

# QF600 ASSETING PRICING

## HomeWork 2

```
In [3]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import statsmodels.api as sm
```

```
In [4]: %whos
```

Variable	Type	Data/Info
np	module	<module 'numpy' from '/Us<...>kages/numpy/__init__.p y'>
pd	module	<module 'pandas' from '/U<...>ages/pandas/__init__.p y'>
plt	module	<module 'matplotlib.pyplo<...>es/matplotlib/pyplot.p y'>
sm	module	<module 'statsmodels.api'<...>ages/statsmodels/api.p y'>

## Capital Asset Pricing Model (CAPM)

```
In [5]: industry_portfolios = \
    pd\
        .read_csv("/Users/lu/Desktop/Industry_Portfolios.csv")

mkt_portfolio = \
    pd\
        .read_csv("/Users/lu/Desktop/Market_Portfolio.csv")

industry_portfolios
```

Out [5]:

	Date	NoDur	Durbl	Manuf	Enrgy	HiTec	Telcm	Shops	HLth	Utils	Otl
0	200401	0.06	-1.07	-0.62	0.44	4.53	1.41	0.45	3.09	1.92	2.0
1	200402	4.25	-0.07	1.95	4.69	-2.92	-0.52	6.09	0.89	2.07	2.0
2	200403	-0.09	-1.15	-0.27	-0.13	-2.55	-2.07	0.29	-3.96	1.13	-0.0
3	200404	1.42	2.30	-0.17	2.52	-4.91	-0.48	-2.70	3.54	-3.55	-3.0
4	200405	-1.89	-1.64	1.61	0.39	4.85	-2.95	0.30	-0.42	1.28	1.0
...	...	...	...	...	...	...	...	...	...	...	...
115	201308	-4.00	-1.00	-1.95	-1.83	-0.12	-3.28	-4.21	-3.49	-4.43	-3.0
116	201309	1.94	6.46	5.20	2.03	3.77	4.33	4.46	4.19	1.05	3.0
117	201310	4.75	0.72	4.56	4.86	3.80	5.52	5.08	3.47	3.35	3.0
118	201311	1.29	1.81	2.95	0.85	3.65	0.27	3.67	4.54	-1.81	4.0
119	201312	2.65	1.18	3.13	2.95	4.04	3.96	0.20	0.71	1.79	3.0

120 rows × 11 columns

In [6]: mkt\_portfolio

Out [6]:

	Date	Market
0	200401	2.22
1	200402	1.46
2	200403	-1.23
3	200404	-1.75
4	200405	1.23
...	...	...
115	201308	-2.69
116	201309	3.76
117	201310	4.17
118	201311	3.12
119	201312	2.81

120 rows × 2 columns

In [7]: *# merge two data frames*

```
merged_data =\
    pd\
        .merge(industry_portfolios,
                mkt_portfolio,
                on='Date',
                how='inner')
```

merged\_data

Out [7]:

	Date	NoDur	Durbl	Manuf	Enrgy	HiTec	Telcm	Shops	Hlth	Utils	Otl
0	200401	0.06	-1.07	-0.62	0.44	4.53	1.41	0.45	3.09	1.92	2.07
1	200402	4.25	-0.07	1.95	4.69	-2.92	-0.52	6.09	0.89	2.07	2.07
2	200403	-0.09	-1.15	-0.27	-0.13	-2.55	-2.07	0.29	-3.96	1.13	-0.09
3	200404	1.42	2.30	-0.17	2.52	-4.91	-0.48	-2.70	3.54	-3.55	-3.55
4	200405	-1.89	-1.64	1.61	0.39	4.85	-2.95	0.30	-0.42	1.28	1.28
...	...	...	...	...	...	...	...	...	...	...	...
115	201308	-4.00	-1.00	-1.95	-1.83	-0.12	-3.28	-4.21	-3.49	-4.43	-3.49
116	201309	1.94	6.46	5.20	2.03	3.77	4.33	4.46	4.19	1.05	3.14
117	201310	4.75	0.72	4.56	4.86	3.80	5.52	5.08	3.47	3.35	3.35
118	201311	1.29	1.81	2.95	0.85	3.65	0.27	3.67	4.54	-1.81	4.54
119	201312	2.65	1.18	3.13	2.95	4.04	3.96	0.20	0.71	1.79	3.96

120 rows × 12 columns

Assume that the (net) risk-free rate is 0.13% per month.

In [8]: risk\_free\_rate = 0.13

USING FORMULA:  $\tilde{R}_i - R_f = \alpha_i + \beta_i(\tilde{R}_m - R_f)$

```
In [11]: #R_m - R_f (mkt excess return)
merged_data["mkt_excess_returns"] = \
    merged_data["Market"] \
    - \
    risk_free_rate

merged_data
```

Out [11]:

	Date	NoDur	Durbl	Manuf	Enrgy	HiTec	Telcm	Shops	HLth	Utils	...
0	200401	0.06	-1.07	-0.62	0.44	4.53	1.41	0.45	3.09	1.92	...
1	200402	4.25	-0.07	1.95	4.69	-2.92	-0.52	6.09	0.89	2.07	...
2	200403	-0.09	-1.15	-0.27	-0.13	-2.55	-2.07	0.29	-3.96	1.13	...
3	200404	1.42	2.30	-0.17	2.52	-4.91	-0.48	-2.70	3.54	-3.55	...
4	200405	-1.89	-1.64	1.61	0.39	4.85	-2.95	0.30	-0.42	1.28	...
...	...	...	...	...	...	...	...	...	...	...	...
115	201308	-4.00	-1.00	-1.95	-1.83	-0.12	-3.28	-4.21	-3.49	-4.43	...
116	201309	1.94	6.46	5.20	2.03	3.77	4.33	4.46	4.19	1.05	...
117	201310	4.75	0.72	4.56	4.86	3.80	5.52	5.08	3.47	3.35	...
118	201311	1.29	1.81	2.95	0.85	3.65	0.27	3.67	4.54	-1.81	...
119	201312	2.65	1.18	3.13	2.95	4.04	3.96	0.20	0.71	1.79	...

120 rows × 23 columns

In [12]:

```
# R_i - R_f(for each industry excess return)
industry_columns = ['NoDur', 'Durbl', 'Manuf', 'Enrgy', 'HiTec', 'Telcm',

for industry in industry_columns:
    merged_data\
    [f'{industry}_Excess>Returns'] =\
    merged_data[industry]\
    -\
    risk_free_rate

merged_data
```

Out [12]:

	Date	NoDur	Durbl	Manuf	Enrgy	HiTec	Telcm	Shops	HLth	Utils	...
0	200401	0.06	-1.07	-0.62	0.44	4.53	1.41	0.45	3.09	1.92	...
1	200402	4.25	-0.07	1.95	4.69	-2.92	-0.52	6.09	0.89	2.07	...
2	200403	-0.09	-1.15	-0.27	-0.13	-2.55	-2.07	0.29	-3.96	1.13	...
3	200404	1.42	2.30	-0.17	2.52	-4.91	-0.48	-2.70	3.54	-3.55	...
4	200405	-1.89	-1.64	1.61	0.39	4.85	-2.95	0.30	-0.42	1.28	...
...	...	...	...	...	...	...	...	...	...	...	...
115	201308	-4.00	-1.00	-1.95	-1.83	-0.12	-3.28	-4.21	-3.49	-4.43	...
116	201309	1.94	6.46	5.20	2.03	3.77	4.33	4.46	4.19	1.05	...
117	201310	4.75	0.72	4.56	4.86	3.80	5.52	5.08	3.47	3.35	...
118	201311	1.29	1.81	2.95	0.85	3.65	0.27	3.67	4.54	-1.81	...
119	201312	2.65	1.18	3.13	2.95	4.04	3.96	0.20	0.71	1.79	...

120 rows × 23 columns

## Table of the intercept and slope coefficients for the ten industry portfolios.

```
In [13]: res = {}
for industry in industry_columns:
    x = \
        merged_data['mkt_excess_returns']

    y = \
        merged_data[f'{industry}_Excess_Returns']

    x = \
        sm\
        .add_constant(x)

    model = \
        sm\
        .OLS(y, x)\
        .fit()

    alpha, beta = \
        model\
        .params

    res[industry] = \
        {'Alpha': alpha,
         'Beta': beta}

res_df = \
    pd\
    .DataFrame(res)\
    .T

res_df
```

```
Out [13]:
```

	Alpha	Beta
<b>NoDur</b>	0.369443	0.652647
<b>Durbl</b>	-0.415599	1.648536
<b>Manuf</b>	0.159771	1.169846
<b>Enrgy</b>	0.501719	0.969850
<b>HiTec</b>	-0.064020	1.132969
<b>Telcm</b>	0.194691	0.900729
<b>Shops</b>	0.275492	0.826492
<b>HLth</b>	0.237841	0.673036
<b>Utils</b>	0.444585	0.538086
<b>Other</b>	-0.387135	1.207309

## Explanation

The economic significance of the intercept ( $\alpha$ ) means the abnormal performance and abnormal return of assets, the pricing implication is whether assets have a reasonable price to the market, where  $\alpha > 0$  indicates Excess return and undervaluation;  $\alpha < 0$  means a shortfall and overvaluation, and  $\alpha = 0$  implies the asset return matches market expectations without excess return.

The slope coefficients( $\beta$ ) reflects sensitivity of an asset to market risk, where  $\beta > 1$  means higher volatility than the market,  $\beta < 1$  indicates lower volatility,  $\beta = 1$  means equal volatility, and  $\beta < 0$  shows inverse volatility to the market.

## Security Market Line (SML)

```
In [24]: # mean return of 10 industries portfolios and the market portfolio
mean_industry_returns =\
    merged_data[industry_columns]\
        .mean()

mean_mkt_return =\
    merged_data['Market']\
        .mean()

df = mean_industry_returns.to_frame()
df.columns = ['industry']
df
```

```
Out [24]:
```

	industry
<b>NoDur</b>	0.902833
<b>Durbl</b>	0.733333
<b>Manuf</b>	1.012833
<b>Enrgy</b>	1.231167
<b>HiTec</b>	0.766250
<b>Telcm</b>	0.881417
<b>Shops</b>	0.916333
<b>HLth</b>	0.783833
<b>Utils</b>	0.907167
<b>Other</b>	0.489083

```
In [15]: mean_mkt_return
```

```
Out [15]: np.float64(0.7480833333333334)
```

```
In [32]: all_beta = res_df["Beta"]
df["beta"] = all_beta
market_data = {'industry': mean_mkt_return, 'beta': 1}
df.loc['market'] = market_data

df
```

Out [32]:

	industry	beta
<b>NoDur</b>	0.902833	0.652647
<b>Durbl</b>	0.733333	1.648536
<b>Manuf</b>	1.012833	1.169846
<b>Enrgy</b>	1.231167	0.969850
<b>HiTec</b>	0.766250	1.132969
<b>Telcm</b>	0.881417	0.900729
<b>Shops</b>	0.916333	0.826492
<b>HLth</b>	0.783833	0.673036
<b>Utils</b>	0.907167	0.538086
<b>Other</b>	0.489083	1.207309
<b>market</b>	0.748083	1.000000

```
In [36]: X = sm.add_constant(df['beta'])
Y = df['industry']
model = sm.OLS(Y, X).fit()

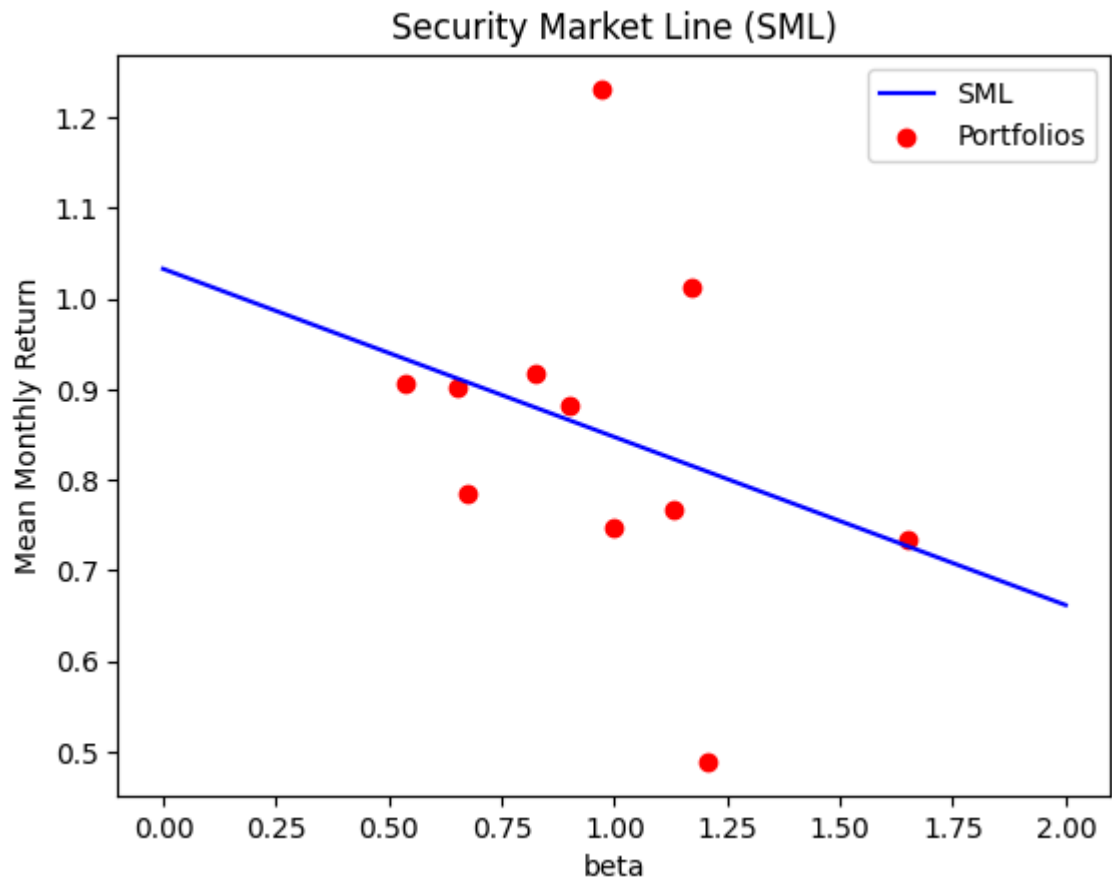
intercept = model.params['const']
slope = model.params['beta']
```

```
In [38]: beta_range = np.linspace(0, 2, 100)
sml_values = intercept + slope * beta_range # SML
plt.plot(beta_range, sml_values, label='SML', color='blue')

plt.scatter(df['beta'], df['industry'], color='red', label='Portfolios')

plt.xlabel('beta')
plt.ylabel('Mean Monthly Return')
plt.title('Security Market Line (SML)')
plt.legend()

plt.show()
```



## Explanation

The intercept of SML represents the market risk premium, while its slope shows the return from risk-free assets. SML measures whether assets are reasonably priced if the asset portfolio is on the SML, that means the asset is reasonably priced. If assets above SML indicate that the asset is undervalued, otherwise, it is overvalued.