

# COMPUTER SCIENCE



## Database Management System

### FD's & Normalization

Lecture\_11

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An orange diamond-shaped sign with a black border, mounted on a white pole. The sign contains the text 'TOPICS TO BE COVERED' in black, bold, sans-serif capital letters.

**TOPICS  
TO BE  
COVERED**

A red diamond-shaped sign with a white border, containing the number '01' in white, bold, sans-serif font.

**01**

**Lossless Join Decomposition**

A red diamond-shaped sign with a white border, containing the number '02' in white, bold, sans-serif font.

**02**

**Dependency Preserving**



## Lossless Join Decomposition

Lossless Join

: If Common Attribute of  $R_1$  &  $R_2$   
either a Super key of  $R_1$

(OR)

Super key of  $R_2$

$$R_1 \cup R_2 \cup R_3 \dots \cup R_n = R$$

# CHASE TEST

11<sup>th</sup> Aug YouTube.

$R_1( )$	-	-	-		
$R_2( )$			-	-	-



Q.1

R(ABC)



A	B	C
1	5	5
2	5	8
3	8	8

Decomposed into

Q.1  $R_1(AB)$  &  $R_2(BC)$

Lossy

Q.2

R(ABC)



A	B	C
1	5	5
2	5	8
3	8	8

Decomposed into

Q.2  $R_1(AB)$  &  $R_2(AC)$

Lossless.

## Lossless – Join Decomposition

- For the case of  $R = (R_1, R_2)$ , we require that for all possible relations  $r$  on schema  $R$

$$r = \pi_{R_1}(r) \bowtie \pi_{R_2}(r)$$

- A decomposition of  $R$  into  $R_1$  and  $R_2$  is lossless join if at least one of the following dependencies is in  $F^+$ :

- ❖  $R_1 \cap R_2 \rightarrow R_1$

- ❖  $R_1 \cap R_2 \rightarrow R_2$

$$\underline{X \rightarrow y}$$

If  $t_1.x = t_2.x$  then  $t_1.y = t_2.y$  must be same.



Q.1

$R(ABCDEFG)$   $\{AB \rightarrow CD, D \rightarrow E, E \rightarrow FG\}$

Decomposed into  $R_1(ABCD)$  and  $R_2(DEFG)$

By CHASE TEST.

$AB \rightarrow CD$

$D \rightarrow E$

$E \rightarrow FG$

$R_1(ABCD)$

$R_2(DEFG)$

	A	B	C	D	E	F	G
$R_1(ABCD)$	a	a	a	a	a	a	a
$R_2(DEFG)$				a	a	a	a

getting a Tuple with all a entries

Lossless Join

Q.2.

$R(ABCDEFGG) \{ \underline{AB} \rightarrow C, C \rightarrow \underline{D}, D \rightarrow \underline{EFG} \}$

Decomposed into  $R_1(ABCE)$  and  $R_2(DEFG)$

By CHASE TEST.

$\times AB \rightarrow C$

$\times C \rightarrow D$

$\times D \rightarrow EFG$

$R_1(ABCE)$

$R_2(DEFG)$

	A	B	C	D	E	F	G
$R_1(ABCE)$	a	a	a		a		
$R_2(DEFG)$				a	a	a	a

Not getting any one Tuple with all 'a' entries  
Lossy Join





$R(ABCDEFG) \{AB \rightarrow C, AC \rightarrow B, AD \rightarrow E, B \rightarrow D, BC \rightarrow A, E \rightarrow G\}$

Decomposed into  $R_1(ABC)$   $R_2(ACDE)$  and  $R_3(ADG)$

$AB \rightarrow C$   
 $\checkmark AC \rightarrow B$   
 $\checkmark AD \rightarrow E$   
 $\checkmark B \rightarrow D$   
 $BC \rightarrow A$   
 $E \rightarrow G$

$R_1(ABC)$

$R_2(ACDE)$

$R_3(ADG)$

	A	B	C	D	E	G
$R_1(ABC)$	a	a	a	a		
$R_2(ACDE)$	a	a	a	a	a	a
$R_3(ADG)$	a			a	a	a

getting a tuple with all 'a' entries.  
Losses



If

$t_1.x = t_2.x$  then  $t_1.y = t_2.y$  must be same.

$x \rightarrow y$

x	y
a	a
a	a

x	y
a	$b_1$
a	$b_1$

Q.1



$R(ABCDEF/G) \{AB \rightarrow C, AC \rightarrow B, AD \rightarrow E, B \rightarrow D, BC \rightarrow A, E \rightarrow CG\}$

1. Decomposed into  $R_1(AB)$   $R_2(BC)$   $R_3(ABDE)$  and  $R_4(EG)$

2. Decomposed into  $R_1(AB)$   $R_2(BC)$   $R_3(ABDE)$  and  $R_4(ECG)$

$\checkmark$   $AB \rightarrow C$   
 $AC \rightarrow B$   
 $AD \rightarrow E$   
 $\checkmark$   $B \rightarrow D$   
 $\checkmark$   $BC \rightarrow A$   
 $E \rightarrow CG$

	A	B	C	D	E	G
$R_1(AB)$	a	a	b <sub>1</sub>	a		
$R_2(BC)$	...	a	a	a		
$R_3(ABDE)$	a	a	b <sub>1</sub>	a	a	a
$R_4(EG)$			b <sub>1</sub>		a	a

Not getting all 'a' entries walaan N/A  
Lossy Join.

$\frac{E \rightarrow C}{E \rightarrow G}$





R(ABCDEFG) {AB  $\rightarrow$  C, AC  $\rightarrow$  B, AD  $\rightarrow$  E, B  $\rightarrow$  D, BC  $\rightarrow$  A, E  $\rightarrow$  CG}

1. Decomposed into  $R_1(AB)$   $R_2(BC)$   $R_3(ABDE)$  and  $R_4(EG)$
2. Decomposed into  $R_1(AB)$   $R_2(BC)$   $R_3(ABDE)$  and  $R_4(ECG)$

✓ AB  $\rightarrow$  C

AC  $\rightarrow$  B

AD  $\rightarrow$  E

✓ B  $\rightarrow$  D

BC  $\rightarrow$  A

E  $\rightarrow$  CG

E  $\rightarrow$  C  
E  $\rightarrow$  G

$R_1(AB)$

$R_2(BC)$

$R_3(ABDE)$

$R_4(EG)$

	A	B	C	D	E	G
$R_1(AB)$	<u>a</u>	<u>a</u>	<del>b</del>	a		
$R_2(BC)$		a	a	a		
$R_3(ABDE)$	<u>a</u>	<u>a</u>	<del>b</del> a	<u>a</u>	<u>a</u>	a
$R_4(EG)$			<del>a</del>		<u>a</u>	<u>a</u>

getting a tuple with all 'a' entries  
So lossless



Q.



Consider the relation  $R (P, Q, S, T, X, Y, Z, W)$  with the following functional dependencies.

$$PQ \rightarrow X; P \rightarrow YX; Q \rightarrow Y; Y \rightarrow ZW$$

Consider the decomposition of the relation  $R$  into the constituent relations according to the following two decomposition schemes.

$$D_1: R = [(P, Q, S, T); (P, T, X); (Q, Y); (Y, Z, W)]$$

$$D_2: R = [(P, Q, S); (T, X); (Q, Y); (Y, Z, W)]$$

Which one of the following options is correct?

[MCQ: 2021: 2M]

- A**  $D_1$  is a lossless decomposition, but  $D_2$  is a lossy decomposition.
- B**  $D_1$  is a lossy decomposition, but  $D_2$  is a lossless decomposition.
- C** Both  $D_1$  and  $D_2$  are lossless decomposition.
- D** Both  $D_1$  and  $D_2$  are lossy decomposition.

# Decomposition

```
graph TD; A[Decomposition] --> B[① Lossless Join]; A --> C[② Dependency Preserving]; B --> D[↳ ① Basic Concept]; B --> E[② Binary Method]; B --> F[③ CHASE TEST];
```

## ① Lossless Join

- ↳ ① Basic Concept
- ② Binary Method
- ③ CHASE TEST

## ② Dependency Preserving





## Dependency Preserving Decomposition:

Let  $R$  be the Relational Schema with FD Set  $F$  is Decomposed into Sub Relations  $R_1 R_2 R_3 \dots R_n$  with FD Set  $F_1 F_2 F_3 \dots F_n$  Respectively.

$$\text{If } F_1 \cup F_2 \cup F_3 \dots \dots \cup F_n \equiv F$$

Dependency Preserving Decomposition

$$\text{If } F_1 \cup F_2 \cup F_3 \dots \dots \cup F_n \subset F$$

Dependency Not Preserved.



# Dependency Preservation

- Let  $F_i$  be the set of dependencies  $F$  that include only attributes in  $R_i$ .
- ❖ A decomposition is dependency preserving,

$$\text{if } (F_1 \cup F_2 \cup \dots \cup F_n) = F$$

Dependency Preserved.



first take the closure of the Attributes then

Write ALL Non Trivial FD in the Respective

Sub Relation.

$X \cap Y = \phi$  &  $X \rightarrow Y$  Must Satisfy FD Defination



Let  $R(A, B, C, D, E)$  be a relational schema with the following function dependencies:

$A \rightarrow B, B \rightarrow C, C \rightarrow D$  and  $D \rightarrow BE$ .

✓ Dep. Preserved

$A \rightarrow B$   
 $B \rightarrow C$   
 $C \rightarrow D$   
 $D \rightarrow BE$  ✓

Decomposed into  $R_1(AB)$   $R_2(BC)$   $R_3(CD)$  and  $R_4(DE)$

$(A)^+ = (AB C D E)$   
 $(B)^+ = (B C D E)$   
 $(C)^+ = (C D B E)$   
 $(D)^+ = (D B E C)$   
 $(E)^+ = (E)$

$R_1(AB)$	$R_2(BC)$	$R_3(CD)$	$R_4(DE)$
$A \rightarrow B$	$B \rightarrow C$ $C \rightarrow B$	$C \rightarrow D$ $D \rightarrow C$	$D \rightarrow E$

$A \rightarrow B, B \rightarrow C, C \rightarrow B, C \rightarrow D, D \rightarrow C, D \rightarrow E$

$A \rightarrow B, B \rightarrow C, C \rightarrow D$

$D \rightarrow E$

$D \rightarrow C, C \rightarrow B$

$D \rightarrow B$





Consider a schema  $R(A, B, C, D)$  and functional dependencies

$A \rightarrow B$  and  $C \rightarrow D$ . Then the decomposition of  $R$  into  $R_1(AB)$  and  $R_2(CD)$  is  $R_1(AB) \cap R_2(CD)$

Lossy (not lossless)

$(A)^+ = (AB)^+$   
 $(B)^+ = (B)$   
 $(C)^+ = (CD)^+$   
 $(D)^+ = (D)$

[MCQ: 2M]

A

Dependency preserving and lossless join

B

Lossless join but not dependency preserving

C

Dependency preserving but not lossless join

D

Not dependency preserving and not lossless join

$R_1(AB)$	$R_2(CD)$
$A \rightarrow B$	$C \rightarrow D$

$(A \rightarrow B) \cup (C \rightarrow D)$

$A \rightarrow B, C \rightarrow D$

Dep. Preserved.

Ans (C)



Let  $R(A, B, C, D)$  be a relational schema with the following function dependencies:

$A \rightarrow B$ ,  $B \rightarrow C$ ,  $C \rightarrow D$  and  $D \rightarrow B$ .

The decomposition of  $R$  into  $(A, B)$ ,  $(B, C)$ ,  $(B, D)$

[MCQ: 2M]

- ☒ A Gives a lossless join, and is dependency preserving
- ☐ B Gives a lossless join, but is not dependency preserving
- ☒ C Does not give a lossless join, but is dependency preserving
- ☒ D Does not give a lossless join and is not dependency preserving



$R(ABCD) \quad \{A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow B\}$

$R_1(AB) \quad R_2(BC) \quad R_3(BD)$

Lossless Join ?

$$R_1(AB) \cap R_2(BC) = B$$

$(B)^+ = [\underline{BCD}]$  Super key of  $R_2$

$$R_1(AB) \cap R_3(BD) = B$$

$(B)^+ = [\underline{BD}C]$  Super key of  $R_3$

$R_{123}(ABCD)$  Lossless Join



$R(ABCD) \quad \{A \rightarrow B, B \rightarrow C, \underline{C \rightarrow D}, D \rightarrow B\}$

$R_1(AB)$

$R_2(BC)$

$R_3(BD)$

Dependency Preserving

$\{A\}^+ = \{A, B, C, D\}$

$\{B\}^+ = \{B, C, D\}$

$\{C\}^+ = \{C, D, B\}$

$\{D\}^+ = \{D, B, C\}$

$R_1(AB)$	$R_2(BC)$	$R_3(BD)$
$A \rightarrow B$	$B \rightarrow C$ $C \rightarrow B$	$B \rightarrow D$ $D \rightarrow B$

$A \rightarrow B, B \rightarrow C, \underline{C \rightarrow B}, B \rightarrow D, D \rightarrow B.$

$A \rightarrow B, B \rightarrow C, D \rightarrow B$

Dependency Preserving

$C \rightarrow D$



$R(ABCD)$

$\{ \underline{A \rightarrow B}, \underline{B \rightarrow C}, \underline{C \rightarrow D}, \underline{D \rightarrow B} \}$

Other Approach

$R_1(AB)$

$R_2(BC)$

$R_3(BD)$

Dependency Preserving

Via

$C \rightarrow D$

$C \rightarrow B$

&

$B \rightarrow D$

$[C]^+ = [CDB]$

$[B]^+ = [BCD]$

FD  $C \rightarrow D$ , indirectly  $C \rightarrow B$  Preserved in  $R_2$   
&  $B \rightarrow D$  Preserved in  $R_3$

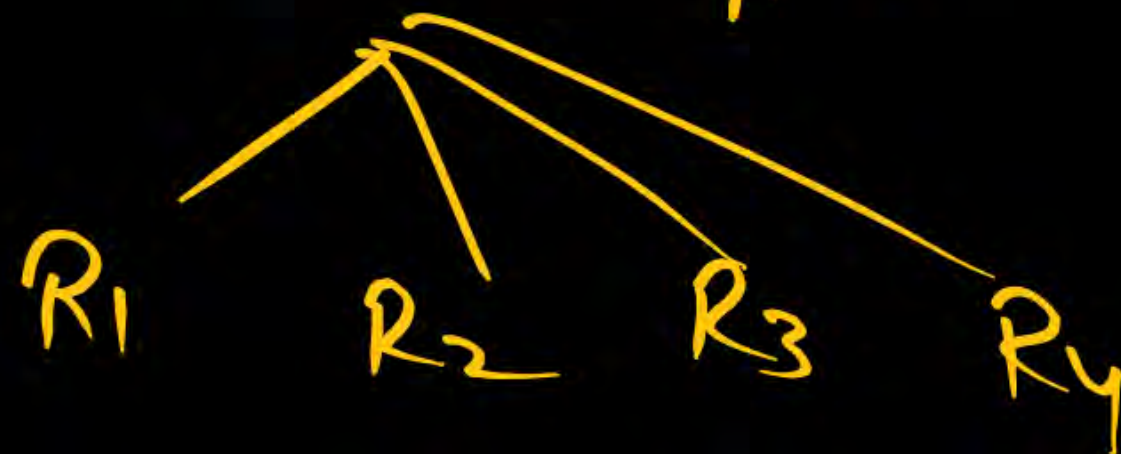
So  $C \rightarrow D$  Preserved.

Dep Preserved.

$R_1(AB)$	$R_2(BC)$	$R_3(BD)$
$A \rightarrow B$	$B \rightarrow C$	$D \rightarrow B$

$R( )$

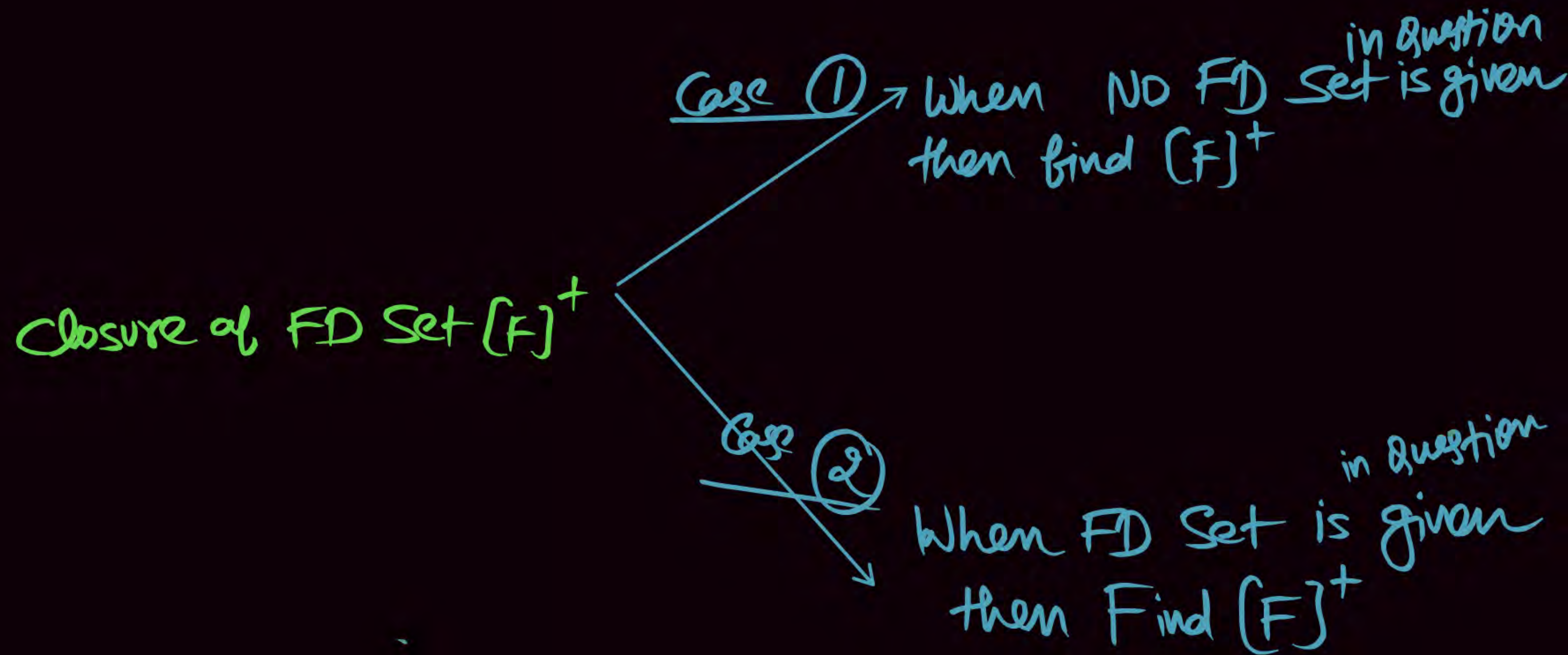
$A \rightarrow \textcircled{E}$





Attribute closure  $[X]^+$  : Set of ALL possible Attribute which is logically determined by attribute  $X$  is called Attribute closure of  $X$ .  $[X]^+$ .

Closure of FD Set  $[F]^+$  : Set of All possible FD's which is determined by given FD Set is called Closure of FD Set.





CASE I: When FD Set is Not given in Question  
then Find  $[F]^+$ ..

CASE I When No FD Set is given then Find  $[F]^+$

eg) R(AB) then Find  $[F]^+$

n: # of  
component

$\phi$   
A  
B  
AB

n=4

$$(n-1) \times n + 1$$

$$3 \times 4 + 1 \quad [F]^+ = 13 \quad \underline{\text{Ans}}$$
$$= \underline{13}$$

$\phi \rightarrow \phi$   
 ~~$\phi \rightarrow A$~~   
 ~~$\phi \rightarrow B$~~   
 $\phi \rightarrow AB$

$A \rightarrow \phi$

$A \rightarrow A$

$A \rightarrow B$

$A \rightarrow AB$

$B \rightarrow \phi$

$B \rightarrow A$

$B \rightarrow B$

$B \rightarrow AB$

$AB \rightarrow \phi$

$AB \rightarrow A$

$AB \rightarrow B$

$AB \rightarrow AB$

$$[F]^+ = \underline{13}$$



## Closure of FD Set $[F]^+$

Set of all possible FD's which can be derived from given FD set is called closure of FD set.  $[F]^+$

$[F]^+$  Closure of FD

R(AB)

$\phi \rightarrow \phi$

$\phi$	$A \rightarrow \phi$	$B \rightarrow \phi$	$AB \rightarrow \phi$
A	$A \rightarrow A$	$B \rightarrow A$	$AB \rightarrow A$
B	$A \rightarrow B$	$B \rightarrow B$	$AB \rightarrow B$
AB	$A \rightarrow AB$	$B \rightarrow AB$	$AB \rightarrow AB$

$$\underline{[F]^+ = 13}$$

Ans

$R(ABC)$  then Find  $(F)^+$  ?

$\phi$   
A  
B  
C  
AB  
BC  $\equiv CB$   
AC  
ABC

$$(n-1) \times n + 1$$

$$\Rightarrow (8-1) \times 8 + 1$$

$$\Rightarrow 7 \times 8 + 1$$

$$= \underline{\underline{57 \text{ Ans}}}$$



**R(ABC)**

$\phi \rightarrow \phi$

$56 + 1 = 57$

$\phi$	$A \rightarrow \phi$
A	$A \rightarrow A$
B	$A \rightarrow B$
C	$A \rightarrow C$
AB	$A \rightarrow AB$
BC	$A \rightarrow BC$
AC	$A \rightarrow AC$
ABC	$A \rightarrow ABC$
<hr/>	
8	

$B \rightarrow \phi$	$C \rightarrow \phi$
$B \rightarrow A$	$C \rightarrow A$
$B \rightarrow B$	$C \rightarrow B$
$B \rightarrow C$	$C \rightarrow C$
$B \rightarrow AB$	$C \rightarrow AB$
$B \rightarrow AC$	$C \rightarrow AC$
$B \rightarrow BC$	$C \rightarrow BC$
$B \rightarrow ABC$	$C \rightarrow ABC$
<hr/>	
8	

$AB \rightarrow \phi$	$BC \rightarrow \phi$	$AC \rightarrow \phi$
$AB \rightarrow A$	$BC \rightarrow A$	$AC \rightarrow A$
$AB \rightarrow B$	$BC \rightarrow B$	$AC \rightarrow B$
$AB \rightarrow C$	$BC \rightarrow C$	$AC \rightarrow C$
$AB \rightarrow AB$	$BC \rightarrow AB$	$AC \rightarrow AB$
$AB \rightarrow BC$	$BC \rightarrow BC$	$AC \rightarrow BC$
$AB \rightarrow AC$	$BC \rightarrow AC$	$AC \rightarrow AC$
$AB \rightarrow ABC$	$BC \rightarrow ABC$	$AC \rightarrow ABC$
<hr/>		
8		

$ABC \rightarrow \phi$
$ABC \rightarrow A$
$ABC \rightarrow B$
$ABC \rightarrow C$
$ABC \rightarrow \underline{AB}$
$ABC \rightarrow BC$
$ABC \rightarrow AC$
$ABC \rightarrow ABC$
<hr/>
8

Case II: When FD Set is given in the Question  
then Find  $[F]^+$ .



R(AB)    [A → B]

then find  $(F)^+$ ?  
 $2^n$  (n: #attribute in closure)

0 Attribute

$\phi \rightarrow \phi$

→ ①

1 Attribute

$$[A]^+ = [AB] = 2^2$$

$$[B]^+ = [B] = 2^1$$

2 Attribute

$$[AB]^+ = [AB] = 2^2$$

④  $\left[ \begin{array}{l} A \rightarrow \phi, A \rightarrow A, \\ A \rightarrow B, A \rightarrow AB \end{array} \right]$

②  $\left[ B \rightarrow \phi, B \rightarrow B \right]$

④  $\left[ \begin{array}{l} AB \rightarrow \phi, AB \rightarrow A \\ AB \rightarrow B, AB \rightarrow AB \end{array} \right]$

$(F)^+ = 11$  Ans

11 Ans

$\phi$   
A  
B  
AB



$R(ABC)$   $[A \rightarrow B, B \rightarrow C]$  then  $\text{bind}(F)^+ = ?$

$\phi$   
A  
B  
C  
AB  
BC  
AC  
ABC

0 Attribute  $\Rightarrow \phi \rightarrow \phi$

1 Attribute:  $(A)^+ = (ABC) \Rightarrow 2^3$

$(B)^+ = (BC) = 2^2$

$(C)^+ = (C) = 2^1$

2 Attribute  $(AB)^+ = (ABC) = 2^3$

$(BC)^+ = (BC) = 2^2$

$(AC)^+ = (ABC) = 2^3$

3 Attribute  $(ABC)^+ = (ABC) = 2^3$

$(F)^+ = 43$

Ans

$(F)^+$

$= L$

$= 8$

$= 4$

$= 2$

$= 8$

$= 4$

$= 8$

$= 8$

43

$[A \rightarrow \phi, A \rightarrow A, A \rightarrow B, A \rightarrow C, A \rightarrow AB, A \rightarrow AC, A \rightarrow ABC]$

$[B \rightarrow \phi, B \rightarrow B, B \rightarrow C, B \rightarrow BC]$

$[C \rightarrow \phi, C \rightarrow C]$

$[AB \rightarrow \phi, AB \rightarrow A, AB \rightarrow B, AB \rightarrow C, AB \rightarrow AB, AB \rightarrow BC, AB \rightarrow AC, AB \rightarrow ABC]$

$[BC \rightarrow \phi, BC \rightarrow B, BC \rightarrow C, BC \rightarrow BC]$

$[AC \rightarrow \phi, AC \rightarrow A, AC \rightarrow B, AC \rightarrow C, AC \rightarrow AB, AC \rightarrow AC, AC \rightarrow BC, AC \rightarrow ABC]$

$[ABC \rightarrow \phi, ABC \rightarrow A, ABC \rightarrow B, ABC \rightarrow C, ABC \rightarrow AB, ABC \rightarrow BC, ABC \rightarrow AC, ABC \rightarrow ABC]$



**R(ABC)**  $[A \rightarrow B, B \rightarrow C]$

$[F]^+ = 43$  Ans.

Ans

$\phi$       0 attribute =  $\phi \rightarrow \phi$

A      1Attribute =  $[A]^+ = [ABC] = 2^3$

B       $[B]^+ = [BC] = 2^2$

C       $[C]^+ = [C] = 2^1$

AB      2Attribute =  $[AB]^+ = [ABC] = 2^3$

BC       $[BC]^+ = [BC] = 2^2$

AC       $[AC]^+ = [ABC] = 2^3$

ABC      3 Attribute =  $[ABC]^+ = [ABC] = 2^3$

$$[A]^+ = \begin{bmatrix} A \rightarrow \phi, A \rightarrow A, A \rightarrow B, A \rightarrow C \\ A \rightarrow AB, A \rightarrow BC, A \rightarrow AC, A \rightarrow ABC \end{bmatrix}$$

$$[B]^+ = [B \rightarrow \phi, B \rightarrow B, B \rightarrow C, B \rightarrow BC]$$

$$[C]^+ = [C \rightarrow \phi, C \rightarrow C]$$

$$[AB]^+ = \begin{bmatrix} AB \rightarrow \phi, AB \rightarrow A, AB \rightarrow B, AB \rightarrow C \\ AB \rightarrow AB, AB \rightarrow BC, AB \rightarrow AC, AB \rightarrow ABC \end{bmatrix}$$

$$[BC]^+ = [BC \rightarrow \phi, BC \rightarrow B, BC \rightarrow C, BC \rightarrow BC]$$

$$[AC]^+ = \begin{bmatrix} AC \rightarrow \phi, AC \rightarrow A, AC \rightarrow B, AC \rightarrow C \\ AC \rightarrow AB, AC \rightarrow BC, AC \rightarrow AC, AC \rightarrow ABC \end{bmatrix}$$

$$[ABC]^+ = \begin{bmatrix} ABC \rightarrow \phi, ABC \rightarrow A, ABC \rightarrow B, ABC \rightarrow C \\ ABC \rightarrow AB, ABC \rightarrow BC, ABC \rightarrow AC, ABC \rightarrow ABC \end{bmatrix}$$



**R(AB)**  $[A \rightarrow B]$

$\phi$       0 attribute = 1

A      1 Attribute =  $[A]^+ [AB] = 2^2$

B       $[B]^+ = [B] = 2^1$

AB      2 Attribute =  $[AB]^+ = [AB] = 2^2$

1	
4	$(A \rightarrow \phi, A \rightarrow A, A \rightarrow B, A \rightarrow AB)$
2	$(B \rightarrow \phi, B \rightarrow B)$
4	$\begin{pmatrix} AB \rightarrow \phi, AB \rightarrow A \\ AB \rightarrow B, AB \rightarrow AB \end{pmatrix}$

**11 Ans.**

Any Doubt ?





**THANK  
YOU!**

