

Q1(a) In the class we showed that the margin is $\frac{2c}{\|w\|}$ and we want to maximize this margin.

The magnitude of c is merely scales w and b in below

$$\max \frac{2c}{\|w\|} \quad \text{s.t.} \quad y^i (w^T x^i + b) \geq c \quad \forall i$$

and because c is constant we need to find the optimum value for $\frac{2c}{\|w\|}$, we can omit c and "2".

hence we can find the statement can be replaced by

$$\frac{1}{\|w\|} \quad \text{s.t.} \quad y^i (w^T x^i + b) \geq 1 \quad \forall i$$

Q1(b) the Lagrangian dual Problem is

$$L(w, a, b) = \frac{1}{2} w w^T + \sum_{i=1}^m a_i (1 - y^i (w^T x^i + b))$$

$$\frac{\partial L(w, a, b)}{\partial w} = w + 0 - \sum_{i=1}^m a_i y^i x^i + 0 = 0$$

$$= w - \sum_{i=1}^m a_i y^i x^i = 0 \Rightarrow w = \sum_{i=1}^m a_i y^i x^i$$

in the HW question $n=m$ & $y^i = y_i$ & $x^i = x_i$.