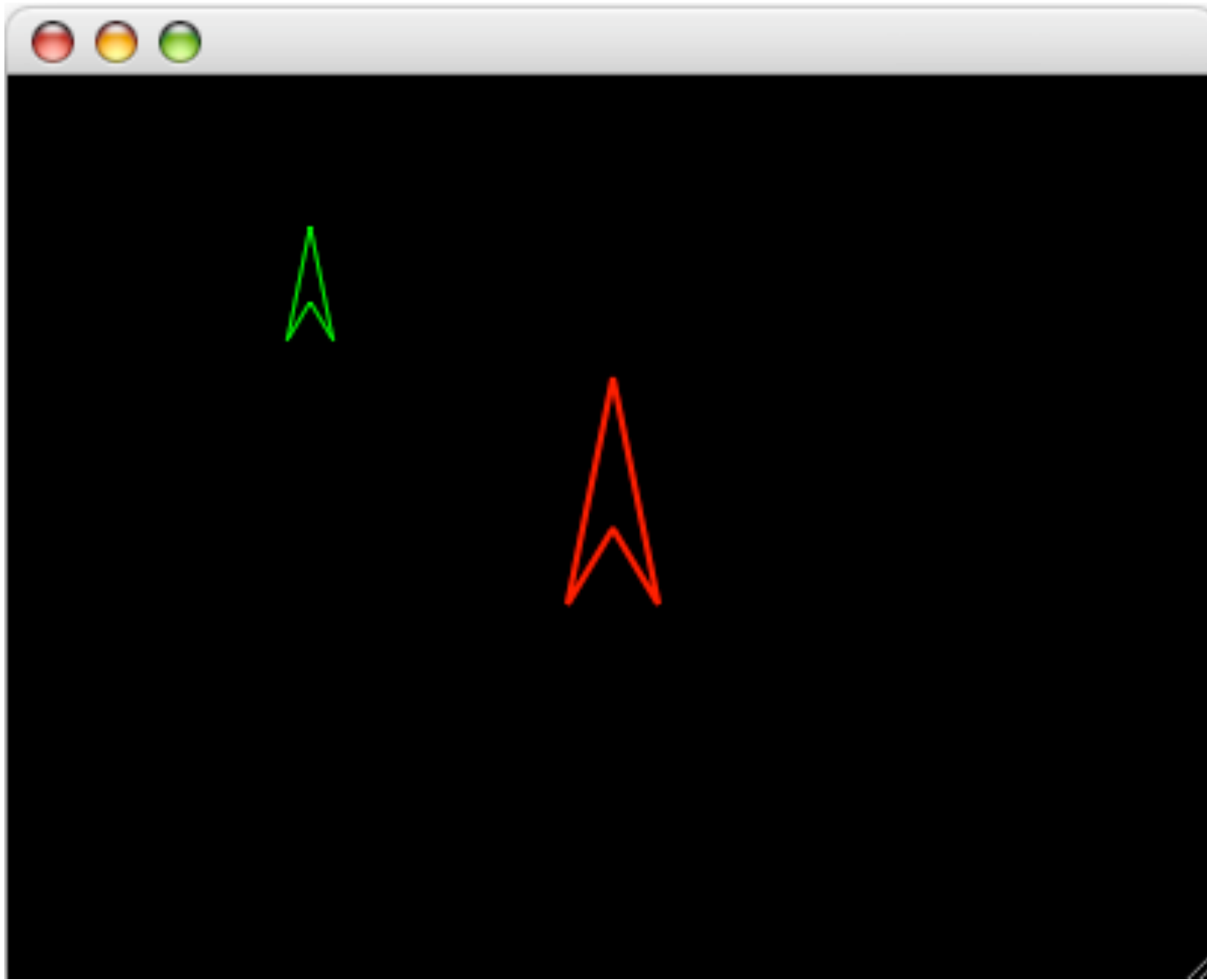
int main(int argc, char* argv[])
{
    QApplication myApp(argc, argv);           // Need application for event loop
    QPixmap myMap(400, 300);                  // Establish pixmap
    myMap.fill(Qt::black);
    QPainter p(&myMap);
    p.setRenderHint(QPainter::Antialiasing, true); // Enable antialiasing

    // Draw arrow
    p.setPen(QPen(Qt::red, 2, Qt::SolidLine, Qt::FlatCap));
    p.setBrush(QBrush(Qt::SolidPattern));
    QPoint points[4] = {QPoint(200, 100), QPoint(215, 175), QPoint(200, 150), QPoint(185, 175)};
    p.drawPolygon(points, 4);

    // Apply rotation and redraw polygon
    p.scale(0.5, 0.5);                         // Scale X and Y by 0.5
    p.setPen(QPen(Qt::green, 2, Qt::SolidLine, Qt::FlatCap));
    p.drawPolygon(points, 4);

    QLabel myLabel;                           // Allocate a Gui widget
    myLabel.setPixmap(myMap);                  // Associate pixmap with Gui widget
    myLabel.show();                           // Make widget visible
    return myApp.exec();                      // Initiate event loop
} // End main()
```

# Graphics Example 05





# Graphics Example 06

- Goals
  - Draw an arrow using a polygon
  - Save pixmap to a file in JPG format without displaying the pixmap
  - Load pixmap from file as a JPG image
  - Render loaded pixmap

# Graphics Example 06

```
//  
// Graphics Example 6  
//  
#include <QApplication>  
#include <QtDebug>  
#include <QPainter>  
#include <QPixmap>  
#include <QPen>  
#include <QBrush>  
#include <QRect>  
#include <QPoint>  
#include <QLabel>  
  
int main(int argc, char* argv[])  
{  
    QApplication myApp(argc, argv);           // Need application for event loop  
  
    { // Generate pixmap and save as a jpg image  
        QPixmap yourMap(400, 300);           // Establish pixmap  
        yourMap.fill(Qt::black);  
        QPainter p(&yourMap);  
        p.setRenderHint(QPainter::Antialiasing, true); // Enable antialiasing  
  
        // Draw arrow  
        p.setPen(QPen(Qt::red, 2, Qt::SolidLine, Qt::FlatCap));  
        p.setBrush(QBrush(Qt::SolidPattern));  
        QPoint points[4] = {QPoint(200, 100), QPoint(215, 175), QPoint(200, 150), QPoint(185, 175)};  
        p.drawPolygon(points, 4);  
  
        // Attempt to save pixmap as jpg  
        // 0 = determine image format by looking at filename; -1 = default image quality  
        if (!yourMap.save("arrow.jpg", 0, -1))  
            qDebug() << "Error - unable to save pixmap";  
    }  
}
```

# Graphics Example 06

```
// Graphics Example 6 -- continued

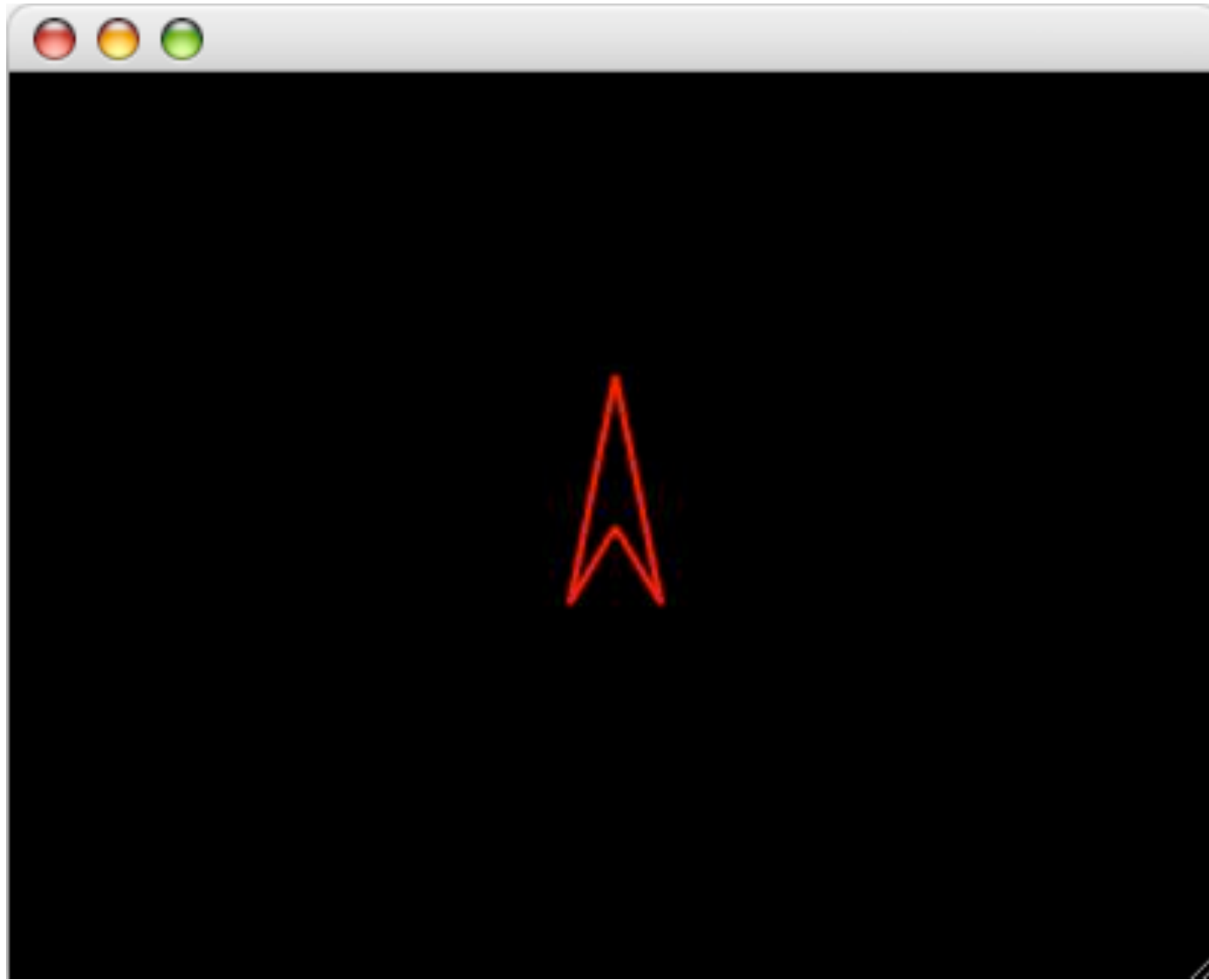
// Load jpeg image from file
QPixmap myMap;

// Attempt to load pixmap as jpg
// 0 = determine image format by looking at filename; auto conversion
if (!myMap.load("arrow.jpg", 0, Qt::AutoColor))
    qDebug() << "Error - unable to load pixmap";

QLabel myLabel;                                // Allocate a Gui widget
myLabel.setPixmap(myMap);                       // Associate pixmap with Gui widget
myLabel.show();                                // Make widget visible

return myApp.exec();                            // Initiate event loop
} // End main()
```

# Graphics Example 06



# Graphics Example 07

- Goals
  - Establish a Window for logical coordinates
  - Draw an arrow as a red polygon
  - Apply translation
  - Redraw arrow as a green polygon

# Graphics Example 07

```
//  
// Graphics Example 7  
//  
#include <QApplication>  
#include <QPainter>  
#include <QPixmap>  
#include <QPen>  
#include <QBrush>  
#include <QRect>  
#include <QPoint>  
#include <QLine>  
#include <QFont>  
#include <QLabel>  
  
int main(int argc, char* argv[])  
{  
    QApplication myApp(argc, argv);          // Need application for event loop  
    QPixmap myMap(400, 300);                 // Establish pixmap  
    myMap.fill(Qt::black);  
    QPainter p(&myMap);  
    p.setRenderHint(QPainter::Antialiasing, true); // Enables antialiasing  
    p.setWindow(-50, -50, 100, 100);          // Define logical coordinate window  
    // Logical (-50, -50) corresponds to Physical (0, 0)  
  
    // Draw arrow using relative coordinates  
    p.setPen(QPen(Qt::red, 2, Qt::SolidLine, Qt::FlatCap));  
    p.setBrush(QBrush(Qt::SolidPattern));  
    QPoint points[4] = {QPoint(0, 25), QPoint(15, -25), QPoint(0, 0), QPoint(-15, -25)};  
    p.drawPolygon(points, 4);
```

# Graphics Example 07

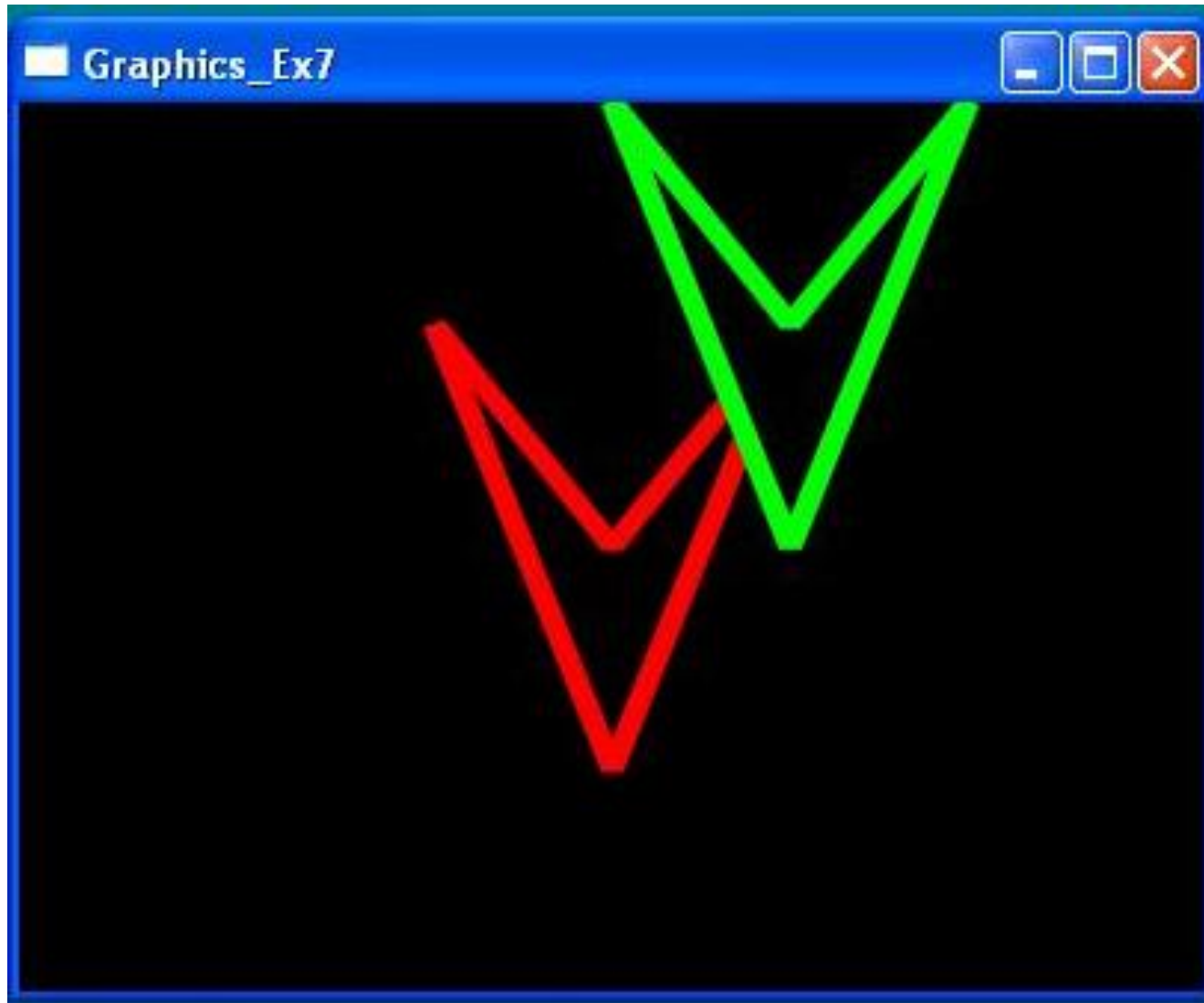
```
// Graphics Example 7 - continued

// Apply translation and redraw polygon
p.translate(15, -25);
p.setPen(QPen(Qt::green, 2, Qt::SolidLine, Qt::FlatCap));
p.drawPolygon(points, 4);

QLabel myLabel;                                // Allocate a Gui widget
myLabel.setPixmap(myMap);                       // Associate pixmap with Gui widget
myLabel.show();                                 // Make widget visible

return myApp.exec();                           // Initiate event loop
} // End main()
```

# Graphics Example 07





# Graphics Example 08

- Goals
  - Establish a Window for logical coordinates
  - Draw an arrow as a red polygon
  - Apply rotation
  - Redraw arrow as a green polygon

# Graphics Example 08

```
//  
// Graphics Example 8  
//  
#include <QApplication>  
#include <QPainter>  
#include <QPixmap>  
#include <QPen>  
#include <QBrush>  
#include <QRect>  
#include <QPoint>  
#include <QLine>  
#include <QFont>  
#include <QLabel>  
  
int main(int argc, char* argv[])  
{  
    QApplication myApp(argc, argv);           // Need application for event loop  
    QPixmap myMap(400, 300);                  // Establish pixmap  
    myMap.fill(Qt::black);  
    QPainter p(&myMap);  
    p.setRenderHint(QPainter::Antialiasing, true); // Enables antialiasing  
    p.setWindow(-50, -50, 100, 100);           // Define logical coordinate window  
    // Logical (-50, -50) corresponds to Physical (0, 0)  
  
    // Draw arrow  
    p.setPen(QPen(Qt::red, 2, Qt::SolidLine, Qt::FlatCap));  
    p.setBrush(QBrush(Qt::SolidPattern));  
    QPoint points[4] = {QPoint(0, 25), QPoint(15, -25), QPoint(0, 0), QPoint(-15, -25)};  
    p.drawPolygon(points, 4);
```

# Graphics Example 08

```
// Graphics Example 8 -- continued
```

```
// Rotate 45 degrees and redraw polygon
```

```
p.rotate(45.0);
```

```
p.setPen(QPen(Qt::green, 2, Qt::SolidLine, Qt::FlatCap));
```

```
p.drawPolygon(points, 4);
```

```
QLabel myLabel;
```

```
myLabel.setPixmap(myMap);
```

```
myLabel.show();
```

```
// Allocate a Gui widget
```

```
// Associate pixmap with Gui widget
```

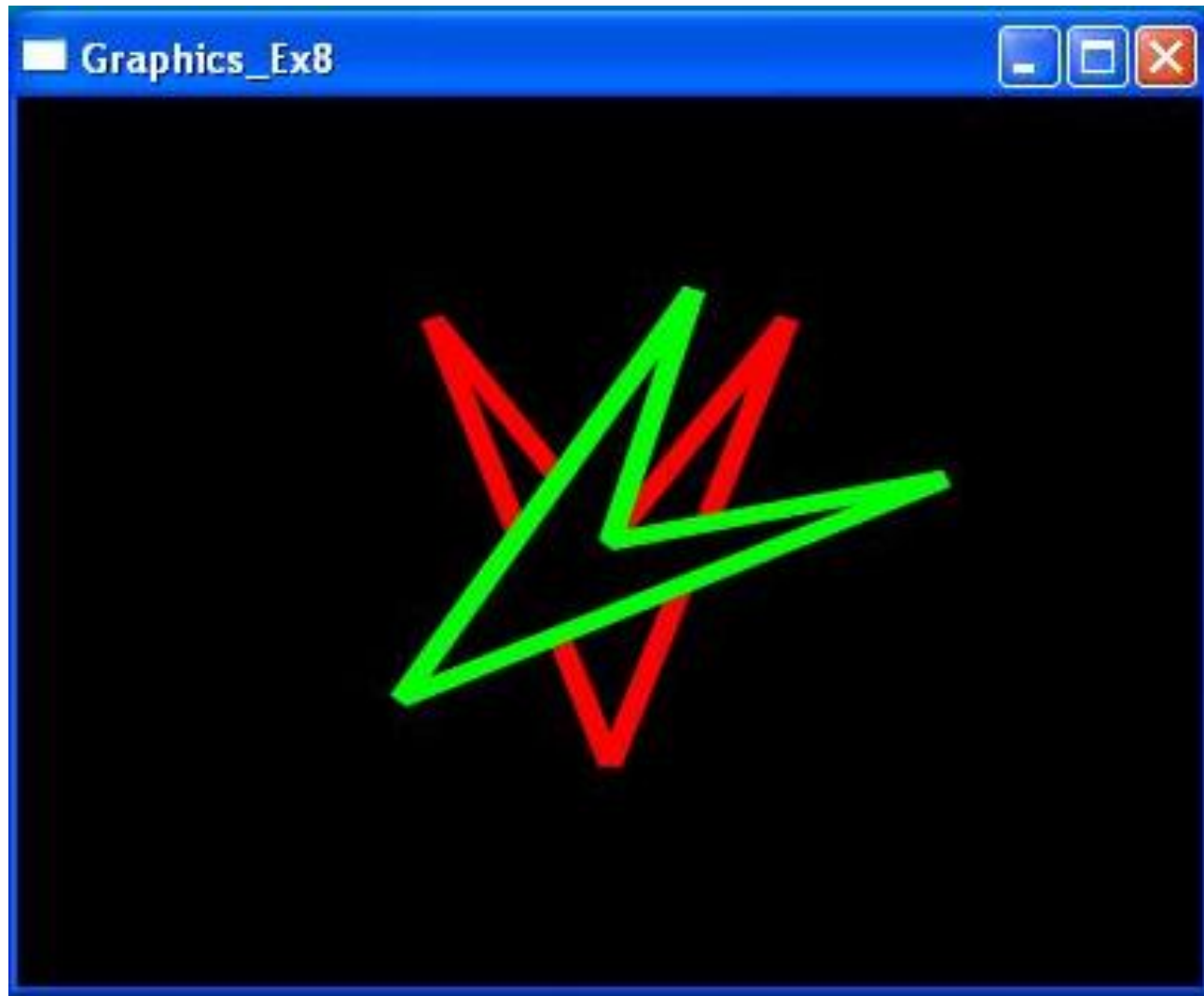
```
// Make widget visible
```

```
return myApp.exec();
```

```
// Initiate event loop
```

```
} // End main()
```

# Graphics Example 08 - 3



# QIcon/QPainter Example

- Goal
  - Create a push button widget that visually indicates toggle status by switching between a Black and Red icon

# QIcon/QPainter Example

```
#include <QtGui/QApplication>
#include "widget.h"
int main(int argc, char *argv[])
{
    QApplication a(argc, argv);
    Widget w;
    w.show();
    return a.exec();
}
```

# QIcon/QPainter Example

```
#ifndef WIDGET_H
#define WIDGET_H

#include <QPushButton>
#include <QPixmap>
#include <QPainter>
#include <QIcon>

class Widget : public QPushButton
{
    Q_OBJECT

public:
    Widget(QWidget *parent = 0);
    ~Widget();

protected:
    void paintEvent(QPaintEvent* pe);    // Override paint event handler

private:
    QPixmap* redPixmap;
    QPixmap* blackPixmap;
    QPainter* painter;
    QIcon* redIcon;
    QIcon* blackIcon;
    bool illuminated;

private slots:
    void togglePixmap();                // Toggles red/black button icon
};
#endif // WIDGET_H
```

# QIcon/QPainter Example

```
#include "widget.h"

Widget::Widget(QWidget *parent) : QPushButton(parent)
{
    illuminated = false;

    blackPixmap = new QPixmap(400,100);
    painter = new QPainter(blackPixmap);
    blackPixmap->fill(Qt::black);
    blackIcon = new QIcon(*blackPixmap);
    delete painter;
    delete blackPixmap;

    redPixmap = new QPixmap(400,100);
    painter = new QPainter(redPixmap);
    redPixmap->fill(Qt::red);
    redIcon = new QIcon(*redPixmap);
    delete painter;
    delete redPixmap;

    this->setIcon(*blackIcon);
    connect(this, SIGNAL(clicked()), this, SLOT(togglePixmap()));
}
```



# QIcon/QPainter Example

```
#include "widget.h"

void Widget::paintEvent(QPaintEvent* pe)
{
    // Adjust icon based upon illuminated flag
    if (illuminated)
        this->setIcon(*redIcon);
    else
        this->setIcon(*blackIcon);

    // Pass on other paint events to parent class event handler
    QPushButton::paintEvent(pe);
}

void Widget::togglePixmap()
{
    // Toggle illuminated flag
    illuminated = !illuminated;

    // Trigger update of widget display
    this->update();
}

Widget::~Widget()
{
}
```

# QIcon/QPainter Example



# QColor Class

- Uses RGB representation
  - Reserves 8-bits (0-255) for each color Red, Green, Blue
  - Also reserves 8-bits for Alpha Channel
    - Describes pixel transparency
  - QColor can work with ints or floats
    - `setRgb()` ints
    - `setRgbF()` floats
  - Hex notation
    - `0xAARRGGBB`

# QColor Class

- Several variants of the QColor constructor
- Example
  - QColor x(255, 127, 64, 0);
    - Red = 255
    - Green = 127
    - Blue = 64
    - Alpha = 0

# QColor Class

- Another Example
  - `QColor y("black");`
    - Predefined SVG color names  
(Scalable Vector Graphics)



# QColor Class

- Also supports other color models
  - HSV (Hue-Saturation-brightnessValue)
  - CMYK (Cyan-Magenta-Yellow-Black)
  - Methods included to convert to/from various color models
    - `toHsv()`, `toCymk()`, `toRgb()`
- Use caution
  - Qt uses RGB internally

# QPixmap vs QImage

- QPixmap
  - Available for QApplication, not QCoreApplication use
  - Operations handled by graphics card
- QImage
  - Available for either QApplication or QCoreApplication use
  - Operations performed by processor
  - Still part of Qt GUI library

# QPixmap vs QImage

- QImage
  - Uses RGB representation
    - Reserves 8-bits (0-255) for each color Red, Green, Blue
    - May or may not include 8-bits for Alpha Channel
      - QImage::Format\_RGB32
      - QImage::Format\_ARGB32



# QPixmap vs QImage

- QImage
  - `scanLine()` can retrieve pixel color information as unsigned char array
  - Byte order can impact interpretation
    - Little Endian
      - LSB first
    - Big Endian
      - MSB first
  - Qt resolves byte order by using `QRgb` type
    - Type reinterpret picks up values in platform byte order
    - See section 10.7.2

## Key Points

- **QPainter** objects may be used to draw on pixmaps within a Qt program
- Standard transformations (rotation, translation, and scaling) may be applied as needed
- Be aware of the coordinate system you are using since the transformations produce different results with respect to absolute and relative coordinate systems.