Assignment 2

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Download all python codes from

https://github.com/TGURUBALAJI/INTERNSHIP -IITH/Assignment2/code

and latex-tikz codes from

https://github.com/TGURUBALAJI/INTERNSHIP -IITH/Assignment2/gbalaji.tex

1 Question No. 2.106 - LINEAR FORMS

Find the values of k for which the line

$$(k-3-(4-k^2))\mathbf{x} + k^2 - 7k + 6 = 0 (1.0.1)$$

is

- a) Parallel to the x-axis
- b) Parallel to the y-axis
- c) Passing through the origin

2 Solution

Given equation of the line,

$$(k-3-(4-k^2))\mathbf{x} + k^2 - 7k + 6 = 0 (2.0.1)$$

2.1 Parallel to x-axis

Equation of x-axis is $\begin{pmatrix} 1 & 0 \end{pmatrix} \mathbf{x} = 0$

$$(1 0)$$
 $\begin{pmatrix} k-3\\ -(4-k^2) \end{pmatrix}$ (2.1.1)

$$k - 3 = 0 \tag{2.1.2}$$

$$k = 3 \tag{2.1.3}$$

Substituting k = 3 in (2.0.1) Equation of line is,

$$\begin{pmatrix} 0 & 5 \end{pmatrix} \mathbf{x} = 6 \tag{2.1.4}$$

2.2 Parallel to y-axis

Equation of y-axis is $(0 \ 1)\mathbf{x} = 0$

$$4 - k^2 = 0 (2.2.2)$$

$$k = \pm 2 \tag{2.2.3}$$

Substituting k = 2 in (2.0.1) Equation of line is,

$$\begin{pmatrix} -1 & 0 \end{pmatrix} \mathbf{x} = 12 \tag{2.2.4}$$

Substituting k = -2 in (2.0.1) Equation of line is,

$$\begin{pmatrix} -5 & 0 \end{pmatrix} \mathbf{x} = -16 \tag{2.2.5}$$

2.3 pasing through origin

Equation of line when passing through origin is

$$\mathbf{n}^{\mathsf{T}}\mathbf{x} = 0 \tag{2.3.1}$$

Hence

$$-k^2 + 7k - 6 = 0 (2.3.2)$$

$$(k-1)(k-6) = 0 (2.3.3)$$

$$k = 1, k = 6 (2.3.4)$$

Substituting k = 1 in (2.0.1)

The equation of line is,

$$\begin{pmatrix} -2 & -3 \end{pmatrix} \mathbf{x} = 0 \tag{2.3.5}$$

Substituting k = 6 in (2.0.1)

The equation of line is,

$$\begin{pmatrix} 3 & 32 \end{pmatrix} \mathbf{x} = 0 \tag{2.3.6}$$

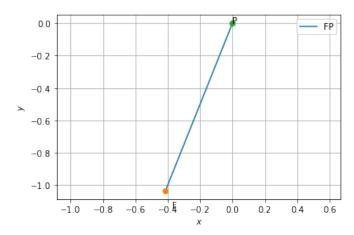


Fig. 0: Plot of line passing through origin