

HW1 of Plasma

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1. according to the pressure formular:

$$P = n \cdot k_B (T_i + T_e) \quad , \quad \text{insert into with}$$

$$n = 10^{14} \text{ cm}^{-3} = 10^8 \text{ m}^{-3} \quad ,$$

$$k_B T_i = k_B T_e = 20 \text{ keV} = 20 \times 10^3 \times 1.602 \times 10^{-19} = 3.204 \times 10^{-15}$$

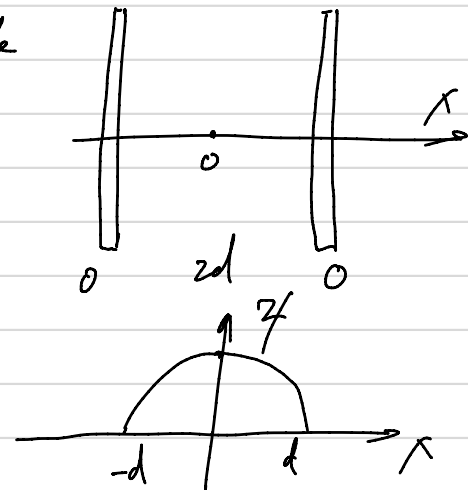
$$\text{so } P = 3.204 \times 10^{-7} \text{ kg} \cdot \text{m}^{-1} \cdot \text{s}^{-2} \quad (2 \times 10^{15} \text{ keV/cm}^3)$$

2. poisson equation : $\nabla^2 \varphi = -\rho/\epsilon_0$, apply the

boundary condition and $\rho = q \cdot n$

$$\frac{d^2}{dx^2} \varphi = -q n / \epsilon_0 \quad , \text{ and } \varphi(\pm d) = 0$$

$$\text{so } \varphi(x) = -\frac{q n}{2 \epsilon_0} (x^2 - d^2) \quad |x| \leq d$$



3. given (2.2.10) , debye length $\lambda_D = 6.9 \sqrt{\frac{T_e}{n_0}} \text{ cm}$

particle numbers in debye sphere would be:

$$N = n_0 \cdot \frac{4\pi}{3} \lambda_D^3 \quad , \quad \text{apply all parameters .}$$

$$N = \frac{4\pi}{3} \cdot (6.9)^3 \cdot (5 \times 10^7)^{\frac{3}{2}} \cdot (10^8)^{-\frac{1}{2}} = 1.539 \times 10^{28}$$

4. given $P = nkT$ $P \propto n$.

also the density follows boltzmann distribution.

$n \propto \exp\left(-\frac{E}{kT}\right)$, take gravitational potential as $E = mgh$.

$\frac{n_{\text{boulder}}}{n_{\text{newyork}}} = \exp\left(-\frac{mg}{kT}(h_b - h_n)\right)$, google tells that $h_b - h_n = 1645$ m.

and $m \propto 29$ g/mol, $g = 9.8$ m/s².

so $\frac{n_b}{n_n} = \exp\left(-\frac{29 \times 10^{-3}}{6.02 \times 10^{23}} \cdot \frac{9.8}{1.38 \times 10^{-23}} \cdot \frac{1645}{20 + 273.15}\right) = 0.8253$

so pressure in Boulder is 17.46% lower than in New York.

5. magnetic field around a moving particle has form of:

$B = \frac{\mu_0 q \cdot v_i}{2\pi d}$, and magnetic force has form of:

$F_B = q \cdot v_i \cdot B$, also the electrostatic force is:

$F_E = \frac{1}{4\pi\epsilon_0} \cdot \frac{q^2}{d^2}$

so $F_B/F_E = 2 \cdot \left(\frac{v_i}{c}\right)^2 \cdot d$

non-relativistic plasma has $v_i \ll c$, and $d \ll 1$

so $\frac{F_B}{F_E} \ll 1$, electrostatic force is much stronger than lorentz force.