Intra-Site Spatial Data Recovery and Visualization

Historical Issues:

- 1. Locations of activities what happened where and why?
- 2. Locations of social groups who lived where and why? -class, gender, ethnicity, etc.

Sources of Data: Archaeological Spatial Structure

- 1. patterns in the location of features: *site structure*
 - -buildings
 - -pits
 - -fences
- 2. patterns in the horizontal distribution of artifacts

Patterns in the horizontal distribution of artifacts

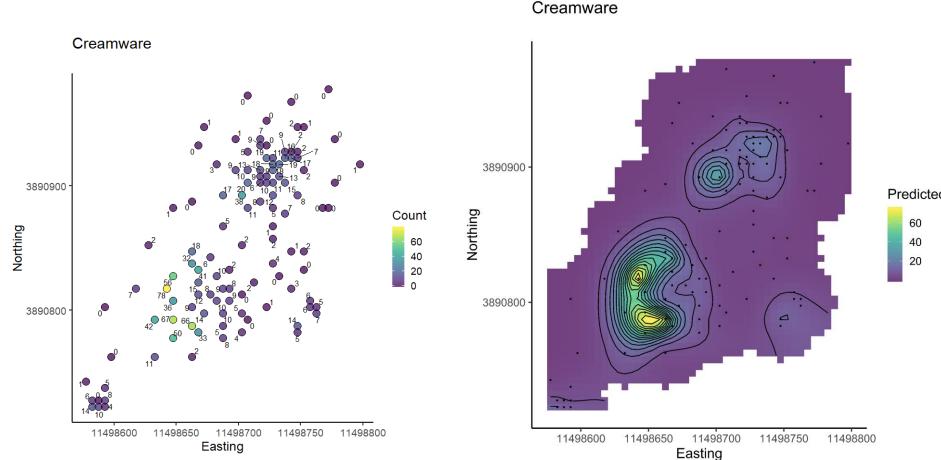
1. The spatial data recovery process

- Model how we collect spatial data.

2. The analysis process

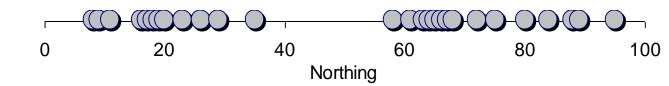
- Mapping raw data and statistical models of them.





Recovery

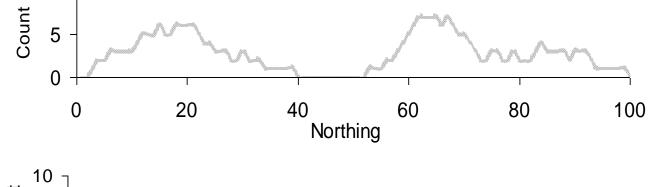
The Point Process:



The Moving-Average Process:

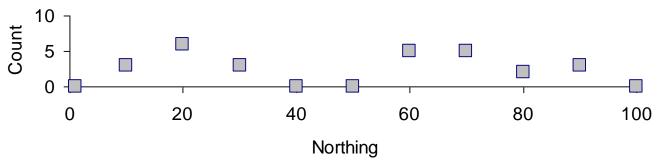
10

(quadrat diameter=10)



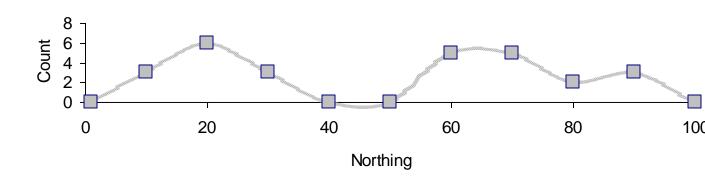
Sample the M-A Process

(quadrat spacing =10)



Analysis

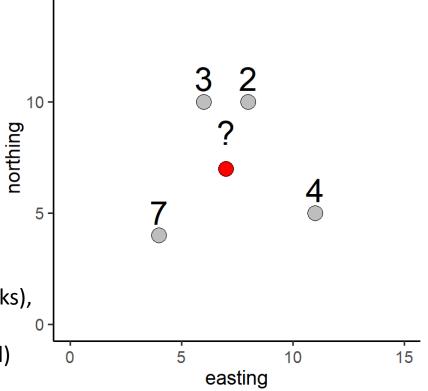
Estimate the M-A Process from the sample:



Interpolation

Many methods...

- 1. Inverse distance weighting (IDW)
- 2. Kriging
- 3. Others
- -TINs (triangulated irregular networks),
- -splines (radial basis functions)
- -polynomial regression (local, global)



1. and 2. both make estimates of value of the z variable at an unsampled point in (x,y) space, as a weighted average of the values at nearby points, where z values are known.

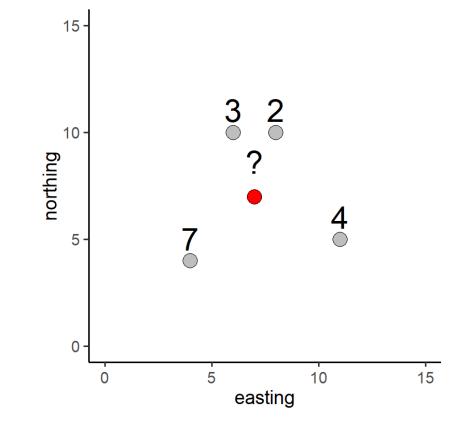
So....

$$\hat{Z}_{j} = \frac{\sum_{i=1}^{n} w_{i} Z_{i}}{\sum_{i=1}^{n} w_{i}}$$

15

Inverse Distance Weighting

$$w_i = \frac{1}{d_{ij}^{p}}$$



Point ID	northing	easting	Z	$Distance = d_{ij}$	$w_i=1/d_{ij}$	W_i^*Z	
1	11	5	4	4.47	0.22	0.89	
2	6	10	3	3.16	0.32	0.95	
3	8	10	2	3.16	0.32	0.63	
4	4	4	7	4.24	0.24	1.65	
Sum					1.09	4.13	

5

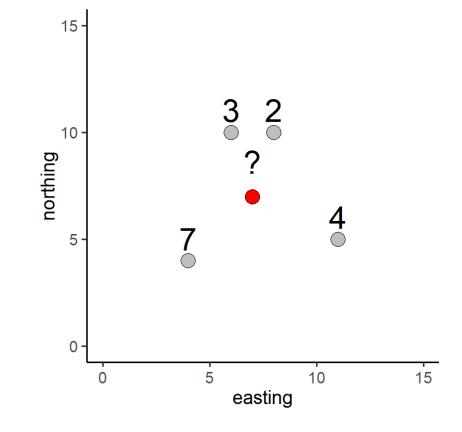
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Inverse Distance Weighting

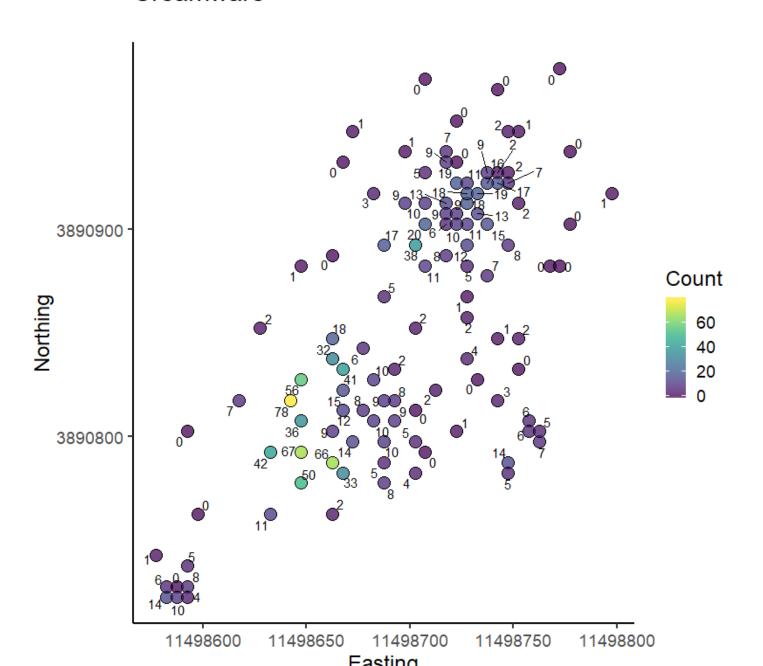
$$w_i = \frac{1}{d_{ij}^p}$$

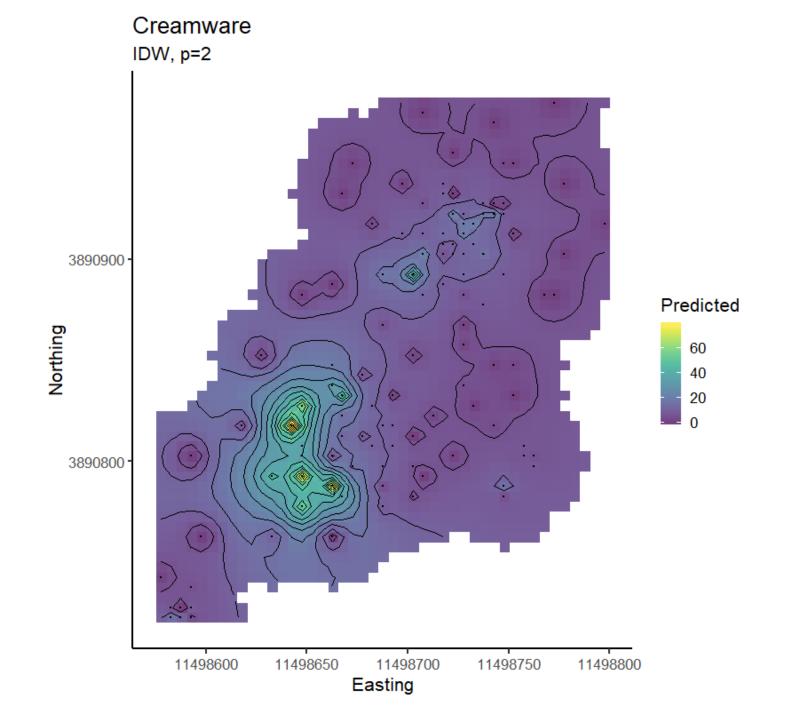


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Sum					1.09	4.13	

5 7 4.13/1.09 = 3.8

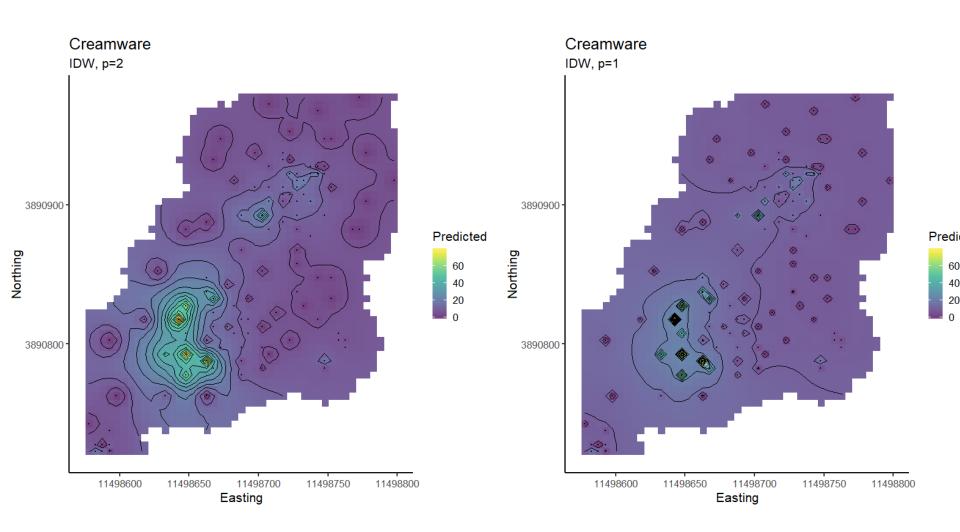
Creamware





Pesky Questions about IDW

- what value for *p*?

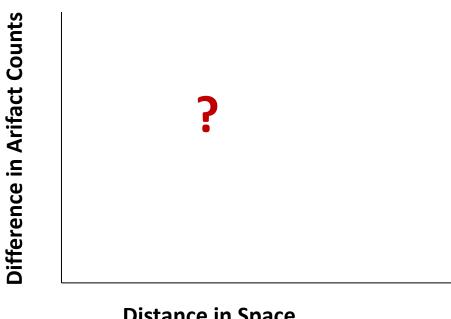


Doing Better than IDW

- p should depend on the manner in which differences between z-values increase with *distances* between *x,y* coordinates....

"Spatial autocorrelation"

To what extent do quadrats that are farther apart in 2-d space (e.g. Easting and Northing) tend to have variable values (e.g. artifact counts) that are more different.



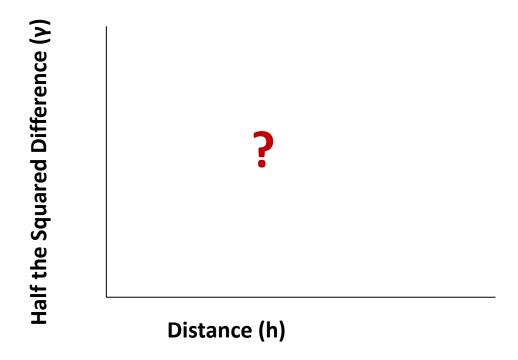
Distance in Space

Kriging (after D.R Krige)

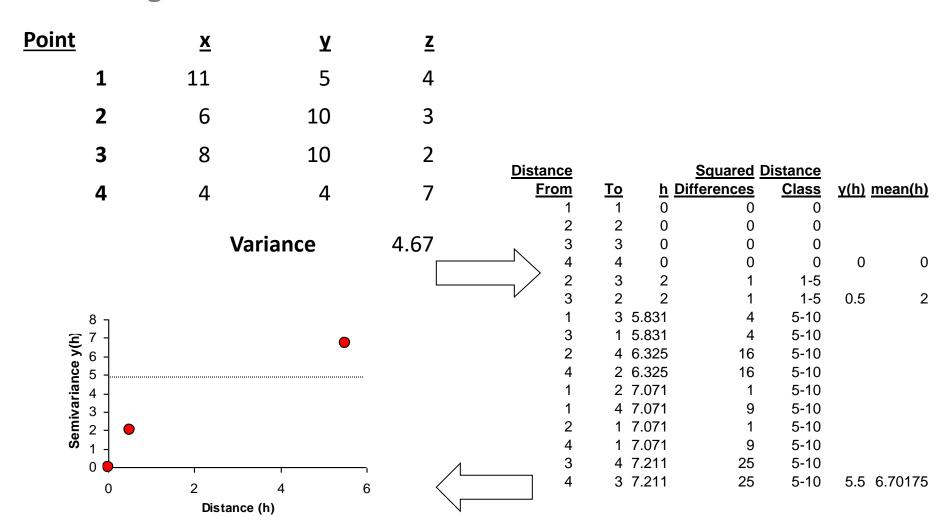
A weighted-averging interpolation method in which the **weights depend on the spatial autocorrelation structure of the data**, AND that produces estimates of Z that are designed to minimize mean-squared prediction error.

Variogram

The graphical tool we use to measure the autocorrelation structure of spatial data.

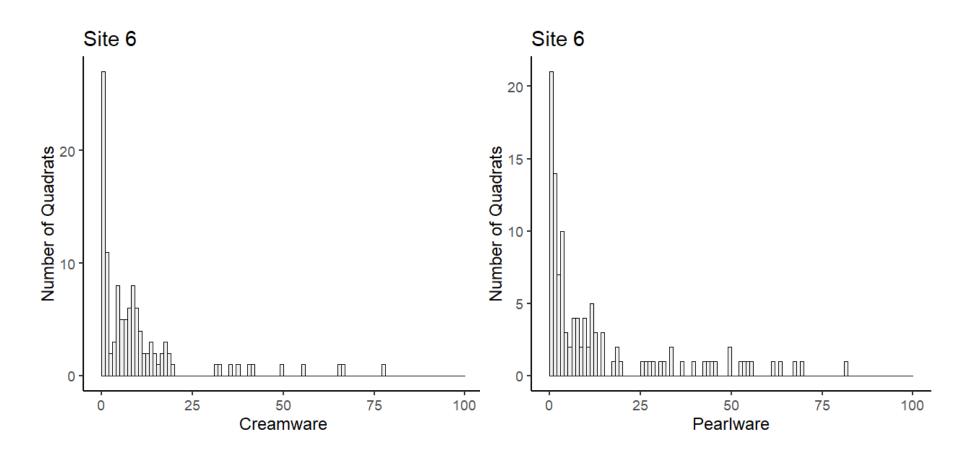


	00	3 . 0				Di	stance			Squared
							<u>From</u>	<u>To</u>	<u>d</u>	<u>Differences</u>
<u>Po</u>	<u>int</u>	<u>X</u>	У	<u>z</u>			1	1	0	0
	1	11	5	4		N	1	2	7.07	1
	2	6	10	3			1	3	5.83	4
	3	8	10	2		r	1	4	7.07	9
	4	4	4	7			2	1	7.07	1
							2	2	0	0
							2	3	2	1
	30 ¬						2	4	6.32	16
red (v)	25				•		3	1	5.83	4
Half the Squared Differerence (y)	20 - 15 -			•			3	2	2	1
off the fferer	10 -				•		3	3	0	0
H a	5 -	•		•		/	3	4	7.21	25
	0	2	4	6	8	1	4	1	7.07	9
Distance (h)							4	2	6.32	16
"The variogram cloud" – each graph						ph	4	3	7.21	25
point reoresent a difference-distance pair.						nce pair	. 4	4	0	0

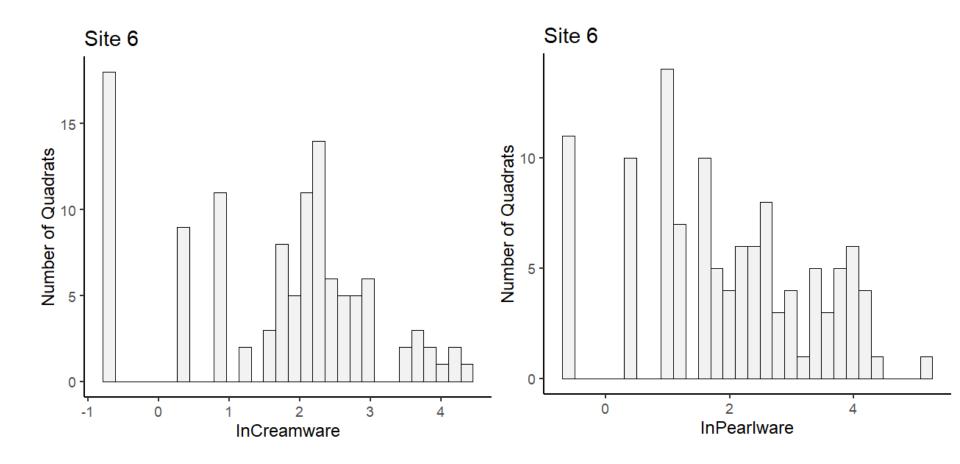


"The variogram" – each graph point represents the means of several difference-distance pairs.

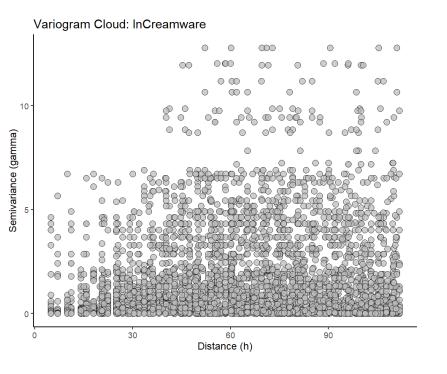
- The mathematical model behind the variogram and kriging assumes that the spatially distbuted variable has a normal of Gaussian distribution.
- But artifact counts always have long right tails...

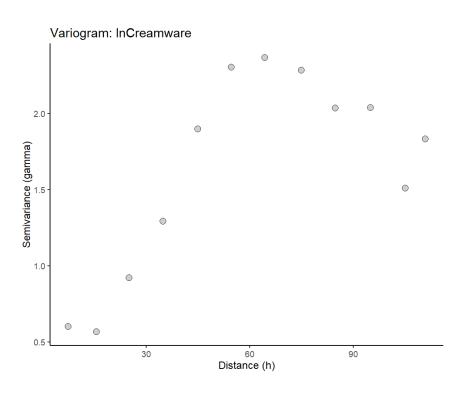


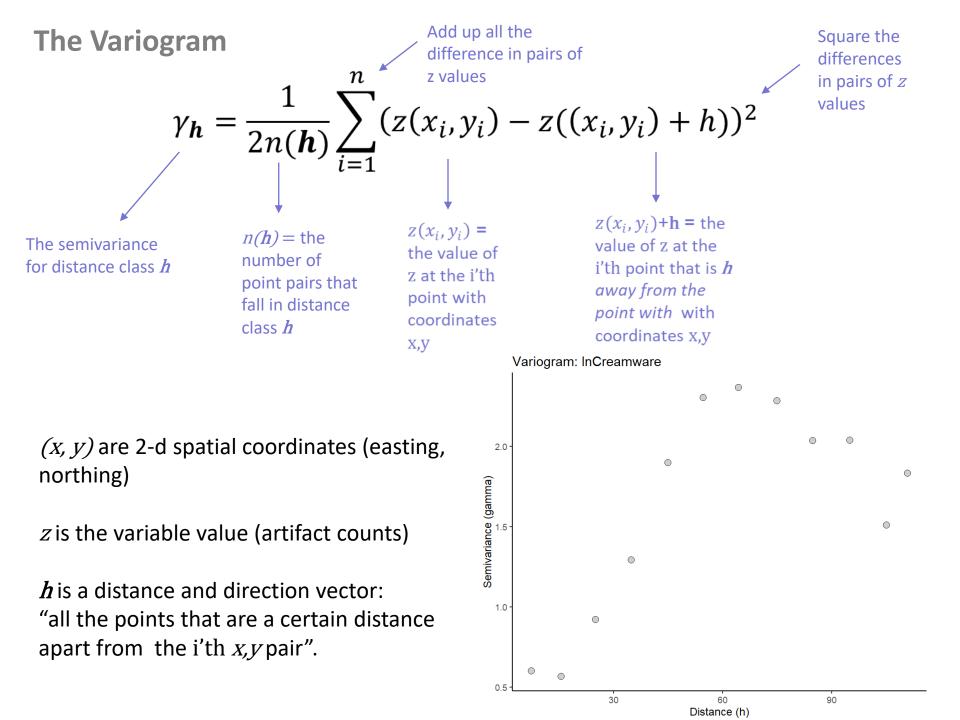
- Transforming the counts to a log scale helps.
- Because In(0) is undefined, we take logs of "started counts"
 - e.g. In(Creamware +.5)



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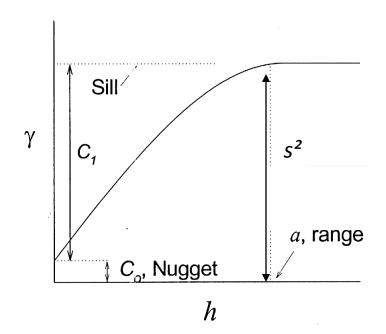




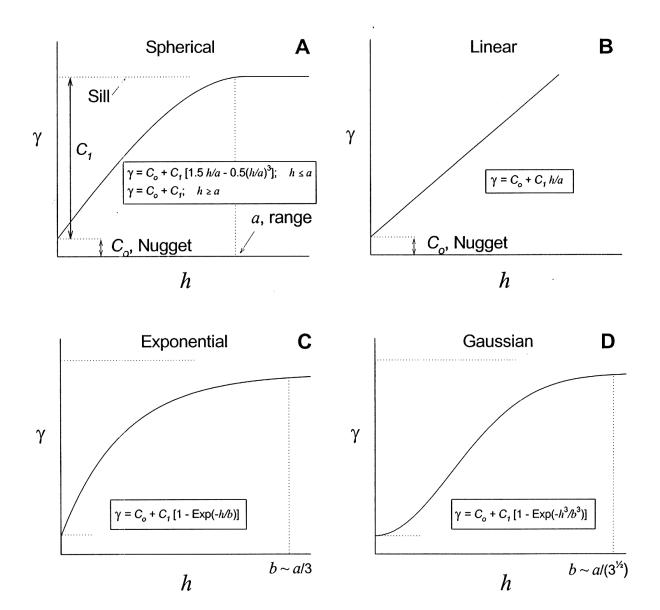


Variogram Lingo

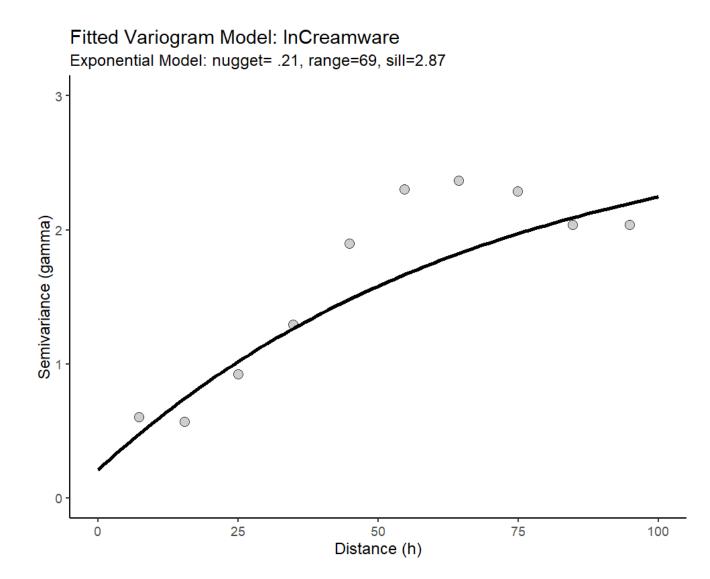
- Sill: for larger values of h the variogram levels out, indicating that there no longer is any auto correlation between data points.
- If the data are "well behaved" (Gaussian and stationary) the sill should be equal to the variance (s²) of the z values.
- Range: is the value of h where the sill occurs (or 95% of the value of the sill).
 This is the distance beyond which pairs of values are no longer autocorrelated.
- Nugget variance: a non-zero value for gamma when h = 0. Produced by various sources of unexplained error (e.g. measurement error).

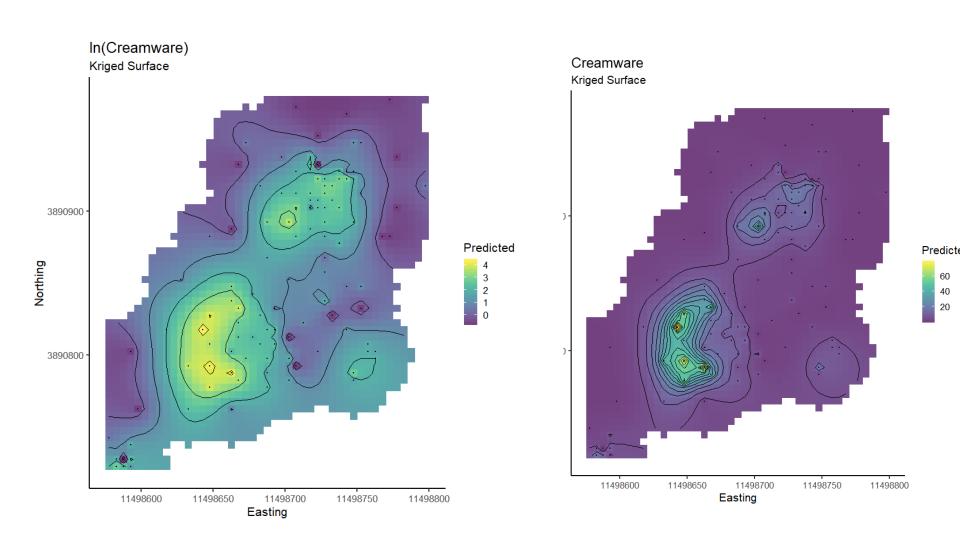


Variogram Models: Differently shaped curves, defined by different equations.



Variogram Models: Differently shaped curves, defined by different equations.





The variogram is a useful spatial data analysis tool !!

You can use it during and excavation to see if your spatial sampling stratrgy is sufficient to capture spatial pattering

- Quadrat size (too small?)
- Quadrat spacing (too far part?)
- Given quadrat size and spacing is interpolation reasonable?

