Inapplicable algorithm description

The following passes are assuming a traversal (or equivalent procedure) to visit each node of a given tree.

1 First downpass

- 1. For any pair of nodes/tips, **if** there is any state in common between both descendants, go to 2; **else** go to 3.
- 2. If the state in common is only the inapplicable state, and both descendants have an applicable state, set the node's state to be the union of the descendants' states. Else, set the node's state to be the state in common between both descendants then go to 4.
- 3. If both descendants have an applicable state, set the node's state to be the union of both descendants states without the inapplicable state. Else, set the node's state to be the union of its descendants states. Then go to 4.
- 4. Once all nodes have been visited, end the first downpass.

2 First uppass

- 1. For any node; **if** the node has the inapplicable state, *go* to 2; **else**, leave the node's state unchanged and *go* to 6.
- 2. If the node also has an applicable state, go to 3; else, go to 4.
- 3. If the node's ancestor has the inapplicable state, set the node's state to be the inapplicable state only and go to 6; else remove the inapplicable state from the current node states. Then go to 6.
- 4. If the node's ancestor has the inapplicable state, set the node's state to be the inapplicable state only and go to 6; else go to 5.
- 5. If any of the descendants have an applicable state, then set the node's state to be the union of the applicable states of its descendants; else set the node's state to be the inapplicable state only. Then go to 6.
- 6. **If** one of the node's descendants is an unvisited tip, *go* to 7; **else** go to 1 until all the nodes have been visited.

- 7. If the unvisited tip has both inapplicable and applicable states, then go to 8 else go to 6
- 8. If the current node is inapplicable, solve the tip as inapplicable only; else remove the inapplicable state from the tip then go to 6.

3 Initialise tracker

- 1. For any tip; **if** the tip only contains an inapplicable state, *set* its tracker to "off" **then** move to the next tip and *go* to 1; **else** *go* to 2.
- 2. **If** the tip does not contain the inapplicable state, *set* its tracker to "on" **then** move to the next tip and *go* to 1. **Else** *go* to 3.
- 3. If the tip's ancestor contains an inapplicable state, set the tip's tracker to "off" else, set the tip's tracker to "on". Then go to the next tip and go to 1.

4 Second downpass

- 1. For any pair of nodes/tips; **if** the trackers of either descendants is "on", set this node's tracker to "on". **Else** set it to "off". **Then**, go to 2
- 2. **If** the node had an applicable state in the previous pass (first up), go to 3; **else** leave the node state unchanged and go to 8.
- 3. If there is any state in common between both descendants, go to 4; else, go to 5.
- 4. If the states in common are applicable, set the node's state to be these states in common without the eventual inapplicable token; else set the node's state to be the inapplicable state. Then qo to 8.
- 5. Set the node's state to be the union of the applicable states of both descendants (if present) and go to 6.
- 6. If both descendants have an applicable state, *increment* the tree length (change increment) and go to 8; else go to 7.
- 7. **If** both of the node's descendants' trackers are "on", *increment* the tree length (applicable region increment) **then** go to 8; **else** just go to 8.
- 8. Once all nodes have been visited, end the second downpass.

5 Second uppass

- 1. For any node; **if** the node has any applicable state, *go* to 2; **else**, *go* to 9.
- 2. If the node's ancestor has any applicable state, go to 3; else, go to 10.
- 3. If the node states are the same as its ancestor, go to 10; else, go to 4.
- 4. If there is any state in common between the node's descendants, go to 5; else go to 6.
- 5. Add to the current node any state in common between its ancestor and its descendants. Then go to 10.
- 6. If the union between the node's descendants contains the inapplicable state, go to 7; else go to 8.
- 7. If there is any state in common between either of the node's descendants and its ancestor, set the node's states to be its ancestor's; else add to the current node states the applicable states also found in its descendants and ancestor. Then go to 10.
- 8. Add to the node's states the states of its ancestor. Then go to 10.
- 9. If both of the node's descendants' trackers are "on", *increment* the tree length (applicable region increment) then go to 8; else just go to 10.
- 10. Once all nodes have been visited, end the second uppass.

The tree length is then equal to the number of state changes and the number of additional applicable regions.