

HW1

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Problem 1

1

Preimage resistant: Given the output y of n bits, it will take $O(2^n)$ time to find the preimages x such that $y = h(x)$.

Collision resistant: Given an output size of n bits, it will take $O(2^{\frac{n}{2}})$ time to find two distinct values x and x' such that $h(x) = h(x')$.

Second preimage resistant: Given an output of n bits and a message x , it will take $O(2^n)$ time to find another message x' such that $h(x) = h(x')$.

2

False, the hash value of the message is encrypted with a user's private key.

3

RSA and Elliptic Curve can be used for digital signature.

4

For any point G on the elliptic curve, a new point $Q = kG$ for a scalar k forms a cyclic subgroup. Given G and Q , it is computationally infeasible to find k . Suppose $k = 2^n$, it will take $O(2^n)$ time to find k .

Problem 2

Given $n = 1.2\sqrt{N}$.

$$\begin{aligned} Pr[r_i = r_j | i \neq j] &= 1 - \frac{N-1}{N} \frac{N-2}{N} \dots \frac{N-n+1}{N} = 1 - \prod_{i=1}^{n-1} \left(1 - \frac{i}{N}\right) \\ &\geq 1 - \prod_{i=1}^{n-1} e^{-\frac{i}{N}} = 1 - e^{-\frac{1}{N} \sum_{i=1}^{n-1} i} \geq 1 - e^{-\frac{n^2}{2N}} \end{aligned} \quad (1)$$

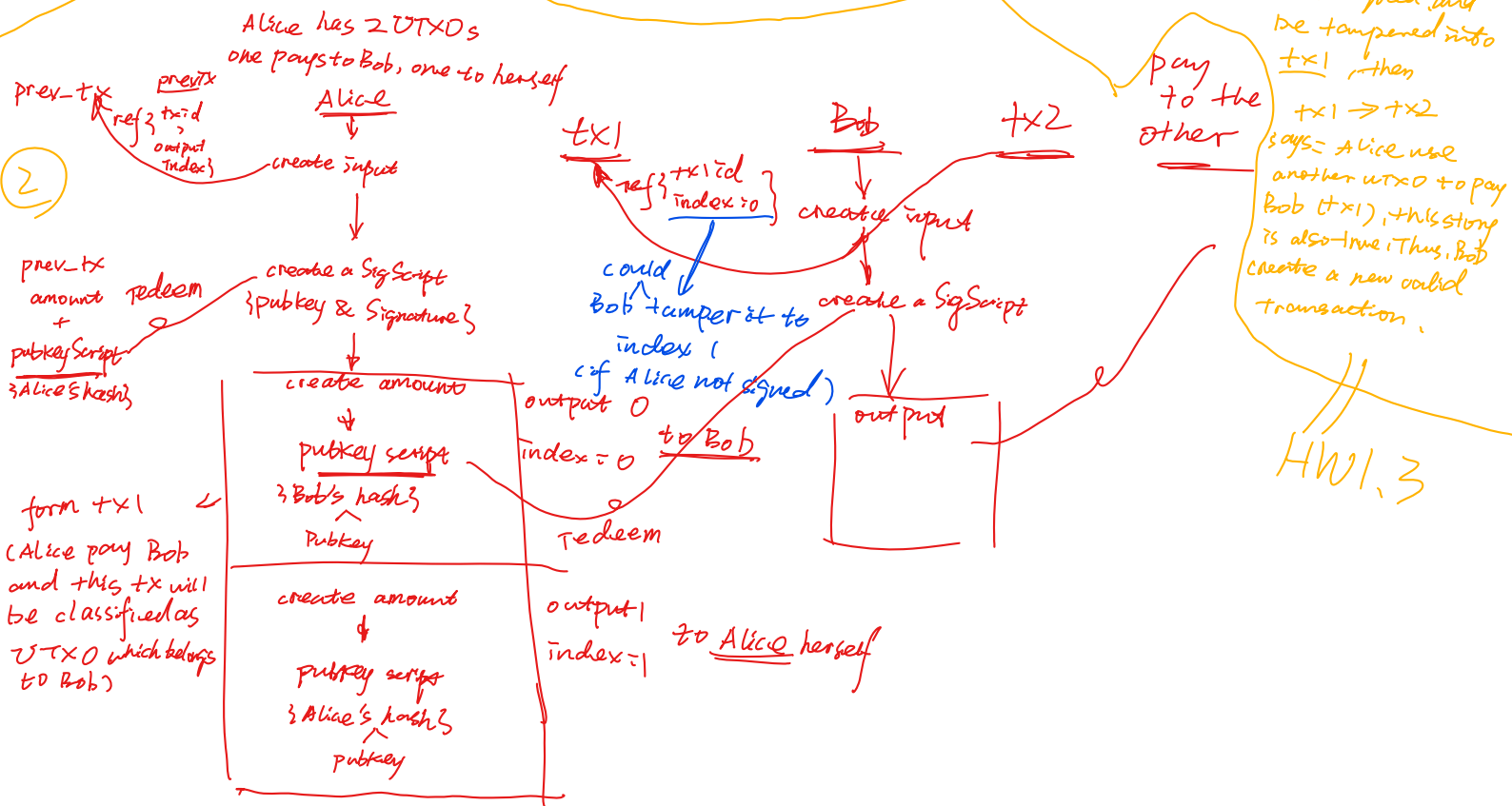
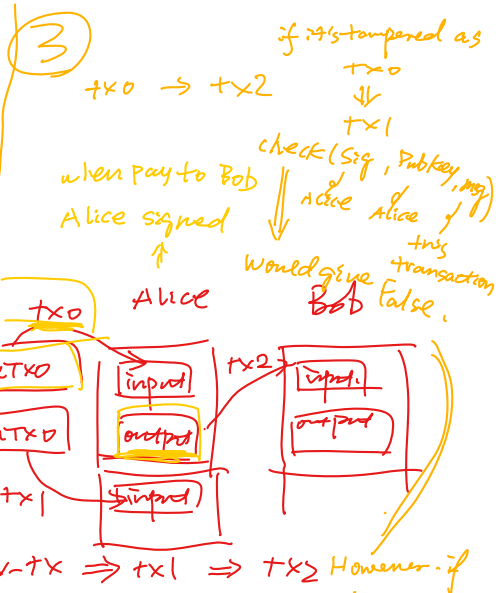
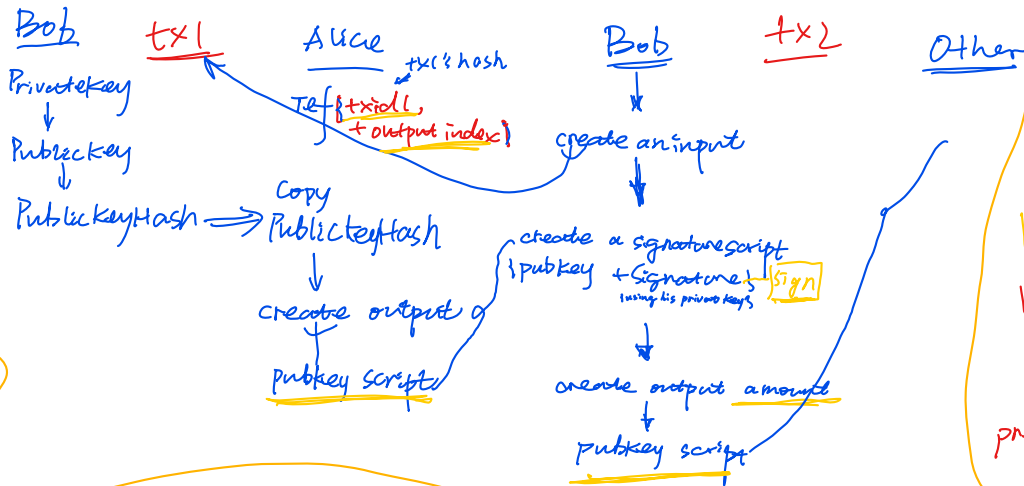
$$n = 1.2\sqrt{N} \Rightarrow \frac{n^2}{2N} = 0.72 \Rightarrow (1) \geq 1 - e^{-0.72} = 0.53 \geq \frac{1}{2} \quad (2)$$

Problem 3

1

General TX Model

Alice \rightarrow Bob \rightarrow Other
tx1 tx2



HW1.3