

## I. INTRO

The Markov chain for the system can be defined by the transition matrix as below.

$$\mathbf{X} = \begin{pmatrix} 0 & A & B & C & \cdots & 0 \\ 0 & 0 & A & B & \cdots & 0 \\ \cdots & & & & & \\ 0 & 0 & 0 & 0 & \cdots & 0 \end{pmatrix}, \mathbf{X} \in \mathbb{R}^{n \times n}$$

(1)

where from this we can compute for the output distribution.

$$v_{in} = (1 \quad 0 \quad 0 \quad \cdots \quad 0), \quad (2)$$

$$v_{out} = v_{in} \mathbf{X}^i, \quad (3)$$

$$v_{out}, v_{in} \in \mathbb{R}^{1 \times n}. \quad (4)$$

where  $\mathbf{X}$  is the transition matrix,  $A, B, C$  are the respective probabilities of transition,  $i$  is the number of iteration,  $n$  is the number of possible states.