

Q1 (a) In the class we showed that the margin is  $\frac{2c}{\|w\|}$  and we want to maximize this margin.

The magnitude of  $c$  is merely scales  $w$  and  $b$  in below

$$\max \frac{2c}{\|w\|} \quad \text{s.t.} \quad y^i (w^T x^i + b) \geq c \quad \forall i$$

and because  $c$  is constant we need to find the optimum value for  $\frac{2c}{\|w\|}$ , we can omit  $c$  and "2".

hence we can find the statement can be replaced by

$$\frac{1}{\|w\|} \quad \text{s.t.} \quad y^i (w^T x^i + b) \geq 1 \quad \forall i$$

Q1 (b) the Lagrangian dual Problem is

$$L(w, a, b) = \frac{1}{2} w w^T + \sum_{i=1}^m a_i (1 - y^i (w^T x^i + b))$$

$$\begin{aligned} \frac{\partial L(w, a, b)}{\partial w} &= w + 0 - \sum_{i=1}^m a_i y^i x^i + 0 = 0 \\ &= w - \sum_{i=1}^m a_i y^i x^i = 0 \Rightarrow w = \sum_{i=1}^m a_i y^i x^i \end{aligned}$$

in the HW question  $n=m$  &  $y^i = y_i$  &  $x^i = x_i$ .