Physics 5150Homework Set # 10

Due 5 pm Thursday 4/19/2018

Problem 1: Sound waves

Derive the dispersion relation for sound waves in a neutral gas (e.g., air) with an adiabatic equation of state $(P \sim \rho^{\gamma})$, using the gas dynamics (fluid) equations. What are the phase and group velocities of these waves?

<u>Problem 2:</u> Energy Partitioning in Plasma Oscillations

Consider Langmuir's electron plasma oscillations in an unmagnetized cold plasma (treat ions as a stationary uniform neutralizing background, $n_i = \text{const}$, $u_i = 0$). What is the greater: the electron kinetic energy density due to the perturbed electron velocity, $\mathcal{E}_{kin} = n_0 m_e |u_{e,1}|^2/2$, or the energy density of the perturbed electric field, $\mathcal{E}_{el} = |E_1|^2/(8\pi)$, and by what factor? For definiteness, just consider the oscillation amplitudes for both energy density components.

Problem 3: Radio Blackout

A space capsule making a reentry into the Earth's atmosphere suffers a communication blackout because a plasma is generated by the shock wave in front of the capsule. If the radio operates at a frequency of 300 MHz, what is the minimum plasma density during the blackout?