

$$* 1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2}$$

$$* 1 + 3 + 5 + \dots + (2n-1) = n^2$$

$$* 1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}$$

$$* 2^2 + 4^2 + 6^2 + \dots + (2n)^2 = \frac{2n(2n+1)(2n+2)}{6}$$

$$* 1^3 + 2^3 + 3^3 + \dots + n^3 = \left(\frac{n(n+1)}{2} \right)^2$$

$$* 1^5 + 2^5 + 3^5 + \dots + n^5 = \frac{n^2(n+1)^2(2n^2+2n-1)}{12}$$

$$* 1.2 + 2.3 + 3.4 + \dots + n(n+1) = \frac{n(n+1)(n+2)}{3}$$

$$* 1.2.3 + 2.3.4 + 3.4.5 + \dots + (n-1)n(n+1) = \frac{(n-1)n(n+1)(n+2)}{4}$$

$$* \frac{1}{1.2} + \frac{1}{2.3} + \frac{1}{3.4} + \dots + \frac{1}{n(n+1)} = 1 - \frac{1}{n+1} = \frac{n}{n+1}$$

$$* \frac{1}{1.2.3} + \frac{1}{2.3.4} + \frac{1}{3.4.5} + \dots + \frac{1}{n(n+1)(n+2)} = \frac{n(n+3)}{4(n+1)(n+2)}$$

$$* \frac{3}{(1.2)^2} + \frac{5}{(2.3)^2} + \frac{7}{(3.4)^2} + \dots + \frac{2n+1}{(n(n+1))^2} = \frac{n(n+2)}{(n+1)^2}$$

$$* 1 + p + p^2 + p^3 + \dots + p^n = \frac{p^{n+1} - 1}{p - 1}$$

$$* 1 - p + p^2 - p^3 + \dots + p^{2n} = \frac{p^{2n+1} + 1}{p + 1}$$

$$* 1 + p^d + p^{2d} + p^{3d} + \dots + p^{nd} = \frac{p^{(n+1)d} - 1}{p^d - 1}$$

$$* 1 - p^d + p^{2d} - p^{3d} + \dots + p^{2nd} = \frac{p^{(2n+2)d} + 1}{p^d + 1}$$

$$* 1 + 2p + 3p^2 + 4p^3 + \dots + (n+1)p^n = \frac{(n+1)p^{n+1}}{p-1} - \frac{p^{n+1} - 1}{(p+1)^2}$$