# Iron Ore Quality Prediction

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2023-01-23

### Introduction

Flotation is a process in which pulp containing some mineral ore deposit is fed into a plant with some reagents such that at the end of the process, pure mineral is collected while all impurities stay in the plant. In this project, the mineral of interest is iron ore. The quality of iron ore in a mining flotation plant is determined by the amount of silica (SiO<sub>2</sub>) in the ore concentrate; a higher silica amount is indicative of a more impure sample. In this project the objective is to use other variables from the plant to try and predict the silica content. This will be helpful in improving productivity as there is at least one hour that has to be waited before obtaining the silica content reading of each sample sent to the lab, and many samples are sent in a day, creating a lot of dead time. Prediction using machine learning would save this time. The R code used to create this report is found in the iron\_ore\_code.R file that goes with this report.

### Dataset

The data dataset taken from kaggle contains 7 37 453 entries of 24 variables from an iron ore mining flotation plant. The variables are attributes of the plant like pulp density, pulp pH and flow rate, amount of iron and silica in the feed, flow rates of the reagents used in the plant. Below are the first six lines of the dataset.

##			date XIrd	n.Feed	XSilica.Feed	Starch.Flow	Amina.Flow				
##	1	2017-03-10 01	:00:00	55,2	16,98	3019,53	557,434				
##	2	2017-03-10 01	:00:00	55,2	16,98	3024,41	563,965				
##	3	2017-03-10 01	:00:00	55,2	16,98	3043,46	568,054				
##	4	2017-03-10 01	:00:00	55,2	16,98	3047,36	568,665				
##	5	2017-03-10 01	:00:00	55,2	16,98	3033,69	558,167				
##	6	2017-03-10 01	:00:00	55,2	16,98	3079,1	564,697				
##		Ore.Pulp.Flow	Ore.Pulp.pH	Ore.Pul	lp.Density Flota	ation.Column	.01.Air.Flow				
##	1	395,713	10,0664		1,74		249,214				
##	2	397,383	10,0672		1,74		249,719				
##	3	399,668	10,068		1,74		249,741				
##	4	397,939	10,0689		1,74		249,917				
##	5	400,254	10,0697		1,74		250,203				
##	6	396,533	10,0705		1,74		250,73				
##		Flotation.Column.02.Air.Flow Flotation.Column.03.Air.Flow									
##	1		253,2	235		250,576					
##	2		250,5	32		250,862					
##	3		247,8	374	250,313						
##	4		254,4	87	250,049						
##	5		252,1	.36	249,895						
##	6		248,9	06		249,521					
##		Flotation.Col	umn.04.Air.Fl	ow Flot	Flotation.Column.O5.Air.Flow						
##	1		295,0	96		306,4					

```
## 2
                            295,096
                                                             306,4
## 3
                            295,096
                                                             306,4
## 4
                            295,096
                                                             306,4
## 5
                            295,096
                                                             306,4
## 6
                            295,096
                                                             306,4
##
     Flotation.Column.06.Air.Flow Flotation.Column.07.Air.Flow
## 1
                            250,225
                                                           250,884
## 2
                            250,137
                                                           248,994
## 3
                            251,345
                                                           248,071
## 4
                            250,422
                                                           251,147
## 5
                            249,983
                                                           248,928
                            250,356
## 6
                                                           251,873
##
     Flotation.Column.01.Level Flotation.Column.02.Level Flotation.Column.03.Level
## 1
                        457,396
                                                    432,962
                                                                                 424,954
## 2
                                                     429,56
                                                                                 432,939
                        451,891
## 3
                          451,24
                                                     468,927
                                                                                  434,61
## 4
                        452,441
                                                     458,165
                                                                                 442,865
## 5
                        452,441
                                                       452,9
                                                                                 450,523
## 6
                                                    443,269
                        444,384
                                                                                 460,449
##
     Flotation.Column.04.Level Flotation.Column.05.Level Flotation.Column.06.Level
## 1
                        443,558
                                                    502,255
                                                                                  446,37
## 2
                        448,086
                                                    496,363
                                                                                 445,922
## 3
                        449,688
                                                     484,411
                                                                                 447,826
## 4
                         446,21
                                                    471,411
                                                                                 437,69
## 5
                          453,67
                                                    462,598
                                                                                 443,682
## 6
                          439,92
                                                    451,588
                                                                                 433,539
##
     Flotation.Column.07.Level X..Iron.Concentrate X..Silica.Concentrate
## 1
                        523,344
                                                66,91
                                                                         1,31
                                                66,91
## 2
                        498,075
                                                                         1,31
## 3
                        458,567
                                                66,91
                                                                         1,31
## 4
                        427,669
                                                66,91
                                                                         1,31
## 5
                        425,679
                                                66,91
                                                                         1,31
## 6
                        425,458
                                                66,91
                                                                         1,31
```

### Cleaning The Dataset

All variables except date are numeric, but are not written in the correct format, with commas making them character strings. The date variable is also not in the datetime type. Cleaning this dataset will just be about making all variables numeric and datetime for the date variable, and also renaming the long variable names to shorter versions that will be quicker to write. Hourly entries will also have to be aggregated, because as seen in the dataset, there are different readings of all the other variables for each 60 entries with the same silica content reading. This is because all those entries belong to a single batch of ore taken to the lab to obtain the silica content reading, that comes after one hour. These values will be combined and an average taken for each variable to correspond with each unique value of silica concentrate. Below are the first six lines of the cleaned dataset.

##		date	<pre>iron_feed</pre>	silica_feed	starch_flow	amina_flow	pulp_flow
## 1 203	17-03-10	01:00:00	55.2	16.98	3162.625	578.7867	398.7534
## 2 203	17-03-10	02:00:00	55.2	16.98	3133.256	537.2197	399.8718
## 3 203	17-03-10 (	03:00:00	55.2	16.98	3479.483	591.9067	398.7638
## 4 203	17-03-10	04:00:00	55.2	16.98	3228.036	593.1701	399.8670
## 5 203	17-03-10	05:00:00	55.2	16.98	3327.281	619.7108	399.6151
## 6 203	17-03-10	06:00:00	55.2	16.98	3405.162	621.8785	399.7493

```
pulp_ph pulp_density air_flow_1 air_flow_2 air_flow_3 air_flow_4 air_flow_5
##
## 1 10.113487
                    1.729558
                                251.1667
                                            250.2261
                                                        250.1783
                                                                     295.096
                                                                                   306.4
                                            250.2140
## 2 10.129742
                    1.667784
                                249.8806
                                                        250.0333
                                                                     295.096
                                                                                   306.4
## 3 10.048403
                    1.732711
                                            250.1042
                                                                     295.096
                                250.1613
                                                        250.0463
                                                                                   306.4
##
  4
      9.918614
                    1.731056
                                250.2088
                                            250.2048
                                                        250.1209
                                                                     295.096
                                                                                   306.4
## 5
                                249.9178
      9.746029
                    1.765879
                                            250.1605
                                                        250.0135
                                                                     295.096
                                                                                   306.4
  6
##
      9.892237
                    1.765064
                                249.8983
                                            250.1110
                                                        250.0754
                                                                     295.096
                                                                                   306.4
     air_flow_6 air_flow_7 column_level_1 column_level_2 column_level_3
##
## 1
       251.2325
                   250.2082
                                   450.3838
                                                    446.8918
                                                                    450.4745
##
  2
       249.9095
                   249.8976
                                   449.3734
                                                    450.2494
                                                                    450.0812
## 3
       250.2422
                   250.4842
                                   449.9729
                                                    450.8687
                                                                    450.9018
##
   4
       249.8251
                   250.1576
                                   487.9407
                                                    491.4621
                                                                    487.3872
##
  5
       250.2496
                   250.0786
                                   549.0315
                                                    549.9832
                                                                    549.4596
   6
##
       249.9425
                   250.1499
                                   550.5996
                                                    549.9291
                                                                    549.0892
##
     column_level_4 column_level_5 column_level_6 column_level_7 iron_concentrate
## 1
           449.9123
                            455.7922
                                            464.3833
                                                            450.5327
                                                                                  66.91
## 2
           450.3288
                            448.7230
                                            455.5015
                                                            451.3877
                                                                                  67.06
## 3
           451.1458
                            451.1342
                                            459.9813
                                                            450.2967
                                                                                  66.97
## 4
           494.5282
                            495.6640
                                            502.7638
                                                            494.9399
                                                                                  66.75
## 5
           549.9755
                            549.5125
                                            560.6963
                                                            550.2718
                                                                                  66.63
##
  6
           549.6097
                            549.2207
                                            561.0516
                                                            551.0908
                                                                                  66.85
##
     silica_concentrate
## 1
                    1.31
## 2
                    1.11
## 3
                    1.27
## 4
                    1.36
## 5
                    1.34
## 6
                    1.15
```

## **Exploratory Data Analysis**

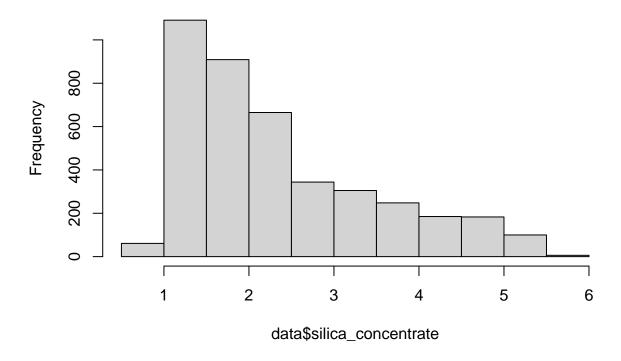
The first step is to check the summary statistics of each variable, to see how variable each one is. Then explore the distribution of the response variable, and then checking how it changes with time. This can be done by plotting silica content against time and observe whether or not there is an obvious pattern. The first plot is the distribution of silica content in the concentrate, is it changing at all and if yes how? The second plot shows silica content over the course of the three months in which these data were collected.

```
##
                                          iron feed
         date
                                                           silica_feed
                                                                 : 1.31
##
    Min.
            :2017-03-10 01:00:00.00
                                                :42.74
                                        Min.
                                                          Min.
    1st Qu.:2017-05-04 23:00:00.00
                                        1st Qu.:52.67
                                                          1st Qu.: 8.94
##
##
    Median :2017-06-16 15:00:00.00
                                        Median :56.08
                                                          Median :13.85
            :2017-06-16 03:26:05.82
                                                :56.29
##
    Mean
                                        Mean
                                                          Mean
                                                                 :14.65
##
    3rd Qu.:2017-07-29 07:00:00.00
                                        3rd Qu.:59.72
                                                          3rd Qu.:19.60
            :2017-09-09 23:00:00.00
##
    Max.
                                        Max.
                                                :65.78
                                                          Max.
                                                                 :33.40
##
     starch flow
                          amina flow
                                           pulp_flow
                                                              pulp_ph
##
                                :242.9
                                                 :376.8
                                                                  : 8.753
    Min.
            : 54.59
                        Min.
                                         Min.
                                                           Min.
##
    1st Qu.:2168.97
                        1st Qu.:436.0
                                         1st Qu.:398.9
                                                           1st Qu.: 9.541
##
    Median :2908.34
                        Median :502.5
                                         Median :399.8
                                                           Median : 9.796
##
    Mean
            :2869.14
                        Mean
                                :488.1
                                         Mean
                                                 :397.6
                                                           Mean
                                                                  : 9.768
##
    3rd Qu.:3528.73
                        3rd Qu.:549.5
                                         3rd Qu.:400.6
                                                           3rd Qu.:10.031
##
    Max.
            :6270.16
                        Max.
                                :737.0
                                         Max.
                                                 :418.1
                                                           Max.
                                                                   :10.807
##
                                         air_flow_2
                                                           air_flow_3
     pulp_density
                        air_flow_1
    Min.
            :1.520
                     Min.
                             :175.9
                                       Min.
                                               :178.2
                                                        Min.
                                                                :177.2
```

```
1st Qu.:1.651
                     1st Qu.:250.1
                                      1st Qu.:250.1
                                                       1st Qu.:250.1
##
                     Median :299.8
                                      Median :299.5
                                                       Median :299.9
    Median :1.696
##
    Mean
           :1.680
                     Mean
                            :280.2
                                      Mean
                                              :277.2
                                                       Mean
                                                               :281.1
##
    3rd Qu.:1.722
                     3rd Qu.:300.0
                                      3rd Qu.:300.0
                                                       3rd Qu.:299.9
##
    Max.
           :1.832
                     Max.
                            :312.3
                                      Max.
                                              :309.9
                                                       Max.
                                                               :302.8
##
      air flow 4
                       air flow 5
                                        air_flow_6
                                                         air flow 7
##
            :293.3
                             :287.1
                                              :196.5
    Min.
                     Min.
                                      Min.
                                                       Min.
                                                               :199.7
                                      1st Qu.:268.7
##
    1st Qu.:299.7
                     1st Qu.:299.7
                                                       1st Qu.:283.2
##
    Median :299.9
                     Median :299.9
                                      Median :299.9
                                                       Median :299.9
##
    Mean
           :299.4
                     Mean
                            :299.9
                                      Mean
                                              :292.1
                                                       Mean
                                                               :290.8
##
    3rd Qu.:300.0
                     3rd Qu.:300.1
                                      3rd Qu.:300.1
                                                       3rd Qu.:300.1
##
            :305.6
                             :307.0
                                              :355.0
                                                               :351.3
    Max.
                     Max.
                                      Max.
                                                       Max.
##
    column_level_1
                     column_level_2
                                      column_level_3
                                                       column_level_4
##
    Min.
            :181.9
                     Min.
                             :224.9
                                      Min.
                                              :135.2
                                                       Min.
                                                               :165.7
##
    1st Qu.:416.5
                     1st Qu.:449.2
                                      1st Qu.:405.4
                                                       1st Qu.:351.5
##
    Median :499.6
                     Median :499.8
                                      Median :499.6
                                                       Median :401.3
##
            :520.2
                            :522.6
                                                               :420.3
    Mean
                     Mean
                                      Mean
                                              :531.4
                                                       Mean
##
    3rd Qu.:599.7
                     3rd Qu.:599.3
                                      3rd Qu.:600.2
                                                       3rd Qu.:496.2
            :859.0
                             :827.8
                                      Max.
                                              :884.8
##
    Max.
                     Max.
                                                       Max.
                                                               :675.6
##
    column level 5
                     column level 6
                                      column level 7
                                                       iron concentrate
##
    Min.
            :214.7
                     Min.
                             :203.7
                                      Min.
                                              :185.1
                                                       Min.
                                                               :62.05
##
    1st Qu.:351.0
                     1st Qu.:354.1
                                      1st Qu.:350.9
                                                       1st Qu.:64.37
    Median :401.1
                     Median :407.5
                                      Median :401.0
                                                       Median :65.21
##
    Mean
           :425.3
                            :429.9
                                              :421.0
##
                     Mean
                                      Mean
                                                       Mean
                                                               :65.05
##
    3rd Qu.:497.8
                     3rd Qu.:497.8
                                      3rd Qu.:462.3
                                                       3rd Qu.:65.86
##
    Max.
           :674.1
                     Max.
                             :698.5
                                      Max.
                                              :655.5
                                                       Max.
                                                               :68.01
##
    silica_concentrate
##
    Min.
            :0.600
##
    1st Qu.:1.440
##
    Median :2.000
##
    Mean
            :2.327
##
    3rd Qu.:3.010
##
    Max.
            :5.530
```

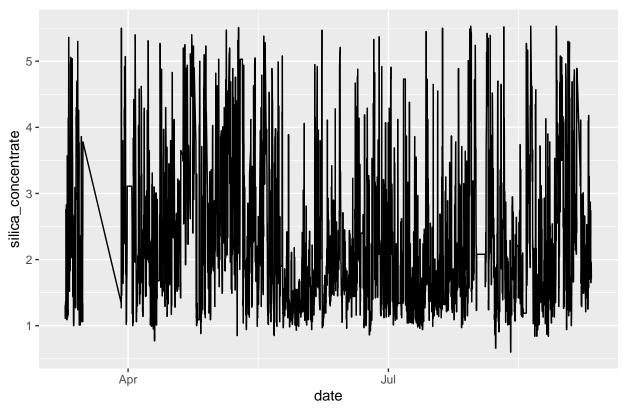
The summary shows that although almost all these variables are in the same order of magnitude, they are not exactly the same. The numbers are similar. Starch flow is the only variable in which the minimum is in the different order of magnitude from the rest of the other numbers.

# Distribution of silica content in the concentrate



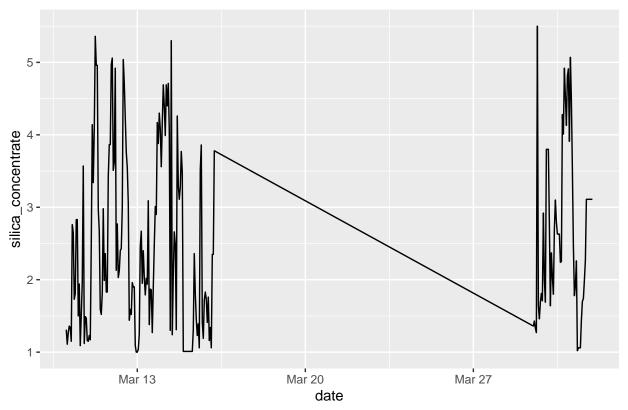
It can be seen that the distribution of the response variable is highly variable.

# Silica content in concentrate over time

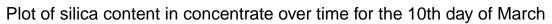


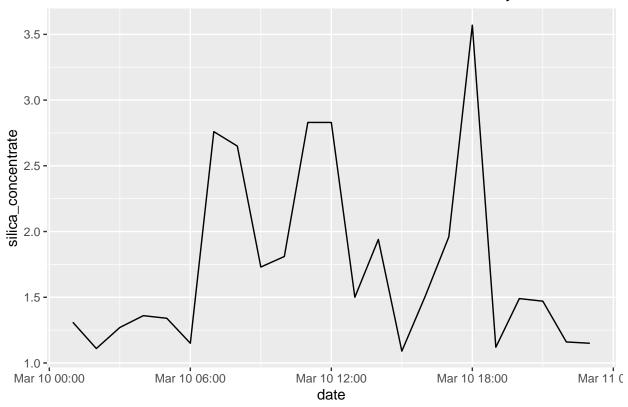
Looking at this plot shows that there is no clear pattern between the response variable and time in the whole of these three months. Maybe zooming in on just one month will be clearer:

# Plot of silica content in concentrate over time for the month of March

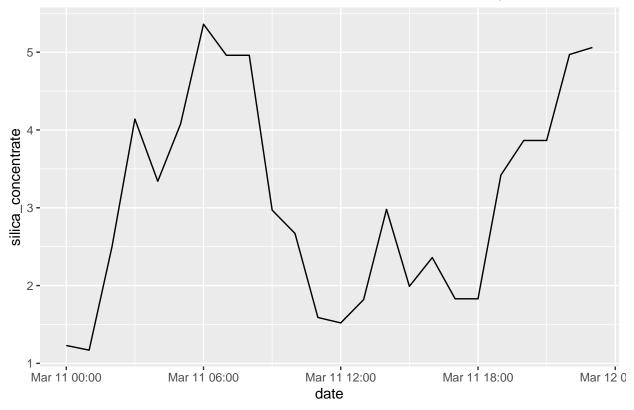


There still is no clear pattern. Below I check by a single day, will pick two random days to see if there is any relationship between silica content and say time of day.

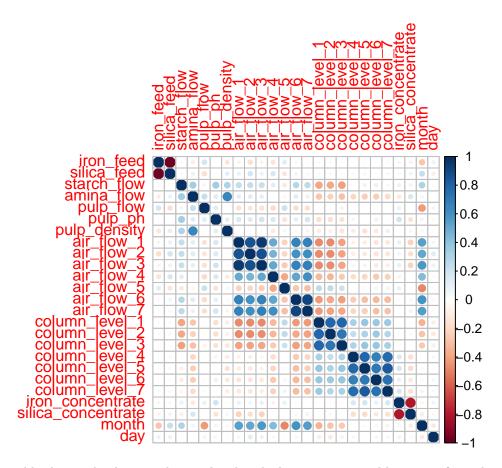




# Plot of silica content in concentrate over time for the 11th day of March



Both plots show that there is no obvious pattern. Next I move on to checking if all these variables are correlated with the response variable and with one another. This is in the correlation plot below:



The only variable that is clearly strongly correlated with the response variable as seen from the plot is iron concentrate, which is the amount of iron in the concentrate. It is a negative correlation and it makes sense because the more iron there is the less contaminant there will be and vice versa. All the variables do not seem to individually have a direct correlation with the response variable, but there are some variables that positively or negatively, correlated with one another.

### Building A Predictive Model

Since all of the variables except date, in the dataset are numeric, the first option algorithm to explore is linear regression. The dataset is split into the training and test sets, and then a model is trained using linear regression and its performance tested on the test set. Because it has already been seen that many of the variables are correlated with one another, it is likely that the model will not fit the data with high efficiency due to the redundance in the features. Therefore, principal component analysis will be used to reduce the dimensions in the features and see whether or not the model fit will improve. Below is the summary of the model run with linear regression:

```
##
## Call:
## lm(formula = .outcome ~ ., data = dat)
##
##
  Residuals:
##
        Min
                   1Q
                        Median
                                      3Q
                                               Max
   -3.05853 -0.39769 -0.03191
                                0.36265
##
                                          2.33681
##
## Coefficients:
```

```
##
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     7.445e+02
                                5.287e+02
                                             1.408 0.159172
## date
                    -4.661e-07
                                3.569e-07
                                            -1.306 0.191688
## iron_feed
                    -2.122e-03
                                            -0.205 0.837468
                                1.035e-02
## silica_feed
                     1.287e-02
                                7.587e-03
                                             1.696 0.089973
## starch flow
                    -6.466e-06
                                1.575e-05
                                            -0.410 0.681491
## amina flow
                     1.102e-03
                                2.065e-04
                                             5.337 1.01e-07 ***
## pulp_flow
                     7.456e-04
                                1.658e-03
                                             0.450 0.652982
## pulp_ph
                     1.716e-02
                                3.534e-02
                                             0.486 0.627270
## pulp_density
                    -2.167e-01
                                2.583e-01
                                            -0.839 0.401546
## air_flow_1
                    -4.626e-03
                                1.479e-03
                                            -3.128 0.001775 **
## air_flow_2
                    -2.995e-03
                                8.744e-04
                                            -3.426 0.000621
                     1.136e-03
                                1.642e-03
                                             0.692 0.489094
## air_flow_3
## air_flow_4
                    -2.083e-03
                                6.507e-03
                                            -0.320 0.748945
## air_flow_5
                     5.048e-03
                                4.105e-03
                                             1.230 0.218897
## air_flow_6
                     3.844e-04
                                1.035e-03
                                             0.371 0.710411
## air_flow_7
                     2.547e-03
                                1.133e-03
                                             2.248 0.024615 *
## column level 1
                    -4.941e-04
                                1.854e-04
                                            -2.665 0.007735
## column_level_2
                    -1.499e-04
                                1.722e-04
                                            -0.871 0.383828
## column level 3
                    -3.869e-07
                                1.412e-04
                                            -0.003 0.997813
## column_level_4
                    -1.048e-04
                                2.555e-04
                                            -0.410 0.681719
## column level 5
                    -2.380e-05
                                3.055e-04
                                            -0.078 0.937891
## column level 6
                    -2.229e-04
                                2.395e-04
                                            -0.931 0.351982
## column level 7
                     2.979e-04
                                3.097e-04
                                             0.962 0.336128
## iron concentrate -7.982e-01
                                1.087e-02 -73.438 < 2e-16 ***
## month
                     1.143e+00
                                9.417e-01
                                             1.214 0.225008
                     4.324e-02
                                             1.406 0.159747
## day
                                3.075e-02
##
                   0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Signif. codes:
##
## Residual standard error: 0.6308 on 3250 degrees of freedom
## Multiple R-squared: 0.6895, Adjusted R-squared: 0.6871
## F-statistic: 288.6 on 25 and 3250 DF, p-value: < 2.2e-16
```

As anticipated, the model does not fit the data well enough, the adjusted R-squared value is 0.6871, so there might still be room for improvement. BUt first the model is tested on test data to see its performance on new data. Below is the RMSE value obtained from comparing predictions on the test set with real values:

### ## [1] 0.6143063

This RMSE value, 0.61 is almost equal to the minimim value of this variable in the dataset, it is a big error that the model makes when trying to predict. Maybe applying pca will bring it down. Below is the summary of model fit after applying pca:

```
## Importance of components:
##
                             PC1
                                    PC2
                                             PC3
                                                     PC4
                                                             PC5
                                                                    PC6
                                                                             PC7
## Standard deviation
                          2.6341 1.8483 1.54072 1.43414 1.24837 1.1336 1.08018
## Proportion of Variance 0.2775 0.1367 0.09495 0.08227 0.06234 0.0514 0.04667
## Cumulative Proportion
                          0.2775 0.4142 0.50914 0.59141 0.65375 0.7052 0.75182
##
                              PC8
                                       PC9
                                              PC10
                                                      PC11
                                                              PC12
                                                                      PC13
## Standard deviation
                          0.99261 0.93657 0.84308 0.79394 0.71872 0.64511 0.56774
## Proportion of Variance 0.03941 0.03509 0.02843 0.02521 0.02066 0.01665 0.01289
## Cumulative Proportion 0.79123 0.82632 0.85475 0.87996 0.90062 0.91727 0.93016
```

```
##
                              PC15
                                      PC16
                                              PC17
                                                       PC18
                                                               PC19
                                                                       PC20
                                                                               PC21
## Standard deviation
                           0.54341 0.50216 0.49677 0.45738 0.42678 0.40593 0.38187
## Proportion of Variance 0.01181 0.01009 0.00987 0.00837 0.00729 0.00659 0.00583
  Cumulative Proportion
                          0.94198 0.95206 0.96193 0.97030 0.97759 0.98418 0.99001
##
                             PC22
                                      PC23
                                             PC24
                                                     PC25
                           0.35570 0.26215 0.1800 0.14861
## Standard deviation
## Proportion of Variance 0.00506 0.00275 0.0013 0.00088
## Cumulative Proportion 0.99507 0.99782 0.9991 1.00000
##
## Call:
## lm(formula = .outcome ~ ., data = dat)
##
## Residuals:
##
                  1Q
                       Median
                                     30
        Min
                                             Max
  -1.56545 -0.19537
                      0.01189
                               0.19806
                                         1.23198
##
## Coefficients:
##
                Estimate Std. Error
                                      t value Pr(>|t|)
                           0.005701
## (Intercept)
                2.327561
                                      408.259
                                               < 2e-16 ***
## PC1
                0.030802
                           0.002165
                                       14.229
                                               < 2e-16 ***
## PC2
                0.287542
                           0.003085
                                       93.208
                                               < 2e-16 ***
## PC3
                0.310894
                           0.003701
                                       84.005
                                               < 2e-16 ***
## PC4
               -0.023537
                           0.003976
                                       -5.920 3.56e-09 ***
## PC5
               -0.578237
                           0.004568 -126.596
                                               < 2e-16 ***
## PC6
               -0.168639
                           0.005030
                                      -33.527
                                               < 2e-16 ***
## PC7
                0.101148
                           0.005279
                                       19.161
                                               < 2e-16 ***
                                               < 2e-16 ***
## PC8
                0.201552
                           0.005744
                                       35.086
## PC9
               -0.026557
                           0.006088
                                       -4.362 1.33e-05 ***
## PC10
               -0.196808
                           0.006763
                                      -29.099
                                               < 2e-16 ***
## PC11
                0.056181
                           0.007182
                                        7.822 6.94e-15 ***
## PC12
                0.030186
                           0.007934
                                        3.805 0.000145 ***
## PC13
                0.101358
                           0.008839
                                       11.467
                                              < 2e-16 ***
## PC14
               -0.016569
                           0.010043
                                       -1.650 0.099103 .
## PC15
                0.068952
                                        6.571 5.79e-11 ***
                           0.010493
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.3263 on 3260 degrees of freedom
## Multiple R-squared: 0.9166, Adjusted R-squared: 0.9163
## F-statistic: 2390 on 15 and 3260 DF, p-value: < 2.2e-16
```

The results show that the adjusted R-squared is now 0.92, a big improvement from a linear regression without pca. They also show that after 15 principal components, 95% of the variance in the data has already been accounted for, so the dimensions can definately be reduced. Below we check how the linear regression model after reducing the dimensions using pca performs on new data by checking the RMSE value returned.

### ## [1] 0.3232659

The RMSE value for the liner regression model after first performing pca is now 0.32, almost half of that without pca.

### Conclusion and further work

The linear regression model build here fits the data fairly well and predicts the target variable on new data with fairly good accuracy too. It makes an error of about 0.32 units when predicting the silica content in the concentrate. However, it is unknown whether or not this error is acceptable for this specific plant, because no further information is given regarding this flotation process. What margin of error can be acceptable for them? And what are the implications of making an error? More information is needed to better understand the process and this could be achieved by talking with the people concerned, about the process. With more information available then maybe more algorithms may be deployed to build a model with even better prediction accuracy.