A PROMPTS

When constructing contrastive learning training data, we use GPT's classification to obtain L_{pos} and L_{neg}. For each entity in the top-T of L_0, determine whether its attributes are consistent with S^{pos} (S^{neg}). If it is consistent, GPT should output 1; otherwise, GPT should output 0. Next, these entities that GPT deems consistent with the attributes of S^{pos} (S^{neg}) will be merged with S^{pos} (S^{neg}) to form L_{pos} (L_{neg}). The prompt to classify entity is shown in Table 13.

In GenExpan, each round uses three example entities to construct $Prompt_g$, which is used to generate entities that are semantically similar to them. $Prompt_g$ is as shown in Table 14.

In the process of enhancing GenExpan with Chain of Thought prompting, we employ LLM to generate fine-grained class names. The prompt, $Prompt_c$, is shown in Table 15.

B IMPLEMENTATION DETAILS OF RETEXPAN

In RetExpan, sentences are tokenized using the WordPiece tokenizer and then fed into a 12-layer Transformer initialized with $BERT_{BASE}$ weights. To optimize training efficiency and preserve semantic knowledge learned by BERT, we freeze the first 11 layers of the encode, thus only the last layer is fine-tuned. When tokenizing, to ensure that mentions of entities in long sentences are not truncated, we have implemented entity focus, guaranteeing the presence of entities within the sentence. During expansion, we use one-shot expansion to directly obtain the preliminary expansion results L_0. In RetExpan with contrastive learning strategy, each epoch during training alternates between computing and optimizing entity prediction loss and contrastive learning loss.

To ensure that the encoder acquires knowledge from the corpus, we trained it for 20 epochs on 8 RTX 3090 GPUs. The hyperparameters for training learning rate, batch size, weight decay, label smoothing factor η were set to 4e-5, 128, 1e-2, and 0.075 respectively.

C IMPLEMENTATION DETAILS OF GENEXPAN

In GenExpan, we use LLaMA-7b as the base model. Initially, we train for 1 epoch on the corpus using 6 A100 GPUs. The training hyperparameters learning rate, batch size, gradient accumulation steps, weight decay, gradient clipping are set to 1e-5, 4, 8, 1e-4, and 1.0 respectively.

During entity generation in GenExpan, we utilize prefix-constrained beam search with a beam size of 40 to generate 40 entities at a round. For entity selection, we compute the positive similarity score for each entity and select those whose scores are in the top 0.7 as the results for the current round. When no new entity is generated for 20 consecutive rounds, the generation process will end and move to re-ranking.

D DETAILS OF ULTRAWIKI

UltraWiki contains 10 fine-grained semantic classes, which fall under 5 coarse-grained semantic categories: Organization, Location, Product, Person, and Miscellaneous. The number of entities in each fine-grained semantic class ranges from 45 to 952. Each fine-grained semantic class has 2 to 3 attributes, and depending on the combination of attributes, several ultra-fine-grained semantic classes can be derived from a single fine-grained class. Detailed data is displayed in Table 11.

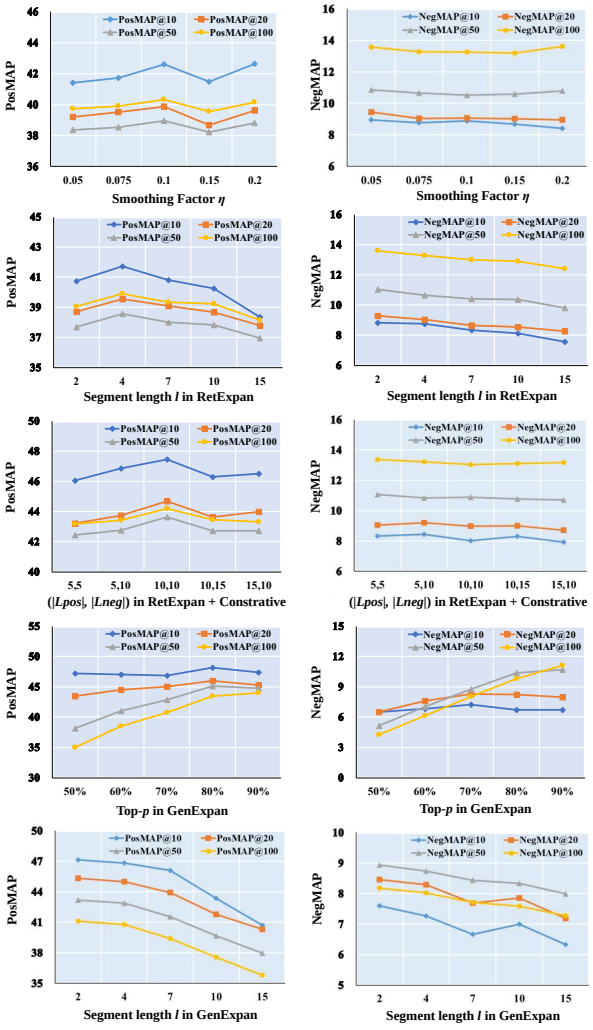

Figure 7: Parameter analysis experiments.

The number of combinations from positive and negative attributes varies significantly, leading to substantial differences in the number of ultra-fine-grained semantic classes. The count of UltraWiki's positive and negative attributes and their corresponding ultra-fine-grained classes are presented in Table 12.

E PARAMETER ANALYSIS

To explore the sensitivity of each key hyperparameter in RetExpan and GenExpan, we conducted a comprehensive analysis of the smoothing factor η and the re-ranking segment length l in RetExpan, as well as the number of positive and negative entities mined in the contrastive learning strategy $|L_{pos}|$ and $|L_{neg}|$, the Top-p of entity selection module in GenExpan, and the re-ranking segment length l, respectively. The results are depicted in Figure 7, from which we can observe that:

Table 11: Fine-grained semantic classes detail. CLS.: Semantic Class

Coarse CLS.	Fine-grained CLS.	#Entities	#Ultra-fine-grained CLS.	Attributes
Organization	Canada universities	99	10	<Loc-Province>, <Type>
Location	China cities	675	50	<Province>, <Prefecture>
	Countries	190	68	<Continent>, <Driving-Side>, <Per-Capita-Income>
	US airports	370	74	<Role>, <Loc-State>
	US national monuments	112	12	<Loc-State> <Agency>
Product	Mobile phone brands	159	7	<Loc-Continent>, <Status>
	Percussion instruments	128	10	<Type>, <Source-Continent>
Person	Nobel laureates	952	11	<Prize>, <Gender>
	US presidents	45	5	<Party>, <Birth-State>
Miscellaneous	Chemical elements	118	14	<Period>, <Phase-at-R.T.>

Table 12: Types of ultra-fine-grained semantic classes. CLS.: Semantic Class

$\lvert\mathcal{A}^{pos}\rvert$	$\lvert\mathcal{A}^{neg}\rvert$	#Ultra-fine-grained CLS.
1	1	238
1	2	5
2	1	9
2	2	7
3	3	2

(1) The label smoothing η serves to mitigate the penalty for entities possessing similar semantics to ground-truth entities. In Ultra-ESE, there are fewer entities exhibiting similarity to ground-truth entities at the ultra-fine-grained semantic level, thereby diminishing the utility of label smoothing. Consequently, the fluctuation in model performance due to parameter variations is relatively not significant.

(2) Excessive segment length l in both RetExpan and GenExpan equates to degrading the segmented re-ranking strategy to a naive re-ranking approach, thereby introducing noise from irrelevant entities, as mentioned in the main text. Hence, there is a general decrease in both PosMAP@K as the segment length increases, with larger K values leading to greater declines.

(3) Regarding the ultra-fine-grained contrastive learning strategy in RetExpan, we observe that mining too many or too few positive and negative entities using GPT-4 results in performance degradation. Insufficient positive and negative entities fail to fully stimulate the potential of contrast learning, whereas an excess of such entities introduces noisy entities. Therefore, as the number of entities to be mined increases gradually, PosMAP initially rises and then falls, and NegMAP exhibits a slight initial decline followed by a rise. However, overall, these two parameters demonstrate robustness, with even the worst-performing set of values outperforming the original RetExpan.

(4) A trade-off is also necessary for the Top-p. A too small Top-p may fail to ensure the diversity of newly generated entities, while a too large Top-p may introduce an excessive number of irrelevant entities during iterative expansion. Consequently, we observe a decrease in PosMAP and a notable increase in NegMAP when Top-p is increased from 80% to 90%, which indicates that there is considerable space for improving the current rejection strategy for negatively targeted entities.

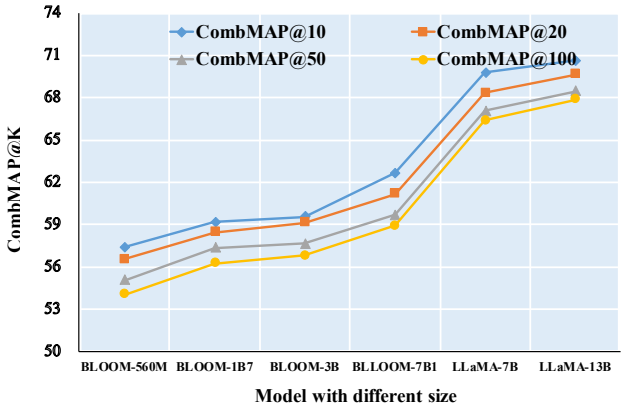

Figure 8: Comparison experiments on different LLM families and sizes.

F ANALYSIS OF MODEL SIZE

We utilize various families and sizes of LLMs as backbone model of GenExpan, including 560M, 1B7, 3B, 7B1 for BLOOM, as well as 7B and 13B for LLaMA. The experiment results depicted in Figure 8 align well with the expectation. Both the BLOOM and LLaMA families satisfy the scaling law: larger models tend to be more effective in Ultra-ESE, yielding better results. Moreover, LLaMA-7B outperforms BLOOM-7B1 at the same scale.

G CASE STUDY

Figure 9 presents some case studies of GenExpan and the corresponding retrieval augmentation, chain-of-thought reasoning techniques. Overall, it is evident that GenExpan predominantly avoids

China Cities				Countries			
GenExpan		GenExpan + RA		GenExpan		GenExpan + CoT	
1	Changge +++	1	Xinmi +++	1	Saint Lucia +++	1	Saint Lucia +++
2	Linqing !!!	2	Gongyi +++	2	Grenada +++	2	Seychelles !!!
3	Gongyi +++	3	Yongcheng +++	3	Saint Kitts and Nevis !!!	3	São Tomé and Príncipe +++
	.....		.....		.....		.....
15	Linyi ---	15	Xinzheng +++	31	Cape Verde +++	31	Sierra Leone +++
16	Tongchuan ---	16	Xinxiang ---	32	Seychelles !!!	32	Guinea-Bissau +++
17	Linxia !!!	17	Xingyang +++	33	Barbados !!!	33	Liberia +++
18	Hanzhong ---	18	Changge +++	34	Trinidad and Tobago !!!	34	Comoros +++
19	Xingyang +++	19	Dengfeng +++	35	Cape Verde +++	35	Mauritius +++
	.....		.....		.....		.....

Positive Seeds	Negative Seeds	Positive Seeds	Negative Seeds
Xiangcheng	Shuozhou	Saint Vincent and the Grenadines	Paraguay
Linzhou	Zhangye	Guinea	Colombia
Yanshi	Lanzho	Libya	Bolivia
Weihui	Pu'er		
Mengzhou			
Positive Attributes		**Positive Attributes**	
<Province>	Henan	<Per_Capita_Income>	Low
Negative Attributes		**Negative Attributes**	
<Prefecture>	Perfecture-level city	<Continent>	South America

Figure 9: Case studies of GenExpan and the retrieval augmentation, chain-of-thought reasoning techniques. +++ and - - - stand for positive and negative target entities, respectively. !!! represents irrelevant entities belonging to the same fine-grained semantic class as the seed entities.

expanding entities that do not belong to the same semantic class as the positive and negative seed entities. This emphasizes the relative tractability of traditional ESE tasks compared to the significant challenges posed by Ultra-ESE for existing LLMs, where the model cannot exclude the expansion of negative target entities and irrelevant entities (belonging to the same fine-grained semantic class).

For retrieval augmentation, more positive target entities are introduced after fetching the additional knowledge. However, for some negative target entities that fulfill positive attributes, the retrieved knowledge may contain the introduction about its positive attributes, conversely misleading the model to overlook its negative attributes. For example, for the negative target entity "Xinxiang" in the second column, it also belongs to Henan province, i.e., it satisfies the requirement of positive attributes. Therefore, after concatenating the retrieved entity introduction "Xinxiang is a prefecture-level city *in northern Henan province*, China.", it is incorrectly introduced instead.

For chain-of-thought reasoning, an interesting example is shown in Figure 9. We find that the ground-truth positive target semantics is "low-income countries", but the model erroneously infers the positive semantic class as "African countries", which encompasses relatively more low-income countries, and thus improves the recall of the positive target entities. Of course, some high-income African countries such as "Seychelles" are also incorrectly introduced. In fact, this error could have been avoided since the provided positive seed entity contains the non-African country "Saint Vincent and the Grenadines". This also shows the potential for improvement in the chain-of-thought reasoning strategy.

Table 13: The prompt used to select the entities that are consistent with the attributes of S^{pos} (S^{neg}) in the top-T entities of L_0 to construct L_{pos} (L_{neg}).

I have a task that involves classifying candidate entities based on their alignment with a seed entity set. The seed entities are grouped together because they share certain attributes, referred to as seed attributes. I will provide a list of seed entities along with their seed attributes. Additionally, I have a list of candidate entities that are similar to the seed entities but may not necessarily share the same seed attributes. I need you to identify the seed attributes and use them to classify each candidate entity into one of two categories: 1) consistent with the seed entity set in terms of seed attributes, or 0) inconsistent with the seed entity set in terms of seed attributes. For the given N candidate entities, please output N values, each being 1 or 0, indicating whether each candidate is consistent (1) or inconsistent (0) with the seed entity set based on the seed attributes.

Input:
Seed entities: [Mark Twain, Ernest Hemingway, F. Scott Fitzgerald]
Candidate entities: [J.K. Rowling, Stephen King, Agatha Christie, John Steinbeck, Harper Lee, Charles Dickens, Virginia Woolf], total 7 entities
Output:
"result": [0,1,0,1,1,0,0]

Input:
Seed entities: [Golden Retriever, German Shepherd, Labrador Retriever]
Candidate entities: [Bengal Tiger, Beagle, Siberian Husky, African Elephant, Pug], total 5 entities
Output:
"result": [0,1,1,0,1]

Input:
Seed entities: [{Entity1}, {Entity2}, {Entity3}]
Candidate entities: [{Entity1'}, {Entity2'}, {Entity3'}, ...], total {} entities
Output:

Table 14: The prompt used to generate entities that are semantically similar to 3 given entities.

iron, copper, aluminum and zinc.
math, physics, chemistry and biology.
{Entity1}, {Entity2}, {Entity3} and _____

Table 15: The prompt used to generate a class name that covers the given entities.

Generate a class name that accurately represents the following entities. This class name should encompass all the given entities and reflect their shared characteristics.
Examples:
[Tiger, Lion, Cheetah] → Big Cats
[Shakespeare, Tolstoy, Hemingway] → Famous Authors
[Mercury, Venus, Mars] → Planets in the Solar System
[{Entity1}, {Entity2}, {Entity3}] → _____