Homework 2

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Due date: Thursday, October 9

- 1. Show that (algebraically) in the absence of censoring $\hat{S}_{\text{KM}}(t) = \hat{S}_{\text{e}}(t)$.
- 2. In the absence of censoring, show that the Greenwood Formula (page 30 on note 2) can be reduced to

$$\frac{\hat{S}_{\text{\tiny KM}}(t) \times \{1 - \hat{S}_{\text{\tiny KM}}(t)\}}{n}.$$

You might assume there are no ties among the observations.

- 3. Consider the Leukemia data from the survival package:
 - > library(survival)
 - > head(aml)

| | time | status | x |
|---|------|-------------------------|--------------------|
| 1 | 9 | 1 | ${\tt Maintained}$ |
| 2 | 13 | 1 | ${\tt Maintained}$ |
| 3 | 13 | 0 | ${\tt Maintained}$ |
| 4 | 18 | 1 | ${\tt Maintained}$ |
| 5 | 23 | 1 | ${\tt Maintained}$ |
| 6 | 28 | 0 | Maintained |

In here, each row represent one patient. aml is the observed survival time, status is the censoring indicator (1 = event, 0 = censored), and x is the treatment indicator. We will ignore the treatment indicator for now.

- a. Plot the Kaplan-Meier survival curve for the data.
- b. Add the Nelson-Aalen survival curve to the Kaplan-Meier plot from (3a).
- 4. The expected survival time for the Leukemia data in #(3) does not exist because the last observation is a censored event. An alternative is to lookInstead of looking at the expected survival time, an alternative is to look at the restricted mean survival time. Compute E(T|T<161) based on the survival curve in (3a).
- 5. Let $N_i(t)$ be the number of events over time interval (0,t] for the *i*th patient in #(3). Let $N(t) = \sum_{i=1}^{n} N_i(t)$ be the aggregated counting process.
 - a. Plot N(t).
 - b. Plot M(t), where $M(t) = N(t) \hat{H}(t)$.