# Electronic Functional Materials and Devices

# 电子功能材料与元器件

#### **QQ** Group:



陈晓龙 Chen, Xiaolong 电子与电气工程系

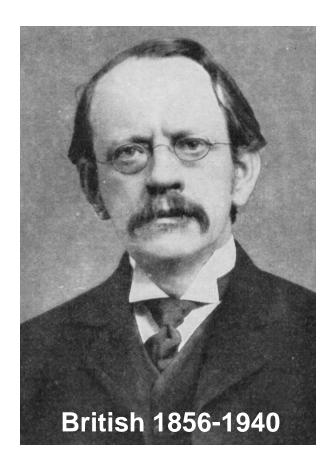
#### 1.1 Structure of atoms



1803: J. Dalton's model



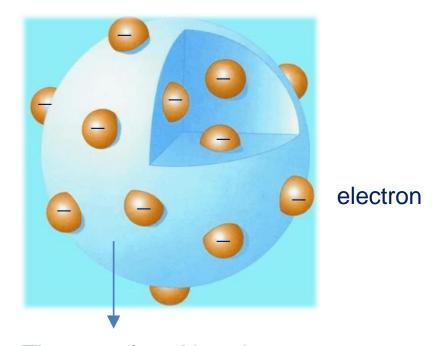
- Solid ball
- Atom is the smallest and indivisible particle



In 1897, J.J. Thomson discovered the electron.

(The experiment costs 7 years)

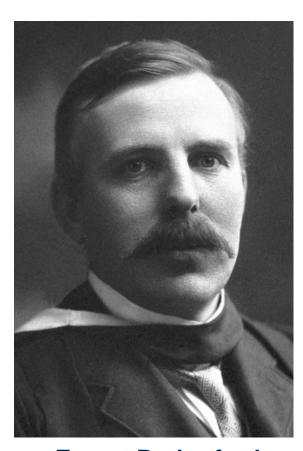
#### 1904 J.J. Thomson's model



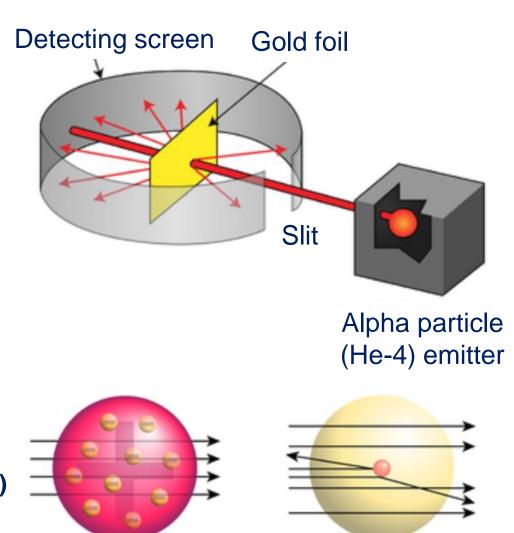
The sea of positive charge

Plum pudding model

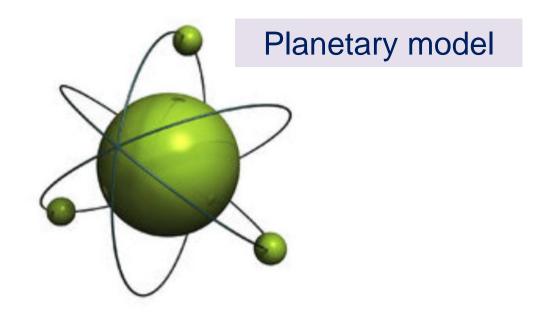
#### 1911: Ernest Rutherford's experimental



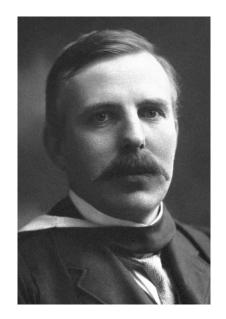
Ernest Rutherford (British, 1871.08.30-1937.10.19)



#### 1911: Ernest Rutherford's model



Nucleus is much heavier than electrons



Ernest Rutherford (1871.08.30-1937.10.19)

- ◆ Born in New Zealand in 1871.08.30
- He has 11 brothers and sisters
- 1890-1893 Bachelor degree, University of New Zealand
- ◆ 1894 Master degree, University of New Zealand
- ◆ 1895 Went to JJ Thomson's lab to purse PhD degree, Trinity College, University of Cambridge,
- 1898 Professor, McGill University

Research assistant Frederick Soddy and postdoc Otto Hahn proposed the radioactive half-life, and proved the transmutation from one element to another one.

Frederick and Otto obtained Nobel Chemistry Prize in 1921 and 1944, respectively.

 1907 Langworthy Professor, University of Manchester ◆ 1908 Nobel Chemistry Prize for the study of transmutation of elements and radioactive substances

Student George de Hevesy from Hungary did the first radioactive tracer test放射性示踪剂 in 1910. He obtained the Nobel Chemistry Prize in 1943.

- ◆ 1911 Rutherford proposed the planetary model of atom
- ◆ 1913 Niels Bohr from Denmark joined Rutherford's group as a postdoc Postdoc Bohr obtained the Nobel Physics Prize in 1922.
- ◆ 1919 Cavendish Professor, Physics Department, University of Cambridge
- ◆ 1920 Rutherford predicted that there were charge-neutral particle inside atom. Chadwick experimentally proved the existence of neutron experimentally in 1932. Chadwick obtained Nobel Physics Prize in 1935.

Assistant Charles Wilson invented the Cloud Chamber 云雾室 which could track the trajectory of particles and allowed discovery of new particles. He obtained the Nobel Physics Prize in 1927.

In 1924, Student Patrick Blackett improved the Cloud Chamber. He discovered that nucleus will absorb alpha-particle before the fission process. He obtained the Nobel Chemistry Prize in 1948.

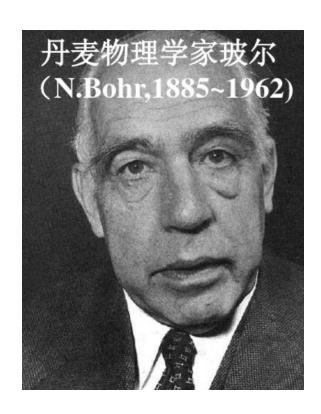
In 1932, Student John Cockcroft and Ernest Walton used the high energy accelerator to achieve the nucleus transformation. They shared the Nobel Chemistry Prize in 1951.

Student Pyotr Kapitsa discovered the superfluid behavior of liquid helium. He obtained the Nobel Physics Prize in 1978.

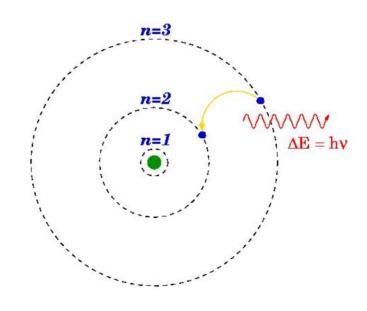




◆ 1977.08 International Union of Pure and Applied Chemistry (IUPAC) announced the No.104 element was called Rf (Rutherfordium) 护 in memory of Rutherford

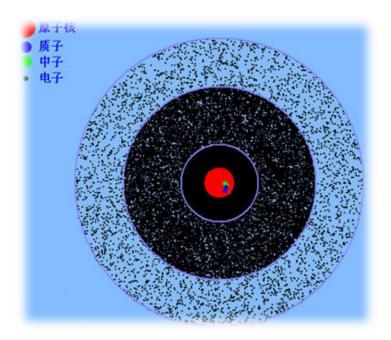


#### 1913: Bohr's model



**Quantized** model

# 1926: Schrodinger's model

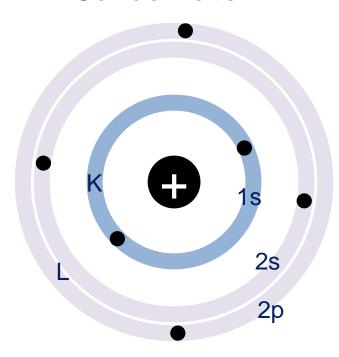


Electron cloud model

Electrons: Probability wave 几率波

#### **Bohr's model**

#### **Carbon atom**



: Nucleus原子核



#### The orbit of electrons

Principle quantum number 主量子数: n

n: 1, 2, 3, 4 ...

The shell is named as K, L, M, N, ...

Every shell has subshells: s, p, d, f...

Orbital quantum number 轨道量子数: ℓ

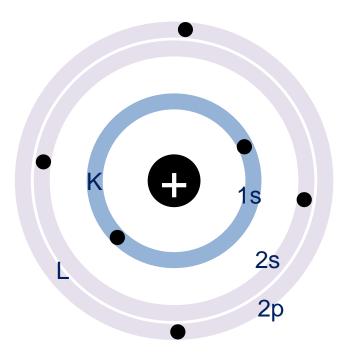
*ℓ*=0, 1, 2, ..., n-1

Nucleus: Proton (质子) and Neutron (中子)

#### The maximum electron numbers in shell and subshell

		Subshell			
		<i>ℓ</i> =0	1	2	3
n	Shell	S	p	d	f
1	K	2			
2	L	2	6		
3	M	2	6	10	
4	N	2	6	10	14

#### Carbon atom



: Nucleus原子核

The electronic construction of carbon atom 碳原子电子构型:

 $1s^22s^22p^2$ 

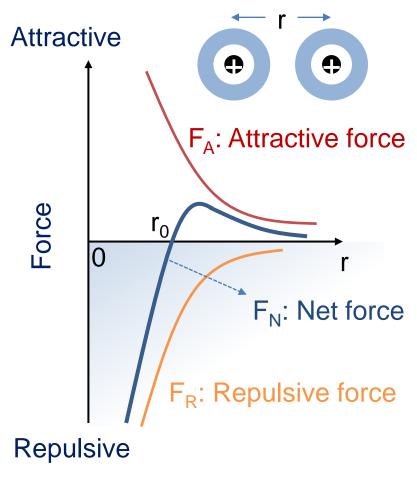
Electrons in the outermost shell: the valence electron 价电子

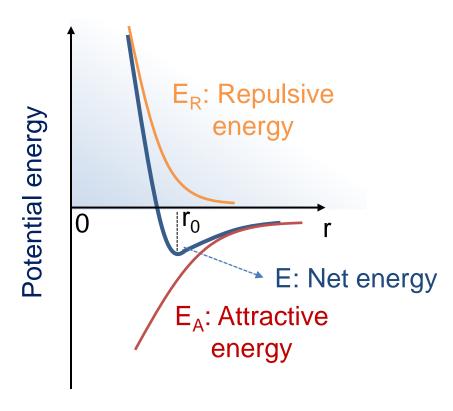
For carbon atom:

4 valence electron in L shell

The most stable atom: the outmost shell is fully filled

#### 1.2 Atomic bond

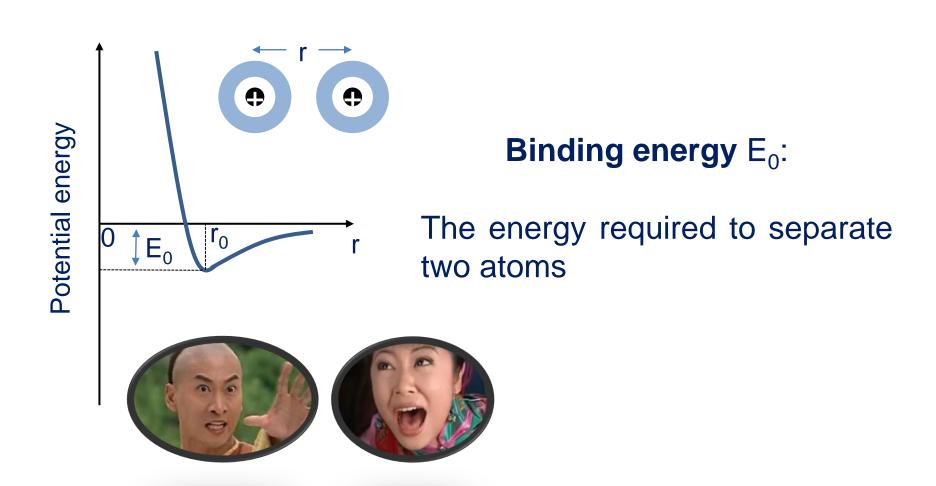




$$F_N = F_A + F_R$$

$$F_{\rm N} = \frac{{
m d}E}{{
m d}r}$$

# Bond/Binding energy 键能



# The types of atomic bond

Covalent bond

Metallic bond

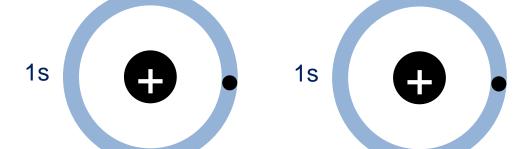
Ionic bond

Secondary bond: van der Waals bond

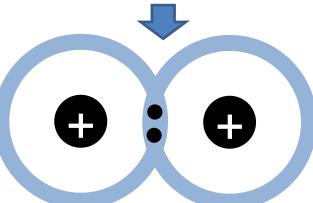
Hybrid bond 混合键

#### **Covalent bond**

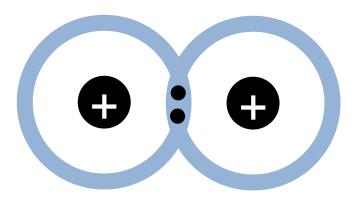
Hydrogen atom



Atoms share the valence electrons and make subshell fully filled

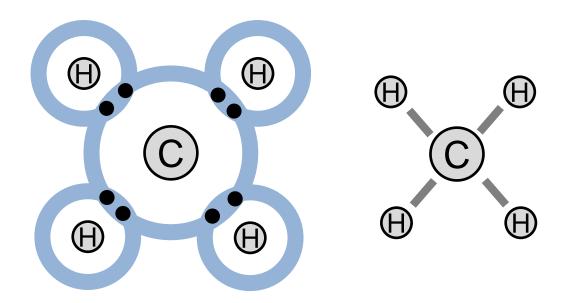


#### **Covalent bond**

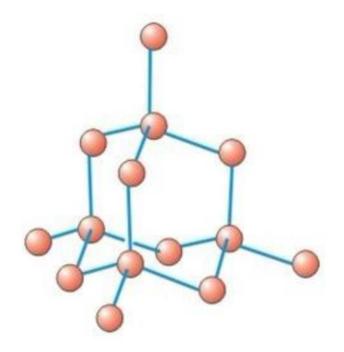


Q1: Which region has the highest electron cloud density?

#### Distribution of valence electrons in methane CH<sub>4</sub>



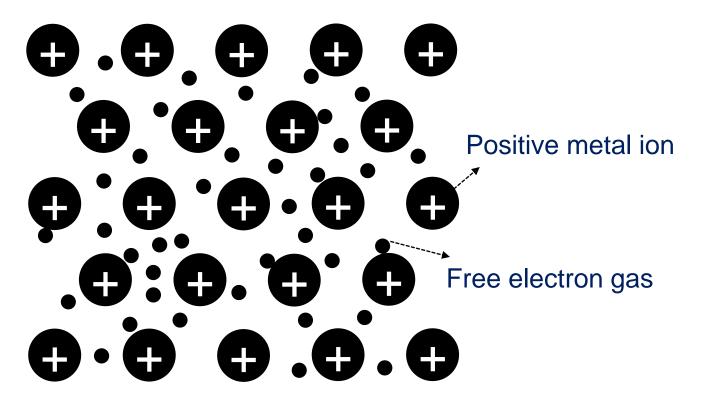
#### Crystalline structure of silicon and diamond



Q: Draw the distribution of valence electrons.

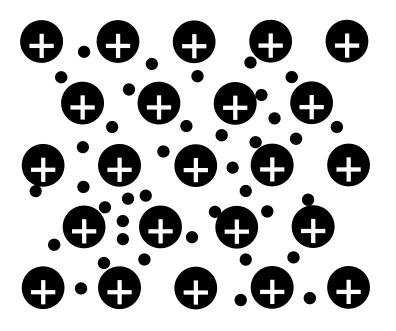
#### **Metallic bond**

Metal atom only has few valence electrons, electrons can easily move around



In metals, the metal ions tends to be as close to each other as possible, and form the close-packed structure 密堆积结构

#### Metal

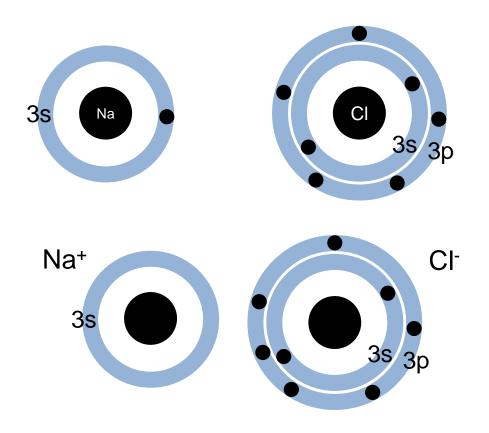


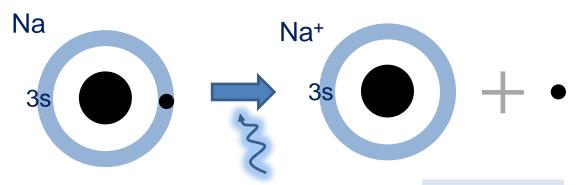
High electronic conductivity

High thermal conductivity

#### **lonic bond**

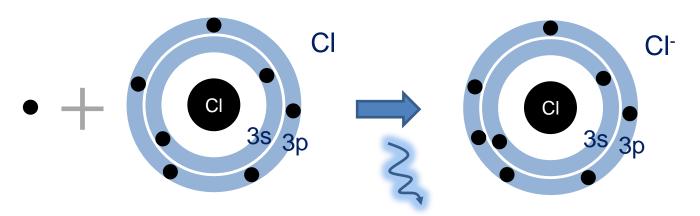
NaCl is a typical ionic crystal





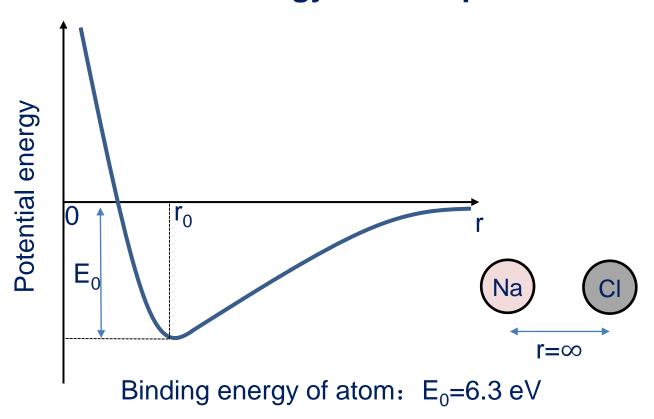
Provide energy: ionization energy 电离能

5.1 eV

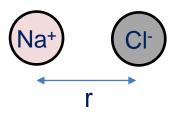


Release energy: **electron affinity energy** 电子亲和能 3.6 eV

#### Potential energy of atom pair



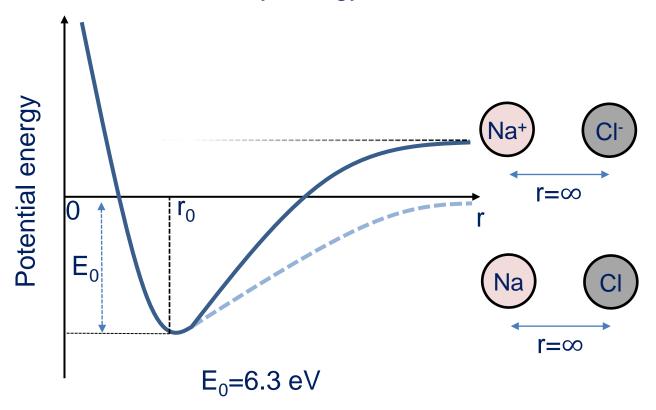
#### Potential energy of ion pair?



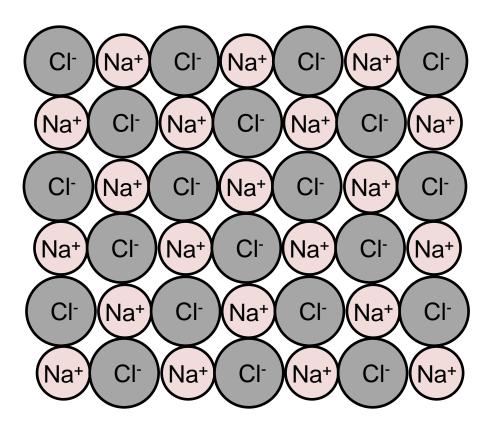
#### Potential energy of ion pair?

Ionization energy of Na: 5.1 eV

Electron affinity energy of CI: 3.6 eV



Binding energy of ion 离子结合能: 6.3 + 5.1 - 3.6=7.8 eV



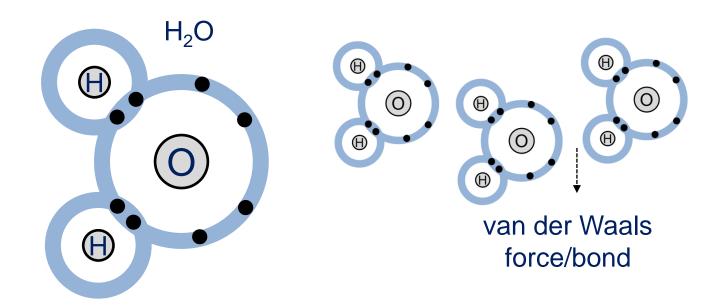
# Van der Waals bond 范德华键



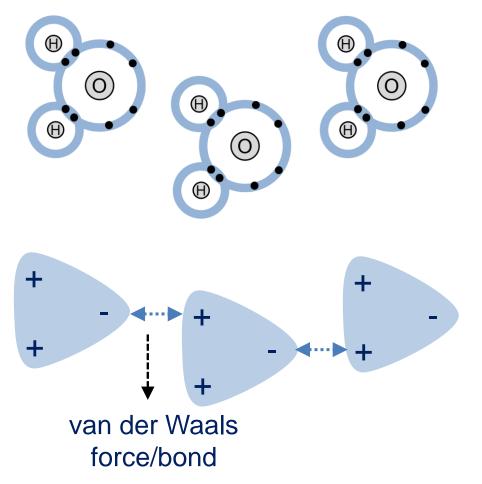


Molecular crystals 分子晶体: ice, dry ice (CO<sub>2</sub>), solid state of other gas

Gas will become solid when temperature is low enough. The force between gas molecular is van der Waals force.



#### The H<sub>2</sub>O molecule is polar and has a net permanent dipole moment







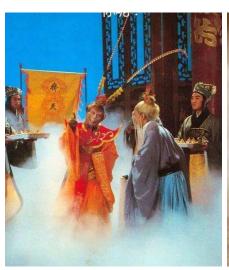


# Dry ice (solid CO<sub>2</sub>)

Density: 1.560 g/cm<sup>3</sup> (-78°C)

Melting point: -57°C

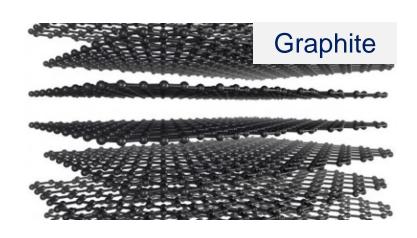
Ice point: -78.5°C

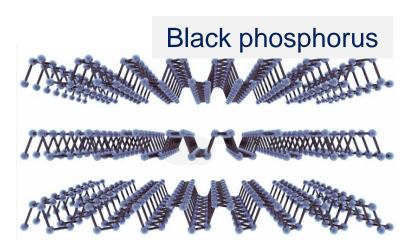


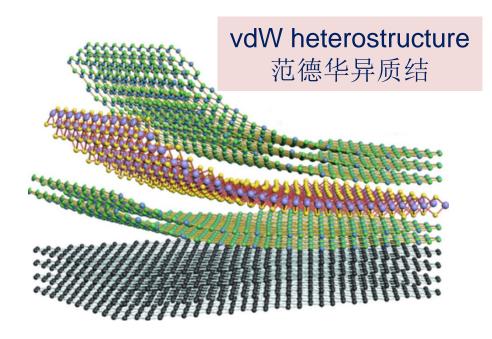


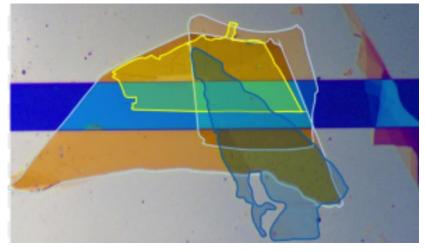


# van der Waals layered material









# van der Waals bond is very weak compared with covalent, metallic and ionic bond

Bond	Material	Binding energy (eV/atom)
Ionic	NaCl	3.2
Metallic	Mg	3.1
Covalent	Si	4
vdWs	Ice	0.52

- ◆ Primary bond 强键: ionic, metallic, and covalent bond
- ◆ Secondary bond 弱键: vdWs bond

## The potential energy of vdWs bond

Lennard – Jones 6-12 formula:

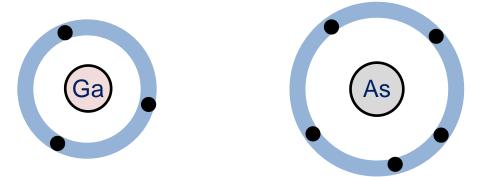
$$E(r) = -Ar^{-6} + Br^{-12}$$

Q: The average distance between atoms/molecules?

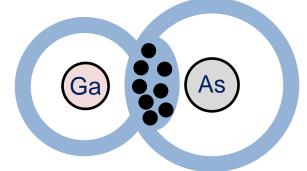
$$\frac{\mathrm{d}E}{\mathrm{d}r} = 0$$

### **Hybrid bond**

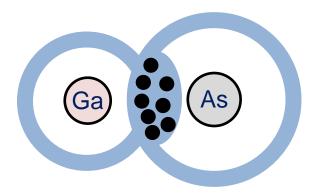
III-V compound: GaAs



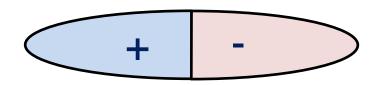
The electron cloud density is higher near As5+ nucleus



The bond has properties of both covalent bond and ionic bond



The bond is also called polar bond 极性键

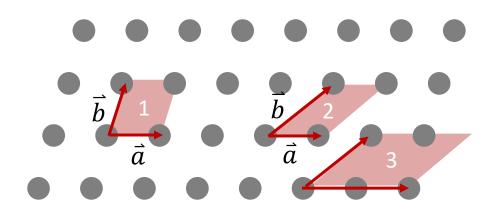


The bond has properties of both covalent bond and ionic bond

# 1.3 Crystal structure

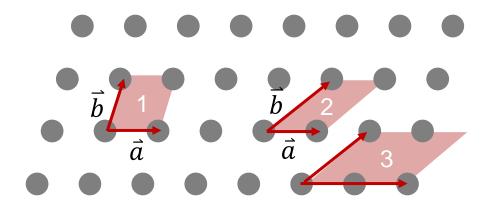
Crystal 晶体: periodic array of atoms

Lattice 晶格 is an infinite periodic array of geometric points in space



The position of atoms:  $\vec{r} = n\vec{a} + m\vec{b}$ 

 $\vec{a}, \vec{b}$  are called the basis



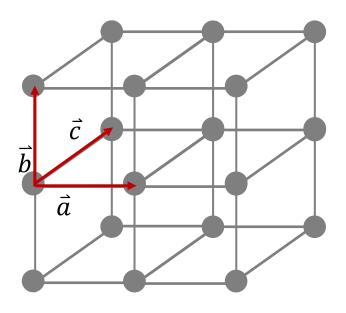
 $\vec{a}, \vec{b}$  are called the basis

The <u>unit cell 晶胞</u> is the most convenient small cell in the crystal structure that carriers the properties of the crystal.

The smallest repeating cell called the primitive cell 原胞

Area 1,2 and 3 are primitive cell?

# **Basis and primitive cell of cubic lattice**

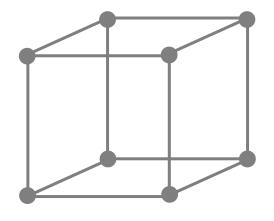


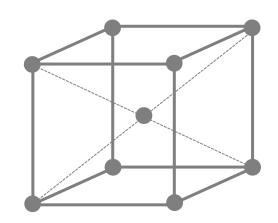
## Cubic lattice立方格子: sc, bcc, fcc,

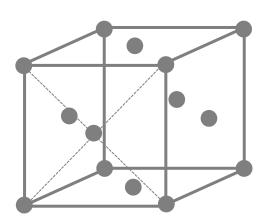
sc: simple cube

bcc: body-centered fcc: face-centered cube

cube



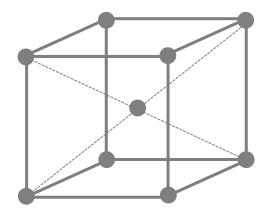




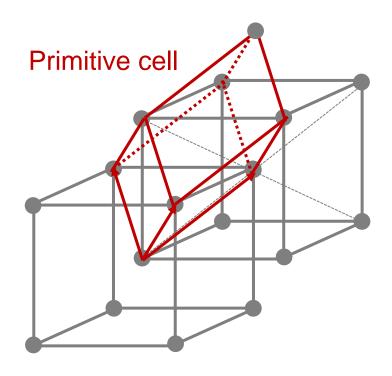
Unit cell or primitive cell?

## bcc: body-centered cube

Unit cell



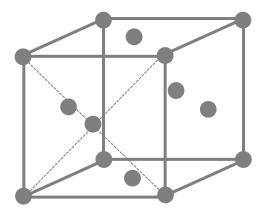
2 atoms in unit cell



1 atoms in primitive cell

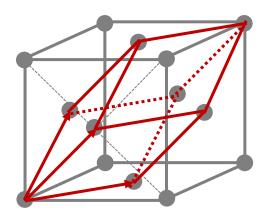
## fcc: face-centered cube

Unit cell



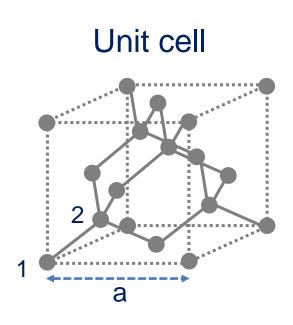
4 atoms in unit cell

Primitive cell

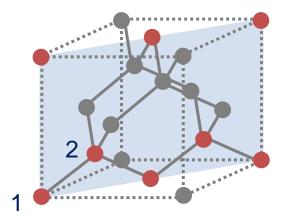


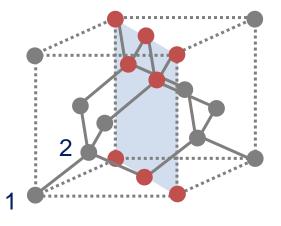
1 atoms in primitive cell

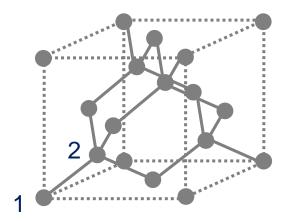
## Crystal structure of silicon/germanium/diamond



Atom 2 is shifted by (a/4, a/4, a/4) respect to atom 1





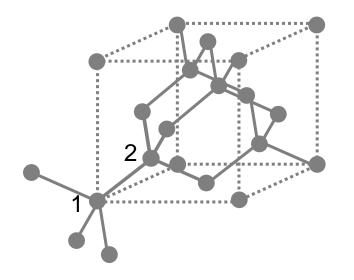


Q1: How many atoms in unit cell?

Q2: Are atom 1 and atom 2 identical?

Q3: Which lattice type?

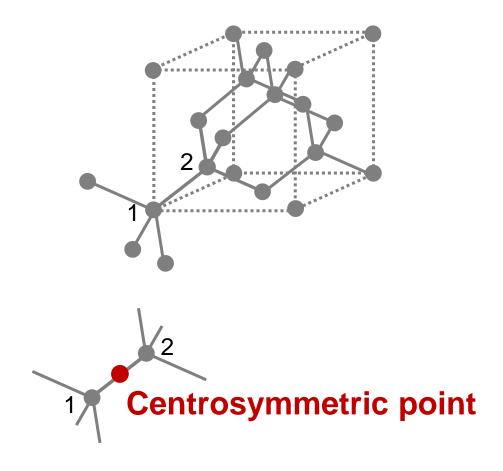
## Q2: Are atom 1 and atom 2 identical?





在一个克隆的世界,怎么判断原子是等价还是不等价的呢?

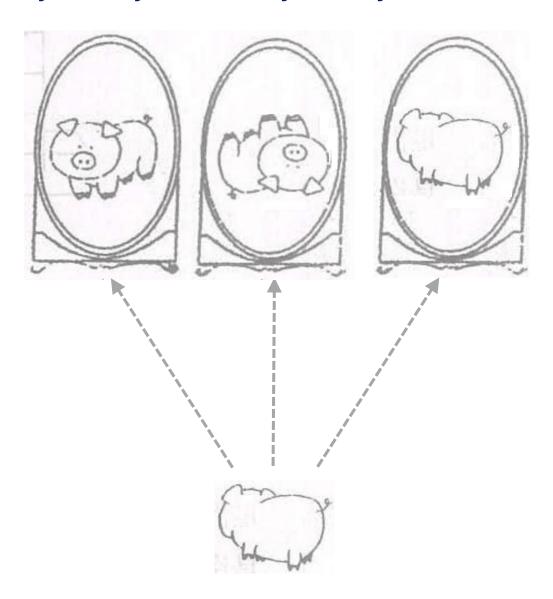
看走位!!



Atom 1 and 2 are not identical!

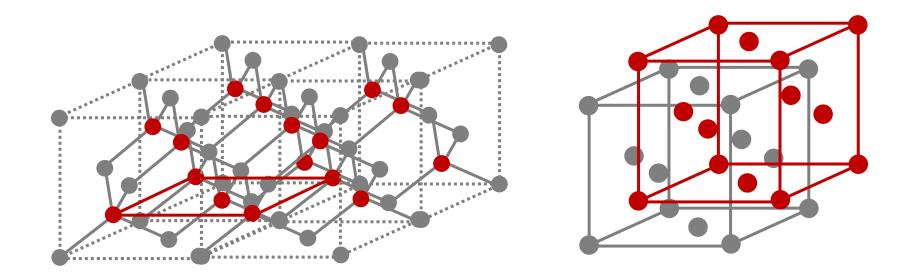
There are two arrays of atoms in unit cell.

## Mirror-symmetry Centro-symmetry Identical



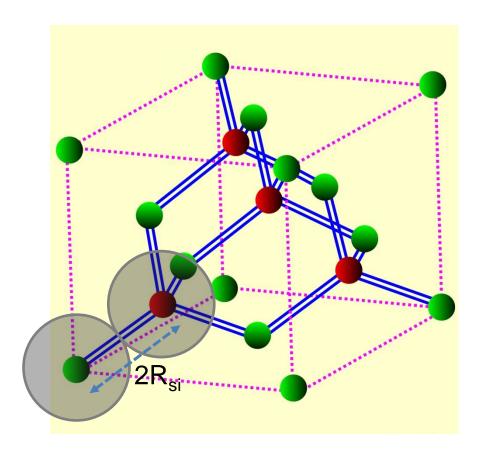
## Crystal structure of silicon/germanium/diamond

## Q3: Which lattice type?



**Constructed by 2 fcc lattice** 

## Q: Which two atoms are closest? Q: The radius of Si atom $R_{si}$ ?

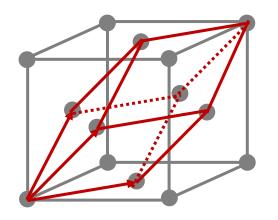


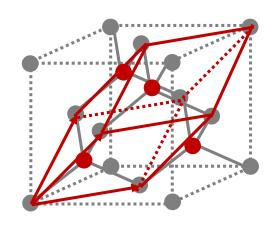
◆ Radius of atom can be calculated as the half of the distance of two nearest atoms in the lattice.

## Q4: Primitive cell?

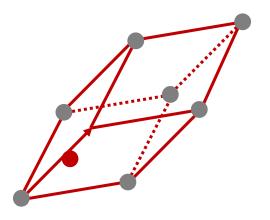
## Primitive cell of fcc







Primitive cell of Si



Find three identical nearest atoms and draw three vectors

Q5: How many atoms in primitive cell?

2 atoms in primitive cell

# If primitive cell contain 1 atom:

Every atom in lattice are identical.

# If primitive cell contain 2 atoms:

◆ There are two array of atoms which are not identical.

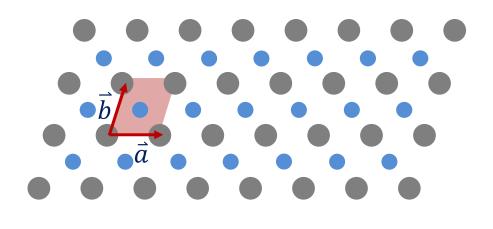
# If primitive cell contain N atoms:

◆ There are N array of atoms which are not identical.

# We call it the <u>compound lattice 复式晶格</u>

## Compound lattice 复式晶格

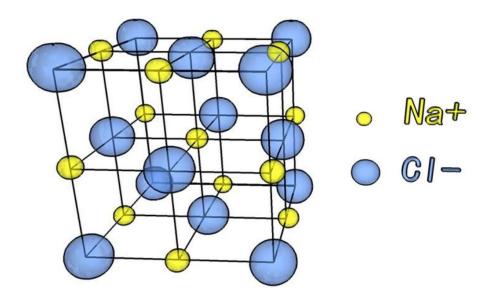
Contains multiple arrays of periodic atoms which are not identical.



Primitive/unit cell

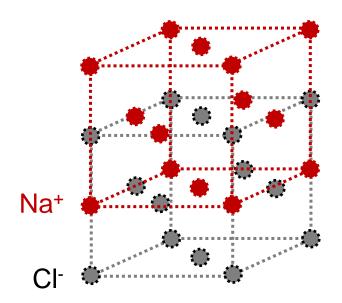


## The crystal structure of NaCl



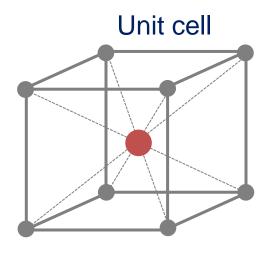
Q: Which lattice type?

## The crystal structure of NaCl

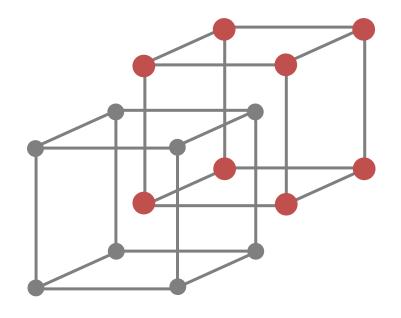


Two interpenetrating fcc unit cell!

## The crystal structure of CsCl



Q: Which lattice type?



Two interpenetrating sc unit cell!

### 立方晶系

#### **CUBIC SYSTEM**

$$a = b = c$$
  $\alpha = \beta = \gamma = 90^{\circ}$ 

Many metals, Al, Cu, Fe, Pb. Many ceramics and semiconductors, NaCl, CsCl, LiF, Si, GaAs



Body centered cubic



Face centered cubic

## 四方晶系

#### TETRAGONAL SYSTEM

$$a = b \neq c$$
  $\alpha = \beta = \gamma = 90^{\circ}$ 

In, Sn, Barium Titanate, TiO<sub>2</sub>



Simple tetragonal 简单四方



Body centered tetragonal 体心四方

#### 正交晶系

#### ORTHORHOMBIC SYSTEM

$$a \neq b \neq c$$
  $\alpha = \beta = \gamma = 90^{\circ}$ 

S, U, Pl, Ga (<30°C), Iodine, Cementite (Fe<sub>3</sub>C), Sodium Sulfate



**Simple** 

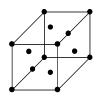
orthorhombic

简单正交

Body centered orthorhombic 体心正交



Base centered orthorhombic 底心正交



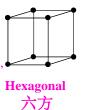
Face centered orthorhombic 面心正交

## 六方晶系

#### HEXAGONAL SYSTEM

$$a = b \neq c$$
  $\alpha = \beta = 90^{\circ}$ ;  $\gamma = 6$ 

Cadmium, Magnesium, Zinc, Graphite



# 一方晶系

## RHOMBOHEDRAL SYSTEM a = b = c $\alpha = \beta = \gamma \neq 90^{\circ}$

Arsenic, Boron, Bismuth, Antimony, Mercury (<-39°C)



#### Rhombohedral

#### 单斜晶系

#### MONOCLINIC SYSTEM

$$a \neq b \neq c$$
  $\alpha = \beta = 90^{\circ}$ ;  $\gamma \neq 90^{\circ}$ 

α-Selenium, Phosphorus Lithium Sulfate Tin Fluoride



Simple monoclinic 简单单斜

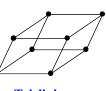


Base centered monoclinic 底心单斜

## 三斜晶系

TRICLINIC SYSTEM  $a \neq b \neq c \quad \alpha \neq \beta \neq \gamma \neq 90^{\circ}$ 

Potassium dicromate



Triclinic 三斜

The seven crystal systems (unit cell geometries) and fourteen Bravais lattices.

## Close-packed structure密堆积结构

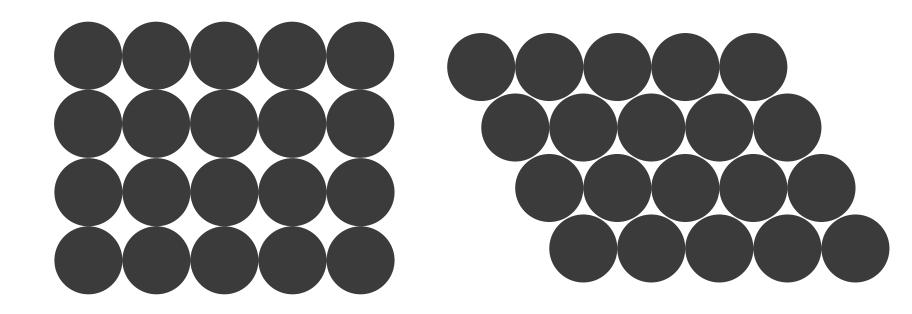
The structure with highest volume of atoms in unit cell.

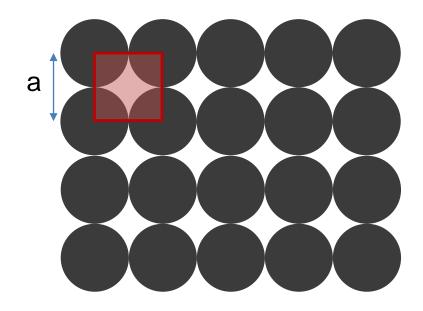


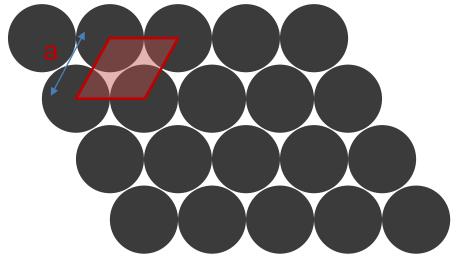


# Close-packed structure密堆积结构

For two-dimensional lattice, what's the close-packed structure?







Area of unit cell:  $S = a^2$ 

Area of atom:  $S = \pi(\frac{a}{2})^2$ 

The fraction of total area occupied by the spheres:

$$\frac{\pi}{4} = 0.79$$

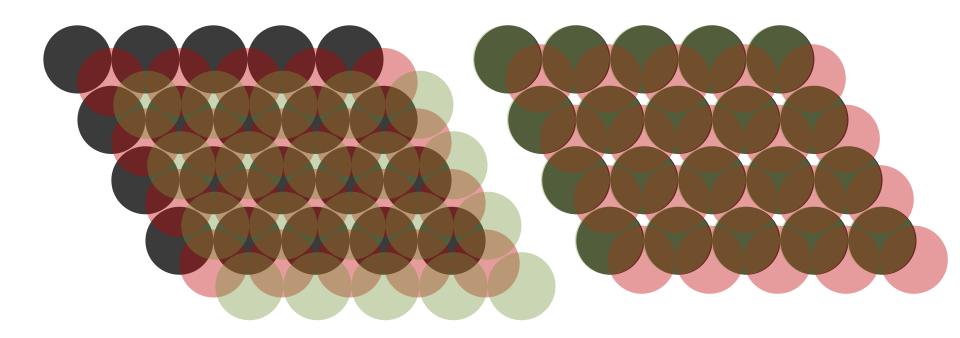
Area of unit cell:  $S = \frac{\sqrt{3}}{2}a^2$ 

Area of atom:  $S = \pi (\frac{a}{2})^2$ 

The fraction of total area occupied by the spheres:

$$\frac{\pi}{2\sqrt{3}} = 0.91$$

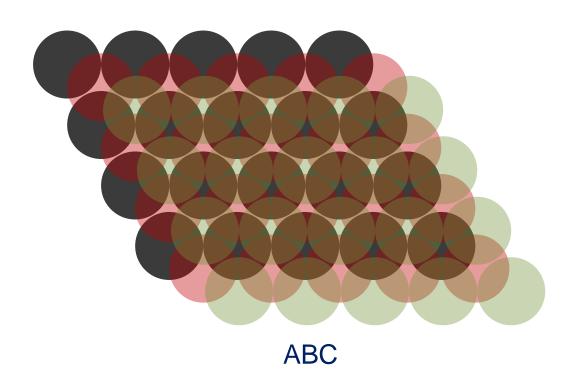
For three-dimensional lattice, what's the close-packed structure?

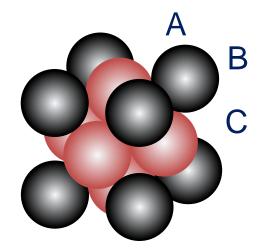


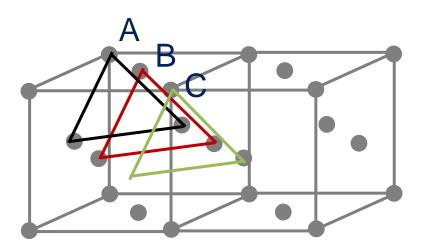
ABCABC...

ABABAB...

# Which lattice type?





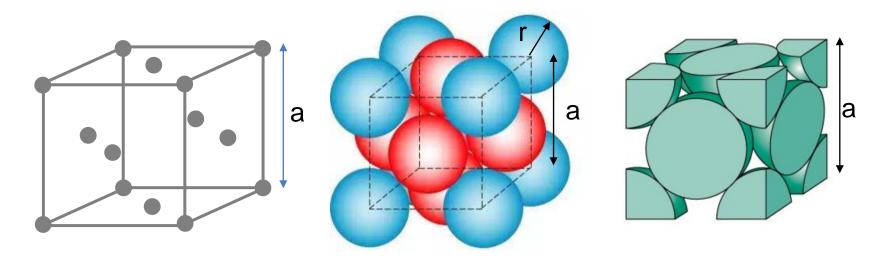




天呐噜!

fcc!!

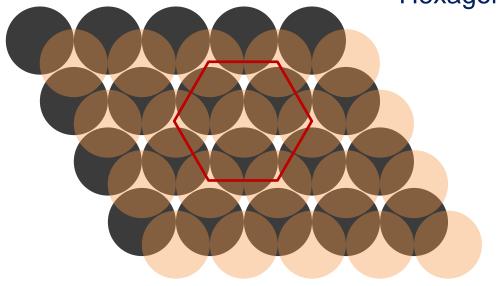
**Atomic packing factor**: the fraction of total volume occupied by the spheres:

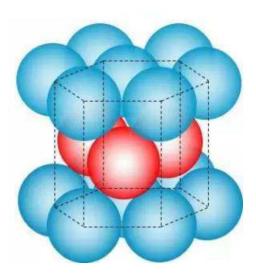


- Volume of unit cell:  $V = a^3$
- Volume of atom:  $V = 4 \times \frac{4}{3}\pi r^3$
- Relationship between r and a:  $4r = \sqrt{2}a$
- Atomic packing factor:  $\frac{\sqrt{2}}{6}\pi = 0.74$

## Which lattice type for ABAB...

Hexagonal close-packed (hcp) structure

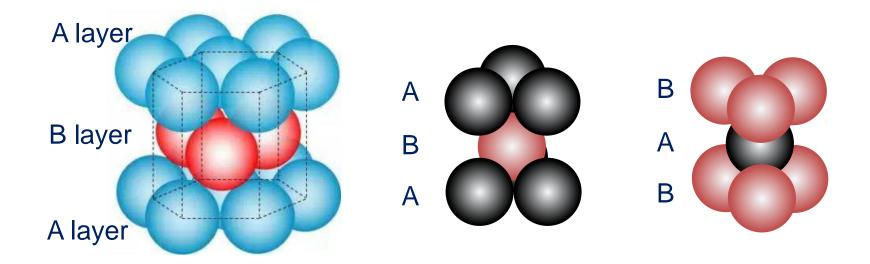




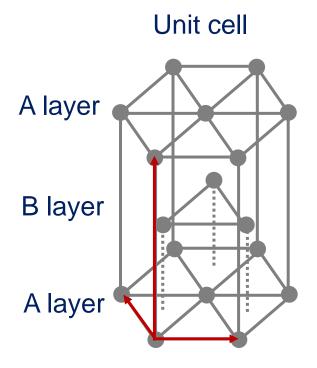
Q: How many atoms in hcp unit cell?

$$\frac{1}{6} \times 12 + \frac{1}{2} \times 2 + 3 = 6$$

## Which lattice type for ABAB...

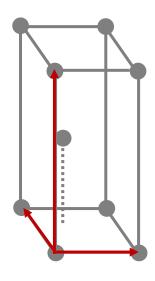


## Primitive cell for hcp structure



Atoms in A and B layer are not identical!

Primitive cell



2 atoms in primitive cell

# **Atomic packing factor?**

