

CS & IT ENGINEERING

'C' Programming

Functions

Lecture No.- 03



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Recap of Previous Lecture



- Recursion

- The Process of calling a function by itself.

- Types of Recursion

- Direct : Head Recursion, Tail Recursion, Tree Recursion, Nested Recursion

- Indirect

- Call-by-Value Vs Call-by-Reference

(formal args
gets effected)

(Actual args
gets effected)



Topics to be Covered



- Types of Recursion

- Head
 - Tail
 - Tree
 - Nested
- } Direct
- Indirect





Topic : Recursion - 2



Head Recursion : If after calling a function, recursively if more body [statement(s)] Exist to Execute.

Syntax : Return type function (argument(s))

{
 // Base Case

 // Recursive Case

 stmt ;

 stmt ;

 ⋮

}

Ex: 1. void fun (int x)

2. {
 if (x < 1) // Base Case
 return ;

3. else

4. {
5. fun (x-1); // Recursive Case

6. printf ("Hi");

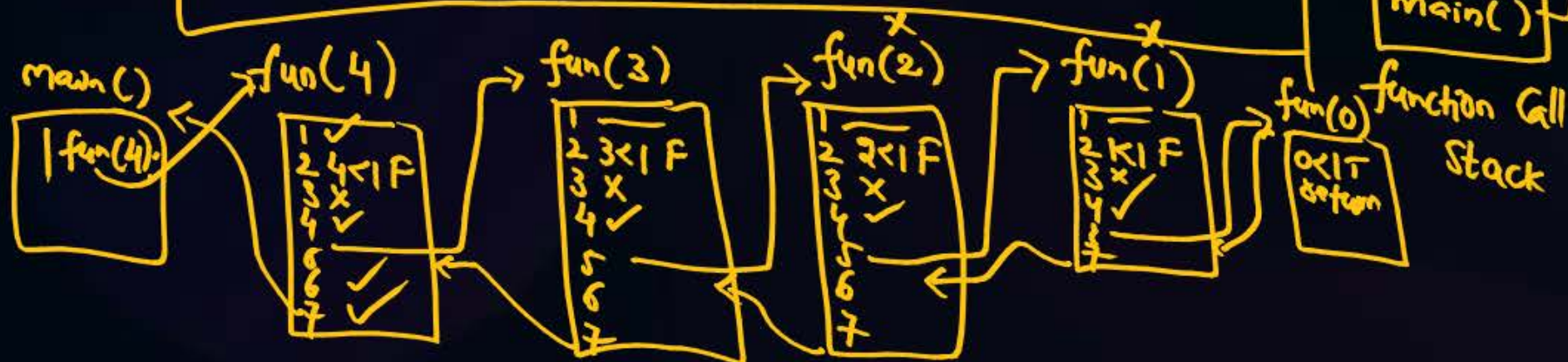
7. printf ("%d", x); } statements after recursive calling

void main ()

{
 fun(4);

}

o/p: Hi 1 Hi 2 Hi 3 Hi 4





Topic : Recursion - 2

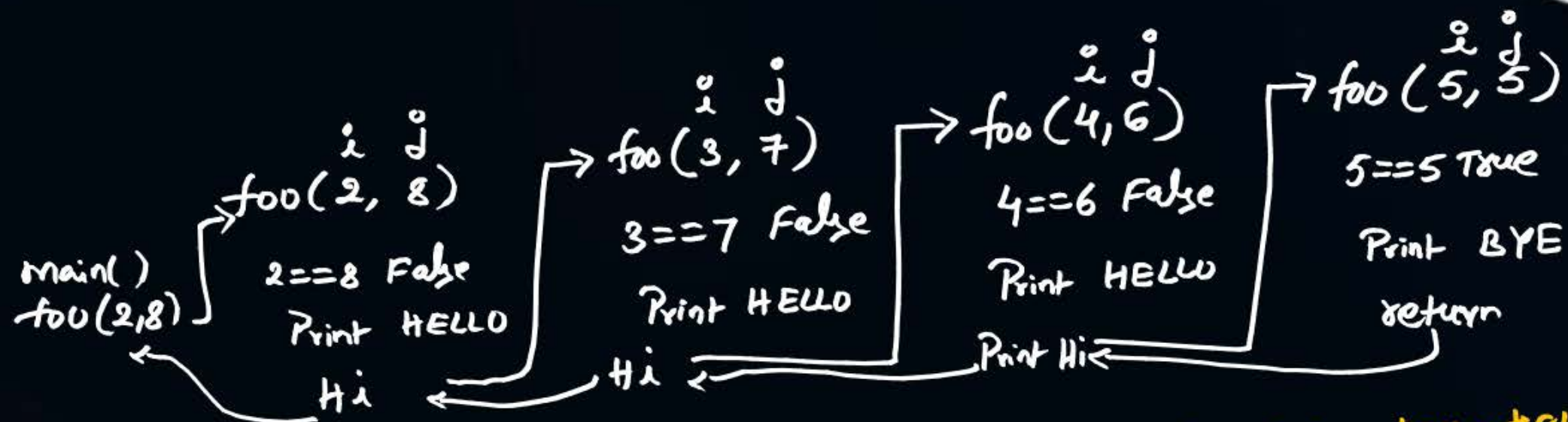
o/p: HELLO HELLO HELLO BYE Hi Hi Hi



Ex:1

```
void foo(int i, int j)
{
    if (i == j)
    {
        printf("BYE ");
        return;
    }
    else
    {
        printf("HELLO");
        foo(i+1, j-1);
        printf("Hi ");
    }
}
```

→ void main()
{
 foo(2, 8);
}



a) HELLO Hi Hi Hi BYE HELLO HELLO HELLO

b) HELLO HELLO HELLO BYE Hi Hi Hi ✓

c) HELLO HELLO Hi Hi BYE

d) HELLO HELLO HELLO Hi Hi Hi



Topic : Recursion - 2



$$x(8,3) = 8+3 - \frac{x(7,4)}{11} + \frac{x(6,6)}{36}$$

$$= 11 - 11 + 36 = 36$$

Ex: 2

```
int X (int i, int j)
```

```
{
  if (i == j)
    return (i * j);
  else if (i < j)
    return (i + j);
```

```
else
  return (i + j - x(i-1, j+1) + x(i-2, j+3));
}
```

```
void main ( )
```

```
{
  printf ("%d", X(10,0))
}
```

o/p: 22

$$x(6,5)$$

$$6+5 - \frac{x(5,6)}{11} + \frac{x(4,8)}{12}$$

$$= 11 - 11 + 12 = 12$$

$$x(7,4)$$

$$7+4 - \frac{x(6,5)}{12} + \frac{x(5,7)}{12}$$

$$= 11$$

$x(10,0)$

$$10+0 - x(9,1) + x(8,3)$$

$$= 10+0 - 24 + 36 = \underline{22}$$

$x(9,1)$

$$9+1 - x(8,2) + x(7,4)$$

$$= 10 - (-3) + 11 = 24$$

$x(8,2)$

$$8+2 - x(7,3) + x(6,5) = 10 - 25 + 12$$

$$= -3$$

$x(7,3)$

$$7+3 - x(6,4) + \frac{x(5,6)}{11} = 10 - (-4) + 11$$

$$= 25$$

$x(6,4)$

$$6+4 - \frac{x(5,5)}{25} + \frac{x(4,7)}{11} = -4$$



Topic : Recursion - 2



Tail Recursion = If Recursive calling is the Last statement of function body, Then it is said to be Tail Recursion.

Syntax:

```
Returntype Name(argument(s))
{
    // Base case

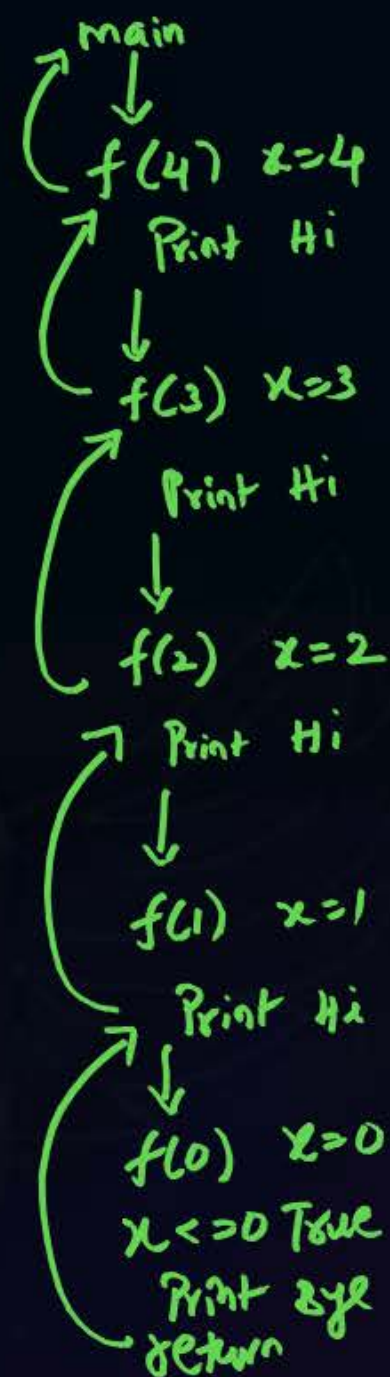
    // stmt;
    // stmt;
    :
    // stmt;
    // Name(arg); // Recursive calling
}
```

Ex:

```
void f(int x)
{
    if (x <= 0)
    {
        printf("Bye ");
        return;
    }
    else {
        printf("Hi");
        f(x-1);
    }
}

void main()
{
    f(4);
}
```

o/p: Hi Hi Hi Hi Bye





Topic : Recursion - 2



$f(1, 7)$ $i=1, j=7$
 $1 < 7 \Rightarrow \text{return}(1+7) = 8$

Ex:

```
int f(int i, int j)
{
    if ( i < j )
        return (i+j)
    else if ( i > j )
        return (i-j)
    else
        return f(i+2, j-3);
}
```

```
void main( )
{
    printf(" %.d", f(1,7));
}
```

8



Topic : Recursion - 2



Ex:

```
void display(int i, int j)
{
    if ((i <= 0) || (j >= 8))
        return;

    printf("%d %d\n", (i-1), (j+2));
    display(i-3, j+2);
}
```

→ void main()
{
 display(5, 2);
}

o/p: 4 4
 1 6

main()
↓
display(5, 2) i=5, j=2
5 <= 0 || 2 >= 8 F || F == F
↓
Print 4 4
↓
display(2, 4) i=2, j=4
2 <= 0 || 4 >= 8 False
↓
Print 1, 6
↓
display(-1, 6) i=-1, j=6
-1 <= 0 || 6 >= 8 T || F == True
↓
return



Topic : Recursion - 2



Tree Recursion

If, In a Recursive function, recursive calling is made multiple times, then it is said to be Tree Recursion.

Ex: void f(int x)

```
{ if(x <= 0)
  return;
```

```
else
```

```
{ f(x-1);
```

```
  printf("%d", x);
```

```
  f(x-1);
```

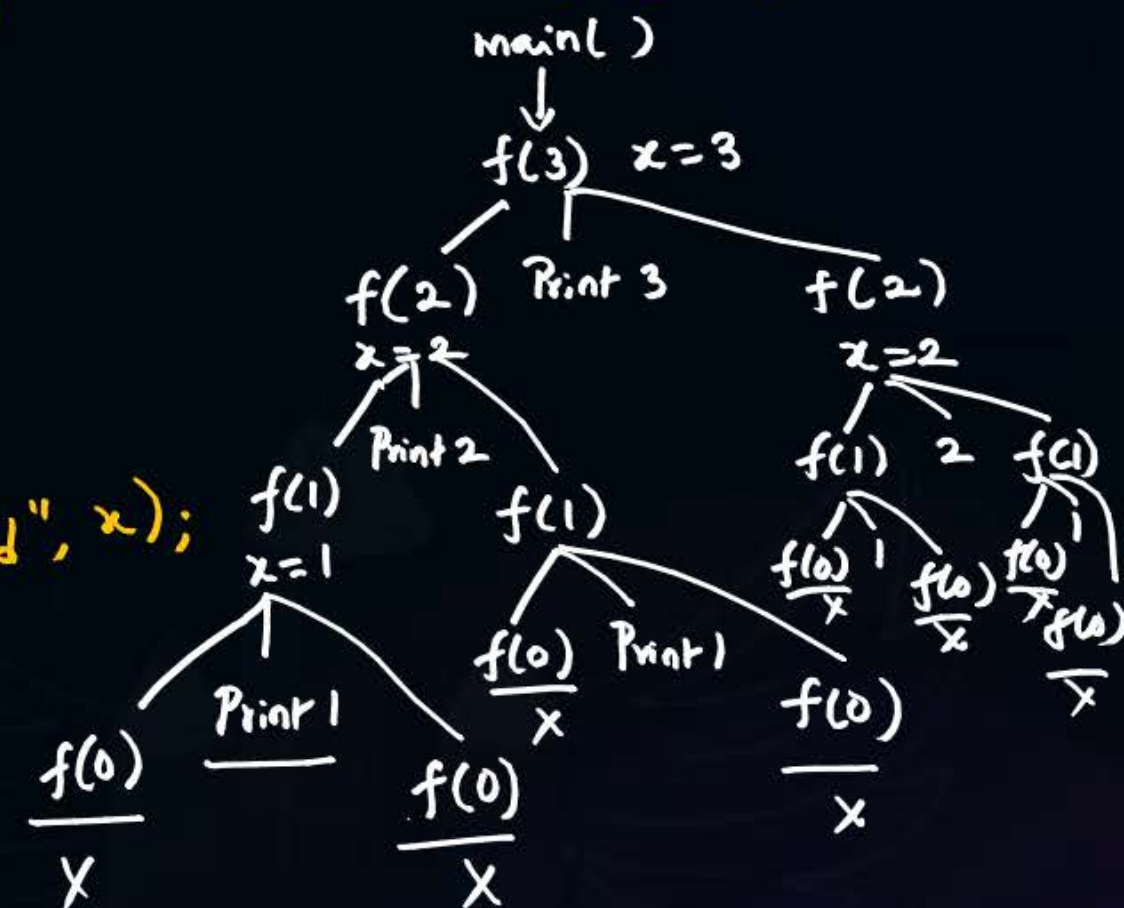
```
}
```

```
void main()
```

```
{
```

```
  f(3);
```

```
}
```

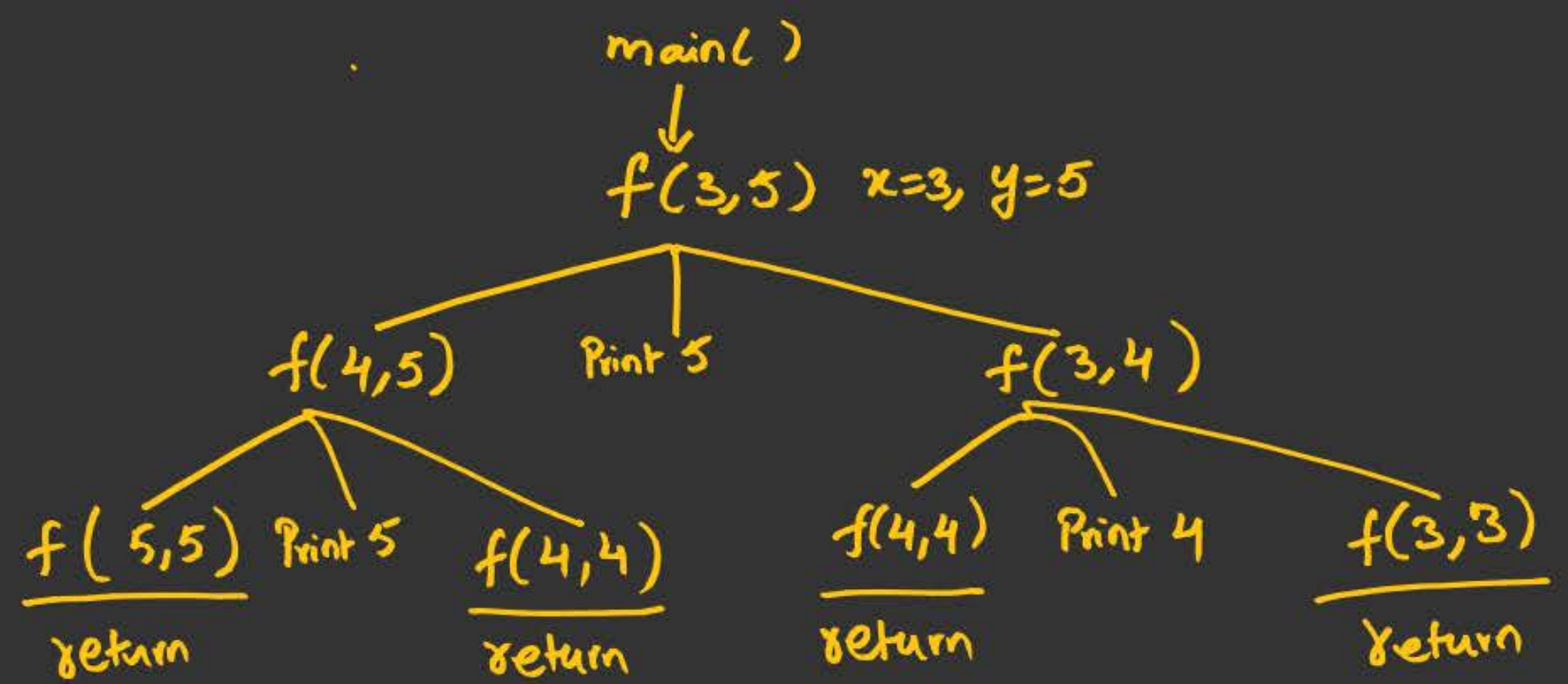


o/p: 1 2 1 3 1 2 1

Ex:-1

```
void main ( )  
{  
    f(3,5);  
}  
void f(int x, int y)  
{  
    if (x == y) return;  
    else if (x < y)  
    {  
        f(x+1, y);  
        printf("%i d", y);  
        f(x, y-1);  
    }  
    else  
    {  
        f(x-1, y);  
        printf("%i d", x);  
        f(x, y+1);  
    }  
}
```

o/p: 5 5 4



Nested Recursion : while a Recursive call, if another recursive call is made, Then it is said to be Nested Recursion.

Syntax:

Return type Name (arguments)

{
// Base Case

// Recursive Case

stmt;

∴
Name (Name (Name (arg-1))) ;

}

Ex:

```
int x(int i)
{
    if (i <= 1)
        return i;
    else
    {
        printf("%d", (i+1));
        return x(x(i-1));
    }
}
```

```
void main()
{
    x(3);
}
```

o/p: 4 3

```
main()
↓
x(3) i=3
Print 4 ✓
↓
x(x(2))
x(1)
returns 1
```

x(2) i=2 ↓ Print 3 ✓ ↓ x(x(1)) x(1) returns 1	x(1) i=1 return 1
---	----------------------

Indirect Recursion : A function is called itself, through some other function(s).

Ex:

```
A ( )  
{  
    B ( );  
}  
B ( )  
{  
    C ( );  
}  
C ( )  
{  
    A ( );  
}
```



Example

```
void A(int x)  
{  
    if(x <= 1) return;  
    else  
    {  
        printf("Hi");  
        B(x+1);  
    }  
}  
void B(int y)  
{  
    if(y >= 5) return;  
    else  
    {  
        printf("Hello");  
        C(y*2);  
    }  
}
```

o/p: Hi Hello Bye Hi

```
void C(int z)  
{  
    if(z / 5 == 0) return;  
    else  
    {  
        printf("Bye");  
        A(z/2);  
    }  
}  
void main ( )  
{  
    A(3);  
}
```

```
main ( )  
↓  
A(3) x=3  
↓  
B(4) y=4  
↓  
C(8) z=8  
↓  
A(4) x=4  
↓  
B(5) y=5  
5 >= 5 True  
return.
```



2 mins Summary



Types of Recursion

- Direct
 - Head
 - Tail
 - Tree
 - Nested
- Indirect





THANK - YOU