

# Artificial Intelligence

[Tasks]

formal task

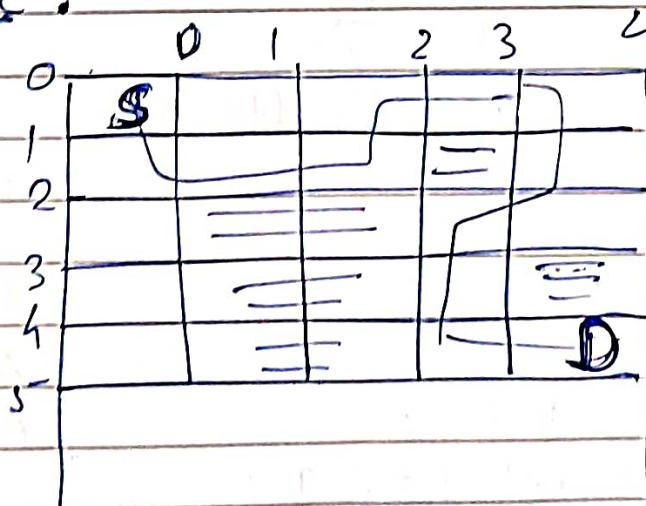
Games  
mathematics

expert task

scientific analysis.

State space search  
Elements :- (i) states :- initial  
final  
(ii) set of Rules

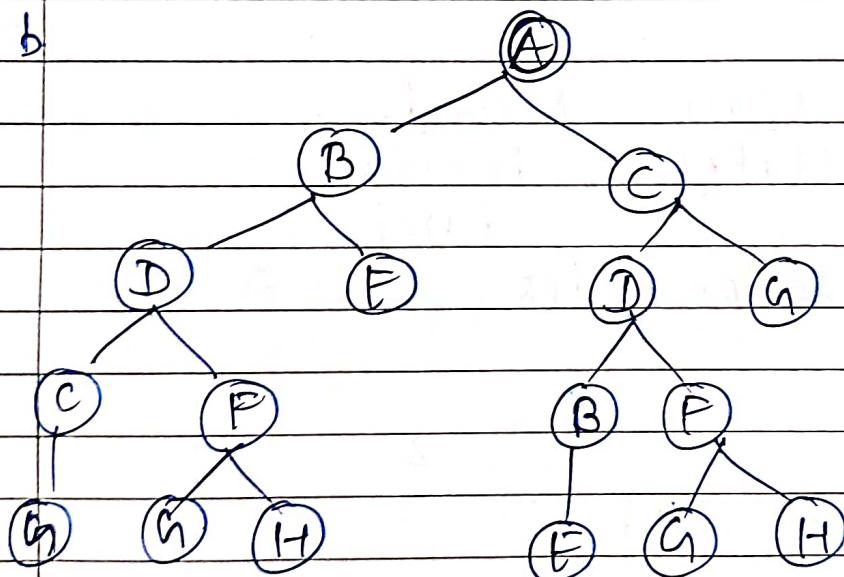
Example :-



## Breadth first search

1. Create a variable called Node list and set it to initial state
2. Until a goal is not reached :-
  - a. Remove the first element from Node list and call it E.
  - If Node list is empty, then quit

b



Node list: A

Node list : B C

Node list : D E C

Node list : ~~E F G C D~~

A

AB

ABC

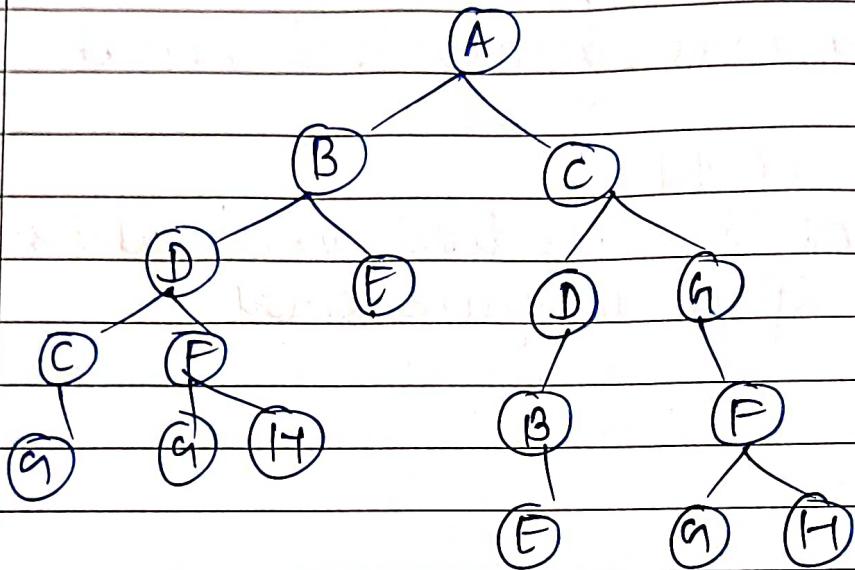
### Advantage of BFS

- simplest search algorithm
- BFS is & gives guaranteed results

### Disadvantage of BFS

- BFS cannot be effectively used unless the search space is quite small

## DFS (Depth first search)



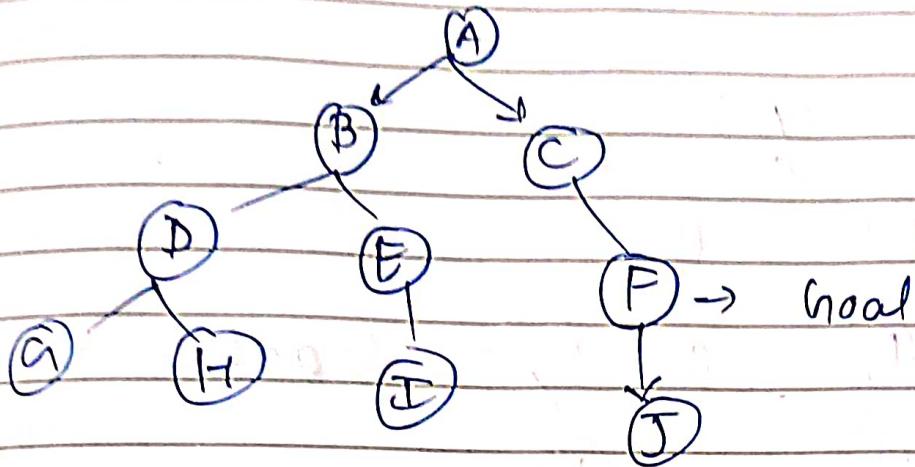
Advantage :-

- consumes less memory space since only the nodes on the current path are stored.

Disadvantage:-

- may find sub optimal solution

## Depth limited search



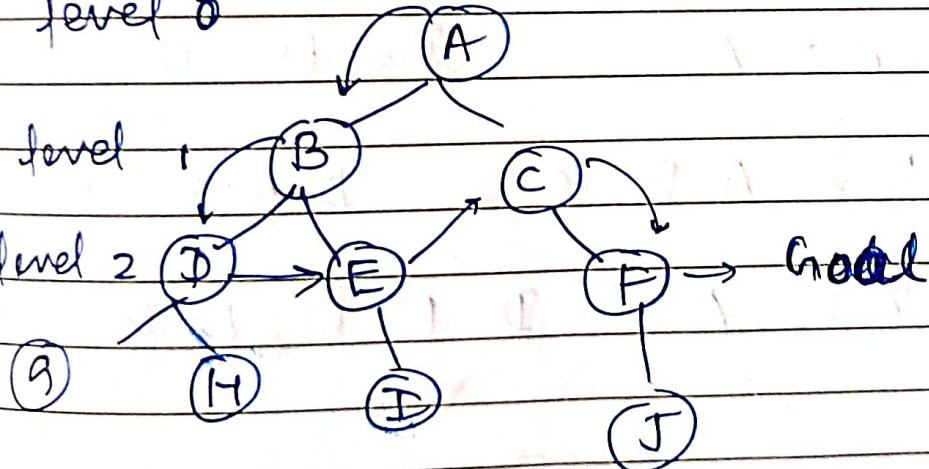
DFS : left of A

$A \rightarrow B \rightarrow D \rightarrow G \rightarrow H \rightarrow E \rightarrow I \rightarrow C \rightarrow [F]$

## Depth limit

level 0

Depth limit - 2



DLS :  $A \rightarrow B \rightarrow D \rightarrow E \rightarrow C \rightarrow F$

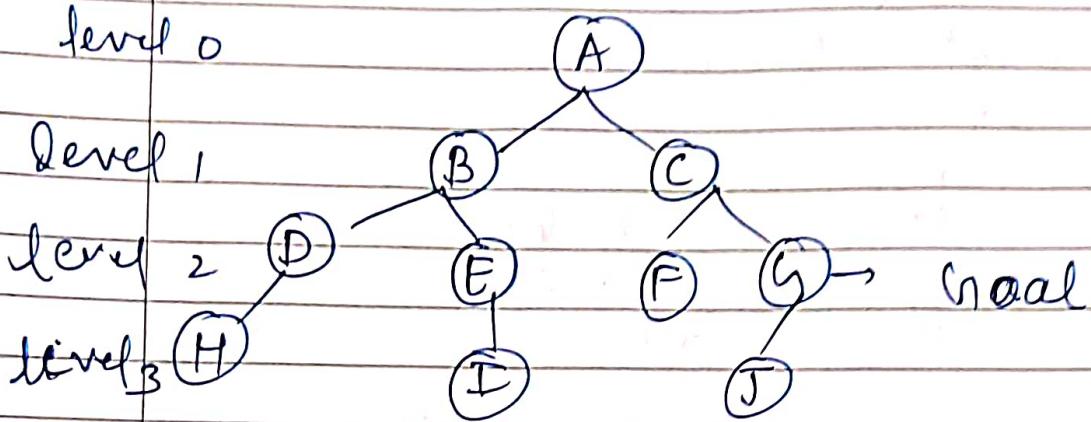
## Iterative Deepening Depth first search

level 0

Level 1

level 2

level 3



DFS :- A → B → D → H → E → I → F → G → C → E → G

iteration 0 : A Depth 0

iteration 1 : A B C Depth 1

iteration 2 : A B D E C F G Depth 2

## Bidirectional search algorithm

Runs two simultaneous searches one from initial called forward search and one from goal node called backward search

It replaces the single search graph with two small subgraph in which one starts the search from initial vertex and other start from goal vertex.

Search stops when these two graphs intersect each other.

BS can use search techniques such as BFS, DFS, DLS etc.

Advantages:

It is fast

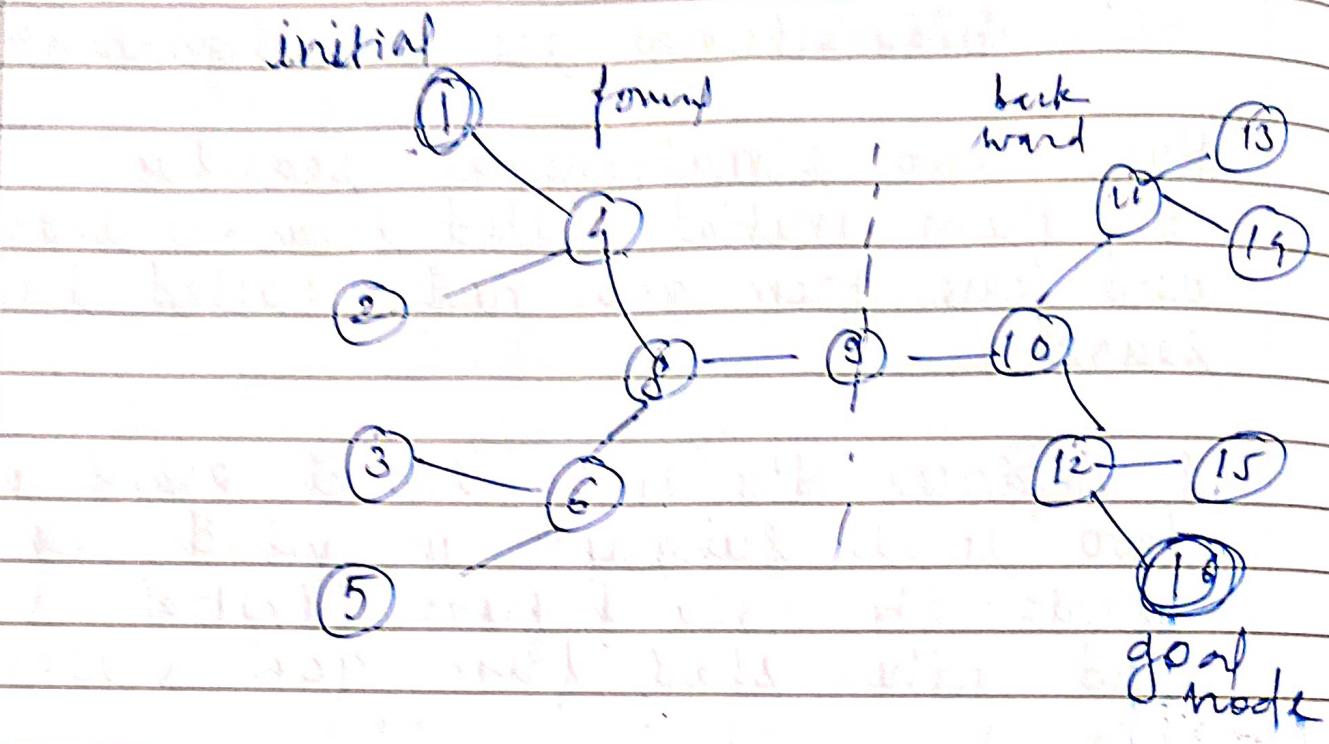
requires less memory.

Disadvantages:

Implementation is difficult.

Should know goal state in advance.

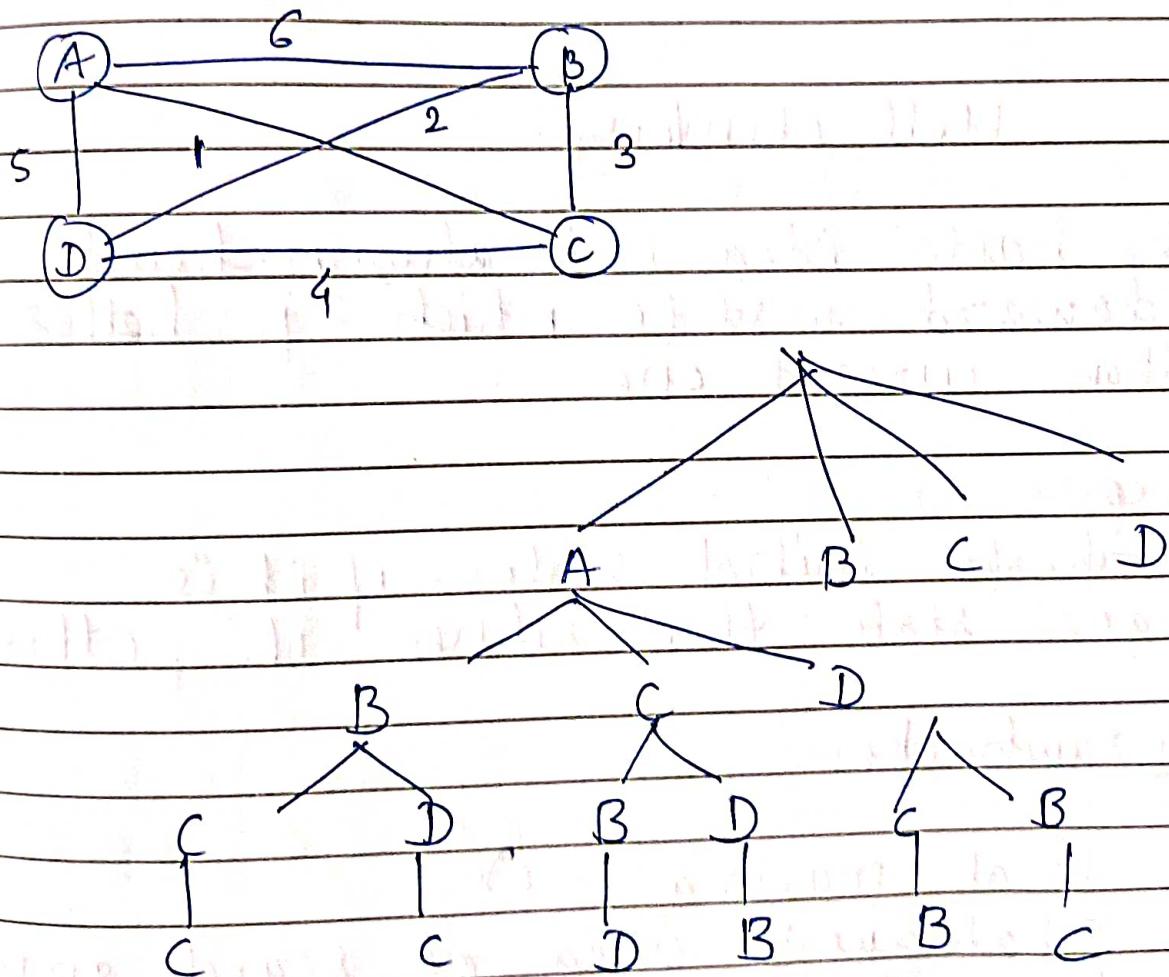
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Comparison:-

## Generate and test algorithm

1. Generate all the possible solutions
2. Select one solution among the possible solutions
3. If solution has been found and acceptable



search for Path length

|   |      |    |
|---|------|----|
| 1 | ABCD | 19 |
| 2 | ABDC | 18 |
| 3 | ACBD | 12 |
| 4 | ACDB | 13 |
| 5 | ADBC | 16 |

### Hill climbing.

The basic idea is to always head toward a state which is better than current one

Steps:-

Evaluate initial state. if it is goal state then return it, otherwise

Drawbacks:-

local maxima

Plateaus:- Area of search space where evaluation function is flat

Ridge

Example :

start

A - 1  
D + 1  
C + 1  
B - 1

①

goal

D +  
C + 1  
B + 1  
A + 1

④

local heuristic

+1 for each block that is resting on thing it is supposed to be resting on

-1 for each block that is resting on wrong thing

A  
D  
C   ⇒   +1 D  
      +1 C  
B   -1 B   A + 1  
      ②

⇒ +1 C   D - 1  
      -1 B   A + 1

|    |   |
|----|---|
| -3 | A |
| -2 | D |
| -1 | C |
| 0  | B |

|   |   |
|---|---|
| D | 3 |
| C | 2 |
| B | 1 |
| A | 0 |

-6

6

-2 D

-1 C

0 B A 0

-1 C D -1

0 B A 0

-3

-2

-1 C

0 B

A 0

D 0



A B C A D

B  
A D CA  
B  
C  
D

Start

|   |   |   |   |    |
|---|---|---|---|----|
| A | D | 3 | A | -3 |
| B | C | 2 | D | -2 |
| C | B | 1 | C | -1 |
| D | A | 0 | B | 0  |

goal

(G)



-2 D

-1 C

0 B

A



-1 C

D -1

0 B

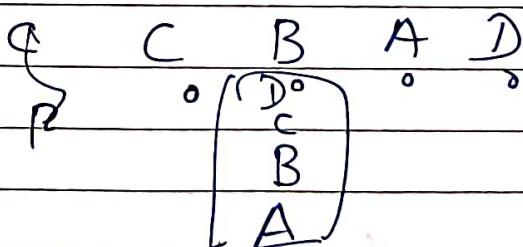
A 0

C

B

A

D



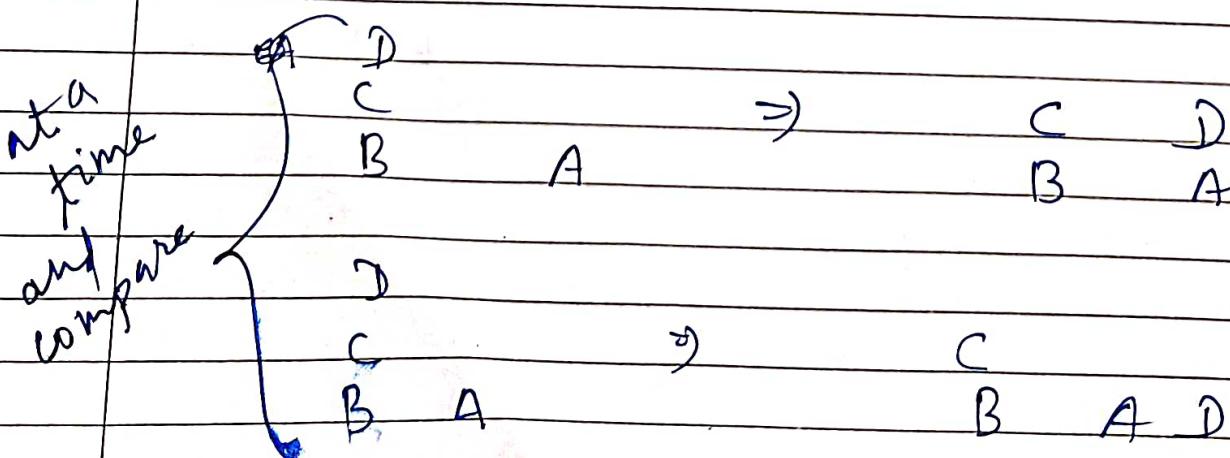
## Difference between Hill climbing and steepest hill climbing method

Basic hill climbing applies one operator and gets new state.

if it is better that becomes current state

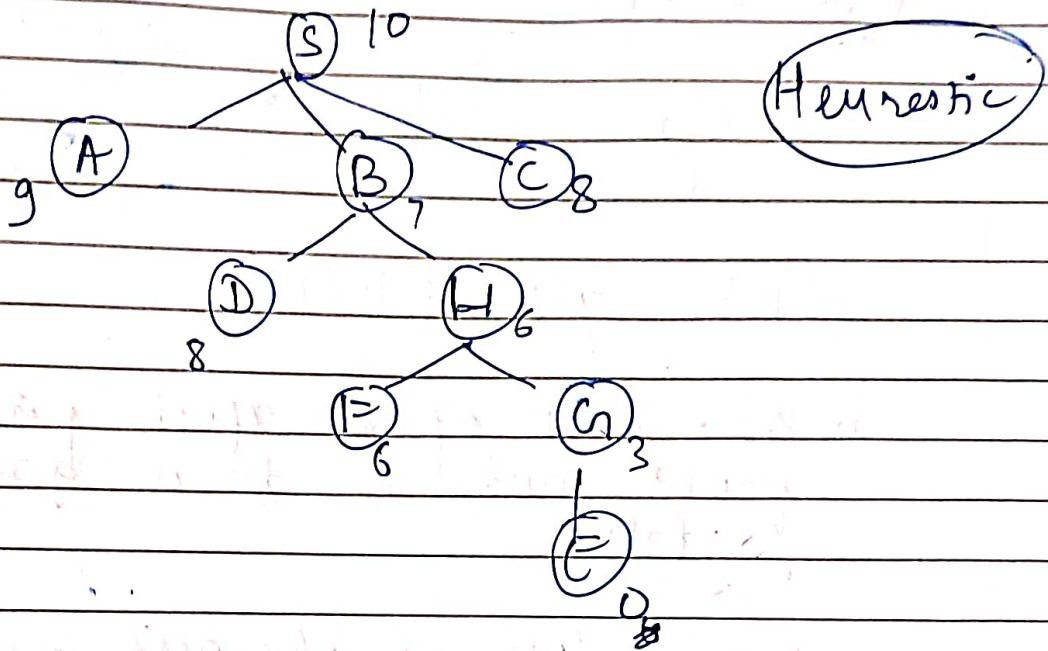
where as in steepest hill climbing we to consider all the moves from current state.

sel.  
Selects best  
one



## Best first search

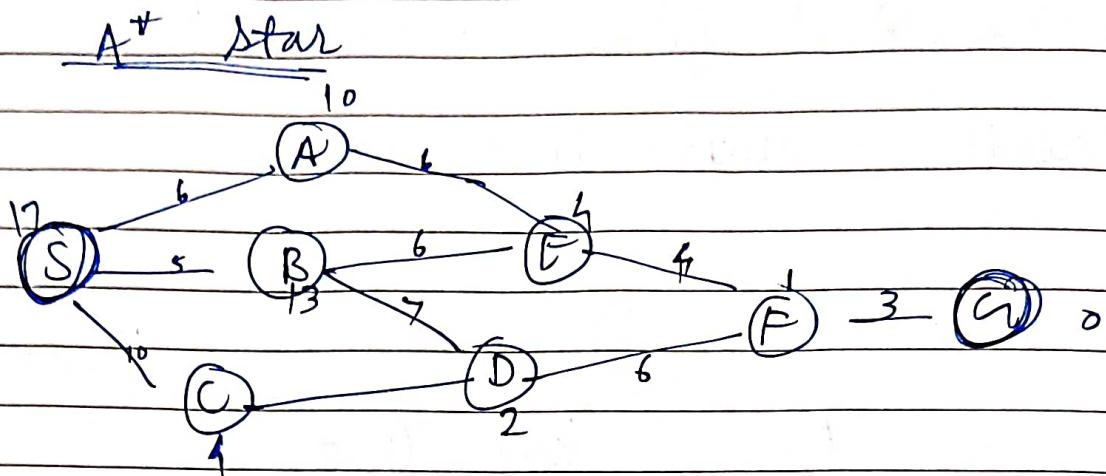
Create 2 empty list OPEN CLOSED



| Open      | Closed      |
|-----------|-------------|
| Node H(n) | Node f H(n) |
| S 10      | S 10        |
| A 9       | B 7         |
| B 7       | C 8         |
| C 8       | A 9         |

| Open      | Closed      |
|-----------|-------------|
| Node H(n) | Node f H(n) |
| H 6       | S 10        |
| C 8       | B 7         |
| D 8       | H           |
| A 9       |             |

S → B → H → G → F



$$f(n) = g(n) + h(n)$$

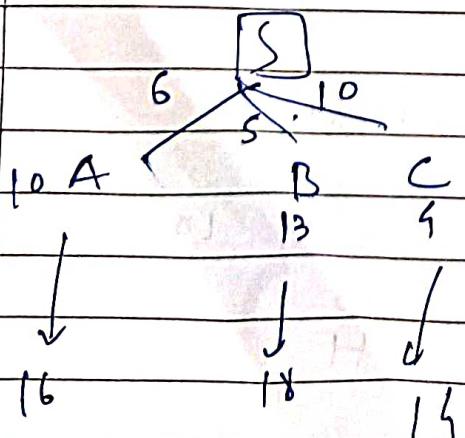
$h(n)$  = cost of cheapest path from node  $n$  to a goal state

$g(n)$  = cost of cheapest path from initial state to node  $n$

17 (S) 17

Queue

S



Queue

S C

S A

S B



## A\* 8 puzzle problem

|   |   |   |
|---|---|---|
| 2 | 8 | 3 |
| 1 | 6 | 4 |
| 7 | 5 | 1 |

initial state

|   |   |   |
|---|---|---|
| 1 | 2 | 3 |
| 8 |   | 4 |
| 7 | 6 | 5 |

final state

$$f(n) = g(n) + h(n)$$

 $g(n) \Rightarrow$  depth of node $h(n) \Rightarrow$  number of misplaced tiles

$$\begin{array}{l} g=0 \\ h=4 \end{array}$$

$$f = 0 + 4 = 4$$

|   |   |   |
|---|---|---|
| 2 | 8 | 3 |
| 1 | 6 | 4 |
| 7 | 5 | 1 |

|   |   |   |
|---|---|---|
| 2 | 8 | 3 |
| 1 |   | 4 |
| 7 | 6 | 5 |

|   |   |   |
|---|---|---|
| 2 | 8 | 3 |
| 1 | 6 | 4 |
| 7 | 5 | 1 |

$$\begin{array}{l} g=1 \\ h=5 \end{array}$$

$$f = 1 + 5 = 6$$

$$\begin{array}{l} g=1 \\ h=3 \end{array}$$

$$f = 1 + 3 = 4$$

$$\begin{array}{l} g=1 \\ h=5 \end{array}$$

$$f = 1 + 5 = 6$$

select minimum

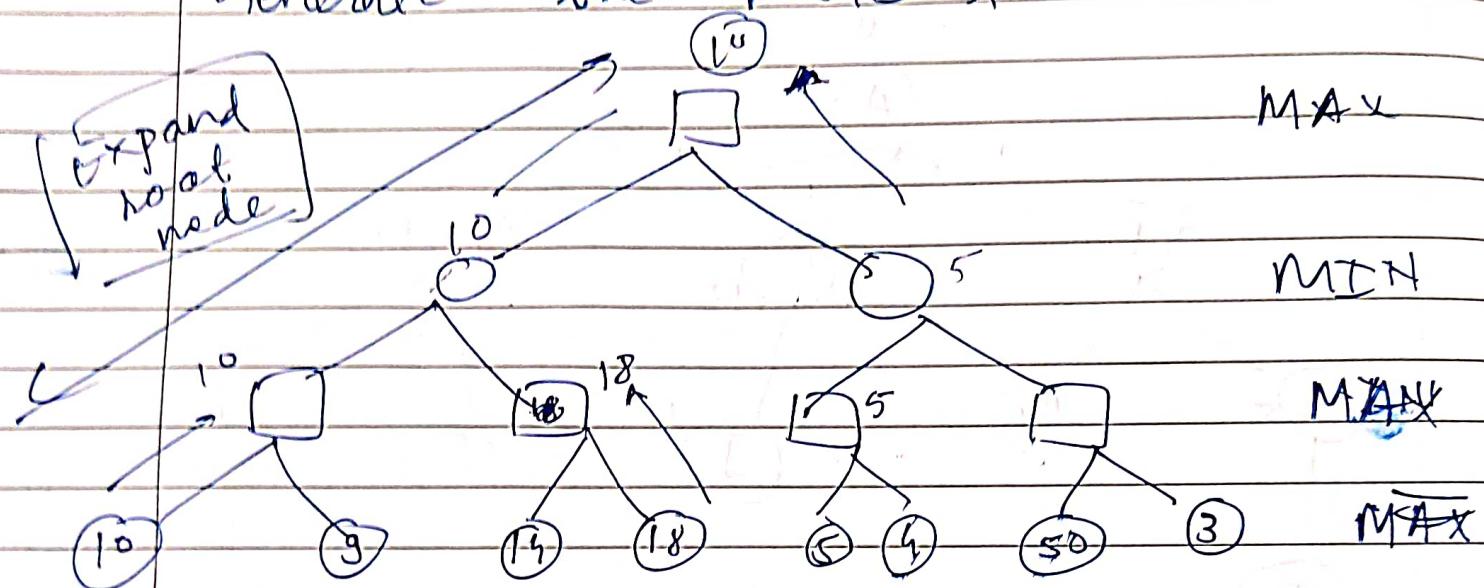
$$F(0,1) = 1+1=2$$

(5) will be replaced by 2

6 will be replaced by 3

### Minimax Algorithm

Generate the whole tree to leaves



Select the path to which  
10 is assigned

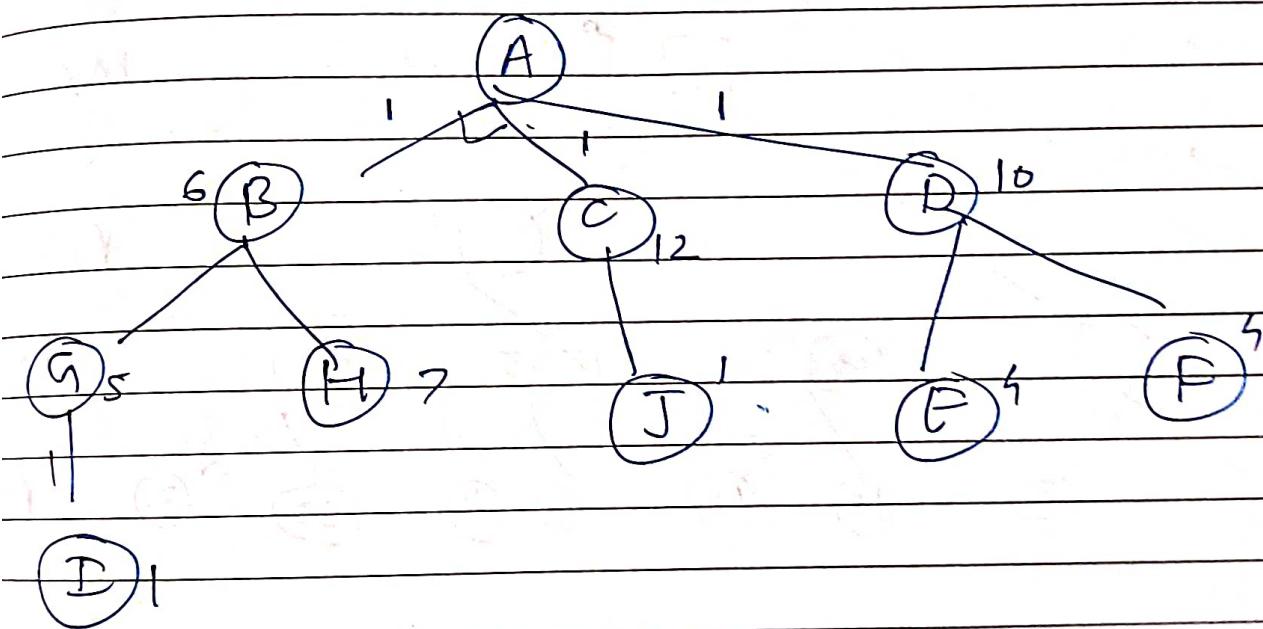


## AO\* search

In AO\* we divide ~~small~~ problems into small problems

and use concept of AND OR graphs

$$f(n) = g(n) + \beta h(n)$$

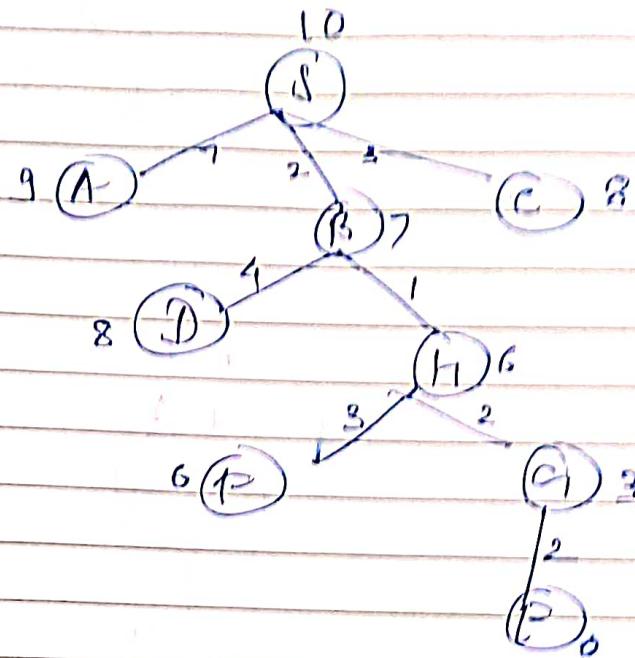


$$f(A) = 10 + 1 = 11$$

$$f(ABC) = 12 + 8 + 1 + 1 = 20$$

$$f(DEF) = 5 + 4 + 1 + 1 + 1 = 10$$

## A\* search



$$\begin{aligned}
 f(n) &= g(n) + h(n) \\
 f(B) &= 2 + 7 \\
 &= 9
 \end{aligned}$$

|      | Open   |        |        |
|------|--------|--------|--------|
| Node | $g(n)$ | $h(n)$ | $f(n)$ |
| S    | 0      | 10     | 10     |
| A    | 7      | 9      | 16     |
| B    | 2      | 7      | 9      |
| C    | 3      | 8      | 11     |

|      | Closed |  |
|------|--------|--|
| Node | parent |  |
| S    |        |  |
| B    | S      |  |
| H    | B      |  |

$$\begin{aligned}
 f(h) &= 3 + 6 \\
 &= 9
 \end{aligned}$$

|   |   |   |   |    |
|---|---|---|---|----|
| D | 9 | 6 | 8 | 15 |
| H | 3 | 6 | 9 |    |

uninformed  
search / Brute force

informed  
search

search without  
information

search with  
information

No knowledge

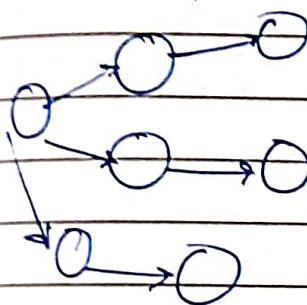
Use  
knowledge  
quick solution

time consuming

more complexity

$(n-1)!$

less complexity



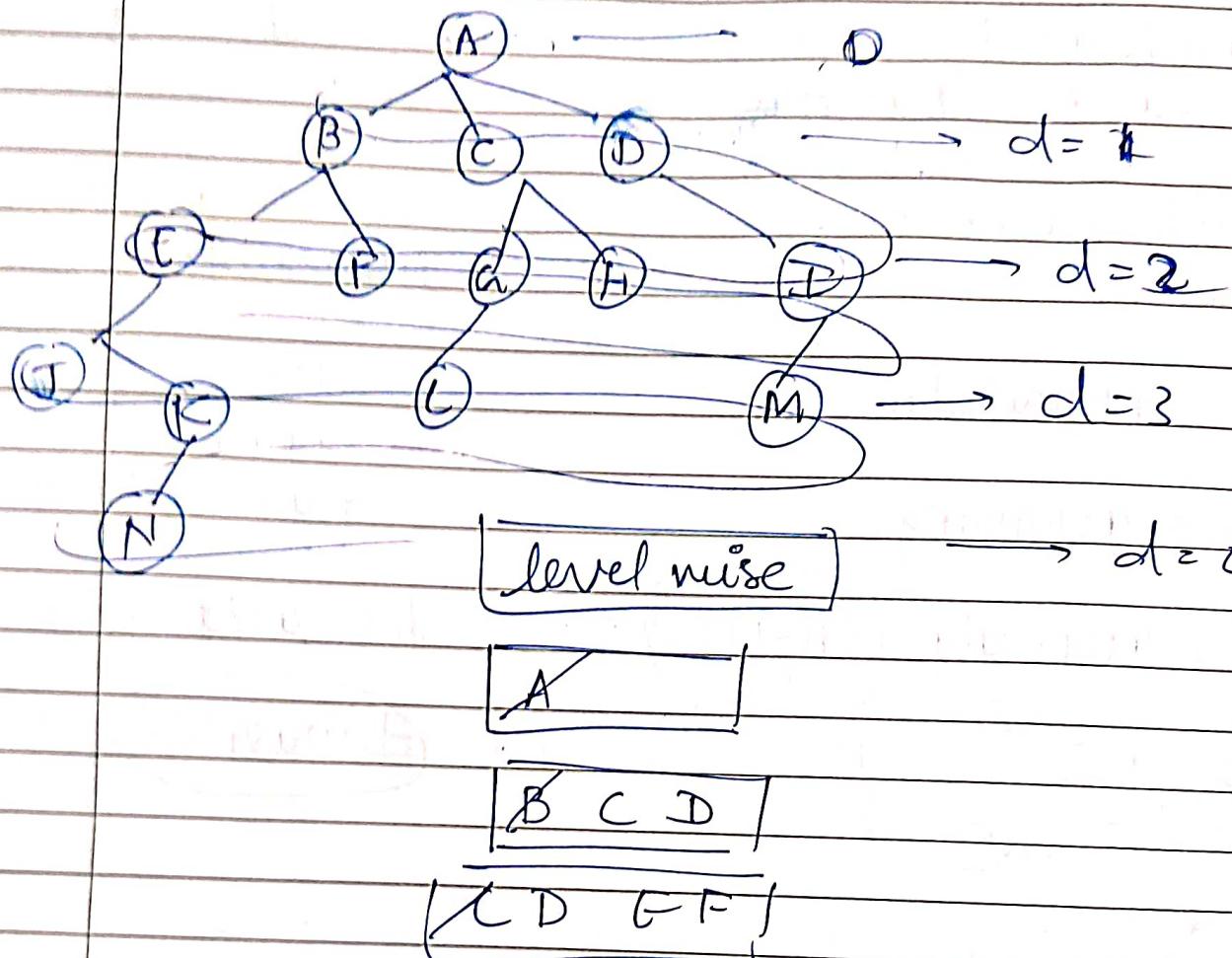
Heuristic

BFS (Breadth first search)

- uninformed search technique → optimal
- FIFO (queue)

fringe  $\rightarrow$  first node

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Time complexity  $O(V+E)$

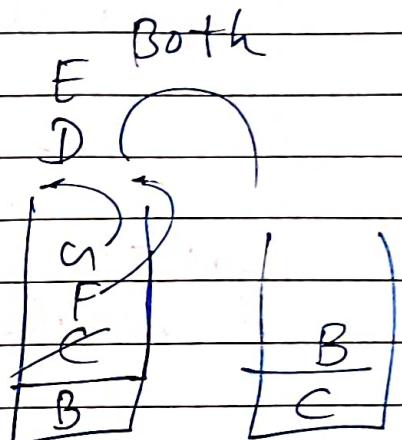
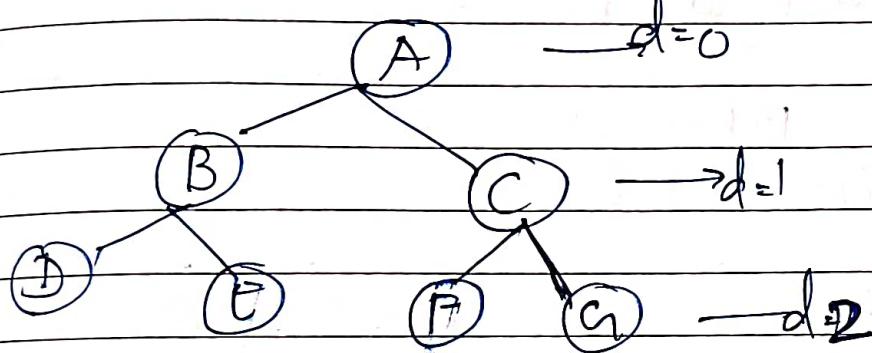
V :- no. of nodes  
E :-  $O(b^d)$   
b :- branch factor

d depth

## Depth first search

Uninformed search → Non optimal  
stack (LIFO)

Deepest Node  
Incomplete.



⇒ A C G F B E D

time complexity →  $O(b^d)$   
branching factor  
depth.

## Bidirectional search

simultaneous search from an initial node to goal and backward from initial to go goal to initial

$$2 \left( \text{at } b^{d/2} \right)$$

Complete in BFS  
incomplete in DFS

Optimal

8-Puzzle using non-heuristic

$$\begin{matrix} \text{BFS} \\ O(b^d) \end{matrix}$$