

BatchName : PreCAT OM25  
Subject Name : Data Structure

### # DS DAY-01:

#### Q. Why there is a need of data structure in programming?

There is a need of data structures in programming to achieve efficiency in operations.

#### Q. What is a data structure?

It is a way to store data elements into the memory (i.e. into the main memory) in an **organized manner** so that operations like **addition, deletion, searching, sorting, traversal etc....** can be performed on it efficiently.

- we want to store marks 100 students:

int m1, m2, m3, m4, ....., m100; //sizeof(int): 4 bytes => 400 bytes

- we want to arrange marks in a descending order => sorting

int arr[ 100 ]; //400 bytes

#### + Array:

An array is **linear/basic data structure**, which is a **collection/ list of logically related similar type of data elements** gets stored into the memory at **contiguous locations**.

int arr[ 5 ] ;

- in an array, to convert array notation into its eq pointer notation is done by the compiler,

**i.e. to maintain link between array elements in an array is the job of compiler.**

- we want to store records of 100 employees:

empid : int  
name : char [ ] / string  
salary : float

- in an array we can collect/combine logically related similar type of data elements only, and hence to overcome this limitation structure data structure has been designed.

### + Structure:

It is a **linear / basic data structure**, which is a **collection / list of logically related similar and dissimilar type of data elements** gets stored into the memory collectively as a single entity / record.

```
struct employee
{
    int empid;//4 bytes
    char name[ 32 ];//32 bytes
    float salary;//4 bytes
};
```

sizeof structure = sum of size of all its members  
sizeof(struct employee): 40 bytes

- there are 2 types of data types:

**1. primitive/predefined/builtin data type:** char, int, float, double, void  
=> data types which are already known to the compiler

**2. non-primitive / derived / user defined data type :** pointer, array, structure, union, enum, function etc...

=> data types which are not already known to the compiler, i.e. need to define/derived by the programmer

user defined data type:  
typedef

```
typedef int INT;//user defined => not a derived data type
typedef int bool_t;//user defined => => not a derived data type
typedef struct employee emp_t;//derived / user defined
int *iptr;//derived data type
```

- there are two types of data structures:

**1. linear / basic data structures:** data structures in which data elements gets stored into the memory in a linear manner/linearly and hence can be accessed linearly (i.e. one after another).

- array
- structure & union
- linked list
- stack
- queue

**2. non-linear / advanced data structures:** data structures in which data elements gets stored into the memory in a non-linear manner (e.g. hierarchical manner), and hence can be accessed non-linearly.

- tree
  - graph
  - binary heap
  - hash table
- etc....

structure is a derived data type =>

```
struct employee
{
    int empid;//4 bytes
    char name[ 32 ];//32 bytes
    float salary;//4 bytes
};
=> compiler
```

```
<data type> <var_name>;
int num;
```

```
struct employee emp;
```

- to learn data structures, is not to learn any programming language, it is nothing but to learn algorithms, data structure algorithms can be implemented in any programming language ( C / C++ / Java / Python ).

**Q. What is a Program? => Machine**

- A Program is a finite set of instructions written in any programming language (i.e. either in low level / high level ) given to the machine to do specific task.

**Q. What is an algorithm? => User/Human Beings**

- An algorithm is a finite set of instructions written in any human understandable language like english, if followed, accomplishes given task.

- Program is an implementation of an algorithm.

- An algorithm is like a blue print / design of a program on paper.

Blue-print => implementation => building

- Pseudocode is a special form of an algorithm for programmer user.

**Q. What is a pseudocode? => Programmer User**

- An algorithm is a finite set of instructions written in any human understandable language like english with some programming constraints, if followed, accomplishes given task, this kind/form of an algorithm is referred as a pseudocode.

- an algorithm to do sum of array elements:

- **traversal on array** => to visit each array element sequentially from first element max till last element.

**algorithm:**

**step-1: initially take sum as 0.**

**step-2: traverse an array and add each array element sequentially into the sum.**

**step-3: return final sum.**

**Pseudocode: => Programmer**

```
Algorithm ArraySum( arr, n){//arr is an array of size n
    sum = 0;
    for( index = 1 ; index <= n ; index++ ){
        sum += arr[ index ];
    }
    return sum;
}
```

**Program: => Machine**

```
int array_sum( int arr[ ], int size ){

    int sum = 0;
    int index;
    for( index = 0 ; index < size ; index++ ){
        sum += arr[ index ];
    }
    return sum;
}
```

**Example:**

**IT Industry:**

**Client ( Algorithm i.e. Requirement ) => Software Architect/Tech Manager**

**Software Architect ( Pseudocode ) => Software Developer**

**Software Developer ( Program ) => Machine.**

- an algorithm is a solution of a given problem.
- an algorithm = solution
- one problem may has many solutions

e.g.

**searching => to search/find an element (let say referred as key element), in a given collection/list/set of elements.**

1. linear search
2. binary search

**sorting => to arrange data elements in a collection/list of elements wither in an ascending order (or in a descending order ).**

1. selection sort
  2. bubble sort
  3. insertion sort
  4. merge sort
  5. quick sort
- etc.....

- if one problem has many solutions, we need to select an efficient solution out of them, and to decide which solution/algorithm is an efficient one, we need to do their analysis.

- **analysis of an algorithm** is a work of calculating/determining how much **time** i.e. computer time and **space** i.e. computer memory it needs to run to completion.

- there are 2 measures of analysis of an algorithm:

1. **time complexity** of an algorithm is the amount of **time** i.e. **computer time** it needs to run to completion.

2. **space complexity** of an algorithm is the **amount of space** i.e. **computer memory** it needs to run to completion.

1. **linear search / sequential search:**

**algorithm:**

step-1: accept key from user (key = element which is to be search)

step-2: start traversal of an array from first element and compare value of key element with each array element sequentially till match is not found or max till last element.

step-3: if the value of key matches with any of the array element then return true other wise return false.

**pseudocode:**

**Algorithm LinearSearch(A, key, n)**

```
{
    for( index = 1 ; index <= n ; index++ ) {
        if( key == A[ index ] )//if key matches with any array ele
            return true;//key is found
    }

    //if key do not matches with any of array element
    return false;//key is not found
}
```

**best case occurs : if key is found at first position =>  $O(1)$**

if size of an array = 10 => no. of comparisons = 1

if size of an array = 20 => no. of comparisons = 1

if size of an array = 50 => no. of comparisons = 1

if size of an array = 100 => no. of comparisons = 1

.

.

.

if size of an array = n => no. of comparisons = 1

**worst case occurs** : if either key is found at last position or key does not exist :  $O(n)$ .

if size of array = 10  $\Rightarrow$  no. of comparisons = 10

if size of array = 20  $\Rightarrow$  no. of comparisons = 20

if size of array = 100  $\Rightarrow$  no. of comparisons = 100

.

.

if size of array =  $n \Rightarrow$  no. of comparisons =  $n$

**best case time complexity** = if an algo takes min amount of time to run to completion.

**worst case time complexity** = if an algo takes max amount of time to run to completion.

**average case time complexity** = if an algo takes neither min nor max amount of time to run to completion.

**+ Asymptotic analysis:** it is a **mathematical** way to calculate time complexity and space complexity of an algorithm without implementing it in any programming language.

- in this kind of analysis, focus is on basic operation in that algorithm

e.g. searching  $\Rightarrow$  basic operation is comparison, and hence analysis can be done depends on no. of comparisons takes places in different cases.

sorting  $\Rightarrow$  basic operation is comparison, and hence analysis can be done depends on no. of comparisons takes places in different cases.

Addition of matrices  $\Rightarrow$  basic operation addition, and hence analysis can be done depends on number addition instructions.

- there are some notations and few assumptions that we need to follow:

there are 3 asymptotic notations:

1. **Big Omega (  $\Omega$  )** - this notation is used to represent **best case time complexity**.

- big omega is referred as asymptotic lower bound

- running of an algo should not be less than its **asymptotic lower bound**.

2. **Big Oh (  $O$  )** - this notation is used to represent **worst case time complexity**

- big oh is referred as asymptotic upper bound.

- running of an algo should not be greater than its asymptotic upper bound.

3. **Big Theta (  $\theta$  )** - this notation is used to represent an **average case time complexity**.

- big theta is referred as asymptotic tight bound.

### Assumption:

- if running time of an algo is having additive / subtractive / multiplicative / divisive constant it can be neglected.

e.g.

$O(n + 3) \Rightarrow O(n)$

$O(n - 5) \Rightarrow O(n)$

$O(n / 3) \Rightarrow O(n)$

$O(2*n) \Rightarrow O(n)$

- if an algo follows divide-and-conquer approach then we get time complexity in terms of log.

### # DS DAY-02:

#### 2. Binary Search

algorithm:

step-1: accept key from user

step-2:

- calculate mid pos by the formula  $\Rightarrow \text{mid} = (\text{left} + \text{right}) / 2$

- by means of calculating mid position, big size array gets divided logically into two subarray's  $\Rightarrow$  left subarray & right subarray

- left subarray is from left to mid-1, and right subarray is from mid+1 to right.

for left subarray  $\Rightarrow$  value of left remains as it is, value of right = mid-1

for right subarray  $\Rightarrow$  value of right remains as it is, value of left = mid+1

step-3: compare value of key with ele at mid pos, if key matches with ele at mid pos return true

step-4: if key do not matches then search key either into the left subarray or into the right subarray

step-5: repeat step-2, step-3 & step-4, till either key not found, or max till subaarray is valid, if subarray is invalid then return false indicates key not found.

if( left <= right )  $\Rightarrow$  subarray is valid

if( left > right )  $\Rightarrow$  subarray is invalid

- in a binary tree, any element is at either one of the following 3 positions:

1. root pos

2. leaf pos

3. non-leaf pos

root node/root pos  $\Rightarrow$  first pos

node which is not having further child node  $\Rightarrow$  leaf node

node which is having child node  $\Rightarrow$  non-leaf node

if key is found at root pos => best case =>  $O(1)$   
no. of comparisons for input size array = 1  
time complexity =  $\Omega(1)$ .

if key is found at non-leaf pos => average case  
 $O(\log n)$   
time complexity =  $\theta(\log n)$

if either key is found at leaf pos or key is not found => worst case  
 $O(\log n)$   
time complexity =  $O(\log n)$

#### + Sorting Algorithms:

**Sorting** => to arrange data elements in a collection/list of elements either in an ascending order or in a descending order.

- when we say sort array elements, by default we need to sort array elements in an ascending order.

#### 1. Selection Sort:

for size of an array is  $n$ ,

in iteration-1: no. of comparisons =  $n-1$

in iteration-2: no. of comparisons =  $n-2$

in iteration-3: no. of comparisons =  $n-3$

.

.

iterations ( $n-1$ ):

total no. of comparisons =  $(n-1) + (n-2) + (n-3) + \dots$

total no. of comparisons =  $n(n-1)/2 \Rightarrow (n^2 - n) / 2$

$T(n) = O((n^2 - n) / 2)$

$\Rightarrow O(n^2 - n)$

$\Rightarrow O(n^2)$

rule/assumption: if running time of an algo is having a polynomial, then in its time complexity only leading term will be considered.

e.g.

$O(n^3 + n + 4) \Rightarrow O(n^3)$

$O(n^2 + 5) \Rightarrow O(n^2)$

$O(n^3 + n^2 + n - 3) \Rightarrow O(n^3)$



SunBeam