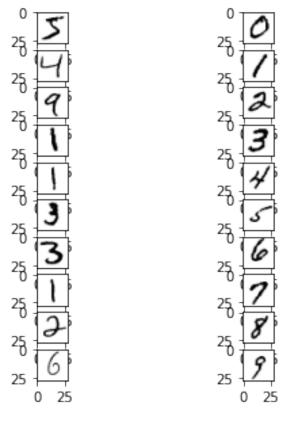
## **COURSE OUTCOME-4**

## PROGRAM NO-1

**Aim:** Programs on feedforward network to classify any standard dataset available in the public domain

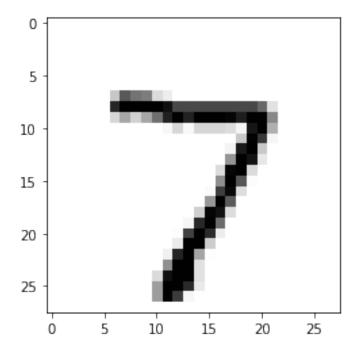
```
import keras
from keras.datasets import mnist
from keras.models import Sequential
from keras.layers import Dense
from tensorflow.keras.optimizers import SGD
from matplotlib import pyplot as plt
(x_train,y_train),(x_valid,y_valid) = mnist.load_data()
x_train.shape
(60000, 28, 28)
y_train.shape
(60000,)
y_train[0:12]
array([5, 0, 4, 1, 9, 2, 1, 3, 1, 4, 3, 5], dtype=uint8)
plt.figure(figsize=(5,5))
for k in range(20):
  plt.subplot(10,2,k+1)
  plt.imshow(x_train[k],cmap='Greys')
  plt.axis('on')
plt.show()
```



```
plt.figure(figsize=(5,5))
for k in range(20):
   plt.subplot(10,2,k+1)
   plt.imshow(x_train[k],cmap='Greys')
   plt.axis('off')
plt.show()
```



plt.imshow(x\_valid[0],cmap='Greys')
<matplotlib.image.AxesImage at 0x7fd83619e610>



y\_valid.shape

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y\_valid[0]

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preprocess data

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x train = x train.reshape(60000,784).astype('float32')
x_{valid} = x_{valid.reshape(10000,784).astype('float32')}
x train/=255
x_valid/=255
from keras import utils as np utils
n classes = 10
y train = keras.utils.np_utils.to_categorical(y_train,n_classes)
y_valid= keras.utils.np_utils.to_categorical(y_valid,n_classes)
y valid[0]
array([0., 0., 0., 0., 0., 0., 1., 0., 0.], dtype=float32)
y train[0]
array([0., 0., 0., 0., 0., 1., 0., 0., 0., 0.], dtype=float32)
x_valid[0]
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y valid[3]
array([1., 0., 0., 0., 0., 0., 0., 0., 0.], dtype=float32)
model = Sequential()
```

```
model.add(Dense(64, activation='sigmoid', input shape=(784,)))
                                                                   #64
neurons in the hidden layer 784 inputs
#final laver
model.add(Dense(10, activation='softmax'))
model.summary()
Model: "sequential"
```

Layer (type)	Output Shape	Param #
dense (Dense)	(None, 64)	50240
dense_1 (Dense)	(None, 10)	650

```
Total params: 50,890
Trainable params: 50,890
Non-trainable params: 0
(64*784) #wi xi total weights at input
50176
(64*784)+64
50240
(10*64)
640
(10*64)+10
650
((10*64)+10) + ((64*784)+64)
50890
model.compile(loss='mean squared error',optimizer=SGD(learning rate=0.
03), metrics=['accuracy'])
history= model.fit(x_train,y_train,batch_size=128,epochs=75,verbose=1)
#overbose=0 will show you nothing
#verbose=1 will show you an animated progress bar like this:
#progress bar
#overbose=2 will just mention the number of epoch like this:
Epoch 1/75
```

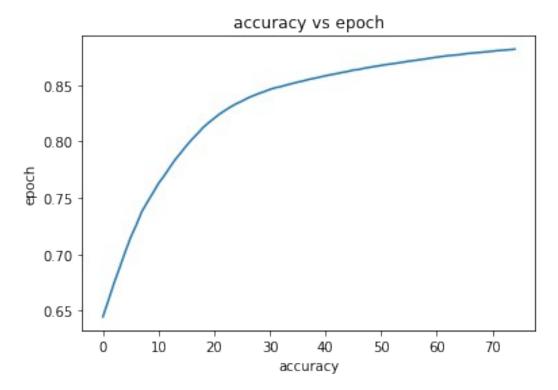
```
- accuracy: 0.6446
Epoch 2/75
- accuracy: 0.6593
Epoch 3/75
- accuracy: 0.6744
Epoch 4/75
- accuracy: 0.6880
Epoch 5/75
- accuracy: 0.7019
Epoch 6/75
469/469 [============= ] - 1s 3ms/step - loss: 0.0526
- accuracy: 0.7151
Epoch 7/75
469/469 [============= ] - 1s 3ms/step - loss: 0.0514
- accuracy: 0.7260
Epoch 8/75
- accuracy: 0.7379
Epoch 9/75
- accuracy: 0.7463
Epoch 10/75
- accuracy: 0.7545
Epoch 11/75
- accuracy: 0.7629
Epoch 12/75
469/469 [============== ] - 2s 3ms/step - loss: 0.0460
- accuracy: 0.7695
Epoch 13/75
- accuracy: 0.7768
Epoch 14/75
469/469 [============= ] - 2s 3ms/step - loss: 0.0441
- accuracy: 0.7839
Epoch 15/75
469/469 [============= ] - 2s 3ms/step - loss: 0.0433
- accuracy: 0.7900
Epoch 16/75
- accuracy: 0.7962
Epoch 17/75
- accuracy: 0.8018
Epoch 18/75
```

```
- accuracy: 0.8069
Epoch 19/75
- accuracy: 0.8123
Epoch 20/75
- accuracy: 0.8166
Epoch 21/75
- accuracy: 0.8205
Epoch 22/75
469/469 [============= ] - 2s 3ms/step - loss: 0.0378
- accuracy: 0.8244
Epoch 23/75
- accuracy: 0.8277
Epoch 24/75
accuracy: 0.8307
Epoch 25/75
- accuracy: 0.8335
Epoch 26/75
- accuracy: 0.8358
Epoch 27/75
- accuracy: 0.8384
Epoch 28/75
469/469 [============= ] - 2s 3ms/step - loss: 0.0341
- accuracy: 0.8405
Epoch 29/75
469/469 [============== ] - 2s 3ms/step - loss: 0.0335
- accuracy: 0.8425
Epoch 30/75
- accuracy: 0.8442
Epoch 31/75
- accuracy: 0.8461
Epoch 32/75
469/469 [============= ] - 2s 3ms/step - loss: 0.0320
- accuracy: 0.8476
Epoch 33/75
- accuracy: 0.8487
Epoch 34/75
- accuracy: 0.8500
```

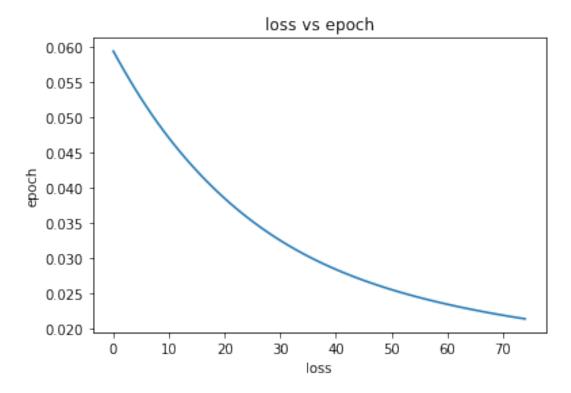
Epoch 35/75
469/469 [====================================
- accuracy: 0.8513
Epoch 36/75 469/469 [====================================
- accuracy: 0.8526
Epoch 37/75
469/469 [====================================
- accuracy: 0.8536 Epoch 38/75
469/469 [====================================
- accuracy: 0.8550
Epoch 39/75
469/469 [====================================
Epoch 40/75
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- accuracy: 0.8571 Epoch 41/75
469/469 [====================================
- accuracy: 0.8582
Epoch 42/75
469/469 [====================================
Epoch 43/75
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- accuracy: 0.8601
Epoch 44/75 469/469 [====================================
- accuracy: 0.8612
Epoch 45/75
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Epoch 46/75
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- accuracy: 0.8633 Epoch 47/75
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- accuracy: 0.8638
Epoch 48/75
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Epoch 49/75
469/469 [====================================
- accuracy: 0.8658
Epoch 50/75 469/469 [====================================
- accuracy: 0.8666
Epoch 51/75
469/469 [====================================

```
- accuracy: 0.8674
Epoch 52/75
- accuracy: 0.8682
Epoch 53/75
- accuracy: 0.8688
Epoch 54/75
469/469 [============= ] - 2s 3ms/step - loss: 0.0249
- accuracy: 0.8696
Epoch 55/75
- accuracy: 0.8703
Epoch 56/75
- accuracy: 0.8712
Epoch 57/75
469/469 [============= ] - 1s 3ms/step - loss: 0.0242
- accuracy: 0.8718
Epoch 58/75
accuracy: 0.8725
Epoch 59/75
469/469 [============= ] - 2s 3ms/step - loss: 0.0238
- accuracy: 0.8731
Epoch 60/75
- accuracy: 0.8740
Epoch 61/75
- accuracy: 0.8747
Epoch 62/75
- accuracy: 0.8753
Epoch 63/75
- accuracy: 0.8760
Epoch 64/75
- accuracy: 0.8764
Epoch 65/75
469/469 [============= ] - 1s 3ms/step - loss: 0.0228
- accuracy: 0.8768
Epoch 66/75
- accuracy: 0.8777
Epoch 67/75
- accuracy: 0.8781
Epoch 68/75
```

```
- accuracy: 0.8786
Epoch 69/75
- accuracy: 0.8790
Epoch 70/75
- accuracy: 0.8795
Epoch 71/75
- accuracy: 0.8800
Epoch 72/75
- accuracy: 0.8806
Epoch 73/75
- accuracy: 0.8809
Epoch 74/75
- accuracy: 0.8813
Epoch 75/75
- accuracy: 0.8818
plt.plot(history.history['accuracy'])
plt.title('accuracy vs epoch')
plt.xlabel('accuracy')
plt.ylabel('epoch')
Text(0, 0.5, 'epoch')
```



```
plt.plot(history.history['loss'])
plt.title('loss vs epoch')
plt.xlabel('loss')
plt.ylabel('epoch')
Text(0, 0.5, 'epoch')
```



**Result:** The program is executed successfully and obtained the output.

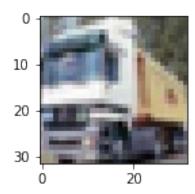
## PROGRAM NO-2

**Aim:** Programs on convolutional neural network to classify images from any standard dataset in the public domain.

```
import tensorflow as tf
from tensorflow.keras import datasets, layers, models
import matplotlib.pyplot as plt
import numpy as np
from sklearn.metrics import classification report
(xtrain,ytrain),(xtest,ytest) = datasets.cifar10.load data()
Downloading data from https://www.cs.toronto.edu/~kriz/cifar-10-
python.tar.gz
xtrain.shape
(50000, 32, 32, 3)
xtest.shape
(10000, 32, 32, 3)
classes =
['airplane','automobile','bird','cat','deer','dog','frog','horse','shi
p','truck']
def plot sample(x,y,index):
 plt.figure(figsize=(14,2))
 plt.imshow(x[index])
 plt.imshow(y[index])
plot sample(xtrain,ytrain,1)
                                     Traceback (most recent call
TypeError
last)
<ipython-input-24-024740e61cba> in <module>()
----> 1 plot sample(xtrain,ytrain,1)
<ipython-input-23-dd56c6c969e7> in plot sample(x, y, index)
        plt.figure(figsize=(14,2))
     3
        plt.imshow(x[index])
---> 4
        plt.imshow(v[index])
/usr/local/lib/python3.7/dist-packages/matplotlib/pyplot.py in
```

```
imshow(X, cmap, norm, aspect, interpolation, alpha, vmin, vmax,
origin, extent, shape, filternorm, filterrad, imlim, resample, url,
data, **kwarqs)
   2649
                filternorm=filternorm, filterrad=filterrad,
imlim=imlim.
   2650
                resample=resample, url=url, **({"data": data} if data
is not
-> 2651
                None else {}), **kwargs)
   2652
            sci( ret)
   2653
            return ret
/usr/local/lib/python3.7/dist-packages/matplotlib/ init .py in
inner(ax, data, *args, **kwargs)
            def inner(ax, *args, data=None, **kwargs):
   1563
   1564
                if data is None:
-> 1565
                    return func(ax, *map(sanitize sequence, args),
**kwargs)
   1566
                bound = new sig.bind(ax, *args, **kwargs)
   1567
/usr/local/lib/python3.7/dist-packages/matplotlib/cbook/deprecation.py
in wrapper(*args, **kwargs)
    356
                        f"%(removal)s. If any parameter follows
{name!r}, they "
                        f"should be pass as keyword, not
    357
positionally.")
--> 358
                return func(*args, **kwargs)
    359
    360
            return wrapper
/usr/local/lib/python3.7/dist-packages/matplotlib/cbook/deprecation.py
in wrapper(*args, **kwargs)
    356
                        f"%(removal)s. If any parameter follows
{name!r}, they "
    357
                        f"should be pass as keyword, not
positionally.")
--> 358
                return func(*args, **kwargs)
    359
    360
            return wrapper
/usr/local/lib/python3.7/dist-packages/matplotlib/axes/ axes.py in
imshow(self, X, cmap, norm, aspect, interpolation, alpha, vmin, vmax,
origin, extent, shape, filternorm, filterrad, imlim, resample, url,
**kwarqs)
   5624
                                      resample=resample, **kwarqs)
   5625
-> 5626
                im.set data(X)
   5627
                im.set alpha(alpha)
   5628
                if im.get clip path() is None:
```

TypeError: Invalid shape (1,) for image data



```
#Normalize
xtrain = xtrain/255
xtest = xtest/255
#model
cnn = models.Sequential([
         #feature extraction
         layers.Conv2D(filters=32,activation='relu',kernel size =
(3,3), input shape=(32,32,3)),
         layers.MaxPooling2D((2,2)),
         layers.Conv2D(filters=64,activation='relu',kernel_size =
(3,3), input shape = (32,32,3)),
         layers.MaxPooling2D((2,2)),
         #classification
         layers.Flatten(),
         layers.Dense(64,activation='relu'),
         layers.Dense(10,activation='softmax')
])
cnn.compile(optimizer='adam',loss='sparse categorical crossentropy',me
trics=['accuracy'])
cnn.fit(xtrain,ytrain,epochs=20)
Epoch 1/20
```

```
2.3028 - accuracy: 0.0963
Epoch 2/20
2.3028 - accuracy: 0.0993
Epoch 3/20
2.3028 - accuracy: 0.0958
Epoch 4/20
2.3028 - accuracy: 0.0975
Epoch 5/20
2.3028 - accuracy: 0.0967
Epoch 6/20
2.3027 - accuracy: 0.0974
Epoch 7/20
2.3028 - accuracy: 0.0972
Epoch 8/20
2.3028 - accuracy: 0.0977
Epoch 9/20
2.3028 - accuracy: 0.0978
Epoch 10/20
2.3027 - accuracy: 0.0979
Epoch 11/20
2.3028 - accuracy: 0.0972
Epoch 12/20
2.3028 - accuracy: 0.0973
Epoch 13/20
2.3028 - accuracy: 0.0977
Epoch 14/20
2.3028 - accuracy: 0.0984
Epoch 15/20
2.3028 - accuracy: 0.0995
Epoch 16/20
2.3028 - accuracy: 0.0981
Epoch 17/20
2.3028 - accuracy: 0.0982
Epoch 18/20
```

```
2.3028 - accuracy: 0.0982
Epoch 19/20
2.3028 - accuracy: 0.0996
Epoch 20/20
2.3028 - accuracy: 0.0966
<keras.callbacks.History at 0x7f9e5c739b50>
ypred = cnn.predict(xtest)
cnn.evaluate(xtest,ytest)
- accuracy: 0.1000
[2.3026859760284424, 0.10000000149011612]
ytest=ytest.reshape(-1,)
ypred=cnn.predict(xtest)
yclasses=[np.argmax(element) for element in ypred]
print('classification report:\
n',classification report(ytest,yclasses))
classification report:
                     recall f1-score
           precision
                                    support
                      0.00
        0
              0.00
                              0.00
                                     1000
        1
              0.10
                      1.00
                              0.18
                                     1000
        2
              0.00
                      0.00
                             0.00
                                     1000
        3
              0.00
                      0.00
                             0.00
                                     1000
        4
              0.00
                      0.00
                             0.00
                                     1000
        5
              0.00
                      0.00
                             0.00
                                     1000
        6
              0.00
                      0.00
                             0.00
                                     1000
        7
              0.00
                      0.00
                             0.00
                                     1000
        8
              0.00
                      0.00
                             0.00
                                     1000
        9
              0.00
                      0.00
                             0.00
                                     1000
                                    10000
   accuracy
                             0.10
              0.01
                      0.10
                              0.02
                                    10000
  macro avq
weighted avg
              0.01
                      0.10
                             0.02
                                    10000
```

/usr/local/lib/python3.7/dist-packages/sklearn/metrics/
\_classification.py:1318: UndefinedMetricWarning: Precision and F-score
are ill-defined and being set to 0.0 in labels with no predicted
samples. Use `zero\_division` parameter to control this behavior.
\_warn\_prf(average, modifier, msg\_start, len(result))
/usr/local/lib/python3.7/dist-packages/sklearn/metrics/ classification

```
.py:1318: UndefinedMetricWarning: Precision and F-score are ill-
defined and being set to 0.0 in labels with no predicted samples. Use
`zero_division` parameter to control this behavior.
    _warn_prf(average, modifier, msg_start, len(result))
/usr/local/lib/python3.7/dist-packages/sklearn/metrics/_classification
.py:1318: UndefinedMetricWarning: Precision and F-score are ill-
defined and being set to 0.0 in labels with no predicted samples. Use
`zero_division` parameter to control this behavior.
    _warn_prf(average, modifier, msg_start, len(result))
```

**Result:** The program is executed successfully and obtained the output.