

Code No: 53007

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD**B.Tech II Year I Semester Examinations, May/June - 2019****MATHEMATICS-III****(Common to EEE, ECE, EIE)****Time: 3 hours****Max. Marks: 75**

Answer any five questions
All questions carry equal marks

- 1.a) Prove that $\beta\left(m, \frac{1}{2}\right) = 2^{2m-1}\beta(m, m)$
 b) Show that $J_n(x) = \frac{1}{\pi} \int_0^\pi \cos(n\theta - x \sin\theta) d\theta$. [7+8]
- 2.a) Show that $(1 - 2xt + t^2)^{-\frac{1}{2}} = P_0(x) + P_1(x)t + P_2(x)t^2 + \dots$
 b) Prove that $P'_n - P'_{n-2} = (2n-1)P_{n-1}$. [8+7]
- 3.a) If $\tan \log(x + iy) = a + ib$, where $a^2 + b^2 \neq 1$. Show that $\tan \log(x^2 + y^2) = \frac{2a}{i - a^2 - b^2}$.
 b) If $u = e^x[(x^2 - y^2)\cos y - 2xysiny]$ is a real part of an analytic function. Find the analytic function. [7+8]
- 4.a) Evaluate $\int_{(0,0)}^{(1,1)} [3x^2 + 5y + i(x^2 - y^2)] dz$ along with $y^2 = x$.
 b) Evaluate $\int_c \frac{e^{2z}}{(z+1)^4} dz$ around $c: |z - 1| = 3$. [8+7]
- 5.a) Find the Laurent series of $\frac{z^2-1}{(z+2)(z+3)}$ for $|z| > 3$.
 b) Find the order of all zeros for the function $e^{\tan z}$. [8+7]
6. Show that using residue theorem, $\int_0^{2\pi} \frac{1}{a + b \sin \theta} d\theta = \frac{2\pi}{\sqrt{a^2 - b^2}}, a > b > 0$. [15]
- 7.a) Under the transformation $w = \frac{1}{z}$. Find the image of the circle $|z - 2i| = 2$.
 b) Find the bilinear transformation which maps the points $(-1, 0, 1)$ into the points $(0, i, 3i)$. [7+8]
- 8.a) Define the following:
 i) A circuit
 ii) Connected graph
 iii) Hamiltonian path.
 b) Prove that number of edges in a bipartite graph with n vertices is at most $(n^2/4)$. [8+7]