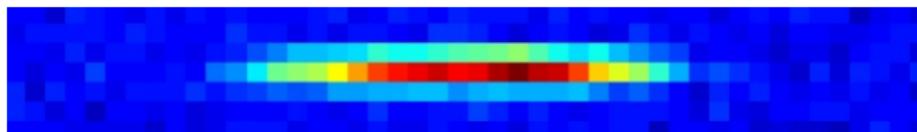




ing correlations in a 1D Bose gas on an atom chip *Mesures de corrélations dans un gaz de Bose 1D*

Thibaut Jacqmin

Laboratoire Charles Fabry
Groupe d'optique atomique



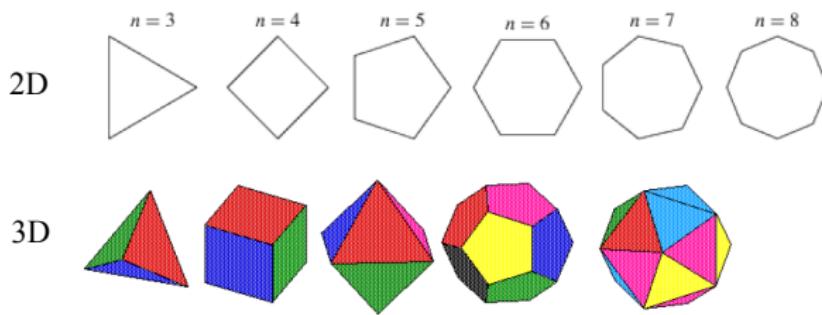
November, 22nd 2012
PhD defense

The influence of dimensionality

tel-00779447, version 1 - 22 Jan 2013



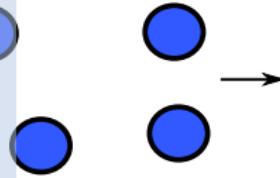
Plato 4th century BC



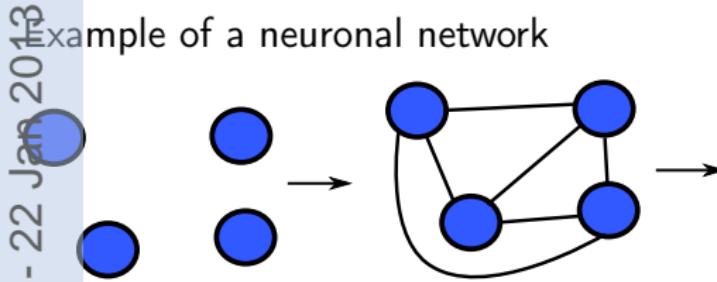
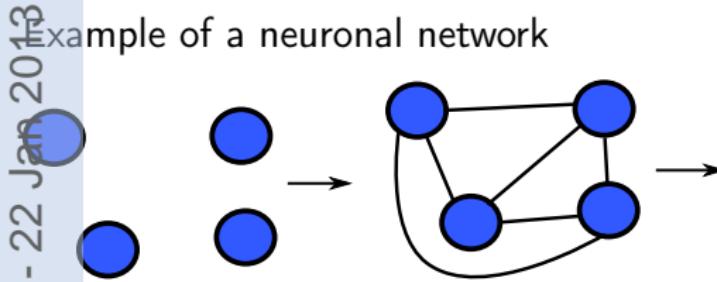
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Example of a neuronal network



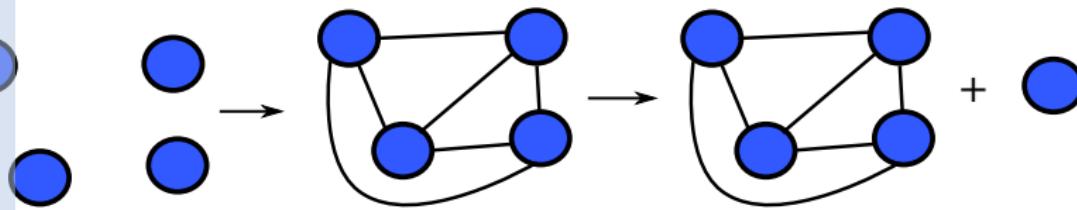
The influence of dimensionality



The influence of dimensionality

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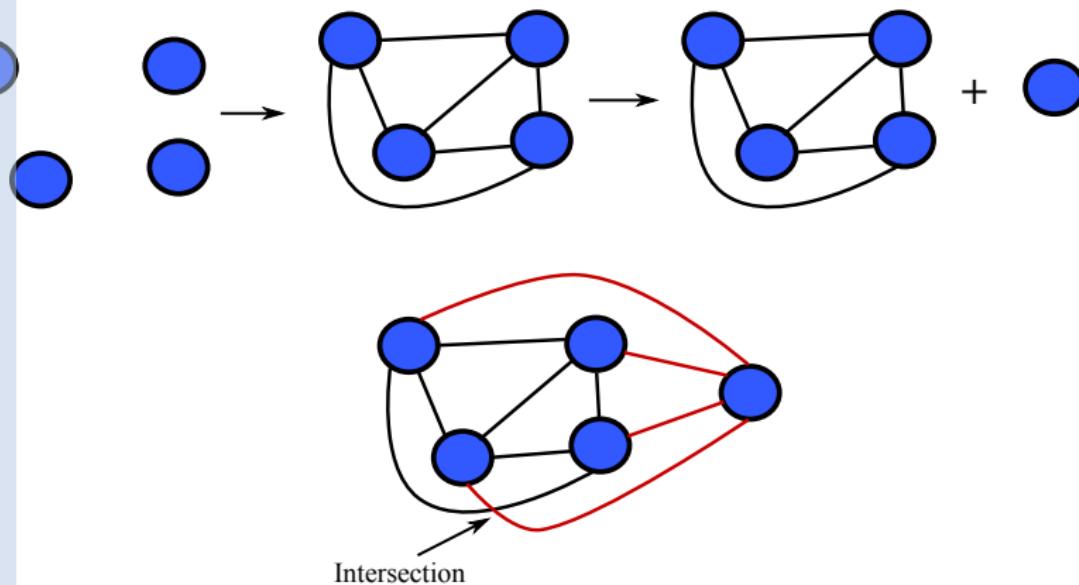
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The influence of dimensionality

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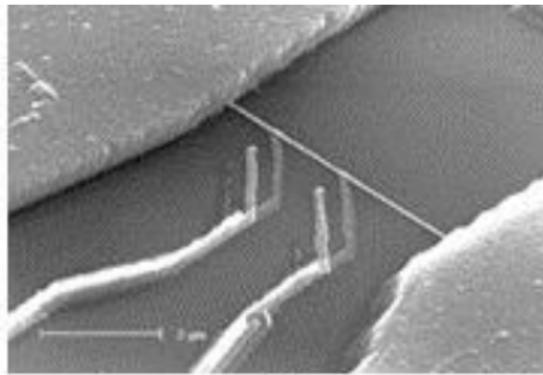
Example of a neuronal network



Impossibility to interconnect more than 4 neurones in 2D.

Why studying systems in dimensions lower than 3 ?

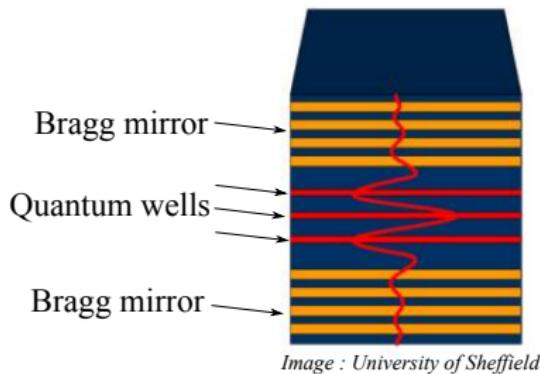
- Effect of interactions enhanced
- A whole bunch of new effects appear
- In quantum physics, thanks to confinement-induced quantization : very good quasi-low dimensional systems



Transport in a 50 nm nanowire (CEA)

Why studying systems in dimensions lower than 3 ?

- Effect of interactions enhanced
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- In quantum physics, thanks to confinement-induced quantization : very good quasi-low dimensional systems



2D electron gas in 1D quantum wells
Density of states modified, more gain
Example : laser diodes

Image : University of Sheffield

Why studying 1D systems ?

Very interesting from the theoretical point of view because :

- Most “simple” strongly correlated many-body system
- There exists powerful theoretical methods
- There are exact results



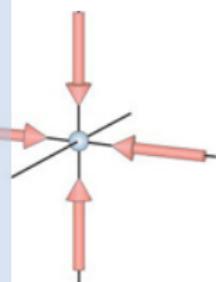
Newton's cradle

Low dimensional gases of ultra-cold atoms

tel-00779447, version 1 - 22 Jan 2013

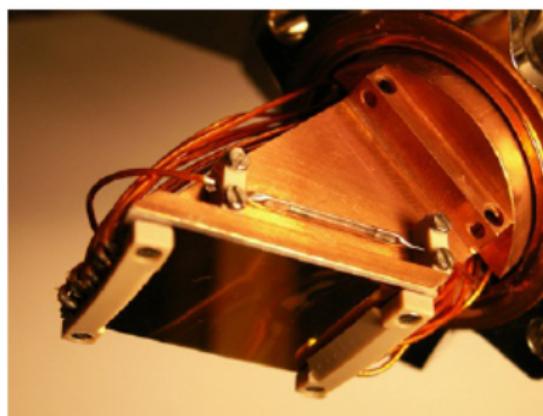
Cold atoms are suitable systems to study this Physics because

- possibility to get a 2D and 1D geometries
- isolated systems
- fine control of all parameters
- many observables



2D optical lattice

I. Bloch *Nature Phys.* 1, 23 - 30 (2005)



Atom chips

general cold atoms can be used to simulate a lot of models :

- Bose-Hubbard
- Hawking radiation
- Anderson localization
- ...

this work → Lieb-Liniger model of 1D bosons with contact repulsive interactions.



Elliott H. Lieb

Producing a 1D gas of bosons on an atom chip

Introduction to the physics of the 1D Bose gas

Density fluctuations in the quasi-condensate regime

Density fluctuations in the strongly interacting regime

Momentum distribution of 1D Bose gases

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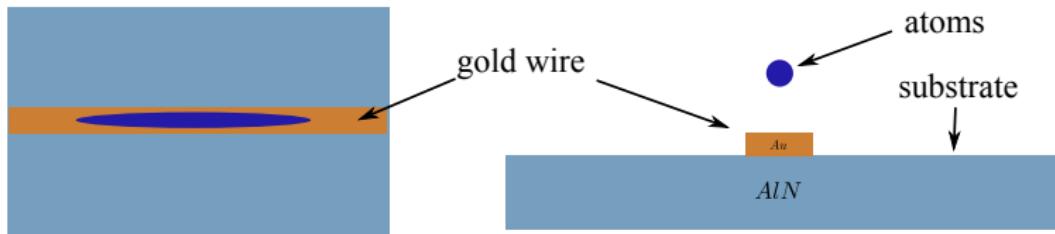
1D criterion

-
- The diagram shows a red parabolic curve representing a transverse harmonic potential well. Inside the well, there are three horizontal black bars representing energy levels. The top level is at a height labeled $h\nu_{\perp}$. The middle level is at a height labeled $h\nu_{\perp}$ below the top level. The bottom level is at a height labeled $h\nu_{\perp}$ below the middle level. A small black circle is positioned at the bottom of the well, near the bottom level.
- 1D criterion
 - $k_B T \ll h\nu_{\perp}$
 - $|\mu| \ll h\nu_{\perp}$
 - Typically, for $T \simeq 40$ nK it requires $\nu_{\perp} \gg 800$ Hz

Transverse trapping with microwires

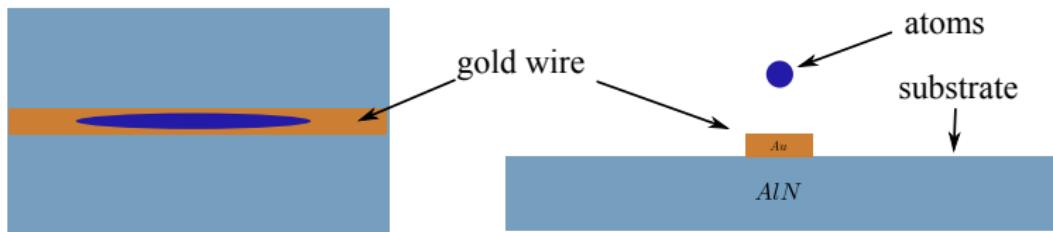
tel-00779447, version 1 - 22 Jan 2013

- The chip



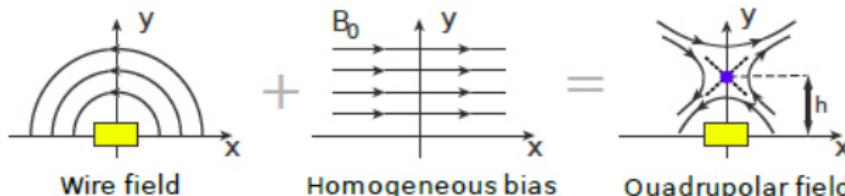
Transverse trapping with microwires

- The chip



- Trapping in two directions with a wire and a homogeneous magnetic field

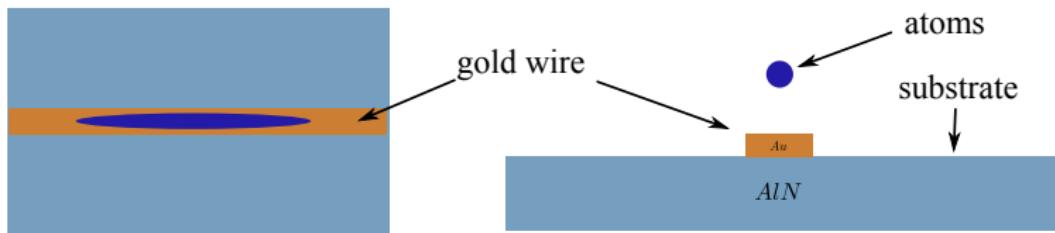
Magnetic potential $V = -\mu_B |\vec{B}|$



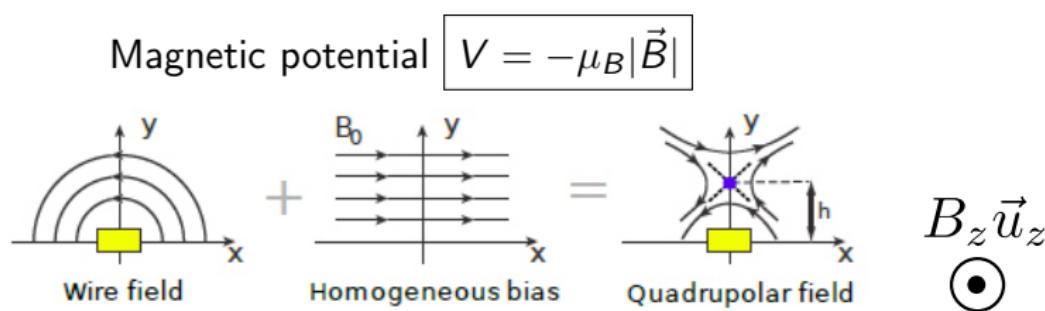
The transverse trapping frequency $\omega_{\perp} \propto 1/h^2$.

Transverse trapping with microwires

- The chip



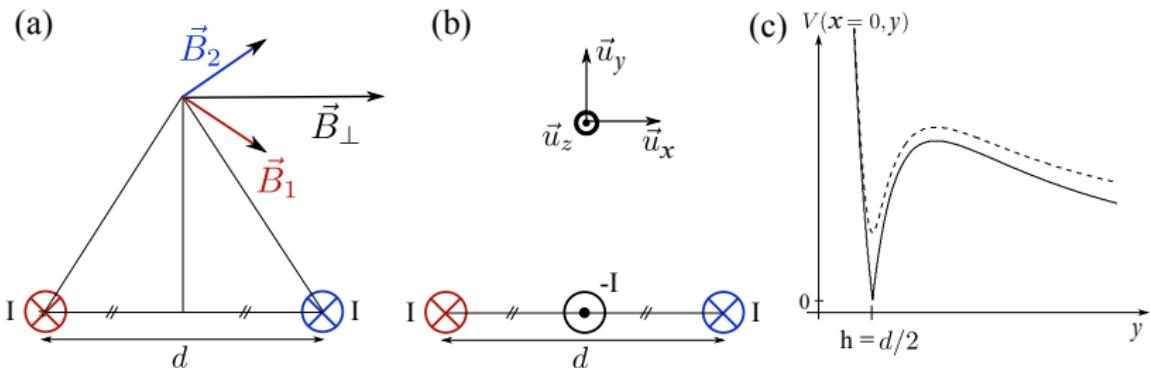
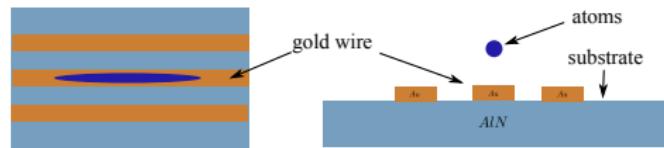
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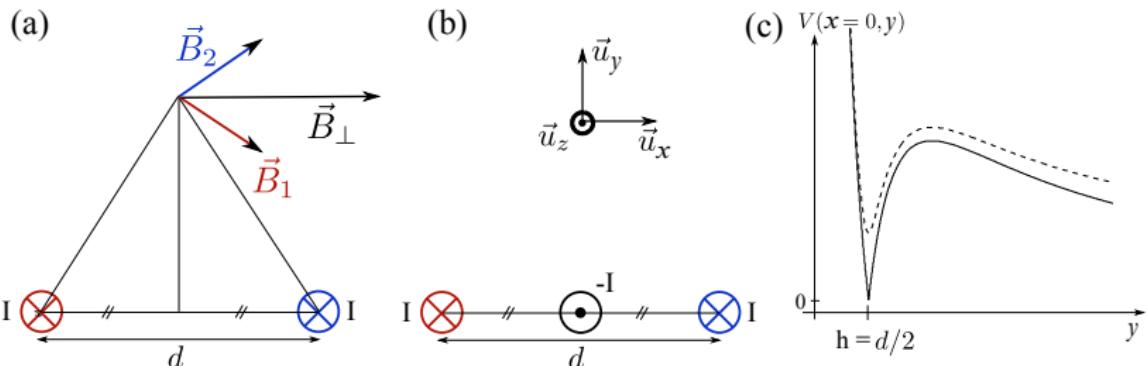
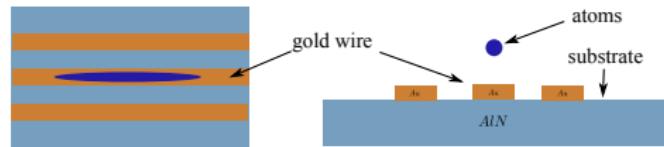
Transverse trapping with microwires

- Trapping in two directions with three parallel wires



Transverse trapping with microwires

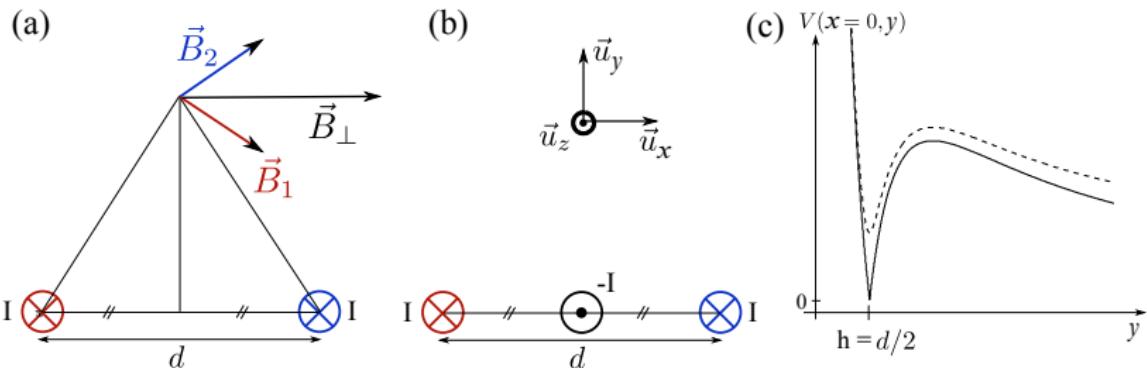
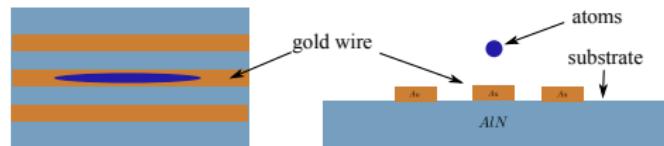
- Trapping in two directions with three parallel wires



- If h is too small : longitudinal roughness of the potential

Transverse trapping with microwires

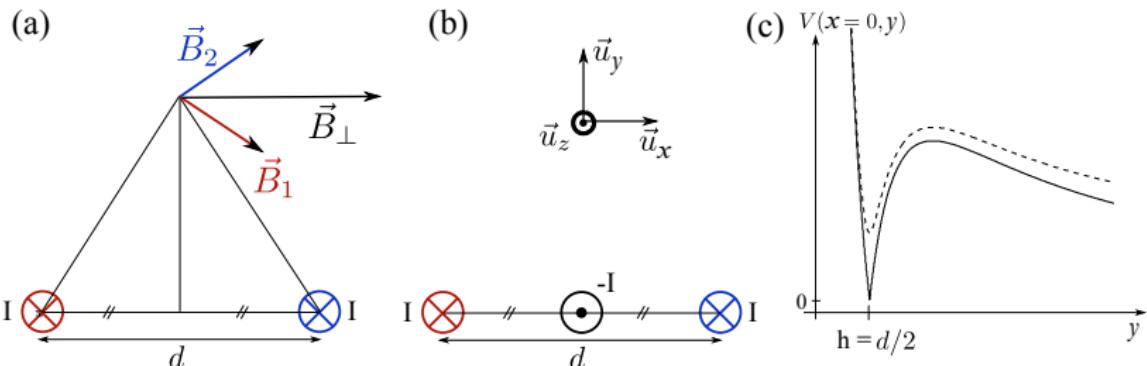
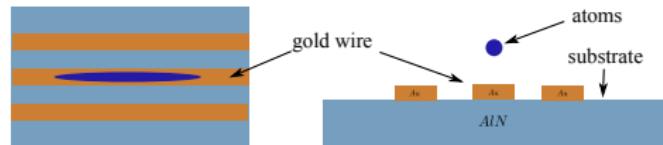
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- Solution : current modulation

Transverse trapping with microwires

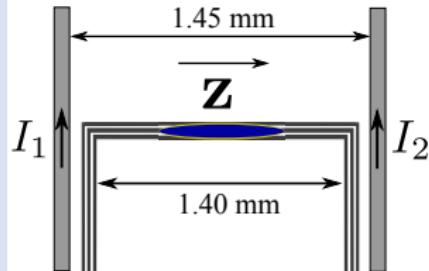
- Trapping in two directions with three parallel wires



- If h is too small : longitudinal roughness of the potential
- Solution : current modulation
- for $h = 15 \mu\text{m}$ and $I \leq 1 \text{ A}$, $\omega_\perp/2\pi = [0.1, 80] \text{ kHz}$

Longitudinal trapping

- Harmonic longitudinal trapping



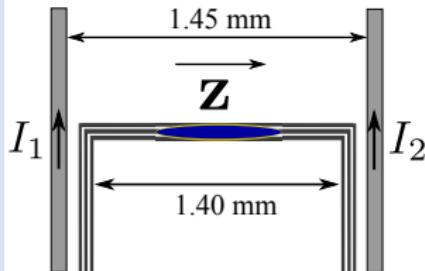
Typical trapping frequencies :

$$\omega_{\parallel}/2\pi = [3, 40] \text{ Hz}$$

$$\omega_{\perp}/2\pi = [0.1, 80] \text{ kHz}$$

Longitudinal trapping

- Harmonic longitudinal trapping

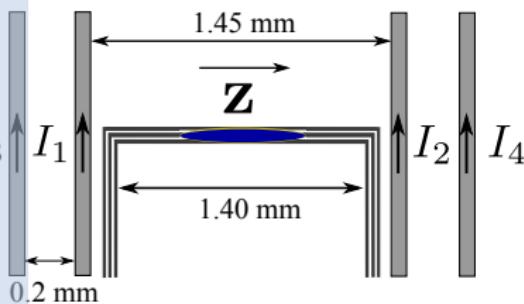


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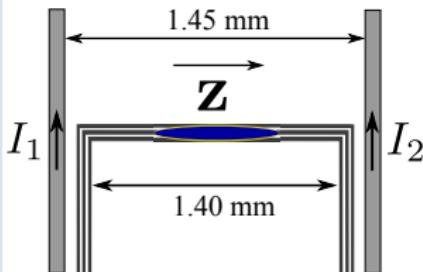
- Other longitudinal geometries



- Quartic trap
- Double well trap
- Fine tuning of anharmonicity

Longitudinal trapping

- Harmonic longitudinal trapping

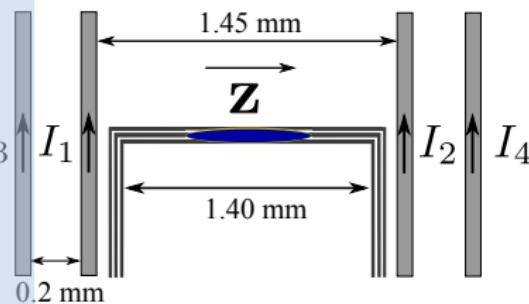


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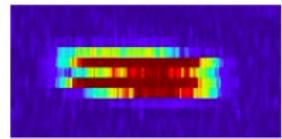
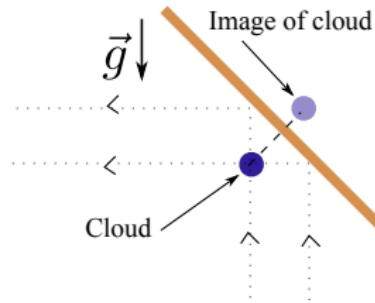
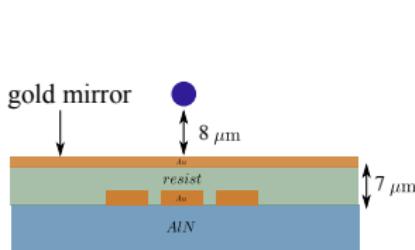


- Quartic trap
- Double well trap
- Fine tuning of anharmonicity

- Longitudinal and transverse traps totally decoupled

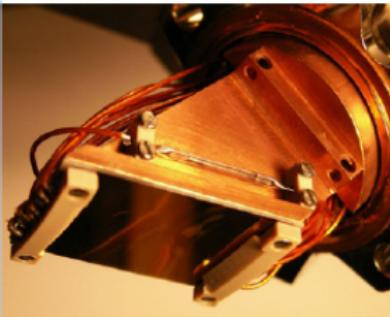
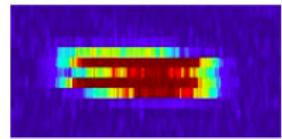
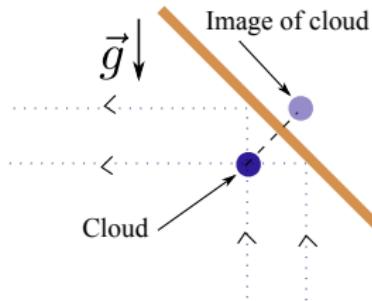
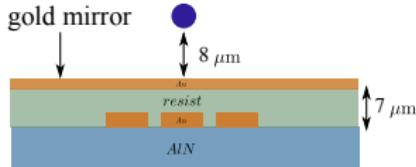
How do we observe the cloud?

- Mirror on chip



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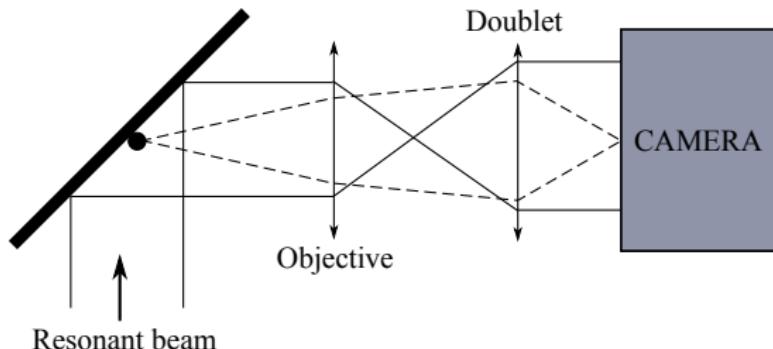
Chip on copper mount



Chip inside vacuum

How do we observe the cloud ?

- Absorption imaging : a resonant laser illuminates the cloud, which is imaged on a CCD camera



- The Beer-Lambert law gives the atomic density ρ

$$\rho \propto \ln \frac{I_2}{I_1}$$

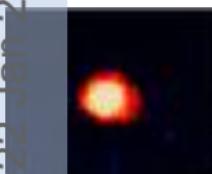
I_2 : intensity in absence of atoms

I_1 : intensity in presence of atoms

- Beer-Lambert \rightarrow not always valid \rightarrow more involved methods

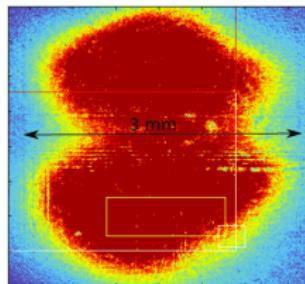
Typical experimental sequence

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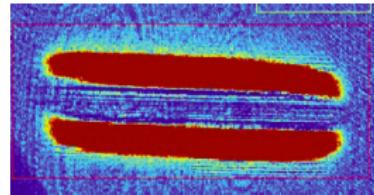
Laser cooling

MOT 1×10^8 at.
 $\simeq 200 \mu K$



Optical molasses
 5×10^7 at. $T \simeq 10 \mu K$

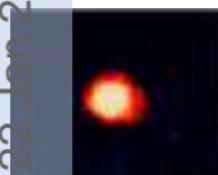
Optical pumping
in the trapped
Zeeman sublevel



Magnetic trap
 5×10^6 at.

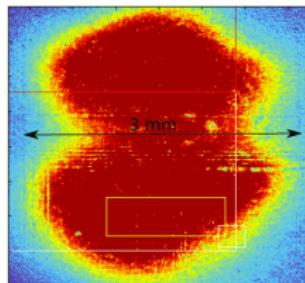
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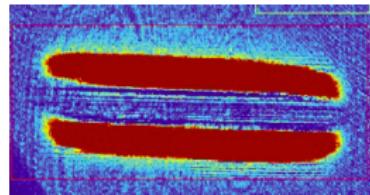
Laser cooling

MOT 1×10^8 at.
 $\approx 200 \mu K$

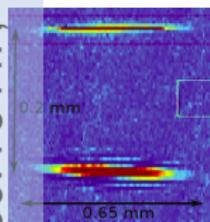


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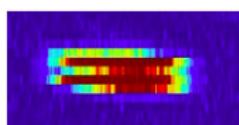


Magnetic trap
 5×10^6 at.



Evaporation for 2.5 s
 3×10^5 at. $T \approx 1 \mu K$

Transport towards
AC trap position
and transfer from
DC trap to AC trap



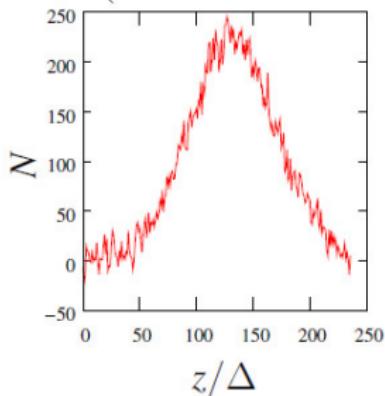
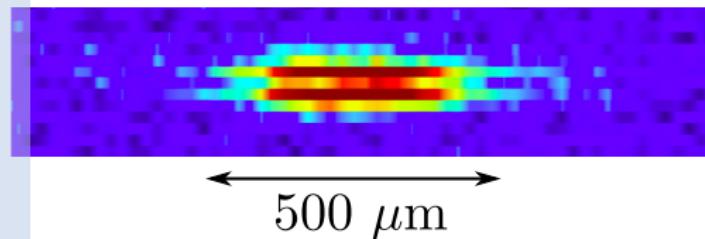
AC Magnetic trap
 8×10^4 at.

Final evaporation
for about 1 s to the
wanted temperature

$300 \rightarrow 10000$ at.
 $T = 20 \rightarrow 120 \text{ nK}$

Typical sequence

- Last step : take a picture
- Compute the longitudinal profile



- pixel size $\Delta = 4.5 \mu\text{m}$
- Cycle time $\simeq 18 \text{ s}$

Outline

Producing a 1D gas of bosons on an atom chip

2 Introduction to the physics of the 1D Bose gas

Density fluctuations in the quasi-condensate regime

Density fluctuations in the strongly interacting regime

Momentum distribution of 1D Bose gases

Introduction to the physics of the 1D Bose gas

- No Bose-Einstein condensation in 1D
- No spontaneous continuous symmetry breaking at finite T
- Lieb-Liniger Hamiltonian ($g > 0$) :

$$H = -\frac{\hbar^2}{2m} \int dz \Psi^\dagger \frac{\partial^2}{\partial z^2} \Psi + \frac{g}{2} \int dz \Psi^\dagger \Psi^\dagger \Psi \Psi$$

Introduction to the physics of the 1D Bose gas

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$$H = -\frac{\hbar^2}{2m} \int dz \Psi^\dagger \frac{\partial^2}{\partial z^2} \Psi + \frac{g}{2} \int dz \Psi^\dagger \Psi^\dagger \Psi \Psi$$

- Two scales : $E_g = \frac{mg^2}{2\hbar^2}$ and $l_g = \frac{\hbar^2}{mg}$
- Thermal equilibrium defined by :
 - Temperature parameter : $t = \frac{k_B T}{E_g}$
 - Interaction parameter : $\gamma = \frac{1}{\rho l_g} = \frac{mg}{\hbar^2 \rho}$ Note that $\gamma \nearrow$ when $\rho \searrow$
- The equation of state can be computed exactly (Yang-Yang)

Introduction to the physics of the 1D Bose gas

- 3D interactions are described by scattering length a_{3D}
- As long as $a_{3D} \ll l_\perp \rightarrow$ 3D interactions
- Effective 1D coupling constant $g = 2\hbar\omega_\perp a_{3D}$

Introduction to the physics of the 1D Bose gas

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Characterization of the system with correlation functions

- One-body correlation function \rightarrow phase coherence

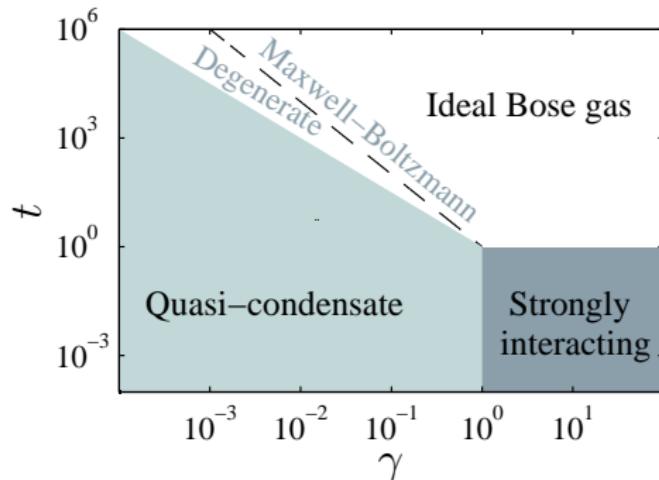
$$g^{(1)}(z) = \frac{\langle \hat{\Psi}^\dagger(z)\hat{\Psi}(0) \rangle}{\rho}$$

- Two-body correlation function \rightarrow density fluctuations

$$g^{(2)}(z) = \frac{\langle \hat{\Psi}^\dagger(z)\hat{\Psi}^\dagger(0)\hat{\Psi}(0)\hat{\Psi}(z) \rangle}{\rho^2}$$

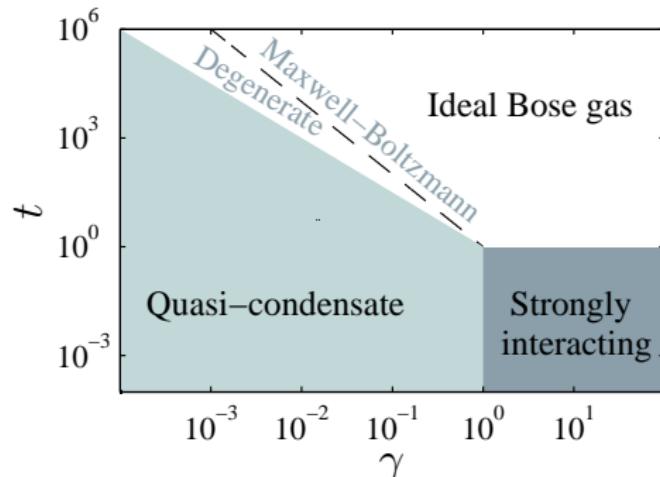
The 1D Bose gas at thermal equilibrium : Phase diagram

tel-00779447, version 1 - 22 Jan 2013



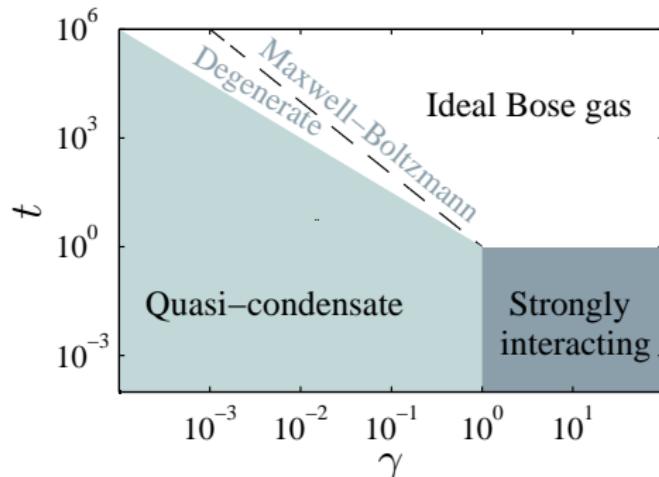
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The 1D Bose gas at thermal equilibrium : Phase diagram



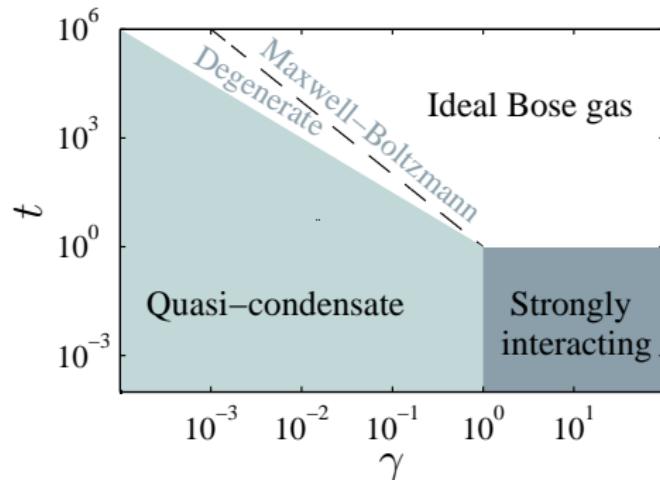
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The 1D Bose gas at thermal equilibrium : Phase diagram



- Negligible interactions : Ideal Bose gas regime $g^{(2)}(0) = 2$
- Density fluctuations reduced because of interactions : Quasi-condensate regime $g^{(2)}(0) \simeq 1$
- Interactions mimicking the Pauli principle for fermions : Strongly interacting regime $g^{(2)}(0) \ll 1$
- No phase transition in only smooth crossovers

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In situ density fluctuations measurements

tel-00779447, version 1
f- 22 Jan 2013

$$\langle \delta\rho(z)\delta\rho(0) \rangle = \rho\delta(z) + \rho^2(g^{(2)}(z) - 1)$$

: pixel size

: correlation length

$$l_c \ll \Delta \rightarrow \boxed{\langle \delta N^2 \rangle = \langle N \rangle + \langle N \rangle \rho \int_{-\infty}^{+\infty} [g^{(2)}(z) - 1] dz}$$

In situ density fluctuations measurements

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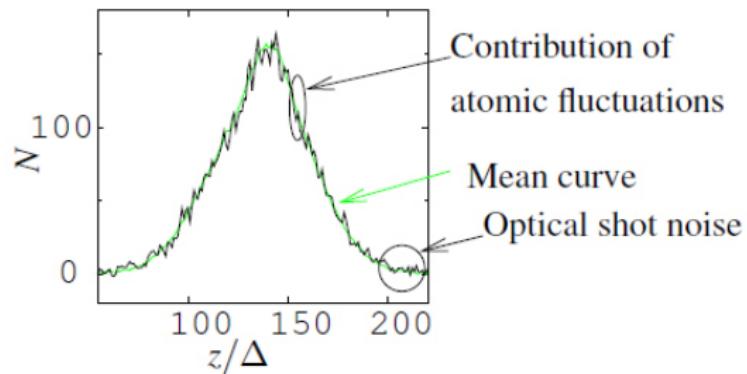
→ Fluctuations-dissipation theorem :

$$\boxed{\langle \delta N^2 \rangle = \Delta k_B T \frac{\partial \rho}{\partial \mu}}$$

- $\langle \delta N^2 \rangle \rightarrow$ Yang-Yang thermodynamics

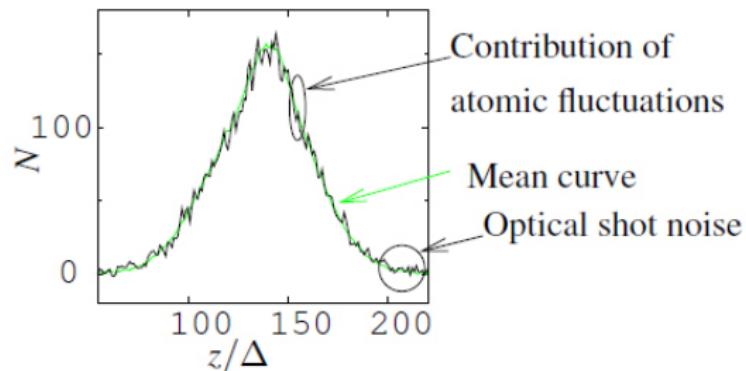
In situ density fluctuations measurements

- Statistical analysis over hundreds of images
- δN binned according to $\langle N \rangle$
- Local density approximation
 - homogeneous system
 - z is not relevant



In situ density fluctuations measurements

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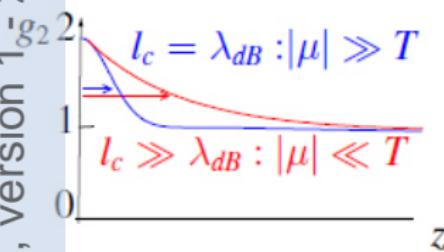
- We plot $\langle \delta N^2 \rangle$ as a function of $\langle N \rangle$
- Contribution of optical shot noise subtracted

Expected behaviour in different regimes

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- Ideal Bose gas regime

$$\langle \delta N^2 \rangle = \langle N \rangle + \langle N \rangle \rho \underbrace{\int [g^{(2)}(z) - 1] dz}_{l_c}$$

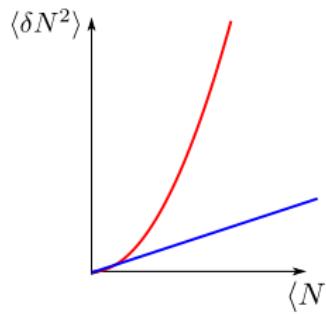


- Classical gas

$$\rho l_c \ll 1 \rightarrow \langle \delta N^2 \rangle \simeq \langle N \rangle$$

- Degenerate gas

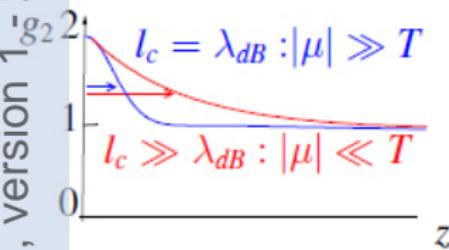
$$\rho l_c \gg 1 \rightarrow \langle \delta N^2 \rangle \simeq \langle N \rangle^2 l_c / \Delta$$



Expected behaviour in different regimes

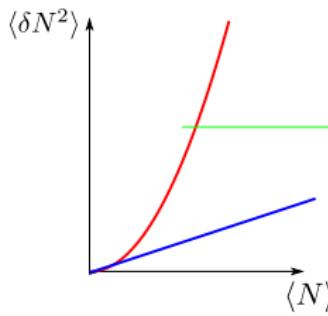
- Ideal Bose gas regime

$$\langle \delta N^2 \rangle = \langle N \rangle + \langle N \rangle \rho \underbrace{\int [g^{(2)}(z) - 1] dz}_{l_c}$$



- Quasi-condensate :
EOS : $\mu \simeq g\rho$
 $\langle \delta N^2 \rangle \simeq \Delta k_B T/g$

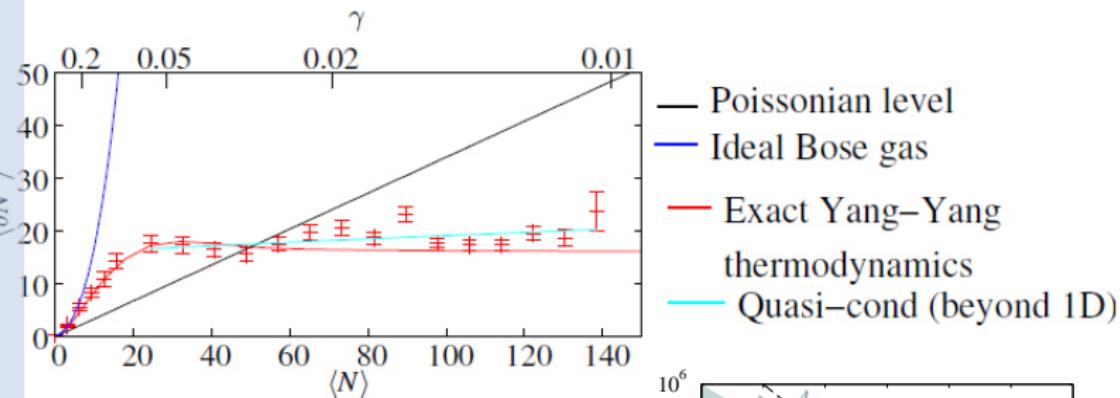
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Experimental results in the quasi-condensate regime

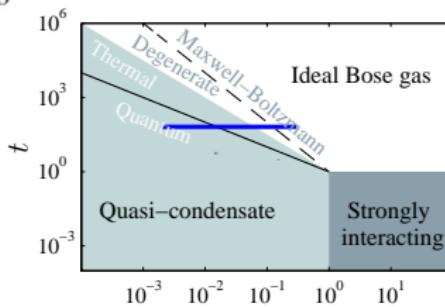
- Bosonic bunching at low densities \rightarrow super-Poissonian fluctuations

tel-00779447, version 1 - 22 Jan 2013



- $T \simeq 15 \text{ nK}$
- $k_B T / \hbar \omega_{\perp} \simeq 0.1$
- $\mu \simeq 30 \text{ nK}$
- $\mu / \hbar \omega_{\perp} \simeq 0.2$

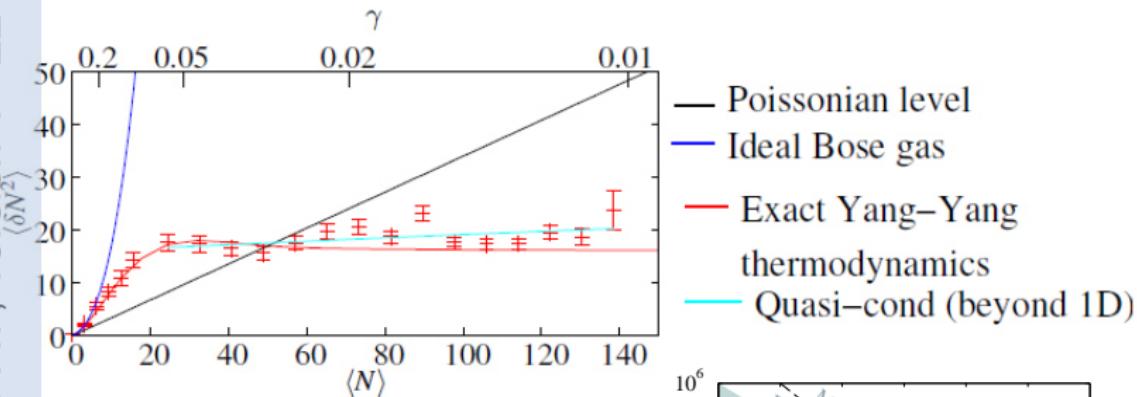
PRL **106**, 230405 (2011)



Experimental results in the quasi-condensate regime

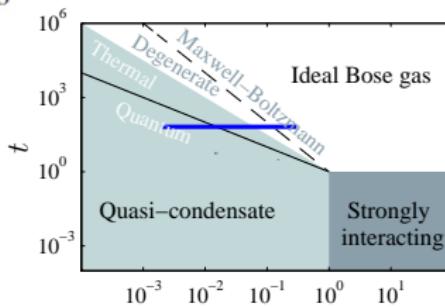
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- Saturation of the density fluctuations in the QBEC regime



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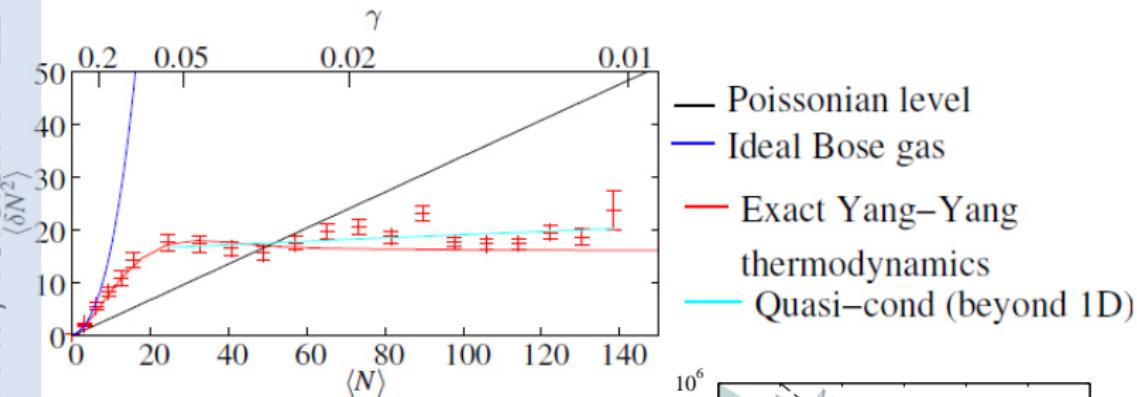
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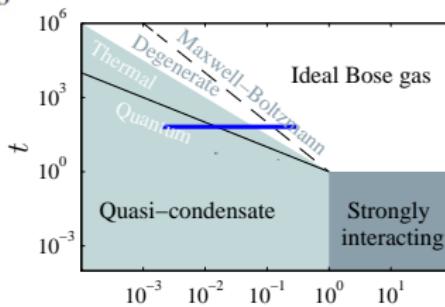
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- Bosonic bunching at low densities \rightarrow super-Poissonian fluctuations
- Saturation of the density fluctuations in the QBEC regime
- In the QBEC regime : super and sub-Poissonian fluctuations



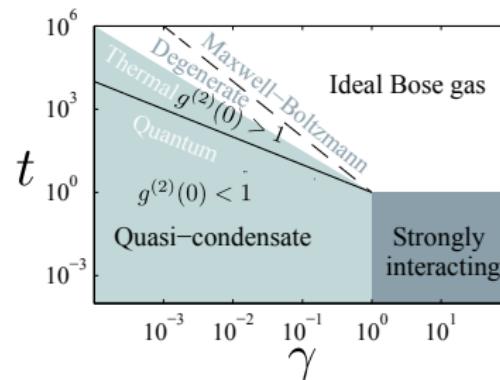
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PRL **106**, 230405 (2011)



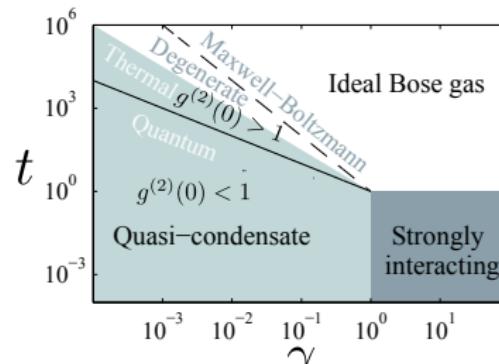
First observation of the quantum quasi-condensate regime

- $\langle \delta N^2 \rangle < \langle N \rangle$ and $\langle \delta N^2 \rangle = \langle N \rangle + \langle N \rangle \rho \int [g^{(2)}(z) - 1] dz$
 $\rightarrow g^{(2)} < 1 \rightarrow g^{(2)}(0)$ dominated by quantum fluctuations.

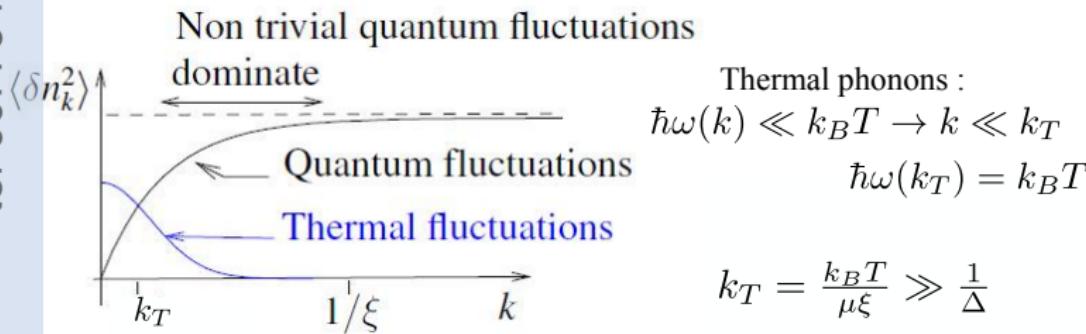


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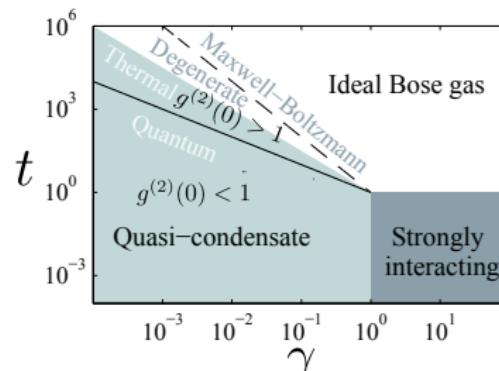


- However we still measure thermal fluctuations.

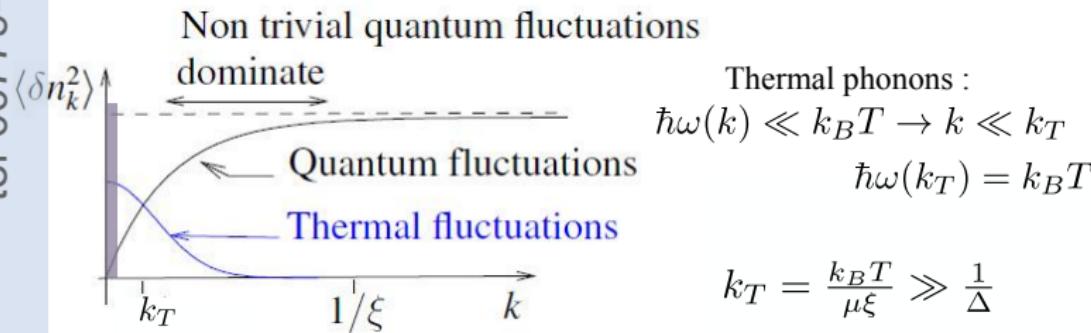


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Outline

Producing a 1D gas of bosons on an atom chip

Introduction to the physics of the 1D Bose gas

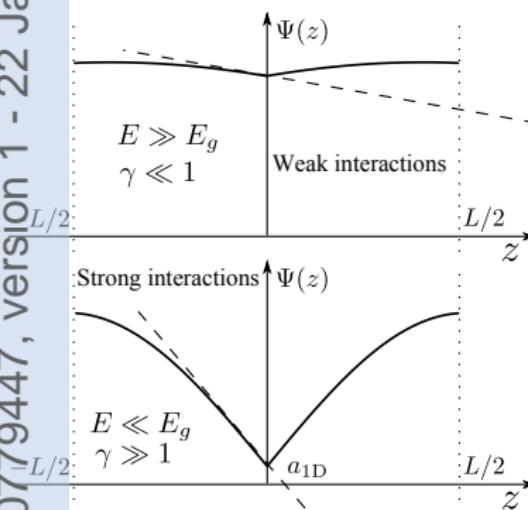
Density fluctuations in the quasi-condensate regime

Density fluctuations in the strongly interacting regime

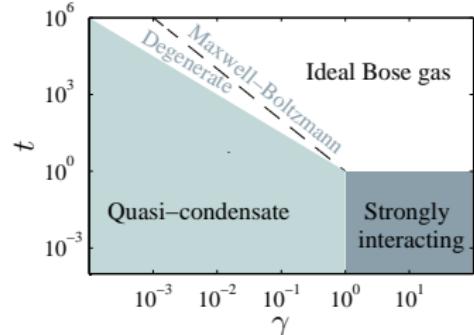
Momentum distribution of 1D Bose gases

The strongly interacting regime

Relative wavefunction of
two bosons in a box at
 $t = 0$:

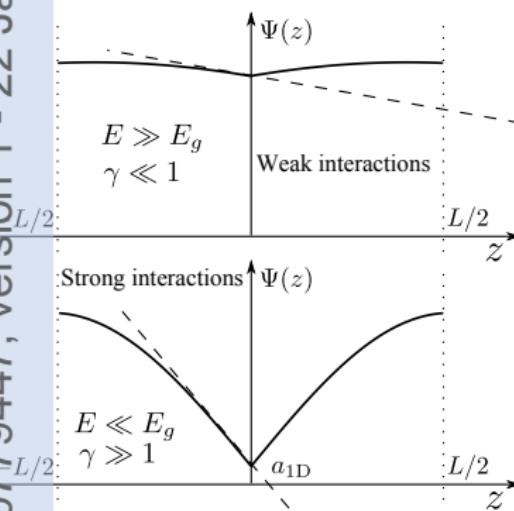


- At finite T , strong interactions if $k_B T \ll E_g \rightarrow t \ll 1$

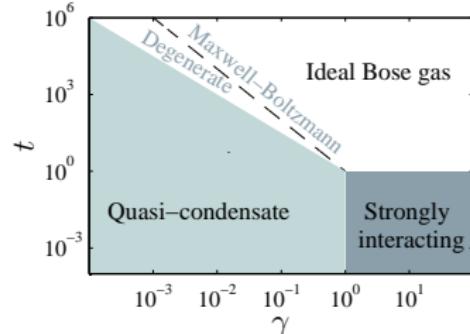


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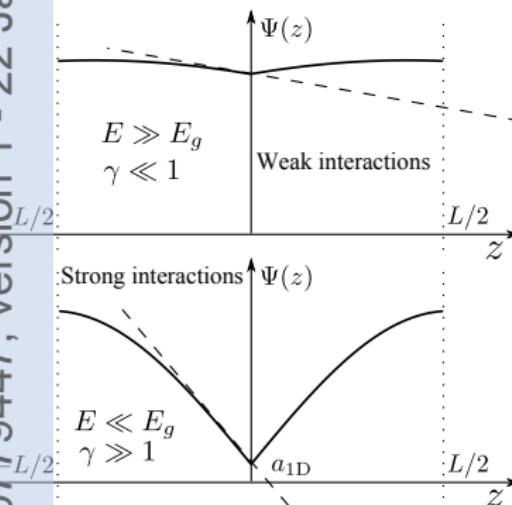


- Bose-Fermi mapping

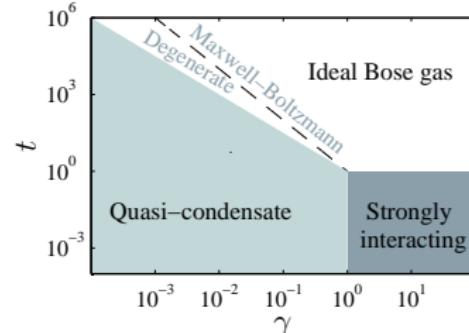
$$\Psi_B(z_1, \dots, z_N) = \mathcal{S}[\Psi_F(z_1, \dots, z_N)]$$

The strongly interacting regime

Relative wavefunction of two bosons in a box at $\omega = 0$:



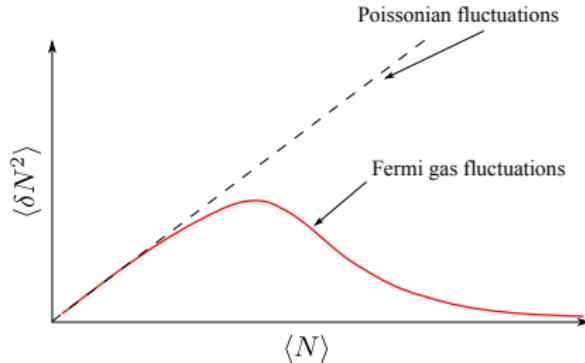
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- Bose-Fermi mapping
 $\Psi_B(z_1, \dots, z_N) = \mathcal{S}[\Psi_F(z_1, \dots, z_N)]$

- Observed in many groups since 2004 in 2D optical lattices
 - Inhomogeneity of atom number, temperature, trapping frequency
 - Only global quantities are accessible
 - No thermometry available

Density fluctuations in a Fermi gas

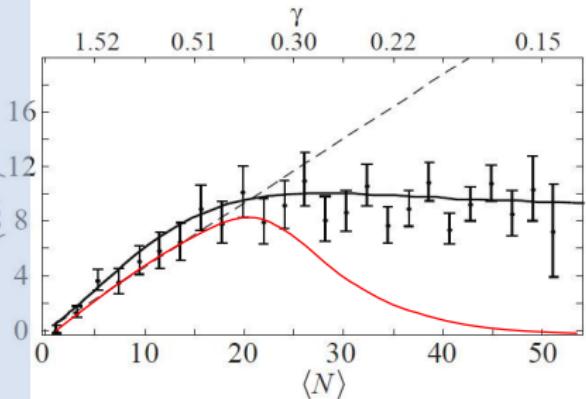


- Poissonian at low densities
- Sub-Poissonian at intermediate densities
- Zero at high densities

Experimental results in the strongly interacting regime

tel-00779447, version 1 - 22 Jan 2013

- $t = 5.4$ with $\nu_{\perp} \simeq 20 \text{ kHz}$
- Absence of super-Poissonian density fluctuations
- Sub-Poissonian density fluctuations at any density

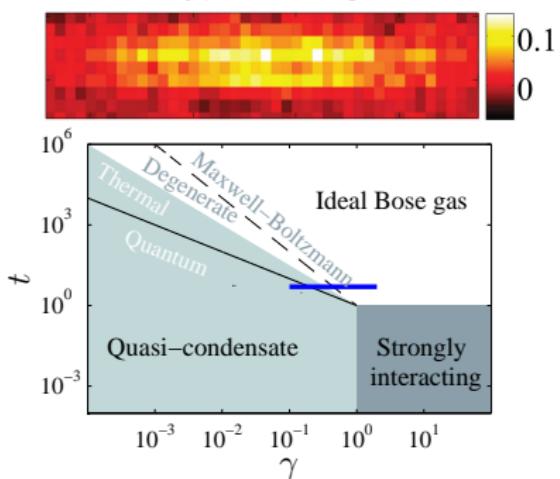


Solid line : Yang-Yang

Dashed line : Poissonian fluctuation

Red line : $t \ll 1$ limit

Typical image



PRL **106**, 230405 (2011)

Outline

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- Introduction to the physics of the 1D Bose gas
- Density fluctuations in the quasi-condensate regime
- Density fluctuations in the strongly interacting regime
- Momentum distribution of 1D Bose gases

- Phase coherence is described by the one body correlation function

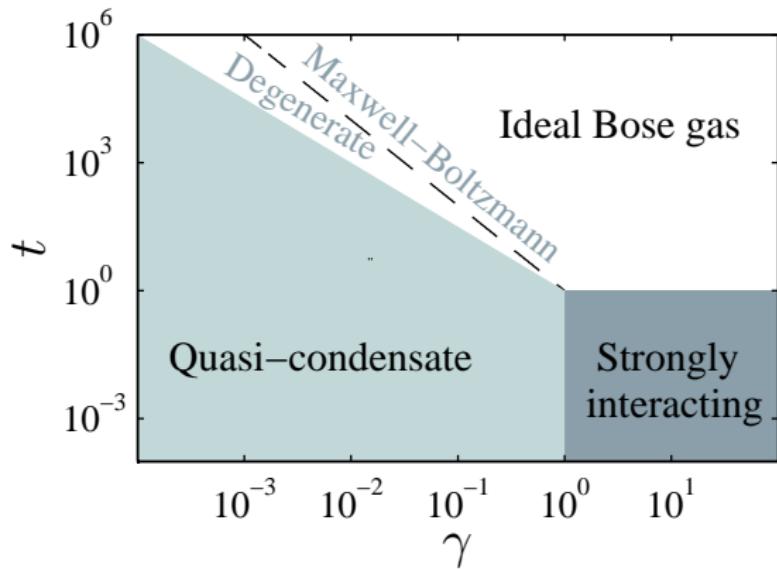
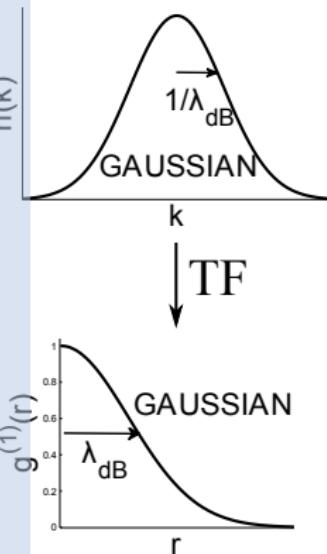
$$g^{(1)}(r) = \frac{\langle \Psi^\dagger(r)\Psi(0) \rangle}{\rho}$$

- $$g^{(1)}(r) = \frac{1}{\rho} \int \langle n_k \rangle e^{-ikr} \frac{dk}{2\pi}$$
 $\langle n_k \rangle$: population of momentum $\hbar k$.
- **Conclusion** : measuring $\langle n_k \rangle$ is equivalent to probing $g^{(1)}(r)$.
- $g^{(1)}(r)$ unknown in general → Quantum Monte Carlo calculations
(Tommaso Roscilde, ENS Lyon)

Non-degenerate Bose gas

tel-00779447, version 1 - 22 Jan 2013

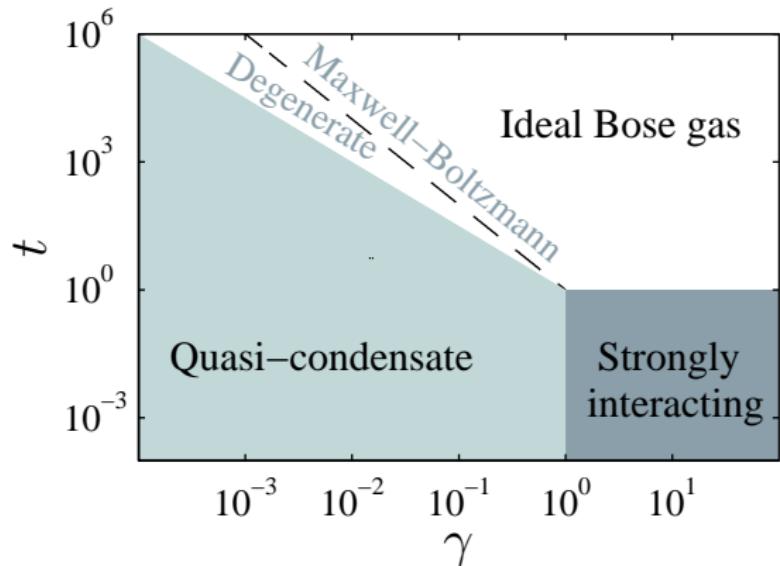
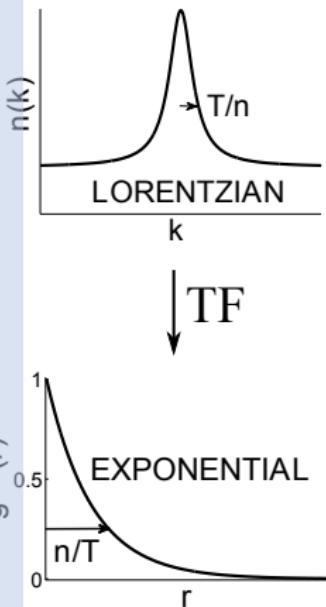
- Maxwell-Boltzmann gas



$$k_B T \gg |\mu| \text{ Bose law limit : } \langle n_k \rangle \propto e^{-\frac{\epsilon_k}{k_B T}}, \text{ with } \epsilon_k = \frac{\hbar^2 k^2}{2m}$$

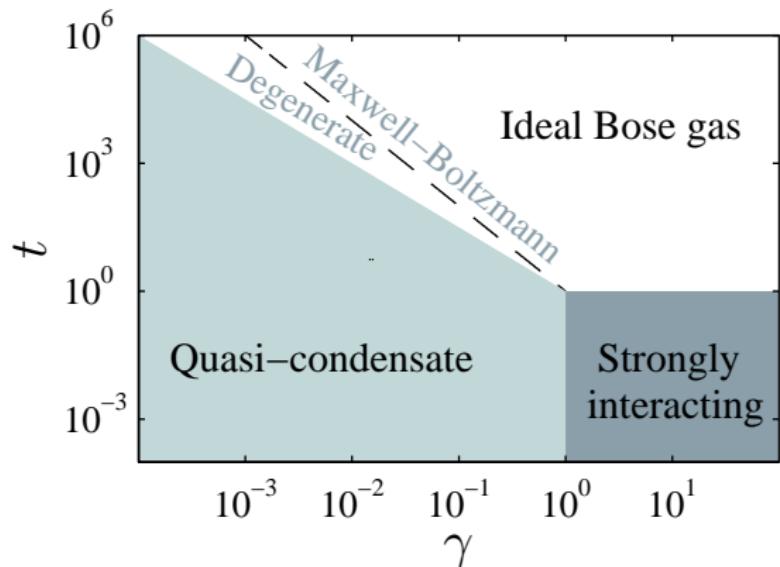
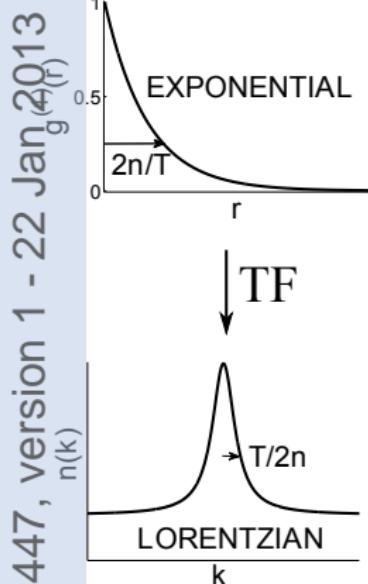
Degenerate Bose gas

tel-00779471 version 1 - 22 Jan 2013



$k_B T \ll |\mu|$ Bose law limit : $\langle n_k \rangle \propto \frac{k_B T}{\epsilon_k - \mu}$, with $\epsilon_k = \frac{\hbar^2 k^2}{2m}$

Quasi-condensate

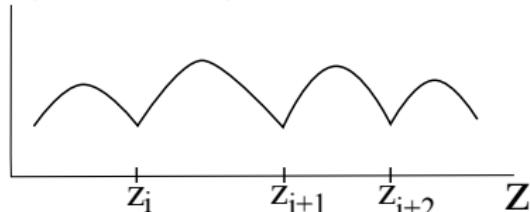


- Contribution of phonons give $g^{(1)}(r) = e^{-Tr/2n}$
- $n(k)$ is Lorentzian in ideal Bose gas degenerate regime and quasi condensate regime. The width differs by a factor 2.

$1/p^4$ tails and kinetic energy

- Short distance correlation (“contact”) properties of the Lieb-Liniger model :

$$\Psi(z_1, \dots, z, \dots, z_n)$$



$$n(k) \propto \frac{1}{k^4} \quad \text{for large } k\text{'s}$$

- $E = E_K + E_{int} \rightarrow$ Yang/Yang

$$E_{int} = \frac{1}{2} N g n g^{(2)}(0)$$

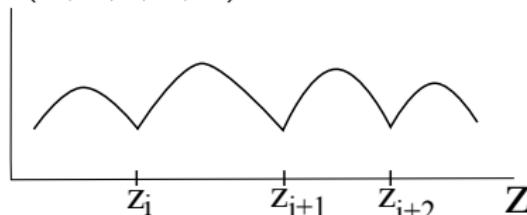
$$g^{(2)}(0) \propto \partial E / \partial g \rightarrow \text{Hellman-Feynman theorem}$$

Conclusion : E_K is a thermodynamic quantity

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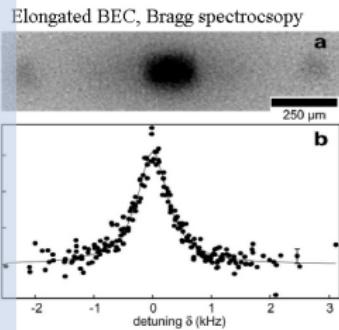
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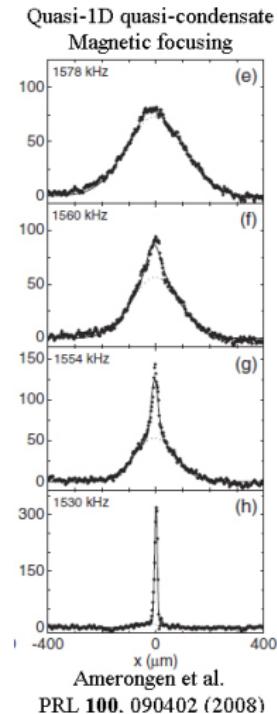
And E_K is the RMS width of the momentum distribution :

$$E_K = \frac{\hbar^2}{2m} \int dk \ k^2 n(k) \rightarrow \text{thermometry}$$

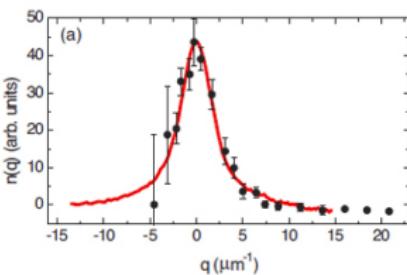
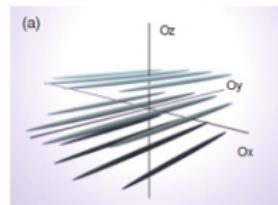
State of the art



Richard et al. PRL 91, 4 (2003)



Array of purely 1D gases
Strongly interacting
Bragg spectroscopy



Focusing method

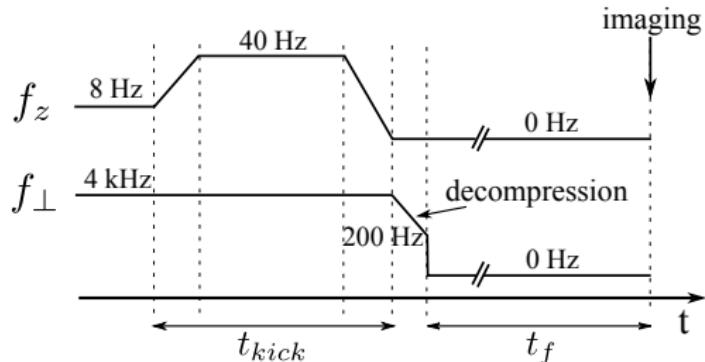
- In optics : Fourier transform of a field → Fourier plane of a lens
- Multiply by quadratic phase and propagate

Adapted from Amerongen's thesis

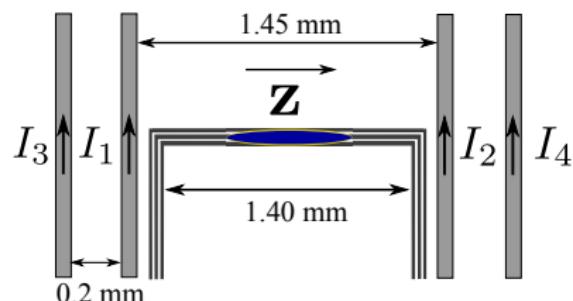
- Quadratic phase → longitudinal harmonic kick potential
- Propagation → time of flight
- Typical parameters :

$$f_{kick} = 40 \text{ Hz}, t_{kick} = 0.7 \text{ ms} \text{ and } TOF = 27 \text{ ms}$$

Focusing sequence

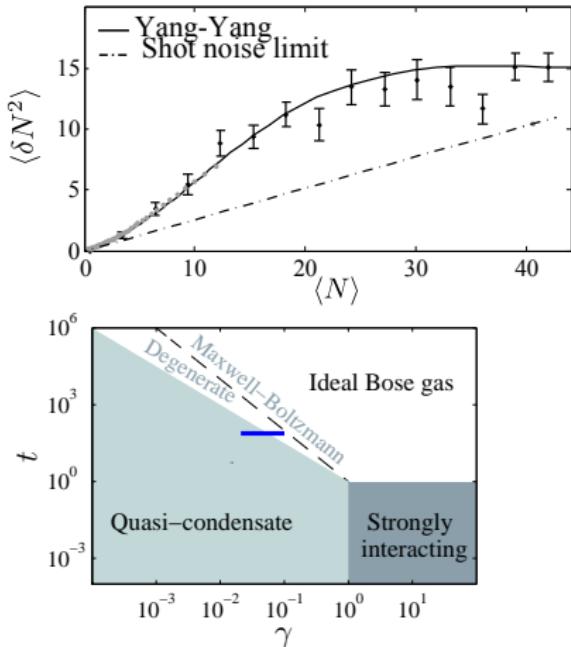
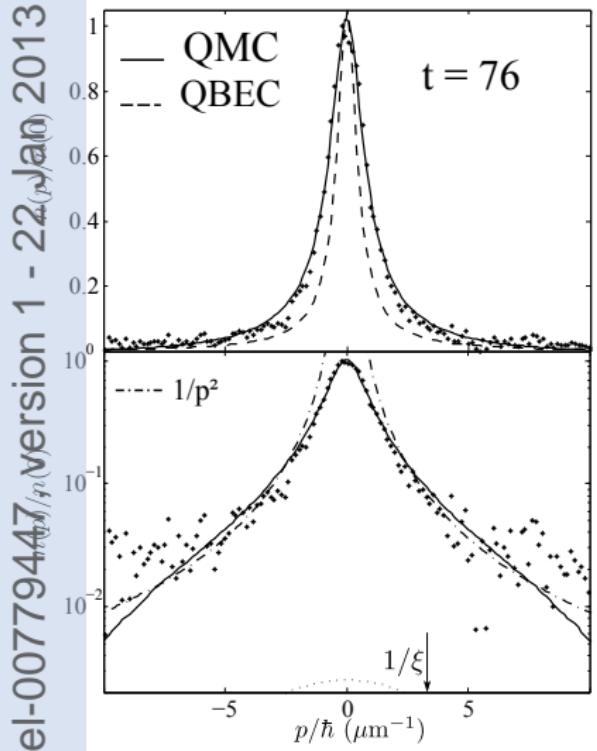


Transverse decompression step to avoid too huge transverse expansion

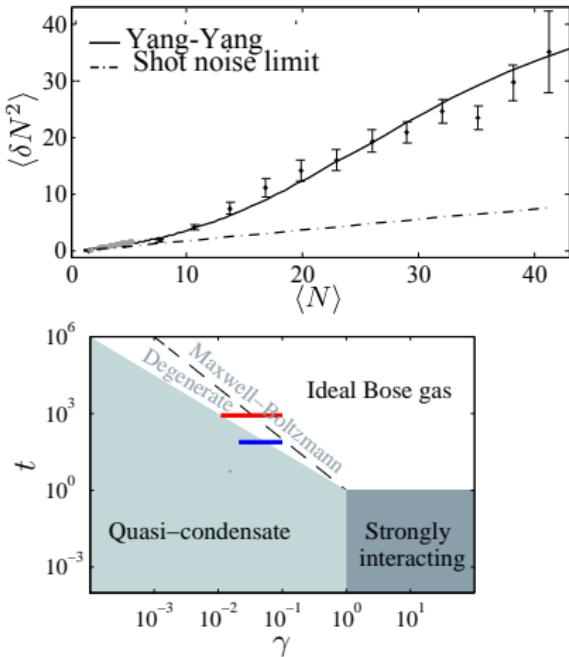
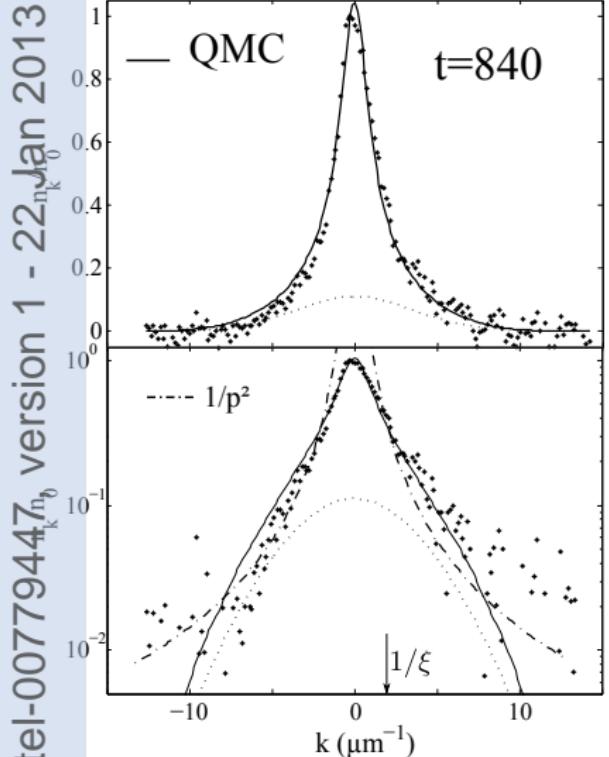


4 wire configuration = very harmonic focusing pulse

Results : quasi-condensate regime



Results : degenerate ideal Bose gas



- Distributions are essentially Lorentzian

Conclusion on momentum distributions

tel-00779447, version 1 - 22 Jan 2013

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Remerciements

- **Atom Ship team**
Isabelle Bouchoule
Bess Fang
Tarik Berrada
Aisling Johnson
Indranil Dutta
Eugenio Cocchi
Nicolas Tancogne
- **LPN (fabrication)**
Sophie Bouchoule
Sandy Phommaly
- **Atelier mécanique**
André Guilbaud
Patrick Roth

- **Ingénieurs électroniciens**
André Villing
Frédéric Moron
- **Collaborations théorie**
Karen Kheruntsyan (YY)
Tommaso Roscilde (QMC)
- **Directeurs**
Chris Westbrook
Christian Chardonnet
Pierre Chavel
Bernard Bourguignon
Alain Aspect
- **Spécialistes du vide**
Antoine Browaeys
Alexei Ourjoumtsev

- **Spécialiste d'Oslo**

Yvan Sortais

- **Enseignement**

Lionel Jacobowietz

Fabienne Bernard

Sylvain Perrot

Julien Moreau

Mathieu Hébert

Gaëlle Lucas-Leclin

Sylvie Lebrun

Thierry Avignon

Cédric Lejeune

...

- **Groupe d'optique atomique**