

# Evaluation: Single Value Metrics (P@n, R-precision and MAP)

**COMP3009J: Information Retrieval**

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# Single Value Metrics

- Using Precision and Recall requires two metrics to be calculated.
- We would prefer to have a single metric that captures the overall performance of the system:
  - Precision at n ( $P@n$ )
  - R-precision
  - Mean Average Precision (MAP)
  - Binary Preference (bpref)
  - Normalised Discounted Cumulated Gain (NDCG)

# Average over several queries

- In our discussion of these metrics, we will see how to calculate a score for one set of results for one query.
- Of course, when evaluating an IR system, we should use several queries for evaluation.
- In this situation, we must first calculate the score for each query, and then get the average over all the queries.

# Precision at $n$

- Sometimes we are interested in the precision amongst the top  $n$  results.
- This is particularly suitable for web search systems where people typically look no further than the first few results.
- For example, we may be interested in the precision after 10 documents have been retrieved.
  - Known as “**Precision at 10**”, or “**P@10**”
- This is a measure of the quality of the results that a user is likely to look at.

# Precision at $n$

- $P @ 3 = 0.67$ 
  - (i.e. 2 of the top 3 results were relevant)
- $P @ 10 = 0.4$ 
  - (i.e. 4 of the top 10 results were relevant)

Rank	Document
1	$d_{123} (r)$
2	$d_{84}$
3	$d_{56} (r)$
4	$d_6$
5	$d_8$
6	$d_9 (r)$
7	$d_{511}$
8	$d_{129}$
9	$d_{187}$
10	$d_{25} (r)$
11	$d_{38}$
12	$d_{48}$
13	$d_{250}$
14	$d_{113}$
15	$d_3 (r)$

# Precision @ n: Problems

- One problem with using  $P@n$  is that its performance is affected by the number of relevant documents available.
- For a query that has only 10 relevant documents, a good  $P@10$  score is difficult.
- If there are 1,000 relevant documents, a good  $P@10$  score is easy.

# R-precision

- A similar metric is **R-precision**, where we are interested in the precision after the top  $R$  documents are returned (where  $R$  is the number of relevant documents).
- This is similar to  $P@n$  except that  $n$  is not fixed for all queries (because the number of relevant documents will be different for each query).

# R-precision

- R-Precision in our example is the same as  $P@10$ , because there are 10 relevant documents for this query.
- Therefore R-Precision = 0.4

Rank	Document
1	$d_{123}$ (r)
2	$d_{84}$
3	$d_{56}$ (r)
4	$d_6$
5	$d_8$
6	$d_9$ (r)
7	$d_{511}$
8	$d_{129}$
9	$d_{187}$
10	$d_{25}$ (r)
11	$d_{38}$
12	$d_{48}$
13	$d_{250}$
14	$d_{113}$
15	$d_3$ (r)



# R-precision

- Another example, with a different set of relevant documents.
- $R = \{d_3, d_{56}, d_{129}\}$
- R-Precision in this example is the same as  $P@3$ , because there are 3 relevant documents for this query.
- Of the first 3 results, 1 is relevant.
- Therefore R-Precision = 0.33

Rank	Document
1	$d_{123}$
2	$d_{84}$
3	$d_{56} (r)$
4	$d_6$
5	$d_8$
6	$d_9$
7	$d_{511}$
8	$d_{129} (r)$
9	$d_{187}$
10	$d_{25}$
11	$d_{38}$
12	$d_{48}$
13	$d_{250}$
14	$d_{113}$
15	$d_3 (r)$

# Mean Average Precision (MAP)

- Mean Average Precision (MAP) has for many years been the most commonly used metric in IR literature to evaluate the performance of systems.
- It is a single-value metric based on precision.
- Unlike simple precision, it rewards systems that rank relevant documents at the beginning of the results returned.
- Unlike P@10, it continues to examine the later stages of the ranked list, although with lesser weight.

# Mean Average Precision (MAP)

■ It involves three steps:

1. Firstly, we must calculate the precision at each recall point (at each rank where a relevant document is found).
2. The **Average Precision** for this query is found by dividing the sum of these precision calculations by the total number of relevant documents.
3. For multiple queries, the same procedure must be performed for each. We must calculate the mean of the queries' average precision values, giving us **Mean Average Precision**.

# Example

- As before, we assume that there were 10 relevant documents available for retrieval.
- Average Precision (for this query):  $\frac{1.0+0.67+0.5+0.4+0.33}{10} = 0.29$
- This is the AP for one query.
- To get the Mean Average Precision (MAP), we calculate the average over all queries.

Rank	Document	
1	d <sub>123</sub>	$P = 1/1 = 1.00$
2	d <sub>84</sub>	
3	d <sub>56</sub>	$P = 2/3 = 0.67$
4	d <sub>6</sub>	
5	d <sub>8</sub>	
6	d <sub>9</sub>	$P = 3/6 = 0.5$
7	d <sub>511</sub>	
8	d <sub>129</sub>	
9	d <sub>187</sub>	
10	d <sub>25</sub>	$P = 4/10 = 0.4$
11	d <sub>38</sub>	
12	d <sub>48</sub>	
13	d <sub>250</sub>	
14	d <sub>113</sub>	
15	d <sub>3</sub>	$P = 5/15 = 0.33$