## A. Experimental Results with 10 Repetitions

Table 1: Mean accuracy (%) of competing methods on four test environments in simulation study with 10 repetitions.

ENV PARTITION	$(p_s^-, p_s^+)$	(0.999, 0.7)				(0.999, 0.8)				(0.999, 0.9)			
	$p_v(t)$	0.9		0.8		0.9		0.8		0.9		0.8	
	TEST ACC	MEAN	Worst	MEAN	Worst	MEAN	Worst	MEAN	Worst	MEAN	Worst	MEAN	Worst
	ERM	76.22	58.81	59.80	25.95	69.34	43.06	55.96	15.60	60.62	23.30	53.10	8.04
	EIIL	39.43	18.22	64.95	48.45	50.26	47.02	68.86	54.91	61.33	52.70	69.82	58.58
Erron	HRM	76.52	59.78	59.98	26.97	69.87	44.49	56.40	16.85	60.57	23.46	53.16	8.37
False	TIVA	82.54	76.74	75.82	70.97	81.53	73.05	69.78	56.23	71.42	49.95	59.47	30.77
	ZIN	87.70	85.86	78.33	76.60	86.78	84.86	77.42	75.12	83.42	78.62	74.03	67.45
	MINMAX-TV- $\ell_1$	88.67	87.83	78.14	76.68	88.55	87.62	78.74	77.56	87.01	85.74	77.31	74.54
	GROUPDRO	72.42	54.90	63.74	43.37	71.09	51.60	62.78	40.21	69.67	47.72	61.81	36.44
TRUE	IRM	87.84	86.20	78.33	76.58	86.84	84.42	77.48	74.80	84.16	77.89	74.53	68.72
	IRM-TV- $\ell_1$	88.03	86.40	78.49	76.88	87.10	84.90	77.95	75.65	84.84	80.06	75.55	70.77

Table 2: Standard deviation (%) of competing methods on four test environments in simulation study with 10 repetitions.

ENV PARTITION	$\mid (p_s^-, p_s^+)$	(0.999, 0.7)				(0.999, 0.8)				(0.999, 0.9)			
	$p_v(t)$	0.9		0.8		0.9		0.8		0.9		0.8	
	TEST ACC	MEAN	Worst	MEAN	Worst	MEAN	Worst	MEAN	Worst	MEAN	Worst	MEAN	Worst
	ERM	1.17	2.06	1.04	2.06	1.23	2.47	0.76	1.42	1.10	2.01	0.62	0.95
	EIIL	1.52	3.18	1.46	1.72	1.70	3.09	1.43	2.26	2.46	1.99	1.58	2.04
FALSE	HRM	1.35	2.71	0.94	2.43	0.75	1.83	0.71	2.33	0.84	1.29	0.45	0.93
FALSE	TIVA	6.12	11.09	3.55	7.18	4.83	9.19	6.46	13.96	5.18	10.34	6.32	13.66
	ZIN	1.05	2.19	1	1.43	1.67	2.73	1.43	2.13	3.52	6.72	2.09	3.86
	MINMAX-TV- $\ell_1$	0.57	0.60	0.84	1.03	0.45	0.50	0.67	0.74	1.28	1.66	0.65	1.13
TRUE	GROUPDRO	8.45	18.08	6.99	16.84	8.42	19.03	6.71	17.27	8.27	18.51	6.52	16.45
	IRM	0.82	2.01	0.91	1.49	1.16	2.34	1.82	3.01	1.98	4.11	3.14	4.52
	IRM-TV- $\ell_1$	0.86	2.08	0.74	1.33	1.35	2.67	1.24	2.22	2.19	4.77	2.92	4.31

Table 3: Average mean squared error of competing methods in house price prediction with 10 repetitions.

			Average		STD			
ENV PARTITION	METHODS	TRAIN	TEST	Worst	TRAIN	TEST	Worst	
	ERM	0.1057	0.4409	0.6206	0.0017	0.0435	0.0641	
	EIIL	0.1103	0.3939	0.5581	0.0020	0.0305	0.0460	
FALSE	HRM	0.5578	0.5949	0.7250	0.0593	0.0025	0.0052	
FALSE	TIVA	0.2575	0.4418	0.6145	0.0002	0.0019	0.0062	
	ZIN	0.2241	0.4293	0.6198	0.1137	0.1994	0.2869	
	MINMAX-TV- $\ell_1$	0.2168	0.3395	0.4983	0.0652	0.0638	0.0958	
	GROUPDRO	0.1271	0.7358	1.0611	0.0029	0.0877	0.1287	
TRUE	IRM	0.5663	0.8168	1.1168	0.1389	0.3115	0.4511	
	IRM-TV- $\ell_1$	0.3261	0.4420	0.6096	0.1279	0.2503	0.3342	

Table 4: Mean accuracy (%) of competing methods on CelebA with 10 repetitions.

			MEAN			STD	
ENV PARTITION	METHODS	TRAIN	TEST	Worst	TRAIN	TEST	Worst
	ERM	63.76	63.99	62.05	14.45	14.16	14.16
	EIIL	59.12	58.15	54.22	8.74	8.48	10.23
Erron	LfF	57.50	57.73	56.18	0.12	0.24	0.57
FALSE	TIVA	64.36	64.23	61.63	1.68	1.99	1.47
	ZIN	78.32	76.73	76.19	1.16	0.87	0.85
	MINMAX-TV- $\ell_1$	85.12	83.68	81.45	0.92	0.33	0.43
	GROUPDRO	81.50	81.19	79.27	0.31	0.48	0.74
TRUE	IRM	85.59	82.54	80.75	1.49	1.35	0.99
	IRM-TV- $\ell_1$	84.79	83.47	81.21	0.59	0.48	0.67

Table 5: Mean accuracy (%) of competing methods on Landcover with 10 repetitions.

		M	IEAN		STD				
METHODS	TRAIN	IID TEST	OOD TEST	Worst	TRAIN	IID TEST	OOD TEST	Worst	
ERM	66.61	66.44	61.54	60.80	1.82	1.56	0.92	0.77	
EIIL	64.11	63.81	60.43	59.53	1.66	1.72	0.88	1.21	
LfF	58.12	57.89	55.76	55.07	2.73	2.45	1.96	1.93	
TIVA	67.49	64.79	52.02	51.46	0.28	0.62	0.98	1.09	
ZIN	70.02	69.42	62.22	61.87	1.09	1.14	1.09	1.21	
MINMAX-TV- $\ell_1$	73.59	71.95	63.77	63.25	0.69	0.63	1.17	1.37	