

Λογική Επιχειρηματολογίας (2)

(Προγραμματισμός Κοινής Λογικής)



- Κάθε σύνολο κανόνων αποτελεί ένα **επιχείρημα** για τα (λογικά) συμπεράσματα που **στηρίζει**.
- Επιχειρήματα που στηρίζουν αντίθετα συμπεράσματα **αντικρούονται** μεταξύ τους – αποτελούν **αντι-επιχειρήματα**.
- Ποιο επιχείρημα **υπερισχύει**?

Αποδεκτά Επιχειρήματα (Acceptable Arguments)

- What is a **good/acceptable** argument?
 - An argument that builds a **coherent case** for its position.
 - Δένει καλά μαζί!
 - An argument that can **defend** itself against all its counter-arguments
 - An argument that **renders** its counter-arguments **incoherent/invalid**
- An argument that has some kind of a **stable property** in the **space of all available arguments**

Αποδεκτά Επιχειρήματα (Acceptable Arguments)

- What is a **good/acceptable** argument?
 - An argument that can **defend** itself against all its counter-arguments
- **Admissible** arguments
- Later we will see how we can improve this to get closer to the informal definition

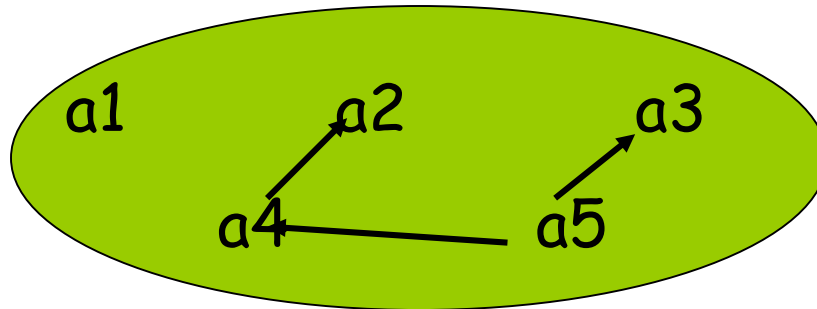
Abstract Argumentation (1)

- An **abstract argumentation framework** is a pair of a set T of arguments and an **attacking relation** on arguments
 - $AF = \langle \text{Args}, \text{Att} \rangle$, where Att is a binary relation on Args
- $S \subseteq T$ is an **Admissible Argument** iff
 - S it does **not attack itself** (i.e. it is **conflict free**), and
 - S attacks (**counter-attacks/defends**) all its attacks
- This is a simple but powerful definition.

Abstract Argumentation (2)

- $S \subseteq \text{Args}$ is an **Admissible Argument** iff
 - S it does not attack itself (i.e. it is conflict free), and
 - S attacks (counter-attacks) all its attacks

- **Example**

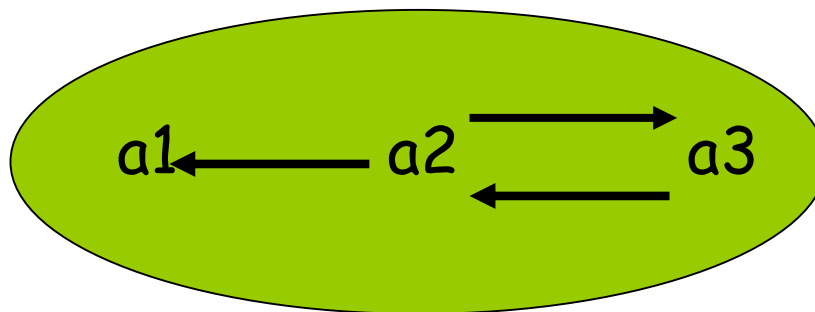


- $\{a2\}$ and $\{a3\}$ are not admissible.
- But $\{a2, a5\}$ is admissible.
- $\{a1\}, \{a5\}$ are admissible.
- $\{a1, a2, a5\}$ is maximally admissible.

Abstract Argumentation (3)

- $S \subseteq \text{Args}$ is an **Admissible Argument** iff
 - S does not attack itself (i.e. it is conflict free), and
 - S attacks (counter-attacks) all its attacks

□ Example 2



- $\{a2\}$ and $\{a3\}$ are admissible.
- $\{a1\}$ is not admissible.
- $\{a1, a3\}$ is admissible (maximally).

“Debate” Example of Argumentation

- **Proposed argument a1:** {Athens should wage war on Thebes.} **a1** {Athens should wage war on Thebes. poses a threat.}
 - **Counter-argument a2:** {Sparta will then consider us a threat and will wage war on us.}
 - **Defending-argument a3:** {Defend against Sparta with an ally. Thebes, an enemy of Sparta, is a possible ally.} **a3** {Defend against Sparta with an ally. Thebes, an enemy of Sparta, is a possible ally.} (As only one ally)
 - **Counter-argument a1:** {Waging war on Thebes prevents Thebes from being an ally.}
 - Hence **a1** is **not acceptable** (It is self-defeating).
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- ```
graph TD; a1((a1)) --> a2((a2)); a2 --> a3((a3)); a3 --> a1;
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# Banana Example

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- **banana(b1)**
  - a1 supports position yellow(b1)
  - {a1, dc} supports position neg(green(b1)).
  - It **attacks** {a2, unripe(b1)} but **NOT** vice-versa.
  - {a1, dc} is the only **admissible** argument.
  - Hence conclude **sceptically** yellow(b1).
  
- **banana(b1), unripe(b1)**
  - a2 supports position green(b1)
  - {a2, dc} supports position neg(yellow(b1)).
  - {a2, dc} **attacks** {a1, dc} and **vice-versa**.
  - Both {a2, dc} and {a1, dc} are **admissible**.
  - Hence conclude **credulously** yellow(b1) and green(b1)!
  - No **sceptical** conclusion on colour of b1.
    - Yet we want to have green(b1) **sceptically! HOW?** <sup>8</sup>



# Example of Argumentation

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- “Sellers who deliver on time are trustworthy”
  - $a1 = \{\text{trusted}(\text{Seller}) \text{ :- } \text{timely}(X)\}$
- “Sellers who deliver wrong are not trustworthy”
  - $a2 = \{\neg \text{trusted}(\text{Seller}) \text{ :- } \text{wrong\_delivery}(X)\}$
- Suppose we “observe”:
  - $\text{timely}(\text{bob})$ :  $a1$  supports  $\text{trusted}(\text{bob})$ .
  - $\text{wrong\_delivery}(\text{bob})$ :  $a2$  supports  $\neg \text{trusted}(\text{bob})$ .
  - $a1$  attacks  $a2$  and vice-versa.
- “Sellers who are trusted get large orders”
  - $a = \{\text{large\_orders}(X) \text{ :- } \text{trusted}(X)\}$
  - $A = \{a1, a\}$  supports  $\text{large\_orders}(\text{bob})$
  - $B = \{a2\}$  attacks  $A$  ( $B$  undercuts  $A$ )

# Example of Argumentation

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- “Sellers who are trusted get large orders”
  - $a = \{\text{large\_orders}(X) \text{ :- trusted}(X)\}$
  - $A = \{a_1, a\}$  supports  $\text{large\_orders}(\text{bob})$
  - $B = \{a_2\}$  attacks A (B undercuts A)
- Both A and B are **admissible**.
  - Hence can we be **sure** about  $\text{large\_orders}(\text{bob})$ ?
- Do we have an argument supporting  $\neg \text{large\_orders}(\text{bob})$ ?
  - $B' = \{a_2, a'\}$  with
    - $a' = \{\neg \text{large\_orders}(X) \text{ :- } \neg \text{trusted}(X)\}$
  - $B'' = \{a_2, a''\}$  with
    - $a'' = \{\neg \text{large\_orders}(\text{bob})\}$  –  $a''$  is a **hypothesis**.
  - Both  $B'$  and  $B''$  are **attacked** by A.
- Both  $B'$  and  $B''$  are **admissible**, supporting  $\neg \text{large\_orders}(\text{bob})$ , because of  $a_2$  that **defends** against A
  - $a''$  **cannot defend** against A because  $a''$  is a **weaker** argument

# Building admissible arguments

## Dialectics

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- Find an argument  $\Delta$  that **supports** the **position (query)** we want.
- Check  $\Delta$  is not self-attacking.
- Consider attacks,  $A$ , against  $\Delta$ .
- Attack/Defend each  $A$  by argument  $D$ .
- Add  $D$  to  $\Delta$  to give new  $\Delta' = \Delta \cup D$ .
- Repeat from 2<sup>nd</sup> step with  $\Delta'$ .

# Example of Dialectic Argumentation

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- **Args** = {a1,a2,a3} **constructed** by:
  - a1={turn\_on\_switch **causes** light\_on,  
light\_on **causes**  $\rightarrow$  darkness} U {turn\_on\_switch@T}
  - a2={power\_cut **causes**  $\rightarrow$  electricity,  
 $\rightarrow$  electricity **implies**  $\rightarrow$  light\_on} U {power\_cut@T}
  - a3={darkness@T **implies** darkness@T<sup>+</sup>} U {darkness@T}
- a1 **supports**  $\rightarrow$  darkness@T<sup>+</sup> ;
- a3 **supports** darkness@T<sup>+</sup>
- **Constructed from:** "The power cut had turned the house into darkness. Bob came home and turned on the light switch. ..."

# Example of Dialectic Argumentation

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- a1 **supports**  $\rightarrow$  darkness@T<sup>+</sup> ; a3 **supports** darkness@T<sup>+</sup>
- **Attacks** between arguments = {(a1,a3), (a2,a1)}
  - a1 **attacks** a3 but **not** vice-versa
    - "Bob expects the house to come out of darkness"
  - a2 **attacks** a1 (on light\_on) but **not** vice-versa
    - a2 **defends** a3 against the attack of a1
- {a3,a2} **acceptable** argument for darkness@T<sup>+</sup>
  - Also {a2} **acceptable** but {a1} is not acceptable.

# Example of Dialectic Argumentation

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- Suppose now that we **also** have an **argument** that the power cut had ended at T, e.g.:
  - **a4** = {short\_power\_cut@T<sup>-</sup> **implies** → power\_cut@T} U {short\_power\_cut@T<sup>-</sup>}
- **Atts** = {(a1,a3), (a2,a1), (a4,a2), (a2,a4)}
  - Args a4 and a2 are **equally strong** on “power\_cut”
    - No **preference** between them
    - They **defend** against each other.
- {a3,a2} **acceptable** argument for darkness@T<sup>+</sup>
- {a1,a4} **acceptable** argument for → darkness@T<sup>+</sup>

# Another Example - Dialectics

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- What is a good argument? - EXAMPLE
  - Position: Attend this talk
  - Arg: This is the reason we came to the conference
  - C-Arg1: The speaker is known to be boring
    - But the title of the talk is interesting - **Separate Defence**
  - C-Arg2: A friend wants to meet (for coffee I think)
    - But my sense of professional responsibility is generally stronger than that of self satisfaction - **Arg is Stronger than C-Arg2**
  - C-Arg2': The friend is not well and wants help
    - My sense of social responsibility is generally stronger than professional responsibility - **Arg is Weaker than C-Arg2'**
    - I have been assigned to write up a report on this afternoons talk
      - **Argument for social resp. is weaker than that of professional resp.**
      - **Hence, Arg is Stronger than C-Arg2**