# Shape Analysis Using Separation Logic

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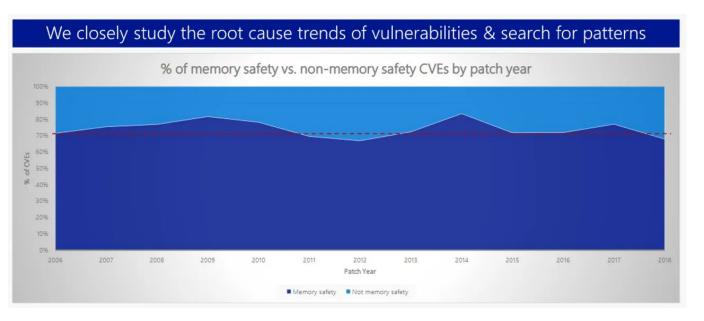
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#### Motivation



- Manual memory management creates a whole class of bugs
- Memory errors are a common source of security vulnerabilities
- Dynamic analysis does not prove correctness
- There is space for static analysis and possibly formal verification



Microsoft: Around 70% of CVEs are memory related

#### Introduction

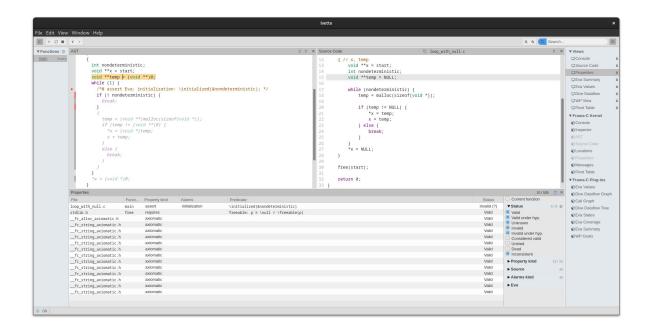


- The goal is to develop a prototype of a static shape analyser
- Use separation logic to represent program states
- Focus on programs that work with linked lists
- Utilize the Frama-C framework to simplify implementation
- Use the Astral solver to efficiently work with separation logic

#### I Frama-C



- Modular framework for analysis of C code
- The program is represented in the C Intermediate Language (CIL)
- CIL is based on a modified AST with extra information
- a GUI frontend called Ivette is under development

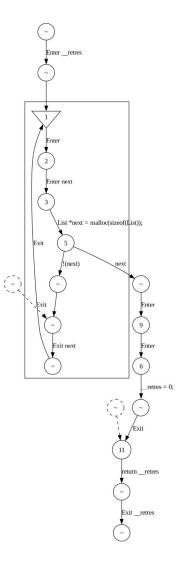




## I Dataflow Analysis



- Runs on the Control Flow Graph (CFG) of the input code
- Each node of the CFG is assigned an analysis state
- States of all nodes are updated until a fixpoint is found for all of them
- The plugin defines a transfer function that computes new states for nodes based on the states of predecessor nodes
- Updates are propagated along the edges of the CFG



example of a CFG

### Separation Logic



- Developed to solve the problem of globality in analyses
- SL formulae describe the state of the heap
- Enables abstraction over linked lists of arbitrary length
- Dedicated solver for SL Astral

$$\varphi \coloneqq x = y \mid x \neq y \qquad \qquad \text{(pure atoms)}$$
 
$$\mid x \mapsto y \mid \text{ls}(x,y) \qquad \qquad \text{(spatial atoms)}$$
 
$$\varphi \coloneqq \varphi \land \varphi \mid \varphi \lor \varphi \mid \varphi \land_{\neg} \varphi \mid \neg \varphi \qquad \qquad \text{(boolean connectives)}$$
 
$$\varphi \coloneqq \varphi \ast \varphi \mid \varphi - \circledast \varphi \qquad \qquad \text{(spatial connectives)}$$



syntax of SL formulae

### Shape Analysis



- Derives the shapes of data structures on the heap
- Previous work defines abstraction rules for a minimal language
- My objectives:
  - adapt this method to work on a subset of C
  - use Astral for solving SL formulae
- The use of Astral provides greater flexibility than the original method

### I Implementation



- Currently limited to programs without function calls
- Preprocessing is done on the AST to simplify statements
- Constants are removed, field accesses are converted to dereferences
- During the analysis, the formulae are simplified between statements
- Results are reported using Ivette

Original	Preprocessed	
<pre>int main() {</pre>	<pre>int main() {</pre>	
	<pre>void *_nil = 0;</pre>	
List *list = (List *)malloc(sizeof(List));	List *list = malloc(sizeof(List));	
<pre>if (list == NULL) return 1;</pre>	<pre>if (list == _nil) return 1;</pre>	
list->next = NULL;	*list = _nil;	
list->data = 42;		

### I Implementation



The visit of every relevant statement modifies the state formulae

- malloc splits the state into the cases of successful and failed allocation
- Dereference of a list node splits the state according to the length of the list

Analyzed statement	State formulae	
	$\varphi \coloneqq \mathrm{emp}$	
a = malloc(8);		
	$\varphi_1 \coloneqq (a \mapsto l_0)$	
	$\varphi_2\coloneqq (a=\mathrm{nil})$	
	$\varphi := \operatorname{ls}(x, \operatorname{nil})$	
y = x->next;		
	$\varphi_1 \coloneqq (x \mapsto y) * \operatorname{ls}(y, \operatorname{nil})$	
	$\varphi_2 \coloneqq (x \mapsto y) * (y = \mathrm{nil})$	

## Abstraction and simplification



- The abstraction ensures that the analysis will terminate
- Between statements, the formulae are also simplified and deduplicated
- This is done to speed up the analysis

Type of simplification	Input formula	Output formula
abstraction to list segments	$(x \mapsto l_0) * (l_0 \mapsto y)$	ls(x, y)
removal of variables at the end of their scope	$(x = y) * (y \mapsto z)$	$(y \mapsto z)$
removal of irrelevant inequalities	$(x \mapsto y) * (y \neq l_0)$	$(x \mapsto y)$
removal of unsatisfiable formulae	$(x \mapsto y) * (x = y)$	



 The analyzed code constructs a linked list, traverses all nodes, and then deallocates it

The following program works with a singly linked list

```
typedef struct List {
        struct List *next;
        int data;
} List;
```



The program starts by allocating the first node

```
int main() {
   List *start = malloc(sizeof(List));
   if (start == NULL)
     return 1;
```

At this point, the state is represented by a formula

```
(\text{\_nil} = \text{nil}) * (\text{start} \mapsto \text{alloc}_0) * (\text{start} \neq \text{\_nil})
```



• Then the whole list is allocated, up to a nondeterministic length

```
{ // construct a linked list of unknown size
   List *list = start;
   list->next = NULL;
   int nondeterministic;
   while (nondeterministic) {
      List *next = malloc(sizeof(List));
      if (next == NULL)
          return 1;
      list->next = next;
      list = list->next;
   }
   list->next = NULL;
}
```

After this, the state is

```
_{\rm nil} = {\rm nil} * {\rm ls(start, \_nil)} * {\rm start} \neq _{\rm nil}
```



 After traversing the list, the state stays the same since the shape of the data structure did not change

```
{ // walk to the end of the list
  List *list = start;
  while (list != NULL) {
     List *next = NULL;
     next = list->next;
     list->data = 42;
     list = next;
  }
}
```



At last, all nodes are deallocated

```
{ // free the list
   List *list = start;
   while (list != NULL) {
      List *next = NULL;
      next = list->next;
      free(list);
      list = next;
   }
}
```

The state is changed to reflect that

$$(\text{nil} = \text{nil}) * (\text{start} \neq \text{nil})$$

#### **I** Error detection



- The analysis is not only able to detect the shape of data in a correct program, it can also detect memory errors
- If we try to access the list after deallocation, the bug is detected

```
start->next = NULL; // use after free
```

After adding this line below the deallocation, an error is raised

```
[SLplugin] examples/linked_list.c:54: Failure:
    detected a dereference of an unallocated variable
```

#### I Results in Ivette



These results can be viewed using the Ivette GUI extension



#### I Future work



- Support the analysis of function calls, possibly with caching of results
- Preprocess complex statements to enable the analysis of more programs
- Support global and static variables
- Most importantly, extend the analysis to more complex data structures (doubly linked lists, nested lists)
- Benchmark the analysis and compare it to other solutions

### Summary



- Studied topics: Frama-C framework, dataflow analysis, separation logic, Astral solver, shape analysis
- Implemented a prototype of shape analysis using separation logic,
   able to analyze simple programs that work with linked lists