

An Exploration of Finite State Automata

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1 Traffic Light

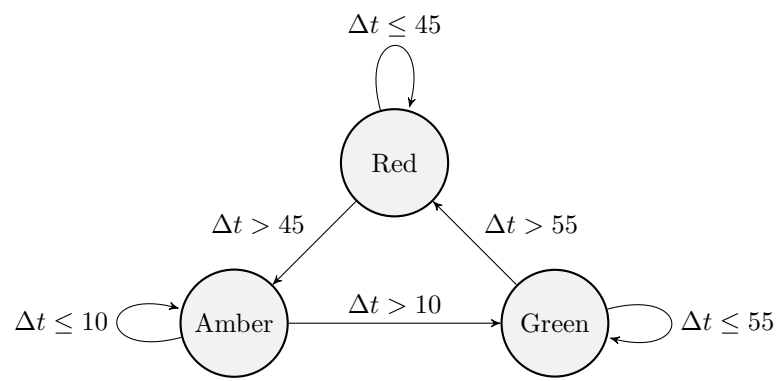


Figure 1: Graph showing the finite state automata where Δt represents the number of ticks, or seconds, since the last state change.

2 Decimal Parser

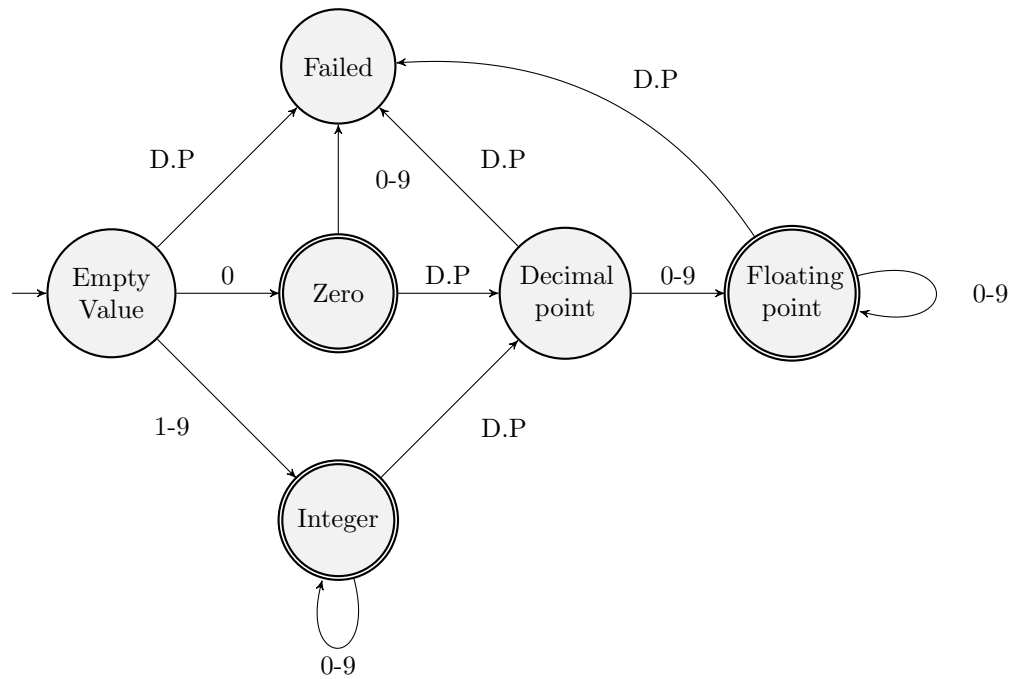


Figure 2: A finite state machine that parses a number from a string one character at a time. The state machine ends when the final character is reached. The parse is considered a success if the ending position is on an accepting node. Any undefined behaviour, such as encountering a character not in $\{ '0', '1', '2', '3', '4', '5', '6', '7', '8', '9', '.' \}$, is automatically assumed to be a fail.

3 Letters to Digits and vice versa converter

3.1 Rules

R_0 : $S \rightarrow \text{STRING}$

R_1 : $\text{STRING} \rightarrow \text{DIGIT STRING}$

R_2 : $\text{STRING} \rightarrow \text{LETTER STRING}$

R_3 : $\text{STRING} \rightarrow \text{DIGIT}$

R_4 : $\text{STRING} \rightarrow \text{LETTER}$

R_5 : $\text{DIGIT} \rightarrow \text{LETTER}$

R_6 : $\text{LETTER} \rightarrow \text{DIGIT}$

R_7 : $\text{DIGIT} \rightarrow 0$

R_8 : $\text{DIGIT} \rightarrow 1$

R_9 : $\text{DIGIT} \rightarrow 2$

R_{10} : $\text{DIGIT} \rightarrow 3$

R_{11} : $\text{DIGIT} \rightarrow 4$

R_{12} : $\text{DIGIT} \rightarrow 5$

R_{13} : $\text{DIGIT} \rightarrow 6$

R_{14} : $\text{DIGIT} \rightarrow 7$

R_{15} : $\text{DIGIT} \rightarrow 8$

R_{16} : $\text{DIGIT} \rightarrow 9$

R_{17} : $\text{LETTER} \rightarrow A$

R_{18} : $\text{LETTER} \rightarrow B$

R_{19} : $\text{LETTER} \rightarrow C$

R_{20} : $\text{LETTER} \rightarrow D$

R_{21} : $\text{LETTER} \rightarrow E$

R_{22} : $\text{LETTER} \rightarrow F$

R_{23} : $\text{LETTER} \rightarrow G$

R_{24} : $\text{LETTER} \rightarrow H$

R_{25} : $\text{LETTER} \rightarrow I$

R_{26} : $\text{LETTER} \rightarrow J$

3.2 Terminal Symbols

$\Sigma = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 0, A, B, C, D, E, F, G, H, I, J\}$

3.3 Non-terminal Symbols

$N = \{\text{STRING}, \text{DIGIT}, \text{LETTER}\}$

3.4 Finite State Machine

