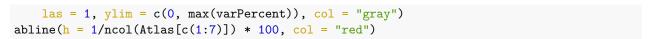
Atlas

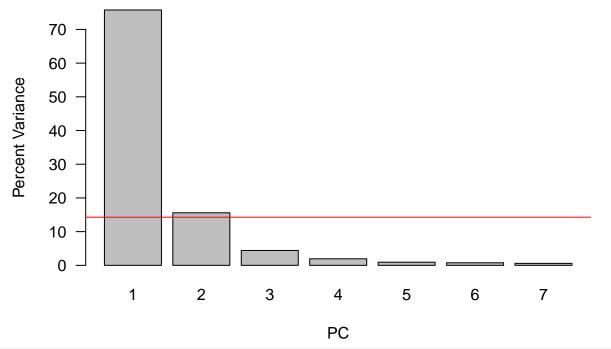
David Ledesma

3/22/2021

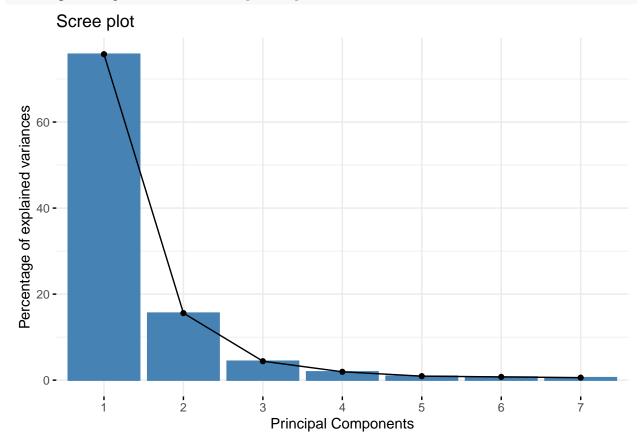
Load in data

```
library(curl)
library(readxl)
Amb_linear_data <- curl("https://raw.githubusercontent.com/TIMAVID/Ambystoma/master/Linear_data/Data/Am
Amb_linear_data <- read.csv(Amb_linear_data)</pre>
Tidy data
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
PCA's
Atlas.pca <- prcomp(Atlas_wofossil_noNA[c(1:7)], center = TRUE, scale = TRUE) # PCA
# Summary stats #
summary(Atlas.pca)
## Importance of components:
                              PC1
                                     PC2
                                             PC3
                                                      PC4
                                                              PC5
                                                                      PC6
                                                                               PC7
                           2.3031 1.0447 0.55567 0.36920 0.25577 0.23039 0.20233
## Standard deviation
## Proportion of Variance 0.7577 0.1559 0.04411 0.01947 0.00935 0.00758 0.00585
## Cumulative Proportion 0.7577 0.9136 0.95775 0.97722 0.98657 0.99415 1.00000
sd <- Atlas.pca$sdev
loadings <- Atlas.pca$rotation</pre>
rownames(loadings) <- colnames(Atlas[c(1:7)])</pre>
scores <- Atlas.pca$x</pre>
# Show variance explained by PC's #
var <- sd^2
varPercent <- var/sum(var) * 100</pre>
barplot(varPercent, xlab = "PC", ylab = "Percent Variance", names.arg = 1:length(varPercent),
```





fviz_eig(Atlas.pca, xlab = "Principal Components")

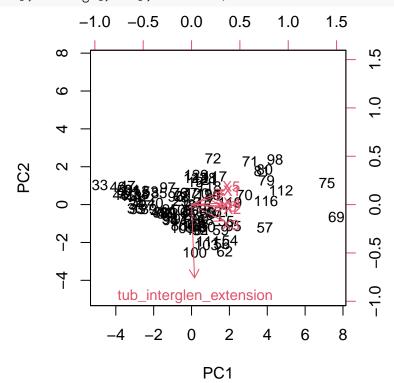


```
# Show loadings #
loadings
```

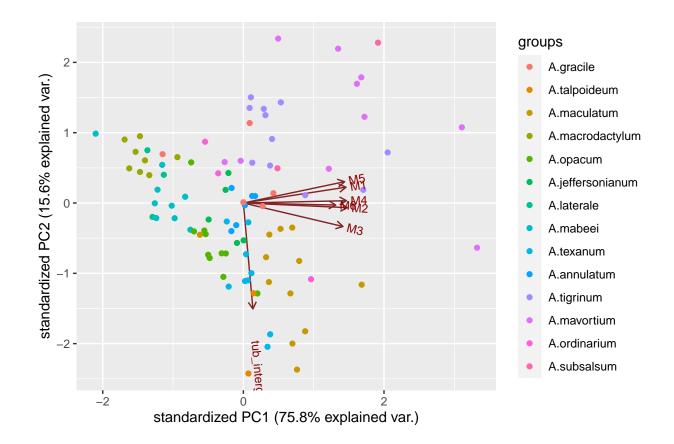
```
PC1
                                         PC2
                                                  PC3
##
                                                             PC4
## tub interglen extension 0.03870518 -0.94714699 0.1063967 -0.23874181
                        ## X1
## X2
                        0.42197173 -0.04128891
                                             0.1441653
                                                      0.29389133
## X3
                        0.40400635 -0.21003360 -0.0244320 0.71347417
## X4
                        0.41821678 0.02044259
                                             0.1837650 -0.49111174
## X5
                        ## X6
                        0.37455058 -0.01813215 -0.9000098 -0.18314807
##
                               PC5
                                         PC6
                                                    PC7
## tub_interglen_extension 0.01387657 -0.16293082 -0.07973435
                         0.48873145 -0.09764476 -0.69696451
## X1
                         0.47031170 -0.27244438  0.64626642
## X2
## X3
                        -0.39377589 0.30964846 -0.17911119
## X4
                        -0.03666985 0.70273932 0.23351511
## X5
                        -0.61565777 -0.53937106 0.03398159
## X6
                         0.06570612 -0.09511705 -0.04957562
sqrt(1/ncol(Atlas[c(1:7)])) # cutoff for 'important' loadings
```

[1] 0.3779645

dev.new(height=7, width=7) biplot(scores[, 1:2], loadings[, 1:2], cex = 0.9)

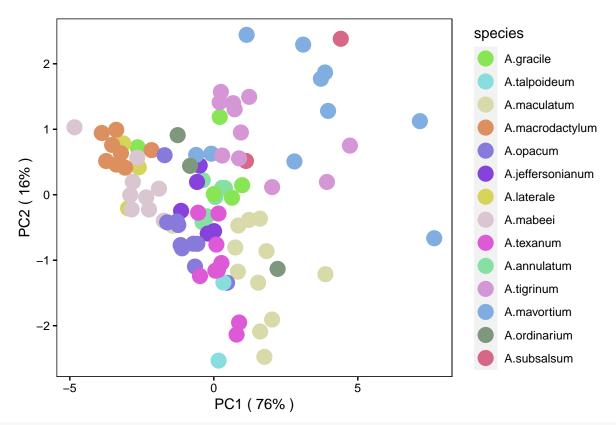


ggbiplot(Atlas.pca, ellipse = FALSE, groups = Atlas_wofossil_noNA\$species)



Plot

```
scores <- as.data.frame(scores)</pre>
scores$species <- Atlas_wofossil_noNA$species # reattach species</pre>
theme <- theme(panel.background = element_blank(), panel.border = element_rect(fill = NA),
    panel.grid.major = element_blank(), panel.grid.minor = element_blank(),
    strip.background = element_blank(), axis.text.x = element_text(colour = "black"),
    axis.text.y = element_text(colour = "black"), axis.ticks = element_line(colour = "black"),
    plot.margin = unit(c(1, 1, 1, 1), "line"))
percentage <- paste(colnames(scores), "(", paste(as.character(round(varPercent)),</pre>
    "%", " )", sep = ""))
n <- 14
palette <- distinctColorPalette(n)</pre>
p \leftarrow ggplot(scores, aes(x = PC1, y = PC2, color = species))
p <- p + geom_point(size = 5) + theme + xlab(percentage[1]) + ylab(percentage[2]) +
    scale_color_manual(values = palette)
# p + stat_ellipse()
p
```



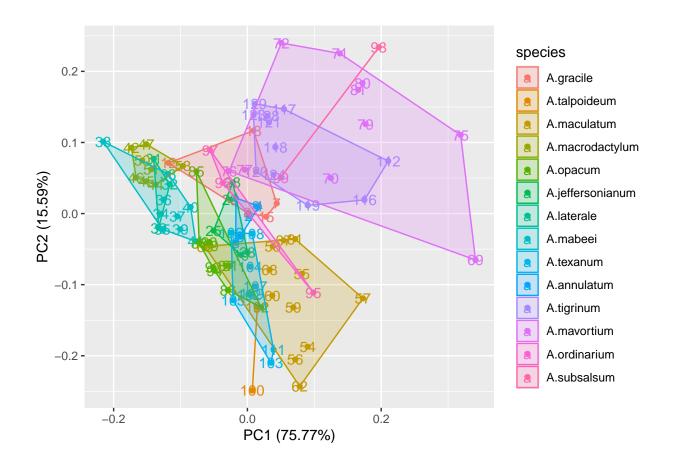
```
## Warning: `select_()` was deprecated in dplyr 0.7.0.
```

^{##} Please use `select()` instead.

^{##} Warning: `group_by_()` was deprecated in dplyr 0.7.0.

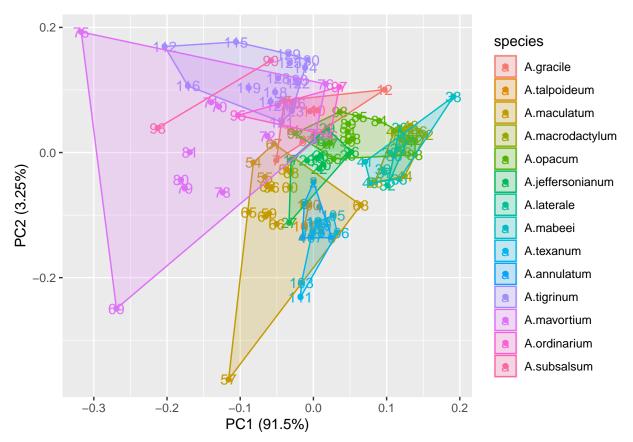
^{##} Please use `group_by()` instead.

^{##} See vignette('programming') for more help



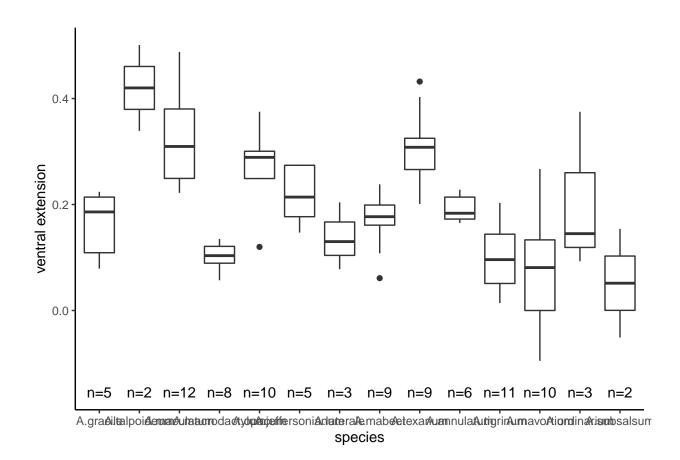
No tuberculum interglenoideum ventral extent measurement

```
Atlas_wofossil_noTub <- Atlas_wofossil[, -1]
Atlas_wofossil_noTub <- na.omit(Atlas_wofossil_noTub) # remove rows with N/A's
Atlas_wofossil_noTub$species <- as.factor(Atlas_wofossil_noTub$species)
Atlas_wofossil_noTub$species <- factor(Atlas_wofossil_noTub$species, levels = c("A.gracile",
    "A.talpoideum", "A.maculatum", "A.macrodactylum", "A.opacum", "A.jeffersonianum",
    "A.laterale", "A.mabeei", "A.texanum", "A.annulatum", "A.tigrinum", "A.mavortium",
    "A.ordinarium", "A.subsalsum")) # Reorder species
Atlas.pca_2 <- prcomp(Atlas_wofossil_noTub[c(1:6)], center = TRUE, scale = FALSE) # PCA
autoplot(Atlas.pca_2, data = Atlas_wofossil_noTub, colour = "species", frame = TRUE,
    label = TRUE)
```



Tuberculum interglenoideum plot library(EnvStats)

```
##
## Attaching package: 'EnvStats'
  The following objects are masked from 'package:stats':
##
##
##
       predict, predict.lm
## The following object is masked from 'package:base':
##
       print.default
Tub_dat <- Atlas_wofossil_noNA[c(1, 9)]</pre>
ventral_extension_p <- ggplot(data = Tub_dat, aes(x = species, y = (tub_interglen_extension)))</pre>
ventral_extension_p <- ventral_extension_p + geom_boxplot(na.rm = TRUE)</pre>
ventral_extension_p <- ventral_extension_p + theme(axis.text.x = element_text(angle = 90))</pre>
ventral_extension_p <- ventral_extension_p + ylab("ventral extension") + stat_n_text() +</pre>
    theme_classic()
ventral extension p
```



Statistical Tests

Various ckecks for MANOVA

```
\# Atlas\_wofossil\_noTub\_sub <- Atlas\_wofossil\_noTub\_sub %>% add\_column(id = 1)
# rownames(Atlas_wofossil_noTub_sub), .after = 8)
# Check sample sizes:PASS
Atlas\_wofossil\_noTub\_sub \ \%>\% \ dplyr::group\_by(species) \ \%>\% \ dplyr::summarise(N = n())
## # A tibble: 10 x 2
##
      species
                             N
##
      <fct>
                         <int>
##
    1 A.gracile
                             8
    2 A.maculatum
                             14
   3 A.macrodactylum
                             12
```

```
## 4 A.opacum
                          13
## 5 A.jeffersonianum
                          11
## 6 A.mabeei
                           9
## 7 A.texanum
                           9
## 8 A.annulatum
                           6
## 9 A.tigrinum
                          17
## 10 A.mavortium
                          12
# Identify univariate outliers for each variable:FAIL
Atlas_wofossil_noTub_sub %% dplyr::group_by(species) %>% identify_outliers(5) #input variable column
## # A tibble: 15 x 10
##
      species
                     M1
                           M2
                                 МЗ
                                       M4
                                             M5
                                                   M6 specimen_num
                                                                         is.outlier
##
      <fct>
                  <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dr>
                                                                         <1g1>
                                                 0.98 A.gracile_UTEP_16~ TRUE
##
   1 A.gracile
                   2.27
                        2.34
                              0.86
                                    1.67
                                           2.68
                                                 0.97 A.maculatum_UTEP_~ TRUE
   2 A.maculatum
                  2.58
                        2.97
                              1.24
                                     1.95
                                           2.47
                                                 0.96 A.macrodactylum_U~ TRUE
   3 A.macrodac~
                  2.62 2.68 0.98
                                    1.86
                                          2.28
                                                 0.83 A.opacum_UTEP_1276 TRUE
## 4 A.opacum
                   1.93
                        2.18 0.85
                                    1.47
                                           2.13
## 5 A.opacum
                   2.05
                        2.34 0.78
                                    1.25
                                           2.09
                                                 0.78 A.opacum_UTEP_1280 TRUE
## 6 A.opacum
                   2.54
                        2.53 0.87
                                    1.74
                                           2.49
                                                 0.84 A.opacum_UTEP_1285 TRUE
## 7 A.opacum
                                           3.35
                                                 1.17 A.opacum_UTEP_1310 TRUE
                   3.46 3.39
                              1.27
                                    2.6
## 8 A.jefferso~
                  2.89
                        2.79
                                           2.63
                                                 0.99 A.jeffersonianum_~ TRUE
                              1.14
                                    2.11
                                                 0.78 A.mabeei UTEP 1576 TRUE
## 9 A.mabeei
                   1.75
                        1.44 0.6
                                     1.19
                                           1.72
## 10 A.mabeei
                   2.51 2.71 1.01 1.94
                                           2.6
                                                 1.15 A.mabeei_UTEP_1584 TRUE
## 11 A.texanum
                   2.8
                         3.19
                              1.28
                                    2.31
                                           2.62
                                                 1.26 A.texanum_UTEP_17~ TRUE
                                                 1.73 A.tigrinum_UTEP_1~ TRUE
## 12 A.tigrinum
                   4.52 4.54
                              1.87
                                     3.63
                                           5.38
## 13 A.tigrinum
                  3.69 3.67
                              1.47
                                    3.35
                                           4.49
                                                 1.51 A.tigrinum_UTEP_1~ TRUE
                                                1.79 A.tigrinum_UTEP_1~ TRUE
## 14 A.tigrinum
                   4.46 4.35 1.66
                                    3.36
                                           4.91
## 15 A.mavortium 5.65 5.13 1.74 4.97
                                           6.03
                                                 2.18 A.mavortium_UTEP_~ TRUE
## # ... with 1 more variable: is.extreme <lgl>
Atlas_wofossil_noTub_sub %>% dplyr::group_by(species) %>% identify_outliers(6) #input variable column
## # A tibble: 7 x 10
##
     species
                      M2
                            МЗ
                                  M4
                                        M5
                                              M6 specimen_num is.outlier is.extreme
     <fct>
             <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dr>
                                                              <1g1>
                                                                         <1g1>
## 1 A.macu~
             3.68 4.18
                         1.58
                                3.13
                                      3.71
                                           3.29 A.maculatum~ TRUE
                                                                         TRUE
## 2 A.mabe~
             2.51 2.71 1.01
                              1.94
                                     2.6
                                            1.15 A.mabeei_UT~ TRUE
                                                                         FALSE
             3.38 3.38
                                2.32
                                      2.73
                                            1.08 A.annulatum~ TRUE
## 3 A.annu~
                         1.17
                                                                         FALSE
## 4 A.tigr~ 4.52 4.54
                                     5.38
                                            1.73 A.tigrinum_~ TRUE
                                                                         FALSE
                         1.87
                                3.63
## 5 A.tigr~ 3.45 2.99
                         1.51
                                     3.56
                                           1.11 A.tigrinum_~ TRUE
                                                                         FALSE
                                2.18
## 6 A.tigr~ 4.46 4.35 1.66
                                3.36
                                     4.91
                                           1.79 A.tigrinum_~ TRUE
                                                                         FALSE
## 7 A.mavo~ 4.92 5.12 2.22 3.87 5.32 3.65 A.mavortium~ TRUE
                                                                         TRUE
# Detect multivariate outliers: MOSTLY PASS
head(mahalanobis_distance(Atlas_wofossil_noTub_sub[, 1:6]))
                                M6 mahal.dist is.outlier
      M1
           M2
                МЗ
                     M4
                          M5
## 1 3.38 3.38 1.17 2.32 2.73 1.08
                                        6.035
                                                   FALSE
## 2 3.36 3.21 1.31 2.49 2.91 1.22
                                        6.431
                                                   FALSE
## 3 3.50 3.42 1.29 2.46 2.96 1.30
                                        4.895
                                                   FALSE
## 4 3.42 3.61 1.30 2.57 2.87 1.28
                                        4.941
                                                   FALSE
## 5 3.12 3.44 1.24 2.29 2.77 1.24
                                        2.674
                                                   FALSE
```

FALSE

4.128

6 3.05 3.18 1.24 2.27 2.61 1.38

```
# Check univariate normality assumption: FAIL
Atlas_wofossil_noTub_sub %>% group_by(species) %>% shapiro_test(M1, M2, M3,
   M4, M5, M6) %>% arrange(variable)
## # A tibble: 60 x 4
##
      species
                       variable statistic
##
      <fct>
                       <chr>
                                    <dbl>
                                            <dbl>
## 1 A.gracile
                       M1
                                    0.782 0.0183
## 2 A.maculatum
                                    0.787 0.00350
                                    0.968 0.894
## 3 A.macrodactylum M1
                       M1
## 4 A.opacum
                                    0.957 0.703
## 5 A.jeffersonianum M1
                                    0.945 0.576
## 6 A.mabeei
                       M1
                                    0.909 0.308
## 7 A.texanum
                       M1
                                    0.972 0.910
## 8 A.annulatum
                       M1
                                    0.885 0.293
## 9 A.tigrinum
                       M1
                                    0.787 0.00136
## 10 A.mavortium
                       M1
                                    0.961 0.791
## # ... with 50 more rows
# Check Multivariate normality:FAIL
Atlas_wofossil_noTub_sub %>% dplyr::select(, 1:6) %>% mshapiro_test()
## # A tibble: 1 x 2
    statistic p.value
##
         <dbl>
                  <db1>
         0.482 4.95e-18
## 1
# Identify multicollinearity:FAIL
Atlas_wofossil_noTub_sub %>% cor_test(, 1:6)
## # A tibble: 36 x 8
##
      var1 var2
                                         p conf.low conf.high method
                    cor statistic
##
      <chr> <chr> <dbl>
                            <dbl>
                                     <dbl>
                                              <dbl>
                                                        <dbl> <chr>
##
                                  0.
   1 M1
            M1
                            Inf
                                                               Pearson
                   1
                                              1
                                                         1
                   0.94
##
   2 M1
           M2
                             30.2 1.02e-54
                                              0.921
                                                        0.962 Pearson
## 3 M1
           МЗ
                   0.85
                             17.1 1.29e-32
                                              0.793
                                                        0.897 Pearson
## 4 M1
           M4
                   0.93
                             25.9 2.59e-48
                                              0.896
                                                        0.950 Pearson
                  0.93
## 5 M1
           M5
                             27.0 4.50e-50
                                              0.903
                                                        0.953 Pearson
## 6 M1
           M6
                   0.76
                             12.1 7.33e-22
                                              0.664
                                                        0.827 Pearson
## 7 M2
                                                        0.962 Pearson
           M1
                   0.94
                             30.2 1.02e-54
                                              0.921
## 8 M2
           M2
                   1
                            Inf
                                 0.
                                              1
                                                        1
                                                               Pearson
## 9 M2
            МЗ
                   0.92
                             23.8 5.21e-45
                                              0.880
                                                        0.942 Pearson
## 10 M2
                   0.92
                             24.8 1.22e-46
                                              0.888
                                                        0.946 Pearson
           M4
## # ... with 26 more rows
# PROBLEM!!: Absence of multicollinearity. The dependent (outcome) variables
# cannot be too correlated to each other. No correlation should be above r =
# 0.90 [Tabachnick and Fidell (2012)].
cor(Atlas_wofossil_noTub_sub[, 1:6])
                       M2
                                 МЗ
                                           M4
## M1 1.0000000 0.9449857 0.8533793 0.9272517 0.9326445 0.7568932
## M2 0.9449857 1.0000000 0.9158753 0.9217077 0.8823482 0.7989239
## M3 0.8533793 0.9158753 1.0000000 0.8476626 0.8159639 0.7816608
## M4 0.9272517 0.9217077 0.8476626 1.0000000 0.9208258 0.7833759
## M5 0.9326445 0.8823482 0.8159639 0.9208258 1.0000000 0.7618434
```

MANOVA#:*Failed multiple checks

```
Atlas.man <- manova(cbind(M1, M2, M3, M4, M5, M6) ~ species, data = Atlas_wofossil_noTub_sub)
summary(Atlas.man)
##
             Df Pillai approx F num Df den Df
                                                Pr(>F)
                                   54
## species
              9 2.1061
                          6.07
                                         606 < 2.2e-16 ***
## Residuals 101
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary.aov(Atlas.man)
   Response M1:
##
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
                9 40.104 4.4560 27.517 < 2.2e-16 ***
## species
## Residuals
              101 16.355 0.1619
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
   Response M2:
               {\tt Df \; Sum \; Sq \; Mean \; Sq \; F \; value}
                9 37.119 4.1244 26.124 < 2.2e-16 ***
## species
             101 15.945 0.1579
## Residuals
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
   Response M3:
##
               Df Sum Sq Mean Sq F value
                9 5.5115 0.61239 21.615 < 2.2e-16 ***
## species
## Residuals
              101 2.8615 0.02833
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Response M4:
##
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
                9 21.584 2.39828 16.607 < 2.2e-16 ***
## species
## Residuals 101 14.586 0.14441
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
   Response M5:
##
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
                9 52.724 5.8582 35.407 < 2.2e-16 ***
## Residuals
             101 16.711 0.1655
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Response M6:
##
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
              9 8.1785 0.90872 9.1615 4.933e-10 ***
## species
## Residuals 101 10.0181 0.09919
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Permutation MANOVA ## *Overcome failed checks

```
# Permutational Multivariate Analysis of Variance Using Distance Matrices
adonis(Atlas_wofossil_noTub_sub[, 1:6] ~ species, data = Atlas_wofossil_noTub_sub,
   method = "euclidean")
##
## Call:
## adonis(formula = Atlas_wofossil_noTub_sub[, 1:6] ~ species, data = Atlas_wofossil_noTub_sub,
## Permutation: free
## Number of permutations: 999
## Terms added sequentially (first to last)
##
##
              Df SumsOfSqs MeanSqs F.Model
                                                R2 Pr(>F)
                   165.222 18.3580 24.245 0.68359 0.001 ***
## species
## Residuals 101
                   76.477 0.7572
                                           0.31641
## Total
             110
                   241.698
                                           1.00000
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# pairwise comparisons between group levels with corrections for multiple
# testing
pairwise.perm.manova(Atlas_wofossil_noTub_sub[, 1:6], Atlas_wofossil_noTub_sub$species,
   nperm = 50, progress = FALSE) #needs more permutation but takes a long time
##
## Pairwise comparisons using permutation MANOVAs (test: Pillai)
##
## data: Atlas_wofossil_noTub_sub[, 1:6] by Atlas_wofossil_noTub_sub$species
## 50 permutations
##
##
                    A.gracile A.maculatum A.macrodactylum A.opacum
## A.maculatum
                    0.022
## A.macrodactylum
                   0.022
                              0.022
                    0.098
                              0.022
                                          0.022
## A.opacum
## A.jeffersonianum 0.062
                              0.022
                                          0.022
                                                          0.080
## A.mabeei
                    0.022
                              0.022
                                          0.043
                                                          0.022
## A.texanum
                    0.022
                              0.022
                                          0.022
                                                          0.022
## A.annulatum
                    0.022
                              0.022
                                          0.022
                                                          0.022
## A.tigrinum
                    0.022
                              0.022
                                          0.022
                                                          0.022
## A.mavortium
                    0.062
                              0.022
                                          0.022
                                                          0.022
                    A. jeffersonianum A. mabeei A. texanum A. annulatum A. tigrinum
## A.maculatum
## A.macrodactylum
## A.opacum
## A.jeffersonianum -
## A.mabeei
                    0.022
## A.texanum
                    0.022
                                     0.022
## A.annulatum
                    0.022
                                     0.022
                                              0.022
```

me

```
## A.tigrinum
                   0.022
                                    0.022
                                             0.022
                                                       0.022
## A.mavortium
                   0.022
                                    0.022
                                             0.022
                                                       0.022
                                                                  0.022
## P value adjustment method: fdr
# or using euclidean distances
AtlasPPM <- pairwise.perm.manova(dist(Atlas_wofossil_noTub_sub[, 1:6], "euclidean"),
    Atlas_wofossil_noTub_sub$species, nperm = 999)
AtlasPPM
##
   Pairwise comparisons using permutation MANOVAs on a distance matrix
## data: dist(Atlas_wofossil_noTub_sub[, 1:6], "euclidean") by Atlas_wofossil_noTub_sub$species
## 999 permutations
##
##
                   A.gracile A.maculatum A.macrodactylum A.opacum
## A.maculatum
                   0.0048
## A.macrodactylum 0.0021
                             0.0021
                             0.0021
## A.opacum
                   0.0106
                                         0.0021
## A.jeffersonianum 0.2500
                             0.0021
                                         0.0021
                                                        0.0078
## A.mabeei
                 0.0021
                           0.0021
                                         0.1237
                                                        0.0098
## A.texanum
                   0.0090
                             0.0037
                                         0.0021
                                                        0.0037
## A.annulatum
                 0.0857
                                         0.0037
                             0.0048
                                                        0.0098
## A.tigrinum
                   0.0178
                             0.0263
                                         0.0021
                                                         0.0021
## A.mavortium
                   0.0116
                             0.0178
                                         0.0021
                                                         0.0021
                   A.jeffersonianum A.mabeei A.texanum A.annulatum A.tigrinum
## A.maculatum
## A.macrodactylum
## A.opacum
## A.jeffersonianum -
## A.mabeei
                   0.0021
## A.texanum
                   0.0106
                                    0.0021
## A.annulatum
                   0.1237
                                    0.0021
                                             0.0231
                                    0.0021 0.0021
                                                      0.0048
## A.tigrinum
                   0.0021
## A.mavortium
                   0.0021
                                    0.0021 0.0048
                                                      0.0125
                                                                  0.0259
## P value adjustment method: fdr
```

tuberculum interglenoideum measurement only

##

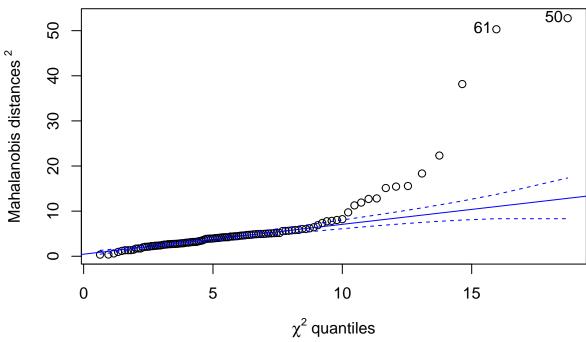
```
## Permutation Analysis of Variance Table
##
## Response: Atlas_wofossil_Tub_only$tub_interglen_extension
## 1000 permutations
                                    Sum Sq Df Mean Sq F value
## Atlas wofossil Tub only$species 0.79265 9 0.088073 16.161 0.000999 ***
## Residuals
                                    0.43597 80 0.005450
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# pairwise comparisons between group levels with corrections for multiple
# testing
library(rcompanion)
##
## Attaching package: 'rcompanion'
## The following object is masked from 'package:psych':
##
##
PT <- pairwisePermutationTest(tub_interglen_extension ~ species, data = Atlas_wofossil_Tub_only,
    method = "fdr")
PT
##
                                  Comparison
                                                  Stat
                                                         p.value p.adjust
## 1
                 A.gracile - A.maculatum = 0
                                                -2.822
                                                        0.004772 0.014320
## 2
             A.gracile - A.macrodactylum = 0
                                                 2.412
                                                         0.01585 0.031010
## 3
                    A.gracile - A.opacum = 0
                                                         0.02051 0.032960
                                                -2.317
## 4
            A.gracile - A.jeffersonianum = 0
                                               -0.9899
                                                          0.3222 0.362500
## 5
                    A.gracile - A.mabeei = 0
                                                 0.539
                                                          0.5899 0.617300
## 6
                   A.gracile - A.texanum = 0
                                                -2.611
                                                       0.009034 0.021400
## 7
                 A.gracile - A.annulatum = 0
                                               -0.3469
                                                          0.7287 0.745300
## 8
                  A.gracile - A.tigrinum = 0
                                                 2.177
                                                         0.02947 0.044200
## 9
                 A.gracile - A.mavortium = 0
                                                 2.255
                                                         0.02415 0.037470
## 10
           A.maculatum - A.macrodactylum = 0
                                                 3.711 0.0002068 0.002126
## 11
                  A.maculatum - A.opacum = 0
                                                 1.505
                                                          0.1323 0.170100
## 12
          A.maculatum - A.jeffersonianum = 0
                                                 2.361
                                                         0.01823 0.032800
## 13
                  A.maculatum - A.mabeei = 0
                                                  3.31
                                                        0.000934 0.004203
## 14
                 A.maculatum - A.texanum = 0
                                                0.7083
                                                          0.4788 0.513000
## 15
               A.maculatum - A.annulatum = 0
                                                 2.744
                                                         0.00607 0.016070
## 16
                A.maculatum - A.tigrinum = 0
                                                   3.9 9.615e-05 0.002126
## 17
               A.maculatum - A.mavortium = 0
                                                 3.798 0.000146 0.002126
## 18
              A.macrodactylum - A.opacum = 0
                                                -3.564 0.0003649 0.002126
## 19 A.macrodactylum - A.jeffersonianum = 0
                                                -3.043
                                                       0.002342 0.008107
## 20
              A.macrodactylum - A.mabeei = 0
                                                -2.511
                                                         0.01205 0.024650
## 21
             A.macrodactylum - A.texanum = 0
                                                  -3.6 0.0003188 0.002126
## 22
           A.macrodactylum - A.annulatum = 0
                                                -3.144 0.001667 0.006450
## 23
            A.macrodactylum - A.tigrinum = 0 -0.04369
                                                          0.9652 0.965200
## 24
           A.macrodactylum - A.mavortium = 0
                                                           0.262 0.318200
                                                 1.122
## 25
             A.opacum - A.jeffersonianum = 0
                                                 1.699
                                                         0.08939 0.120000
## 26
                     A.opacum - A.mabeei = 0
                                                 2.913
                                                        0.003578 0.011500
## 27
                    A.opacum - A.texanum = 0
                                               -0.8956
                                                          0.3705 0.406600
## 28
                  A.opacum - A.annulatum = 0
                                                 2.347
                                                         0.01895 0.032800
## 29
                   A.opacum - A.tigrinum = 0
                                                  3.62 0.0002945 0.002126
## 30
                  A.opacum - A.mavortium = 0
                                                 3.433 0.0005967 0.002984
```

```
## 31
             A.jeffersonianum - A.mabeei = 0
                                                 1.692
                                                          0.09068 0.120000
## 32
                                                         0.03296 0.046350
            A.jeffersonianum - A.texanum = 0
                                                -2.133
## 33
                                                          0.3089 0.356400
          A.jeffersonianum - A.annulatum = 0
                                                 1.017
                                                 2.771
## 34
           A.jeffersonianum - A.tigrinum = 0
                                                         0.00559 0.015720
## 35
          A.jeffersonianum - A.mavortium = 0
                                                 2.548
                                                         0.01084 0.023230
## 36
                                                -3.135
                    A.mabeei - A.texanum = 0
                                                         0.00172 0.006450
## 37
                                                -1.106
                                                          0.2687 0.318200
                  A.mabeei - A.annulatum = 0
                   A.mabeei - A.tigrinum = 0
## 38
                                                 2.139
                                                         0.03245 0.046350
## 39
                  A.mabeei - A.mavortium = 0
                                                  2.32
                                                          0.02033 0.032960
## 40
                 A.texanum - A.annulatum = 0
                                                 2.612 0.009011 0.021400
## 41
                  A.texanum - A.tigrinum = 0
                                                 3.725 0.0001954 0.002126
## 42
                                                        0.000378 0.002126
                 A.texanum - A.mavortium = 0
                                                 3.555
## 43
                A.annulatum - A.tigrinum = 0
                                                 2.562
                                                         0.01041 0.023230
               A.annulatum - A.mavortium = 0
## 44
                                                 2.355
                                                         0.01852 0.032800
## 45
                A.tigrinum - A.mavortium = 0
                                                 1.206
                                                          0.2279 0.284900
pairwise.perm.t.test(Atlas_wofossil_Tub_only$tub_interglen_extension, Atlas_wofossil_Tub_only$species,
    nperm = 999, progress = FALSE)
##
##
   Pairwise comparisons using permutation t tests
##
## data: Atlas_wofossil_Tub_only$tub_interglen_extension and Atlas_wofossil_Tub_only$species
## 999 permutations
##
##
                    A.gracile A.maculatum A.macrodactylum A.opacum
## A.maculatum
                    0.0086
## A.macrodactylum
                    0.0086
                               0.0060
## A.opacum
                    0.0310
                               0.1646
                                           0.0060
## A.jeffersonianum 0.3951
                               0.0208
                                           0.0060
                                                            0.0982
## A.mabeei
                    0.6300
                               0.0060
                                                            0.0086
                                           0.0123
## A.texanum
                    0.0157
                               0.5679
                                           0.0060
                                                            0.3951
                                                            0.0377
## A.annulatum
                    0.7732
                               0.0060
                                           0.0060
## A.tigrinum
                    0.0267
                               0.0060
                                           0.9840
                                                            0.0060
## A.mavortium
                    0.0208
                               0.0060
                                           0.3089
                                                            0.0060
##
                    A.jeffersonianum A.mabeei A.texanum A.annulatum A.tigrinum
## A.maculatum
## A.macrodactylum
## A.opacum
## A.jeffersonianum -
## A.mabeei
                    0.1350
## A.texanum
                    0.0394
                                      0.0060
## A.annulatum
                    0.3197
                                      0.3669
                                               0.0086
## A.tigrinum
                    0.0060
                                      0.0360
                                               0.0060
                                                          0.0187
## A.mavortium
                    0.0086
                                      0.0310
                                               0.0060
                                                          0.0086
                                                                      0.2775
## P value adjustment method: fdr
```

DFA

```
# PROBLEM:Check Multivariate normality:FAIL
mqqnorm(Atlas_wofossil_noTub_sub[, 1:6], main = "Multi-normal Q-Q Plot")
```

Multi-normal Q-Q Plot



```
## [1] 50 61
# DFA# With MASS
library(MASS)
##
## Attaching package: 'MASS'
## The following object is masked from 'package:rstatix':
##
##
       select
## The following object is masked from 'package:EnvStats':
##
##
       boxcox
## The following object is masked from 'package:dplyr':
##
##
       select
AtlasLDA <- lda(species ~ M1 + M2 + M3 + M4 + M5 + M6, data = Atlas_wofossil_noTub_sub,
    CV = FALSE) #DFA no jacknife
AtlasLDA
## Call:
## lda(species ~ M1 + M2 + M3 + M4 + M5 + M6, data = Atlas_wofossil_noTub_sub,
       CV = FALSE)
##
## Prior probabilities of groups:
##
          A.gracile
                         A.maculatum A.macrodactylum
                                                                A.opacum
##
         0.07207207
                          0.12612613
                                            0.10810811
                                                             0.11711712
## A.jeffersonianum
                            A.mabeei
                                             A.texanum
                                                            A.annulatum
                          0.08108108
                                            0.08108108
```

0.05405405

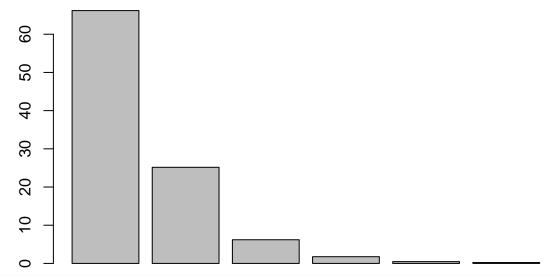
##

0.09909910

```
##
         A.tigrinum
                         A.mavortium
##
         0.15315315
                          0.10810811
##
## Group means:
##
                          M1
                                  M2
                                             МЗ
                   3.301250 3.227500 1.1475000 2.425000 3.305000 1.1750000
## A.gracile
## A.maculatum
                   3.542143 3.787143 1.4935714 2.729286 3.442857 1.4521429
## A.macrodactylum
                   2.200833 2.234167 0.8316667 1.655000 2.088333 0.8066667
## A.opacum
                    2.709231 2.836154 1.0546154 1.982308 2.799231 1.0130769
## A.jeffersonianum 3.144545 3.211818 1.1481818 2.434545 2.997273 1.1618182
## A.mabeei
                   2.218889 2.440000 0.9411111 1.713333 2.268889 0.9200000
                   3.011111 3.490000 1.3822222 2.382222 2.864444 1.3155556
## A.texanum
                   3.305000 3.373333 1.2583333 2.400000 2.808333 1.2500000
## A.annulatum
                   3.534118 3.487059 1.3176471 2.744706 3.968235 1.4082353
## A.tigrinum
## A.mavortium
                   4.222500 4.206667 1.5216667 3.038333 4.310833 1.7458333
##
## Coefficients of linear discriminants:
##
             LD1
                        LD2
                                   LD3
                                               LD4
                                                         LD5
                                                                      LD6
## M1
      0.55663683 -0.8606379 -5.5795956 -0.3483209
                                                   2.989576
                                                             1.097501598
      0.86359598 -2.5415371 1.9312656 -3.1297756 -4.765508
                                                             0.001897505
## M3
      4.33837399 -3.6814217 4.6634719 2.8925828 6.711399
                                                            2.898321950
      3.68648363 0.3634334 -0.8034773 5.2104307 -1.277601 -1.351860806
## M5 -7.27345664 2.1171683 2.6638922 -0.7621234 -0.491493 0.461170573
##
## Proportion of trace:
##
      LD1
            LD2
                   LD3
                           LD4
                                  LD5
                                         LD6
## 0.6619 0.2516 0.0620 0.0176 0.0047 0.0023
AtlasLDA_jack <- lda(species ~ M1 + M2 + M3 + M4 + M5 + M6, data = Atlas_wofossil_noTub_sub,
    CV = TRUE) #DFA with jacknife
# Assess the accuracy of jacknife #
accAtlasLDA <- table(Atlas_wofossil_noTub_sub$species, AtlasLDA_jack$class)</pre>
accAtlasLDA
##
##
                      A.gracile A.maculatum A.macrodactylum A.opacum
##
     A.gracile
                              3
                                          0
                                                          0
                                                                   2
                              0
                                         12
                                                          0
                                                                   0
##
     A.maculatum
##
                              0
                                          0
                                                          9
                                                                   0
     A.macrodactylum
                                                          0
                                                                   9
##
     A.opacum
                              0
                                          1
##
     A.jeffersonianum
                              1
                                          2
                                                          0
                                                                   2
                                          0
##
     A.mabeei
                              0
                                                          3
                                                                   1
##
     A.texanum
                              0
                                          2
                                                          0
                                                                   0
##
     A.annulatum
                              0
                                          0
                                                          0
                                                                   0
##
     A.tigrinum
                              2
                                          0
                                                          0
                                                                   0
##
     A.mavortium
                              1
                                          2
                                                          0
##
##
                      A.jeffersonianum A.mabeei A.texanum A.annulatum A.tigrinum
##
                                                                               0
     A.gracile
                                     2
                                              0
                                                        0
                                                                    0
                                     0
                                              0
                                                        2
                                                                    0
                                                                               0
##
     A.maculatum
                                     0
                                              3
                                                        0
                                                                    0
                                                                               0
##
     A.macrodactylum
##
     A.opacum
                                     2
                                              1
                                                        0
                                                                    0
                                                                               0
##
     A. jeffersonianum
                                     5
                                                        0
                                                                               0
                                              1
                                                                    0
##
     A.mabeei
                                              5
                                                                               0
```

```
0
                                                0
                                                                       0
                                                                                   0
##
     A.texanum
                                       0
                                                0
##
     A.annulatum
                                                                       5
                                                                                   0
     A.tigrinum
                                       0
                                                0
                                                           0
                                                                       0
                                                                                  14
##
##
     A.mavortium
                                       0
                                                0
                                                           0
                                                                       0
                                                                                   4
##
##
                       A.mavortium
##
     A.gracile
     A.maculatum
##
                                 0
##
     A.macrodactylum
                                 0
##
     A.opacum
                                 0
##
     A.jeffersonianum
                                 0
##
     A.mabeei
                                 0
##
     A.texanum
                                 0
                                 0
##
     A.annulatum
##
     A.tigrinum
                                 1
##
     A.mavortium
diag(prop.table(accAtlasLDA, 1))
##
          A.gracile
                          A.maculatum A.macrodactylum
                                                                 A.opacum
##
          0.3750000
                            0.8571429
                                              0.7500000
                                                                0.6923077
## A.jeffersonianum
                             A.mabeei
                                              A.texanum
                                                              A.annulatum
##
          0.4545455
                            0.555556
                                              0.7777778
                                                                0.8333333
##
         A.tigrinum
                          A.mavortium
          0.8235294
                            0.3333333
sum(accAtlasLDA[row(accAtlasLDA) == col(accAtlasLDA)])/sum(accAtlasLDA)
## [1] 0.6576577
# DFA# With MORPHO
```





get the typicality probabilities and resulting classifications all
specimens with a probability of < 0.01 as outliers (assigned to no class)
typprobs <- typprobClass(Atlascva\$CVscores, groups = Atlas_wofossil_noTub_sub\$species,</pre>

```
cross-validated classification results in frequencies
##
##
                       A.annulatum A.gracile A.jeffersonianum A.mabeei
##
     A.gracile
                                  0
                                                               2
                                  0
                                             0
                                                               0
                                                                         0
##
     A.maculatum
                                  0
                                             0
                                                               0
                                                                         3
##
     A.macrodactylum
                                                               2
     A.opacum
                                  0
                                             0
                                                                         1
##
##
     A.jeffersonianum
                                  0
                                             2
                                                               6
                                                                         1
##
     A.mabeei
                                  0
                                             0
                                                               0
                                                                         7
##
     A.texanum
                                             0
                                                               0
                                                                         0
                                  1
                                  5
                                             0
                                                               0
                                                                         0
##
     A.annulatum
##
     A.tigrinum
                                  0
                                             2
                                                               0
                                                                         0
                                                                         0
##
     A.mavortium
                                  0
                                             1
                                                               0
##
##
                       A.macrodactylum A.maculatum A.mavortium A.opacum A.texanum
##
                                                   0
     A.gracile
                                      0
                                                                          2
                                                                                     0
                                                                1
##
     A.maculatum
                                      0
                                                  11
                                                                0
                                                                          0
                                                                                     2
                                      9
##
                                                   0
                                                                          0
                                                                                     0
     A.macrodactylum
                                                                0
##
     A.opacum
                                      0
                                                   1
                                                                0
                                                                          9
                                                                                     0
##
     A.jeffersonianum
                                      0
                                                   1
                                                                0
                                                                          0
                                                                                     1
##
     A.mabeei
                                      2
                                                   0
                                                                0
                                                                          0
                                                                                     0
                                                                                     7
     A.texanum
                                      0
                                                                0
                                                                          0
##
                                                   1
     A.annulatum
                                      0
                                                   0
                                                                          0
##
                                                                0
                                                                                     1
##
     A.tigrinum
                                      0
                                                   0
                                                                1
                                                                          0
                                                                                     0
##
     A.mavortium
                                      0
                                                   1
                                                                4
                                                                          1
                                                                                     0
##
##
                       A.tigrinum none
##
     A.gracile
                                 0
                                      0
##
     A.maculatum
                                 0
                                       1
##
     A.macrodactylum
                                 0
                                      0
                                 0
                                      0
##
     A.opacum
##
     A.jeffersonianum
                                 0
                                      0
                                      0
##
     A.mabeei
                                 0
##
     A.texanum
                                 0
                                      0
                                      0
##
     A.annulatum
                                 0
##
                                12
                                      2
     A.tigrinum
                                       2
##
     A.mavortium
                                 3
##
##
    cross-validated classification result in %
##
##
##
                       A.annulatum A.gracile A.jeffersonianum A.mabeei
##
     A.gracile
                             0.0000
                                      37.5000
                                                         25.0000
                                                                    0.0000
##
     A.maculatum
                             0.0000
                                       0.0000
                                                          0.0000
                                                                    0.0000
                             0.0000
                                       0.0000
                                                          0.0000 25.0000
##
     A.macrodactylum
##
     A.opacum
                             0.0000
                                       0.0000
                                                         15.3846
                                                                   7.6923
##
     A.jeffersonianum
                             0.0000
                                       18.1818
                                                         54.5455
                                                                    9.0909
##
     A.mabeei
                             0.0000
                                       0.0000
                                                          0.0000 77.7778
##
     A.texanum
                            11.1111
                                       0.0000
                                                          0.0000
                                                                    0.0000
                                                          0.0000
                                                                    0.0000
##
     A.annulatum
                            83.3333
                                       0.0000
##
     A.tigrinum
                             0.0000
                                      11.7647
                                                          0.0000
                                                                    0.0000
```

outlier = 0.01, cv = TRUE)

print(typprobs)

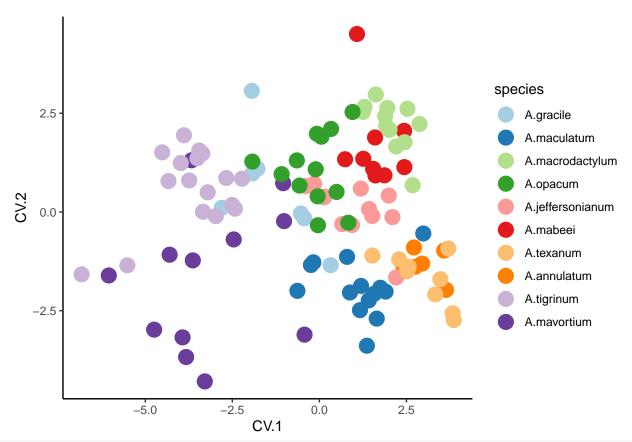
```
0.0000
                                       8.3333
                                                         0.0000
                                                                   0.0000
##
     A.mavortium
##
##
                       A.macrodactylum A.maculatum A.mavortium A.opacum A.texanum
##
                                 0.0000
                                             0.0000
                                                         12.5000
                                                                  25.0000
                                                                              0.0000
     A.gracile
                                 0.0000
##
     A.maculatum
                                            78.5714
                                                          0.0000
                                                                    0.0000
                                                                             14.2857
##
     A.macrodactylum
                               75.0000
                                             0.0000
                                                          0.0000
                                                                    0.0000
                                                                              0.0000
##
     A.opacum
                                 0.0000
                                             7.6923
                                                          0.0000 69.2308
                                                                              0.0000
##
     A.jeffersonianum
                                             9.0909
                                                          0.0000
                                                                    0.0000
                                                                              9.0909
                                 0.0000
##
     A.mabeei
                               22.2222
                                             0.0000
                                                          0.0000
                                                                    0.0000
                                                                              0.0000
##
     A.texanum
                                                          0.0000
                                                                    0.0000
                                 0.0000
                                            11.1111
                                                                             77.7778
##
     A.annulatum
                                 0.0000
                                             0.0000
                                                          0.0000
                                                                    0.0000
                                                                             16.6667
##
                                 0.0000
                                             0.0000
                                                                    0.0000
     A.tigrinum
                                                          5.8824
                                                                              0.0000
                                 0.0000
                                                         33.3333
                                                                    8.3333
                                                                              0.0000
##
     A.mavortium
                                             8.3333
##
##
                       A.tigrinum
                                      none
##
     A.gracile
                           0.0000 0.0000
##
     A.maculatum
                           0.0000 7.1429
                           0.0000 0.0000
##
     A.macrodactylum
##
     A.opacum
                           0.0000 0.0000
##
     A. jeffersonianum
                           0.0000 0.0000
##
     A.mabeei
                           0.0000 0.0000
##
     A.texanum
                           0.0000 0.0000
##
     A.annulatum
                           0.0000 0.0000
##
     A.tigrinum
                          70.5882 11.7647
##
     A.mavortium
                          25.0000 16.6667
##
##
    overall classification accuracy: 65.76577 %
# Assess the accuracy of jacknife #
accJack <- table(Atlascva$groups, Atlascva$class)</pre>
accJack
##
##
                       A.gracile A.maculatum A.macrodactylum A.opacum
##
                                            0
                                                                       2
     A.gracile
                                                             0
                               0
                                                             0
                                                                       0
##
     A.maculatum
                                           12
##
     A.macrodactylum
                               0
                                            0
                                                             9
                                                                       0
##
     A.opacum
                               0
                                            1
                                                             0
                                                                       9
                                            2
                                                                       2
##
     A.jeffersonianum
                                                             0
##
     A.mabeei
                               0
                                            0
                                                             3
                                                                       1
                                            2
##
     A.texanum
                               0
                                                             0
                                                                       0
                               0
                                            0
                                                             0
                                                                       0
##
     A.annulatum
##
                               2
                                            0
                                                             0
                                                                       0
     A.tigrinum
##
     A.mavortium
                               1
                                            2
                                                             0
                                                                       1
##
##
                       A.jeffersonianum A.mabeei A.texanum A.annulatum A.tigrinum
                                       2
                                                0
                                                           0
                                                                                    0
##
     A.gracile
                                                                        0
                                       0
##
     A.maculatum
                                                 0
                                                           2
                                                                        0
                                                                                    0
                                       0
                                                 3
                                                           0
                                                                        0
                                                                                    0
##
     A.macrodactylum
                                       2
##
                                                 1
                                                           0
                                                                        0
                                                                                    0
     A.opacum
                                       5
                                                                                    0
##
     A.jeffersonianum
                                                 1
                                                           0
                                                                        0
                                       0
                                                                        0
                                                                                    0
##
     A.mabeei
                                                5
                                                           0
                                       0
##
     A.texanum
                                                0
                                                           7
                                                                        0
                                                                                    0
     A.annulatum
                                       0
                                                 0
                                                                        5
                                                                                    0
##
```

```
A.tigrinum
                                      0
                                                                                 14
##
     A.mavortium
##
##
##
                       A.mavortium
     A.gracile
##
     A.maculatum
##
                                 0
     A.macrodactylum
##
                                 0
     A.opacum
##
                                 0
     A.jeffersonianum
##
                                 0
##
     A.mabeei
                                 0
##
     A.texanum
                                 0
     A.annulatum
##
                                 0
##
     A.tigrinum
                                 1
     A.mavortium
##
diag(prop.table(accJack, 1))
##
          A.gracile
                          A.maculatum A.macrodactylum
                                                                A.opacum
##
          0.3750000
                            0.8571429
                                             0.7500000
                                                               0.6923077
                             A.mabeei
                                              A.texanum
                                                             A.annulatum
## A.jeffersonianum
          0.4545455
                            0.5555556
                                              0.7777778
                                                               0.8333333
##
         A.tigrinum
                          A.mavortium
          0.8235294
                            0.3333333
##
sum(accJack[row(accJack) == col(accJack)])/sum(accJack)
```

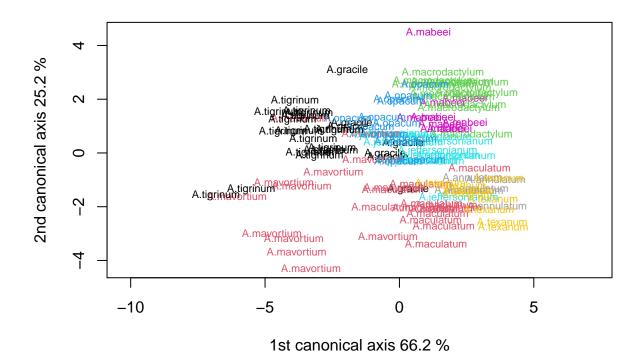
[1] 0.6576577

Plot first two DF axes

```
AT_cva <- data.frame(Atlascva$CVscores, species = Atlascva$groups)
ggplot(AT_cva, aes(CV.1, CV.2)) + geom_point(size = 5, aes(color = species)) +
    theme_classic() + scale_color_brewer(palette = "Paired")</pre>
```

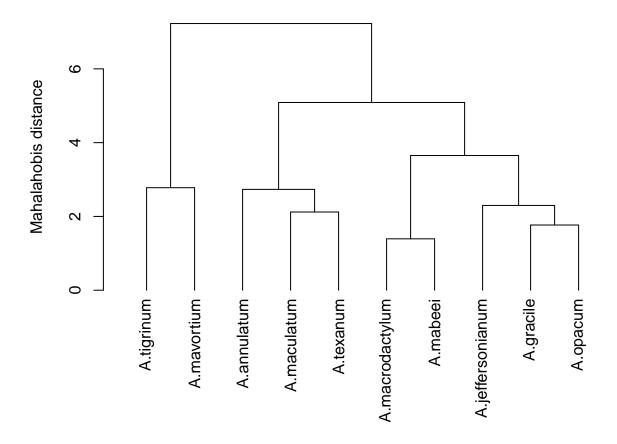


alternative plot



Plot Mahalahobis distances as dendrogram

```
dendroS = hclust(Atlascva$Dist$GroupdistMaha)
dendroS$labels = levels(Atlas_wofossil_noTub_sub$species)
par(mar = c(6.5, 4.5, 1, 1))
dendroS = as.dendrogram(dendroS)
plot(dendroS, main = "", sub = "", xlab = "", ylab = "Mahalahobis distance")
```



Random Forest ###:Non-parametric

```
library(randomForest)
## randomForest 4.6-14
## Type rfNews() to see new features/changes/bug fixes.
##
## Attaching package: 'randomForest'
##
  The following object is masked from 'package:gridExtra':
##
##
       combine
##
  The following object is masked from 'package:psych':
##
##
       outlier
  The following object is masked from 'package:ggplot2':
##
##
##
       margin
## The following object is masked from 'package:dplyr':
##
##
       combine
Atlas.rf <- randomForest(species ~ M1 + M2 + M3 + M4 + M5 + M6, data = Atlas_wofossil_noTub_sub,
    importance = TRUE, proximity = TRUE)
```

```
print(Atlas.rf)
##
## Call:
    randomForest(formula = species ~ M1 + M2 + M3 + M4 + M5 + M6,
                                                                           data = Atlas_wofossil_noTub_sub,
##
                   Type of random forest: classification
##
                         Number of trees: 500
## No. of variables tried at each split: 2
##
           OOB estimate of error rate: 37.84%
##
## Confusion matrix:
##
                     A.gracile A.maculatum A.macrodactylum A.opacum
## A.gracile
                             0
                                          1
                                         12
                                                           0
## A.maculatum
                             0
                                                                     1
                             0
                                          0
                                                          10
                                                                     1
## A.macrodactylum
## A.opacum
                             1
                                          0
                                                           2
                                                                     7
## A.jeffersonianum
                             1
                                          0
                                                           0
                                                                     3
## A.mabeei
                             0
                                          0
                                                           3
                                                                     1
                             0
                                          0
                                                           0
## A.texanum
                                                                     1
## A.annulatum
                                          0
                                                           0
                                                                     0
                                          2
## A.tigrinum
                             0
                                                           0
                                                                     0
## A.mavortium
                                          0
                                                           0
                                                                     1
##
                     A.jeffersonianum A.mabeei A.texanum A.annulatum A.tigrinum
## A.gracile
                                     1
                                              0
                                                         0
                                                                      0
                                                                                 3
## A.maculatum
                                     0
                                              0
                                                         0
                                                                      0
                                                                                 0
## A.macrodactylum
                                     0
                                              1
                                                         0
                                                                      0
                                                                                 0
## A.opacum
                                     1
                                              2
                                                         0
                                                                      0
                                                                                 0
## A.jeffersonianum
                                              0
                                                         0
                                                                      2
                                     5
                                                                                 0
## A.mabeei
                                     0
                                              5
                                                         0
                                                                      0
                                                                                 0
## A.texanum
                                     0
                                              0
                                                         7
                                                                      1
                                                                                 0
                                              0
                                                                      2
## A.annulatum
                                     3
                                                         1
                                                                                 0
                                     0
                                              0
                                                         0
                                                                      0
                                                                                13
## A.tigrinum
## A.mavortium
                                                         0
                                                                      0
                                                                                 1
##
                     A.mavortium class.error
## A.gracile
                                    1.0000000
                               1
## A.maculatum
                                    0.1428571
                               1
                                   0.1666667
## A.macrodactylum
## A.opacum
                                   0.4615385
## A.jeffersonianum
                                   0.5454545
## A.mabeei
                               0
                                   0.444444
## A.texanum
                               0
                                   0.222222
## A.annulatum
                                   0.6666667
                               0
## A.tigrinum
                               2
                                    0.2352941
                                    0.3333333
## A.mavortium
rf acc <- Atlas.rf$confusion
rf_acc <- 1 - rf_acc[, 11] # percent correct classification
rf_acc
##
          A.gracile
                          A.maculatum A.macrodactylum
                                                                  A.opacum
                                                                0.5384615
##
          0.0000000
                            0.8571429
                                              0.8333333
## A.jeffersonianum
                             A.mabeei
                                              A.texanum
                                                              A.annulatum
##
          0.4545455
                            0.555556
                                              0.7777778
                                                                0.3333333
```

A.mavortium

##

A.tigrinum

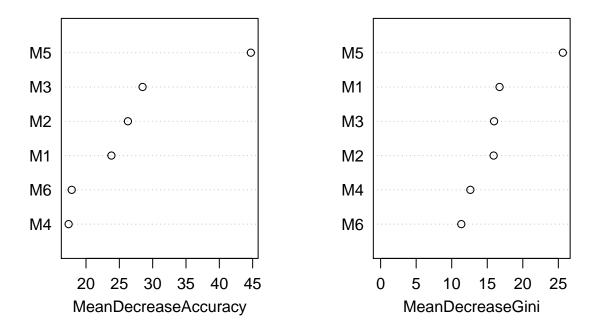
Look at variable importance round(importance(Atlas.rf), 2) ## A.gracile A.maculatum A.macrodactylum A.opacum A.jeffersonianum A.mabeei ## M1 6.14 0.34 11.46 6.79 4.57 17.26 ## M2 -1.98 19.10 20.24 8.11 2.08 7.46 ## M3 -2.57 21.17 12.80 7.88 11.18 1.17 7.29 8.36 ## M4 -0.05 9.17 4.28 6.84 ## M5 6.40 15.53 23.15 9.19 12.69 12.97 ## M6 -1.666.71 11.28 10.61 3.19 4.10 ## A.texanum A.annulatum A.tigrinum A.mavortium MeanDecreaseAccuracy ## M1 10.59 4.43 6.39 17.33 23.81 ## M2 5.95 1.94 1.58 15.02 26.28 ## M3 15.99 10.52 0.54 3.40 28.48 6.54 ## M4 5.59 7.91 0.23 17.39 15.21 30.86 16.50 44.73 ## M5 11.16 ## M6 3.79 -1.068.23 10.29 17.85 ## MeanDecreaseGini 16.73 ## M1 ## M2 15.90 ## M3 15.96 ## M4 12.62 ## M5 25.63 ## M6 11.35 varImpPlot(Atlas.rf)

##

0.7647059

0.6666667

Atlas.rf



K Nearest neighbor ###:Non-parametric

```
library(tidyverse)
library(caret)
## Attaching package: 'caret'
## The following object is masked from 'package:vegan':
##
        tolerance
## The following object is masked from 'package:purrr':
##
##
       lift
Atlas_wofossil_noTub_sub <- column_to_rownames(Atlas_wofossil_noTub_sub, var = "specimen_num")
\#make KNN model using LOOCV to find optimal k
KNNmodel <- train(</pre>
  species ~., data = Atlas_wofossil_noTub_sub, method = "knn",
  trControl = trainControl("LOOCV", number =1),
  preProcess = c("center"), #center the data
  tuneLength = 15)
plot(KNNmodel) # plot accuracy vs k
   Accuracy Leave-One-Out Cross-Validation
        0.65
        0.60
        0.55
        0.50
        0.45
                   5
                                            15
                                                         20
                               10
                                                                      25
                                                                                   30
                                                 #Neighbors
{\tt KNNmodel\$bestTune} \ \textit{\# optimal } k
```

##

k ## 3 9

```
predicted.classes <- KNNmodel %>% predict(Atlas_wofossil_noTub_sub[,1:6]) # predict class based on KNN
head(predicted.classes)
## [1] A.annulatum A.annulatum A.annulatum A.annulatum A.texanum
                                                                       A.texanum
## 10 Levels: A.gracile A.maculatum A.macrodactylum A.opacum ... A.mavortium
mean(predicted.classes == Atlas_wofossil_noTub_sub$species) #overall accuracy
## [1] 0.7387387
# assess accuracy per species
accKNN <- table(Atlas_wofossil_noTub_sub$species,predicted.classes)</pre>
accKNN
##
                      predicted.classes
##
                       A.gracile A.maculatum A.macrodactylum A.opacum
##
     A.gracile
                               0
                                                             0
                                                                       0
                                            1
     A.maculatum
                               0
                                                             0
##
                                           13
                                                                       1
                               0
                                                             11
                                                                       0
##
     A.macrodactylum
                                            0
##
     A.opacum
                               1
                                            0
                                                             2
                                                                       7
                                                                       2
##
     A.jeffersonianum
                               0
                                                             0
                                            1
##
     A.mabeei
                               0
                                            0
                                                             1
                                                                       1
                               0
                                                                       0
##
                                            0
                                                             0
     A.texanum
                                                                       0
##
     A.annulatum
                               0
                                            0
                                                             0
##
     A.tigrinum
                               0
                                            0
                                                             0
                                                                       0
##
                               0
                                                             0
     A.mavortium
                                                                       1
##
                      predicted.classes
##
                       A.jeffersonianum A.mabeei A.texanum A.annulatum A.tigrinum
##
     A.gracile
                                       3
                                                 1
                                                           0
     A.maculatum
                                       0
                                                0
                                                           0
                                                                        0
                                                                                    0
##
##
     A.macrodactylum
                                       0
                                                 1
                                                           0
                                                                        0
                                                                                    0
                                       2
                                                                        0
                                                                                    0
##
                                                 1
                                                           0
     A.opacum
##
     A.jeffersonianum
                                       8
                                                 0
                                                           0
                                                                        0
                                                                                    0
##
     A.mabeei
                                       0
                                                 7
                                                                        0
                                                                                    0
                                                           0
     A.texanum
                                       0
                                                0
                                                                        1
                                                                                    0
##
                                                           8
                                       0
##
     A.annulatum
                                                0
                                                           2
                                                                        4
                                                                                    0
                                       0
                                                 0
                                                           0
                                                                        0
                                                                                   15
##
     A.tigrinum
                                                 0
                                                                        0
##
     A.mavortium
                                                                                    0
                                       1
##
                      predicted.classes
##
                       A.mavortium
##
     A.gracile
                                  0
##
     A.maculatum
                                  0
     A.macrodactylum
##
                                  0
##
     A.opacum
                                  0
##
     A.jeffersonianum
                                  0
##
     A.mabeei
                                  0
##
     A.texanum
                                  0
##
     A.annulatum
                                  0
                                  2
##
     A.tigrinum
     A.mavortium
diag(prop.table(accKNN, 1))
##
          A.gracile
                          A.maculatum A.macrodactylum
                                                                  A.opacum
##
          0.0000000
                            0.9285714
                                              0.9166667
                                                                 0.5384615
```

A.texanum

A.annulatum

A.mabeei

A.jeffersonianum

```
## 0.7272727 0.7777778 0.8888889 0.6666667

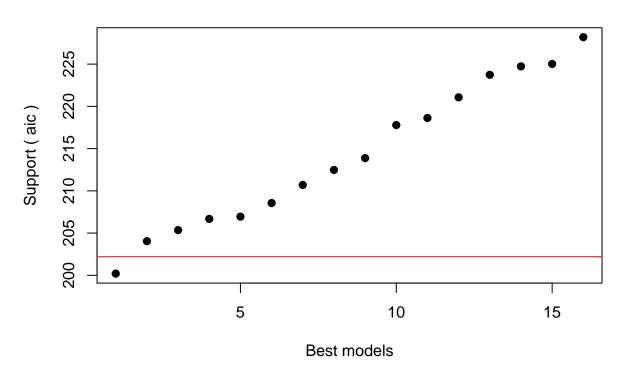
## A.tigrinum A.mavortium

## 0.8823529 0.7500000
```

Model selection (multinominal regression)

```
library(glmulti)
library(nnet)
multinom.glmulti <- function(formula, data, ...) multinom(formula, data, ...)</pre>
res <- glmulti(species ~ ., level = 1, data = Atlas_wofossil_noTub_sub, report = FALSE,
    plotty = FALSE, fitfunction = multinom.glmulti, method = "h", crit = "aic",
    confsetsize = 16)
print(res)
## glmulti.analysis
## Method: h / Fitting: multinom.glmulti / IC used: aic
## Level: 1 / Marginality: FALSE
## From 16 models:
## Best IC: 200.201066755855
## Best model:
## [1] "species ~ 1 + M1 + M3 + M4 + M5 + M6"
## Evidence weight: 0.757413727546765
## Worst IC: 228.189504107244
## 1 models within 2 IC units.
## 3 models to reach 95% of evidence weight.
plot(res)
```

IC profile



```
top <- weightable(res)
top</pre>
```

```
##
                                          model
                                                      aic
                                                               weights
## 1
           species ~ 1 + M1 + M3 + M4 + M5 + M6 200.2011 7.574137e-01
## 2
                species ~ 1 + M1 + M3 + M4 + M5 204.0410 1.110440e-01
## 3
      species ~ 1 + M1 + M2 + M3 + M4 + M5 + M6 205.3535 5.760868e-02
## 4
           species ~ 1 + M1 + M2 + M3 + M4 + M5 206.6808 2.966786e-02
## 5
           species ~ 1 + M2 + M3 + M4 + M5 + M6 206.9433 2.601858e-02
## 6
                species ~ 1 + M3 + M4 + M5 + M6 208.5596 1.159589e-02
## 7
                species ~ 1 + M2 + M3 + M4 + M5 210.7009 3.974899e-03
## 8
                species ~ 1 + M1 + M2 + M3 + M5 212.4752 1.636927e-03
## 9
           species ~ 1 + M1 + M2 + M3 + M5 + M6 213.8743 8.132637e-04
## 10
                     species ~ 1 + M3 + M4 + M5 217.7840 1.151447e-04
## 11
                species ~ 1 + M2 + M3 + M5 + M6 218.6262 7.557261e-05
## 12
                     species ~ 1 + M2 + M3 + M5 221.0684 2.228732e-05
## 13
                     species ~ 1 + M1 + M3 + M5 223.7328 5.881411e-06
## 14
           species ~ 1 + M1 + M2 + M4 + M5 + M6 224.7346 3.564098e-06
## 15
                species ~ 1 + M1 + M3 + M5 + M6 225.0239 3.084009e-06
## 16
                species ~ 1 + M1 + M2 + M4 + M5 228.1895 6.334630e-07
```