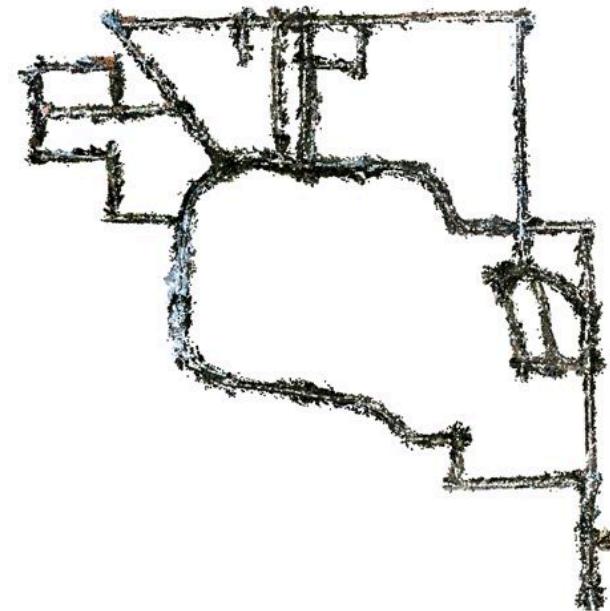


# Stereo Visual Odometry

Chris Beall  
CVPR 2014 Visual SLAM Tutorial

# OUTLINE

- Motivation
- Algorithm Overview
- Feature Extraction and matching
- Incremental Pose Recovery
- Practical/robustness considerations
- What else do you get?
- Results



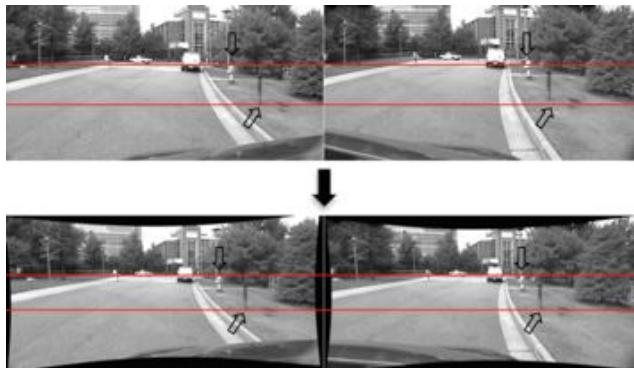
# Motivation

- Why stereo Visual Odometry?
  - Stereo avoids scale ambiguity inherent in monocular VO
  - No need for tricky initialization procedure of landmark depth



# Algorithm Overview

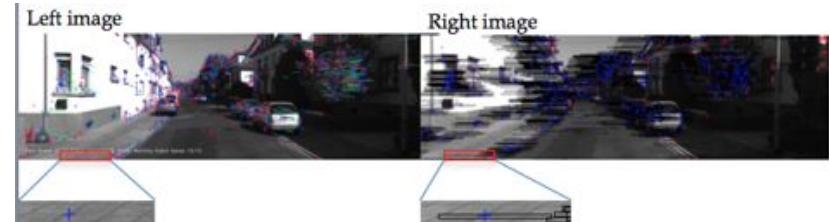
## 1. Rectification



## 2. Feature Extraction



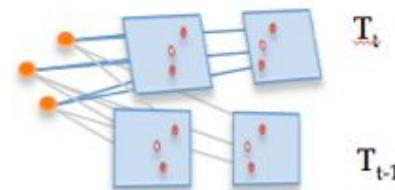
## 3. Stereo Feature Matching



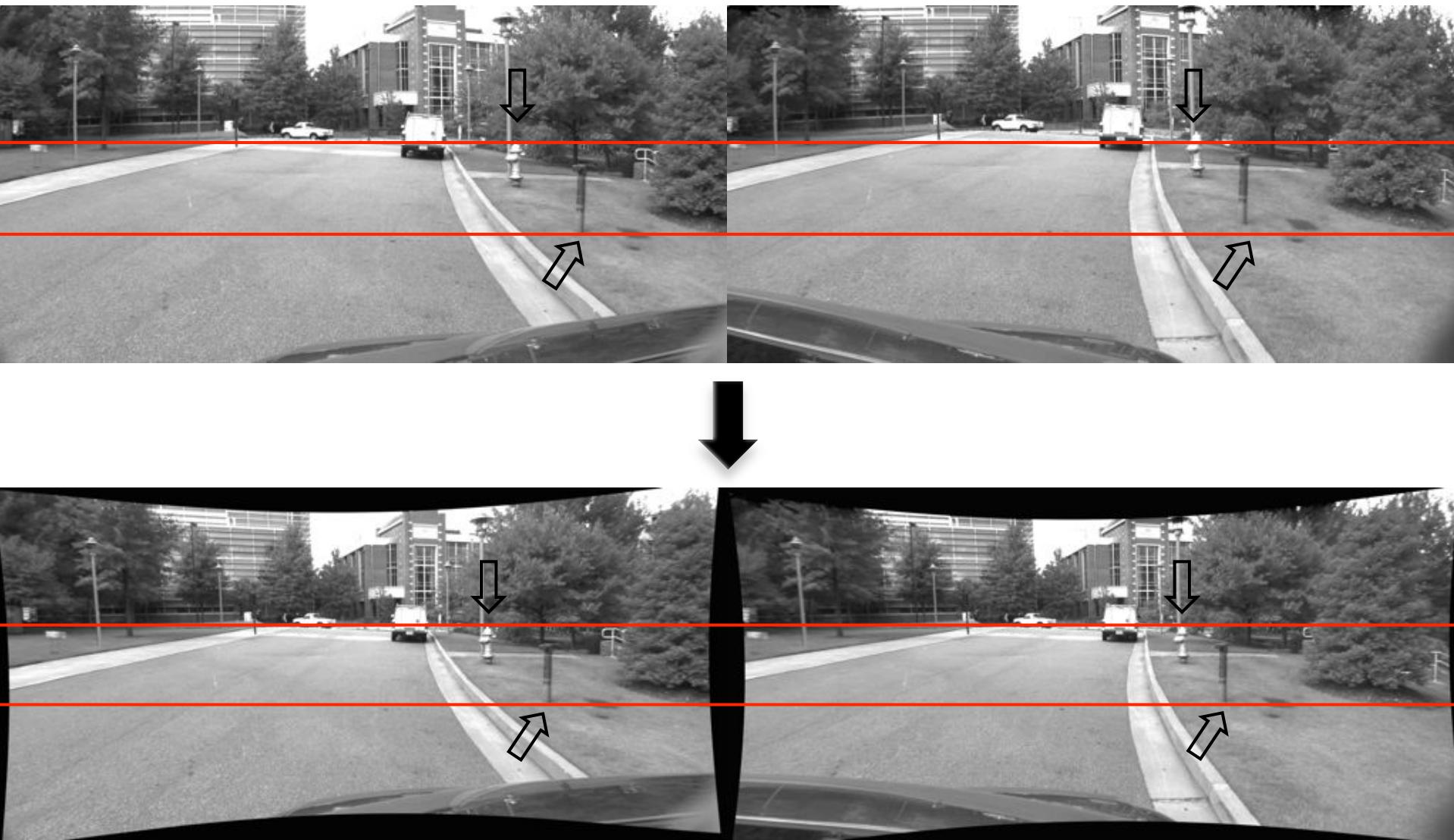
## 4. Temporal Feature Matching



## 5. Incremental Pose Recovery/RANSAC



# Undistortion and Rectification



# Feature Extraction

- Detect local features in each image
  - SIFT gives good results (can also use SURF, Harris, etc.)



Lowe ICCV 1999

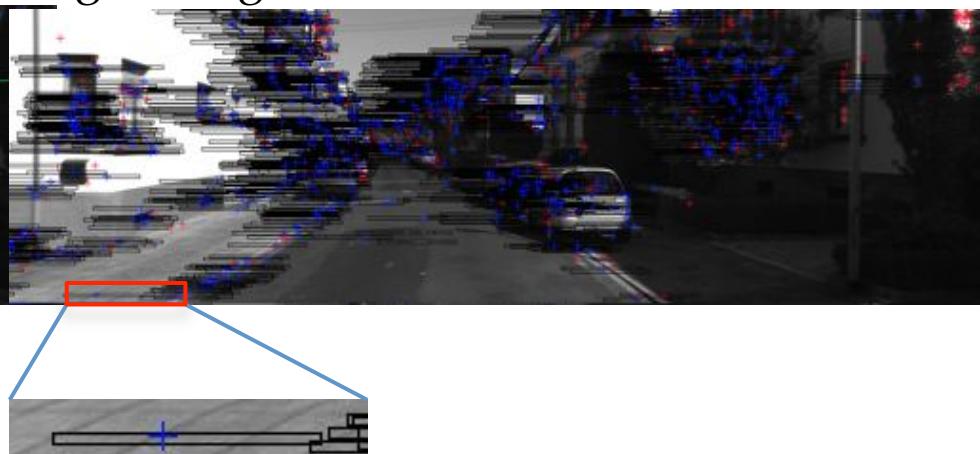
# Stereo Matching

- Match features between left/right images
- Since the images are rectified, we can restrict the search to a bounding box on the same scan-line

Left image



Right image



# Temporal Matching

- Temporally match features between frame  $t$  and  $t-1$

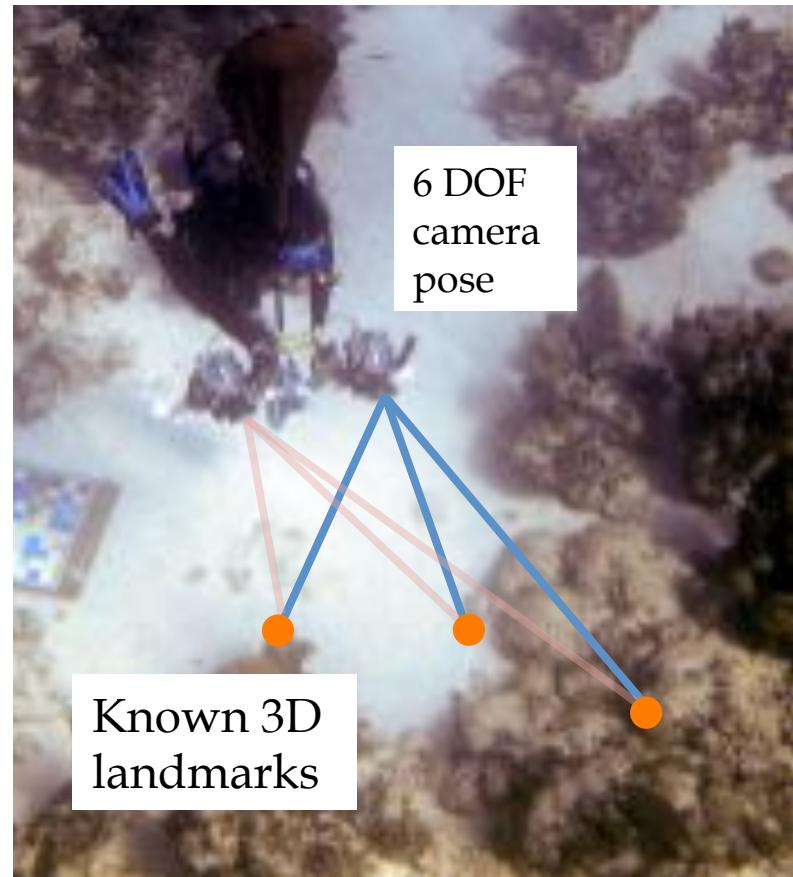


# Relative Pose Estimation/RANSAC

- Want to recover the incremental camera pose using the tracked features and triangulated landmarks
- There will be some erroneous stereo and temporal feature associations → Use RANSAC
  - Select N out of M data items at random (the minimal set here is 3)
  - Estimate parameter (incremental pose from t-1 to t)
  - Find the number K of data items that fit the model (called inliers) within a given tolerance
  - Repeat S times
  - Compute refined model using full inlier set

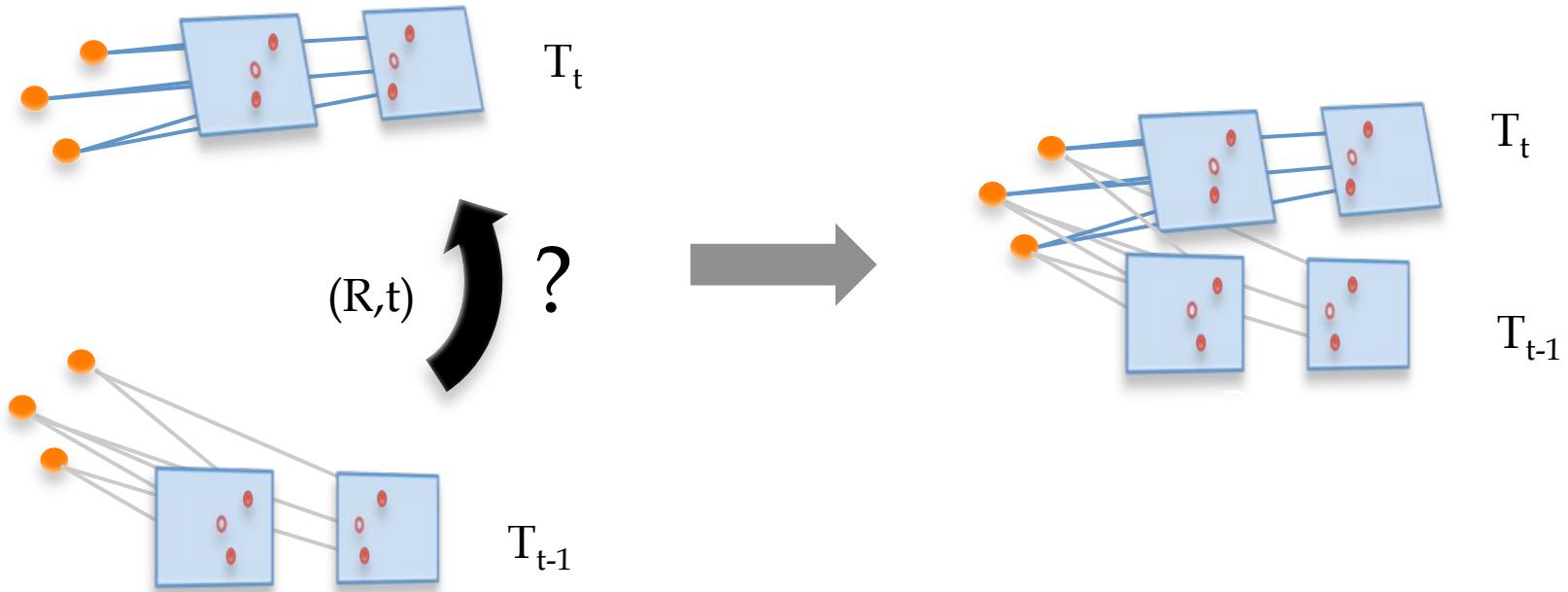
# Relative Pose Estimation

- Camera pose can be recovered given at least three known landmarks in a non-degenerate configuration
- In the case of stereo VO, landmarks can simply be triangulated
- Two ways to recover pose:
  - Absolute orientation
  - Reprojection error minimization



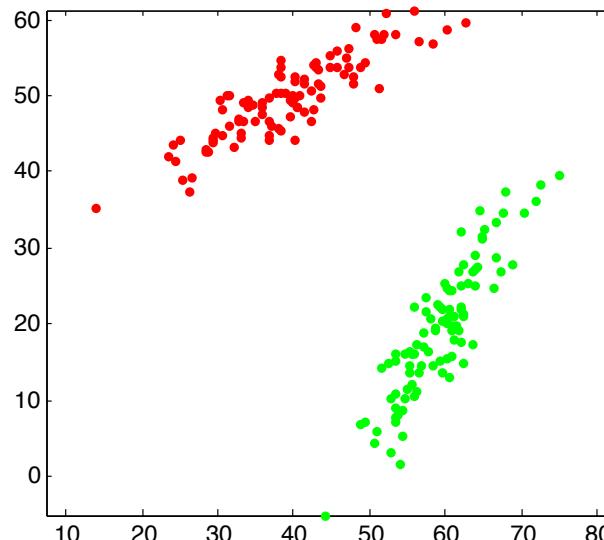
# Absolute Orientation

- Estimate relative camera motion by computing relative transformation between 3D landmarks which were triangulated from stereo-matched features



# Absolute Orientation

- First, in 2D:
  - Given two sets of corresponding points  $\{p_i^l\}$  and  $\{p_i^r\}$  related by a rigid 2D transformation  $T_r^l = (R_r^l, t_r^l)$ :
$$p^l = R_r^l p^r + t_r^l$$
  - First recover rotation (2 points), then translation (1 point)



B. K. P Horn JOSA 1987

# Absolute Orientation

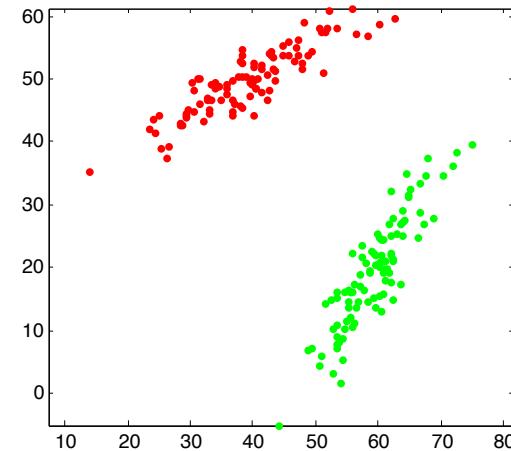
- Rotation:
  - Given two point correspondences  $(p_1^l, p_1^r)$  and  $(p_2^l, p_2^r)$ , the vector  $v$  between the two points will be rotated by the desired angle  $\theta$
  - Specifically, the vectors are related by

$$v^l = (p_2^l - p_1^l) = R_r^l (p_2^r - p_1^r) = R_r^l v^r$$

- Finally, recover the angle

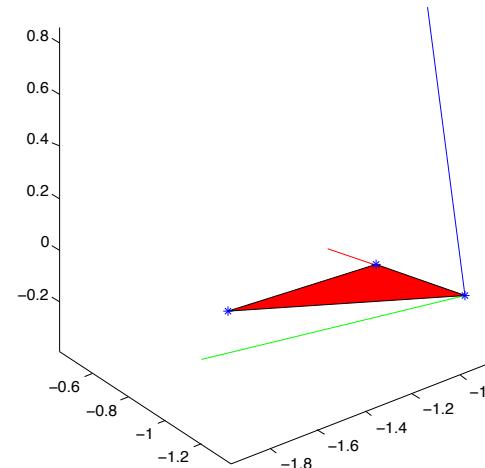
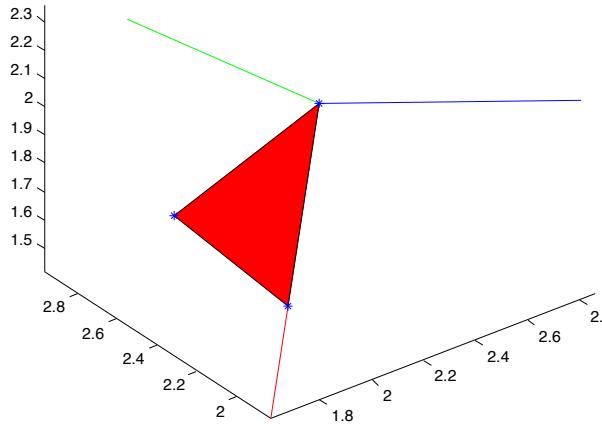
$$\theta = \arccos \frac{v^l \cdot v^r}{\|v^l\| \|v^r\|}$$

and translation  $t_r^l = p^l - R_r^l p^r$



# Absolute Orientation

- Now in 3D:
  - Create coordinate frames from three corresponding points
    - Take x-axis by connecting  $p_1^l$  to  $p_2^l$ :  $\hat{x}_l \propto (p_2^l - p_1^l)$
    - Construct y-axis in the plane formed by three points, perpendicular to x-axis:  $\hat{y}_l \propto (p_3^l - p_1^l) - [(p_3^l - p_1^l) \cdot \hat{x}_l] \hat{x}_l$
    - Complete frame with z-axis:  $\hat{z}_l \propto (\hat{x}_l \times \hat{y}_l)$



# Absolute Orientation

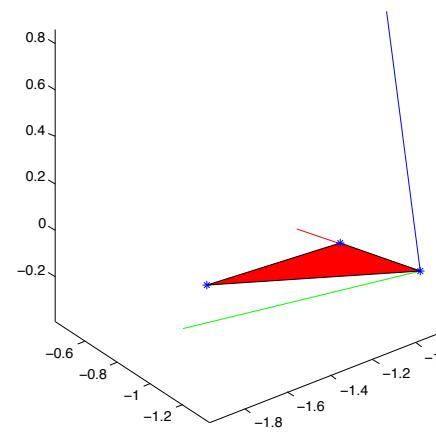
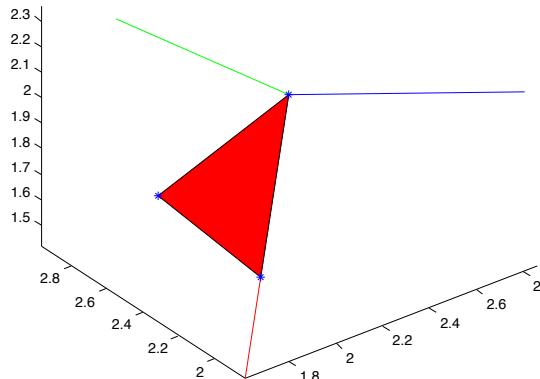
- Normalize the axes and we have the rotation of the frame with respect to the global reference frame,

$$R_l^g = [ \hat{x}_l \quad \hat{y}_l \quad \hat{z}_l ]$$

- Repeat for the right frame, and obtain the relative rotation,

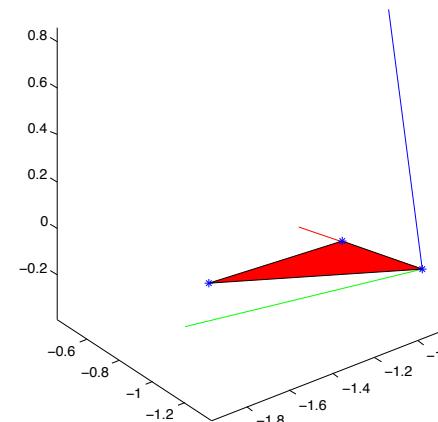
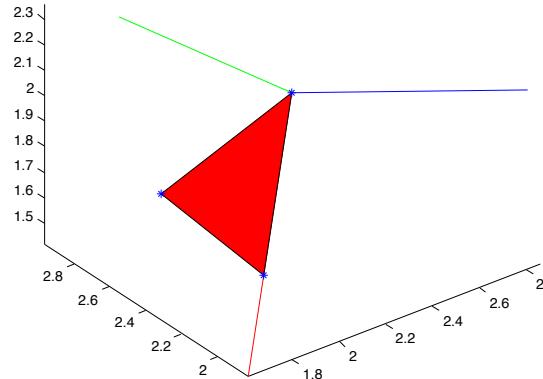
$$R_r^l = R_g^l R_r^g = (R_l^g)^T R_r^g$$

- As in the 2D case, the translation can then be recovered using a single point



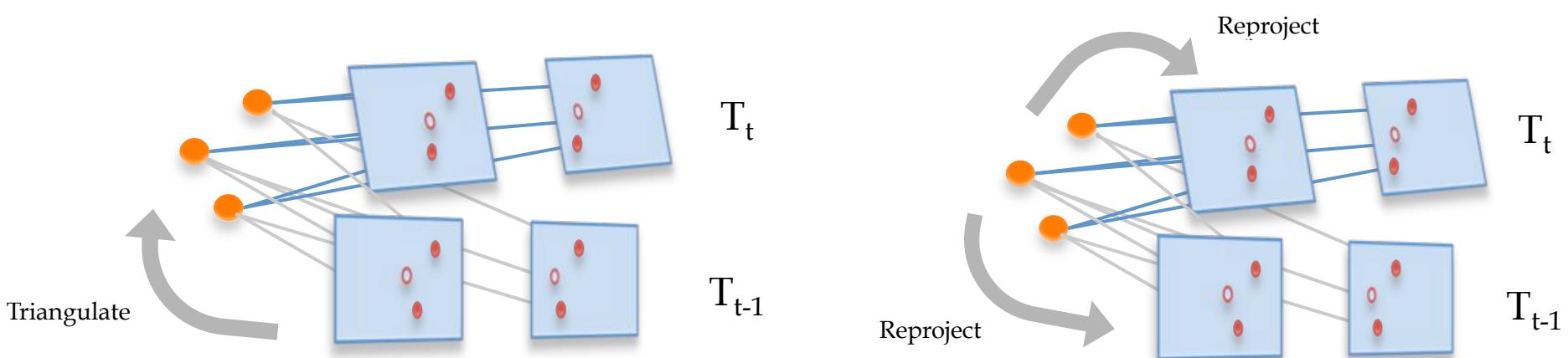
# Absolute Orientation

- The Absolute Orientation approach assumes a relatively noiseless case, and does not work well otherwise
- No simple way to average out noisy points by considering more data
  - Use SVD-based method instead
  - Use different approach based on projective geometry



# Reprojection Error Minimization

- A better approach is to estimate relative pose by minimizing reprojection error of 3D landmarks into images at time  $t$  and  $t-1$



# Practical/Robustness Considerations

- The presented algorithm works very well in feature-rich, static environments, but...
- A few tricks for better results in challenging conditions:
  - Feature binning to cope with bias due to uneven feature distributions
  - Keyframing to cope with dynamic scenes, as well as reducing drift of a stationary camera
- Real-time performance

# Feature Binning

- Incremental pose estimation yields poor results when features are concentrated in one area of the image
- Solution: Draw a grid and keep  $k$  strongest features in each cell



# Challenges: Dynamic Scenes

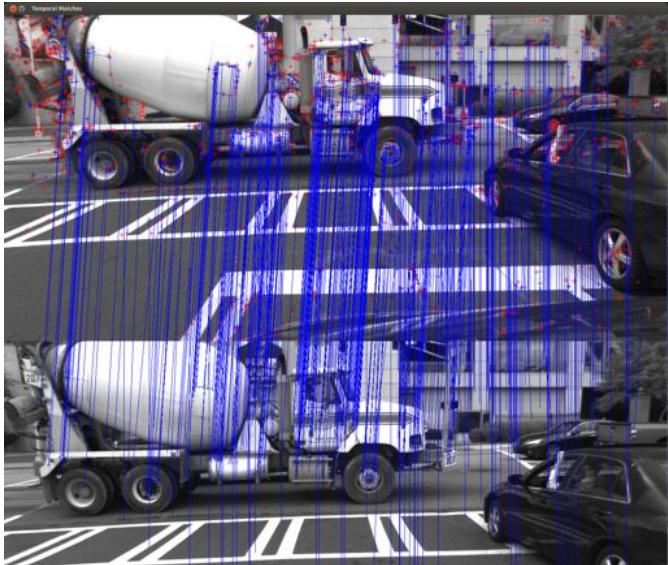
- Dynamic, crowded scenes present a real challenge
- Cannot depend on RANSAC to always recover the correct inlier set
- Example 1: Large van “steals” inlier set in passing



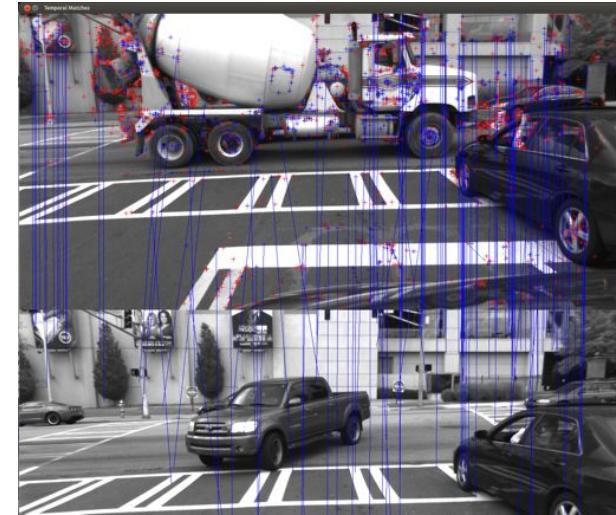
Inliers Outliers

# Challenges: Dynamic Scenes

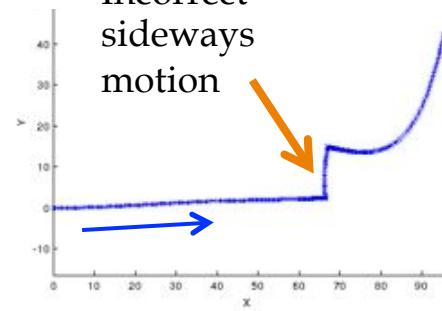
- Example 2: Cross-traffic while waiting to turn left at light



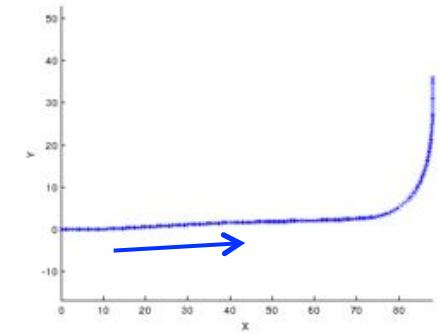
Only accept  
incremental pose if:  
• translation > 0.5m  
• Dominant direction  
is forward



Incorrect  
sideways  
motion



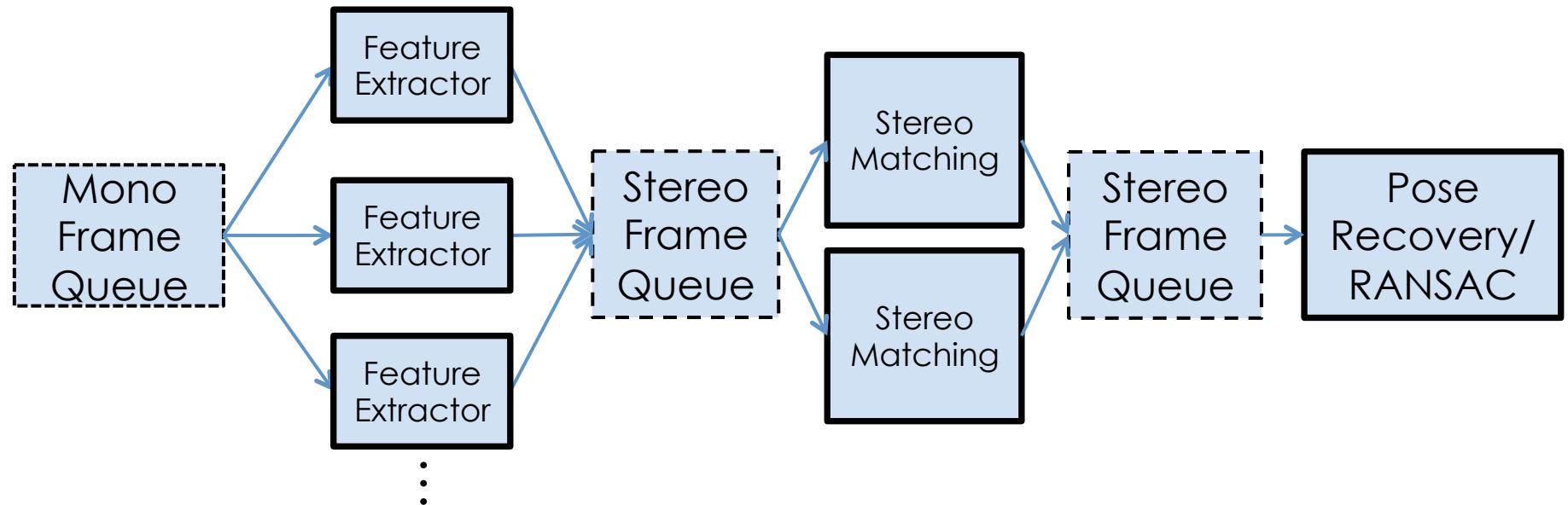
Without keyframing



With keyframing

# Real-time performance

- Parallelization of feature extraction and stereo matching steps allows real-time performance even in CPU-only implementation



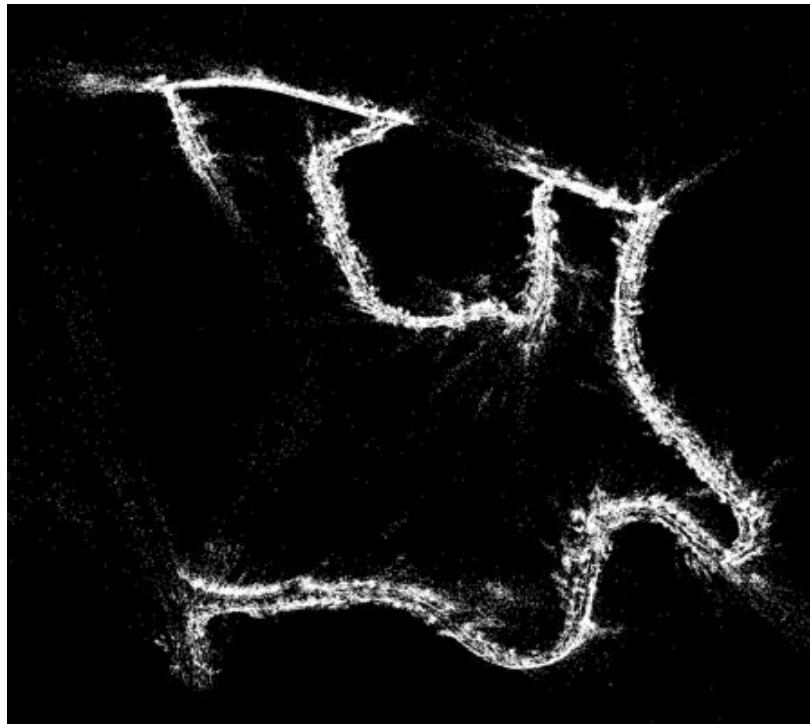
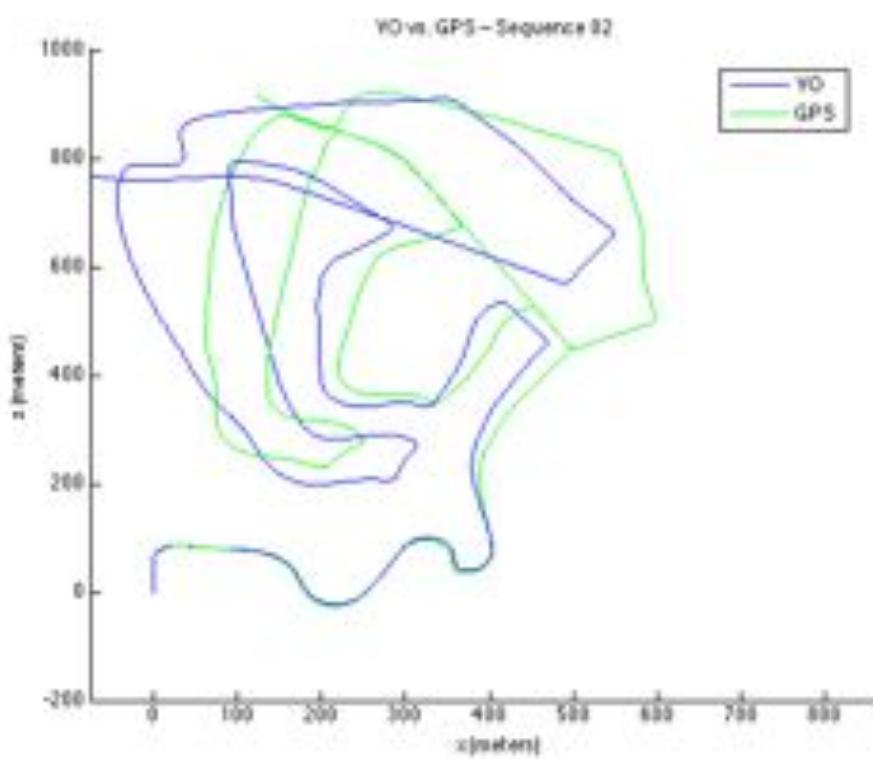
# What else do you get?

- Stereo Visual Odometry yields more than just a camera trajectory!
- Tracked landmarks form a sparse 3D point cloud of the environment
  - Can be used as the basis for localization



# What else do you get?

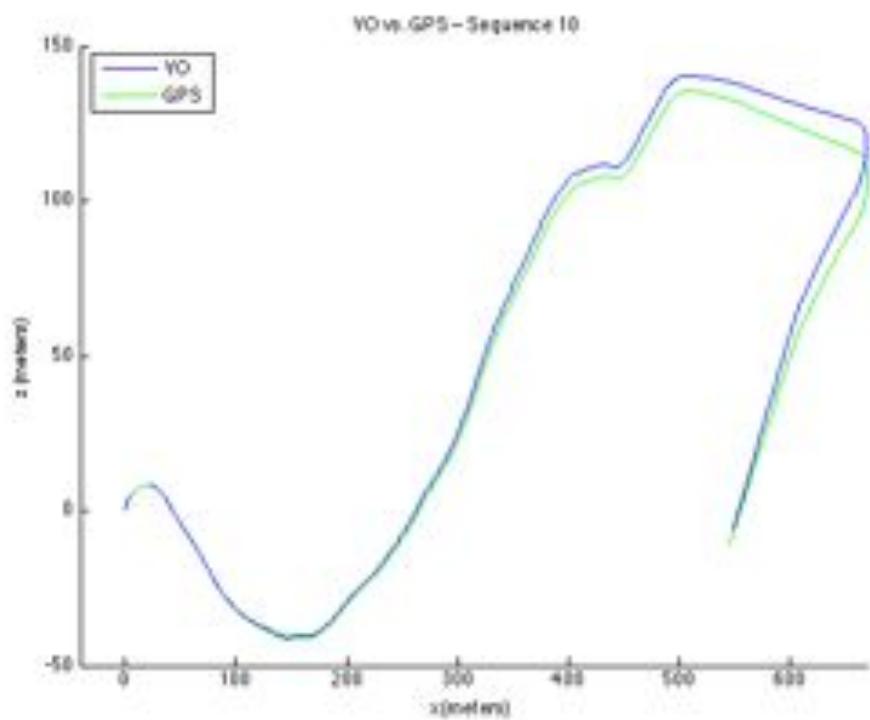
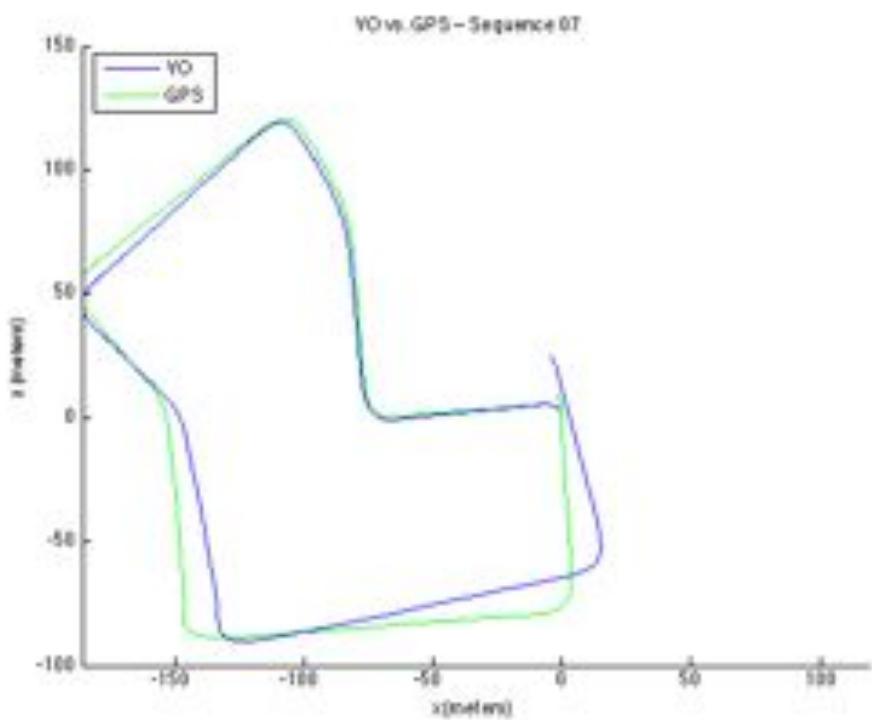
- 3D Point cloud on KITTI Benchmark, Sequence 2



<http://www.cvlibs.net/datasets/kitti/>

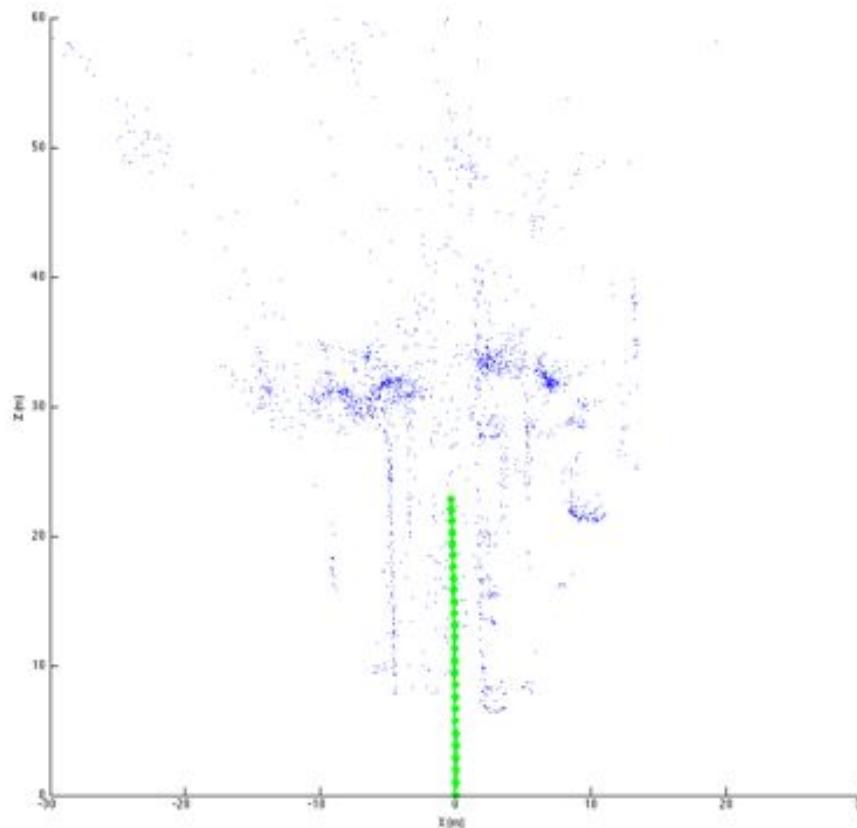
# Results on KITTI Benchmark

- Representative results on KITTI VO Benchmark
  - Average translational/rotational errors are very small
  - Accumulate over time, resulting in drift



# GTSAM VO Example with Point Cloud

- StereoVOExample\_large.m in GTSAM
  - Takes VO output and improves result through bundle adjustment (more on that later!)



[tinyurl.com/gtsam](http://tinyurl.com/gtsam)