

Lab 3 CALCULUS FOR IT - 501031

1 Exercises

Exercise 1: Write a computer program to find the limit of functions

(a)
$$\lim_{x\to 3} |x^2 - x - 7|$$
 (f) $\lim_{x\to 3} \frac{x^2 - 9}{\sqrt{x^2 + 7} - 4}$ (k) $\lim_{x\to \infty} \left(1 - \frac{2}{3+x}\right)^x$ (b) $\lim_{x\to 1} \frac{|x-1|}{x^2 - 1}$ (g) $\lim_{x\to 1} \frac{|x|}{\sin(x)}$ (l) $\lim_{x\to \infty} \sqrt[x]{\frac{1}{x}}$ (c) $\lim_{x\to 1} \sqrt[x]{e}$ (h) $\lim_{x\to 0} \frac{1 - \cos x}{x \sin x}$ (l) $\lim_{x\to \infty} \sqrt[x]{\frac{1}{x}}$ (m) $\lim_{x\to \infty} \frac{-\sqrt[3]{x} + \sqrt[3]{1+x}}{-\sqrt{x} + \sqrt{1+x}}$ (e) $\lim_{x\to -1} \frac{x^3 - x^2 - 5x - 3}{(x+1)^2}$ (j) $\lim_{x\to \infty} \left(\frac{3+x}{-1+x}\right)^x$ (n) $\lim_{x\to \infty} \frac{x!}{x^x}$

Exercise 2: Graph the functions which were defined in the previous exercise, and then show the limit points on the graph if possible.

Exercise 3: The f functions are defined as

1.
$$f(x) = \frac{1}{1 + 2^{\frac{1}{x}}}$$
 2. $f(x) = \frac{x^2 + x}{\sqrt{x^3 + x^2}}$

Find $\lim_{x\to 0^+} f(x)$, $\lim_{x\to 0^-} f(x)$, $\lim_{x\to 0} f(x)$ if they exist then show on the graph.

Exercise 4: Let
$$f(x) = \begin{cases} 0, & x \le 0 \\ sin(\frac{1}{x}) & x > 0 \end{cases}$$

- 1. Does $\lim_{x\to 0^+} f(x)$ exist? If so, what is it? If not, show on the screen to explain
- 2. Does $\lim_{x\to 0^-} f(x)$ exist? If so, what is it? If not, show on the screen to explain
- 3. Does $\lim_{x\to 0} f(x)$ exist? If so, what is it? If not, show on the screen to explain

Exercise 5: Prove that the function is continuous at c.

(a)
$$f(x) = x^2 - 7, c = 1$$

 (b) $f(x) = \sqrt{2x - 3}, c = 2$

Exercise 6: Write a program computer to verify at what points are the functions following continuous?



(a)
$$g(x) = \begin{cases} \frac{x^2 - x - 6}{x - 3} & x \neq 0\\ 5 & x = 0 \end{cases}$$

(c)
$$f(x) = \begin{cases} \frac{x^2 - x - 2}{x - 2} & x \neq 2\\ 1 & x = 2 \end{cases}$$

(a)
$$g(x) = \begin{cases} \frac{x^2 - x - 6}{x - 3} & x \neq 0 \\ 5 & x = 0 \end{cases}$$

(b) $f(x) = \begin{cases} \frac{x^3 - 8}{x^2 - 4} & x \neq 2, x \neq -2 \\ 3 & x = 2 \\ 4 & x = -2 \end{cases}$

(d)
$$f(x) = \begin{cases} \frac{1}{x^2} & x \neq 0\\ 1 & x = 0 \end{cases}$$

Exercise 7: Write a program computer to verify where are each of the following functions discontinuous?

1.
$$f(x) = \frac{x^2 - x - 2}{x - 2}$$

2.
$$f(x) = \frac{x^2 - 2x - 3}{2x - 6}$$

Exercise 8: Write a program computer to verify that the function $f(x) = 1 - \sqrt{1 - x^2}$ is continuous on the interval [-1,1] or not.

- Find the limit of function $\lim_{x \to -1} f(x)$ Find the limit of function $\lim_{x \to 1} f(x)$
- Check $\lim_{x \to -1} f(x)$ equals $\lim_{x \to 1} f(x)$ or not.

Exercise 9: Given $P(1, \theta)$ lies on $y = \sin(10\pi/x)$. Q has $(x, \sin(10\pi/x))$, finding slope of secant PQ with x = 2, 1.5, 1.4, 1.3, 1.2, 1.1, 0.5, 0.6, 0.7, 0.8, 0.9 Write a computer program to show the result.

Exercise 10: Define L so that the functions are continuous

(a)
$$f(x) = \begin{cases} \frac{\sin(x)}{x}, & x \neq 0 \\ L, & x = 0 \end{cases}$$

(b)
$$f(x) = \begin{cases} \frac{x^2 + x - 6}{x^2 - 4} & x \neq 2\\ L & x = 2 \end{cases}$$