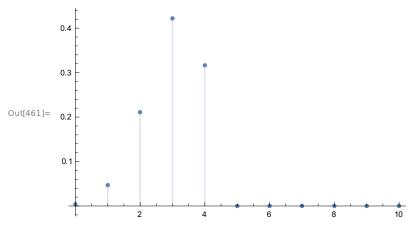
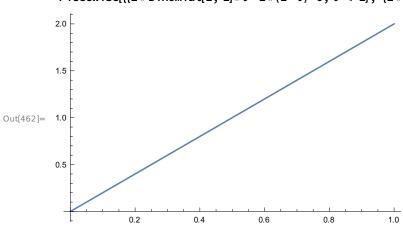
■ Q1b

In[461]:= DiscretePlot[Binomial[4, y] \* 0.75^y \* 0.25^(4-y), {y, 0, 10, 1}]



■ Q1 c n=1,y=1

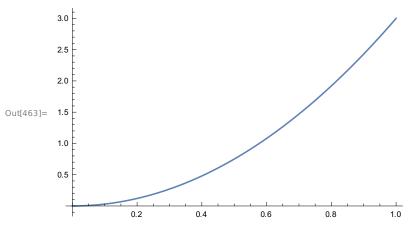
In[462]:= **Plot[** 



■ Q1c n=2, y=2

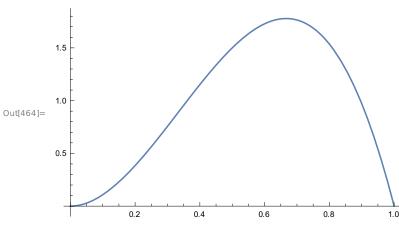
In[463]:= **Plot[** 

 $\label{eq:piecewise} Piecewise[\{\{3*Binomial[2, 2]*\theta^2*(1-\theta)^0, \theta < 1\}, \{3*Binomial[2, 2]*\theta^2, \theta == 1\}\}], \{\theta, \theta, 1\}]$ 



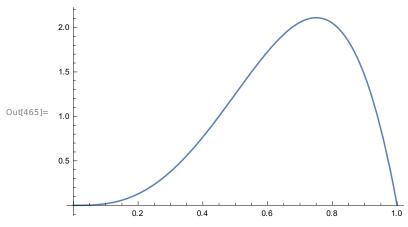
■ Q1 c n=3,y=2

In[464]:= Plot[{4 \* Binomial[3, 2] \*  $\theta^{2}$  \* (1 -  $\theta$ ) 1}, { $\theta$ , 0, 1}]



■ Q1 c n=4, y=3

In[465]:= Plot[ $\{5 * Binomial[4, 3] * \theta ^3 * (1 - \theta)^1\}, \{\theta, 0, 1\}$ ]



Q2 a h1,P(h1) = 0.1

Red line indicates h1, blue line indicates h2, green line indicates h3, purple line indicates h4, yellow line indicates h5.

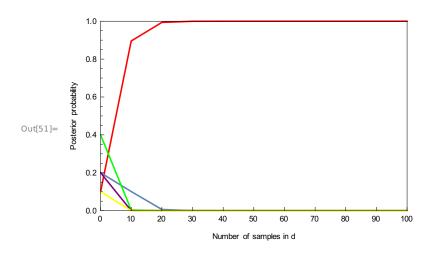
- · For some graphs, only 4 lines are shown since red line and yellow line are totally the same.
- When evaluating graphs for P(dN+1=lime|d1,...,dN) in Mathematica, if it is totally different from my graph in this document, just repeat evaluating the cell. (I don't know why, but the weird things happened several times.)

```
In[32]:=
       binaryData1 = RandomChoice[\{1, 0\} \rightarrow \{0, 1\}, 100]
       myData11 = Array[f11, 10]
       myData12 = Array[f12, 10]
       myData13 = Array[f13, 10]
       myData14 = Array[f14, 10]
       myData15 = Array[f15, 10]
       mySum = Array[s1, 10]
       For[i = 1, i \le 10, i++, f11[i] = 1;
         For[j = 1, j \le i * 10, j + +, If[binaryData1[[j]] == 0, f11[i] = f11[i] * 1, f11[i] = f11[i] * 0];
         f11[i] = f11[i] * 0.1]
       For[i = 1, i \le 10, i++, f12[i] = 1;
         For[j = 1, j \le i * 10, j++, If[binaryData1[[j]] == 0, f12[i] = f12[i] * 0.75, f12[i] = f12[i] * 0.25]];
         f12[i] = f12[i] * 0.2]
       For[i = 1, i \le 10, i++, f13[i] = 1;
         For[j = 1, j \le i * 10, j + +, f[binaryData1[[j]] == 0, f13[i] = f13[i] * 0.5, f13[i] = f13[i] * 0.5];
         f13[i] = f13[i] * 0.4
       For[i = 1, i \le 10, i++, f14[i] = 1;
         For[j = 1, j \le i * 10, j + +, f[binaryData1[[j]] == 0, f14[i] = f14[i] * 0.25, f14[i] = f14[i] * 0.75]];
         f14[i] = f14[i] * 0.2
       For[i = 1, i \le 10, i++, f15[i] = 1;
         For[j = 1, j \le i * 10, j + +, If[binaryDatal[[j]] == 0, f15[i] = f15[i] * 0, f15[i] = f15[i] * 1]];
         f15[i] = f15[i] * 0.1]
       For[i = 1, i \le 10, i++, s1[i] = 0; s1[i] = s1[i] + f11[i] + f12[i] + f13[i] + f14[i] + f15[i]
        For[i = 1, i \le 10, i++, f11[i] = f11[i]/s1[i];
         f12[i] = f12[i]/s1[i];
         f13[i] = f13[i]/s1[i];
         f14[i] = f14[i]/s1[i];
         f15[i] = f15[i]/s1[i]]
       myData11 = Prepend[myData11, 0.1]
       myData12 = Prepend[myData12, 0.2]
       myData13 = Prepend[myData13, 0.4]
       myData14 = Prepend[myData14, 0.2]
```

myData15 = Prepend[myData15, 0.1]

```
Frame → True, FrameLabel → {"Number of samples in d", "Posterior probability"},
                                             FrameTicks → {{Automatic, None},
                                                 \{\{\{1, 0\}, \{2, 10\}, \{3, 20\},
                                                  {4, 30}, {5, 40}, {6, 50}, {7, 60}, {8, 70}, {9, 80}, {10, 90}, {11, 100}}, None}],
                                        ListLinePlot[myData12, PlotRange \rightarrow {{1, 11}, {0, 1}}],
                                        ListLinePlot[myData13, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Green],
                                        ListLinePlot[myData14, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Purple],
                                        ListLinePlot[myData15, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Yellow]]
Out[33]= {0.895628, 0.993694, 0.999643, 0.99998, 0.999999, 1., 1., 1., 1., 1.}
6.37831 \times 10^{-8}, 3.59185 \times 10^{-9}, 2.0227 \times 10^{-10}, 1.13905 \times 10^{-11}, 6.4144 \times 10^{-13}}
Out(35)= \{0.00349855, 3.79064 \times 10^{-6}, 3.72396 \times 10^{-9}, 3.63791 \times 10^{-12}, 3.55271 \times 10^{-15}, 
                                        3.46945 \times 10^{-18}, 3.38813 \times 10^{-21}, 3.30872 \times 10^{-24}, 3.23117 \times 10^{-27}, 3.15544 \times 10^{-30}
Out[36]= \{1.70827 \times 10^{-6}, 1.80752 \times 10^{-12}, 1.7341 \times 10^{-18}, 1.65433 \times 10^{-24}, 1.57772 \times 10^{-30}, 1.57772 \times 10^{-30}, 1.65433 \times 10^{-24}, 1.57723 \times 10^{-2
                                        1.50463 \times 10^{-36}, 1.43493 \times 10^{-42}, 1.36846 \times 10^{-48}, 1.30506 \times 10^{-54}, 1.2446 \times 10^{-60}
Out[37]= \{0., 0., 0., 0., 0., 0., 0., 0., 0., 0.\}
Out[38] = \{0.111654, 0.100635, 0.100036, 0.100002, 0.1, 0.1, 0.1, 0.1, 0.1, 0.1\}
Out[46] = \{0.1, 0.895628, 0.993694, 0.999643, 0.99998, 0.999999, 1., 1., 1., 1., 1.\}
6.37831 \times 10^{-8}, 3.59185 \times 10^{-9}, 2.0227 \times 10^{-10}, 1.13905 \times 10^{-11}, 6.4144 \times 10^{-13}
Out[48]= \{0.4, 0.00349855, 3.79064 \times 10^{-6}, 3.72396 \times 10^{-9}, 3.63791 \times 10^{-12}, 3.55271 \times 10^{-15}, 3.72396 \times 10^{-9}, 3.63791 \times 10^{-12}, 3.55271 \times 10^{-15}, 3.72396 \times 10^{-10}, 3.72396 \times 10^{-10}, 3.63791 \times 10^{-12}, 3.55271 \times 10^{-15}, 3.72396 \times 10^{-10}, 
                                        3.46945 \times 10^{-18}, 3.38813 \times 10^{-21}, 3.30872 \times 10^{-24}, 3.23117 \times 10^{-27}, 3.15544 \times 10^{-30}
 Out[49]= \{0.2, 1.70827 \times 10^{-6}, 1.80752 \times 10^{-12}, 1.7341 \times 10^{-18}, 1.65433 \times 10^{-24}, 1.57772 \times 10^{-30}, 1.65433 \times 10^{-24}, 1.654333 \times 10^{-24}, 1.65433 \times 10^{-24}, 1.65433 \times 10^{-24}, 1.65433 \times 10^{-24}, 1.65433 \times 
                                        1.50463 \times 10^{-36}, 1.43493 \times 10^{-42}, 1.36846 \times 10^{-48}, 1.30506 \times 10^{-54}, 1.2446 \times 10^{-60}}
```

Show[ListLinePlot[myData11, PlotStyle  $\rightarrow$  Red, PlotRange  $\rightarrow$  {{1, 11}, {0, 1}},



In[56]:= myPredict1 = Array[f1, 10]
For[i = 1, i ≤ 10, i++, f1[i] = 0;

f1[i] = f1[i] + 0 \* f11[i] + 0.25 \* f12[i] + 0.5 \* f13[i] + 0.75 \* f14[i] + 1 \* f15[i]

myPredict1 = Prepend[myPredict1, 0.5]

ListLinePlot[myPredict1, PlotRange  $\rightarrow$  {{1, 11}, {0, 1}}, Frame  $\rightarrow$  True,

FrameLabel  $\rightarrow$  {"Number of samples in d", "Probability that next candy is lime"},

FrameTicks → {{Automatic, None},

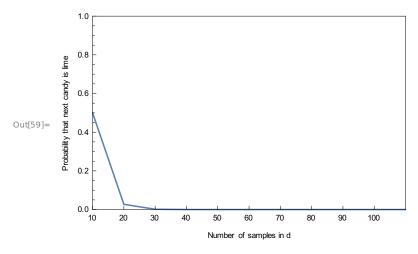
 $\{\{\{1, 10\}, \{2, 20\}, \{3, 30\},$ 

 $\{4, 40\}, \{5, 50\}, \{6, 60\}, \{7, 70\}, \{8, 80\}, \{9, 90\}, \{10, 100\}\}, None\}\}$ 

Out[56]=  $\{0.0269685, 0.0015775, 0.000089261, 5.02819 \times 10^{-6}, 2.83161 \times 10^{-7}, 0.000089261, 0.00008008100000000000000000000000000$ 

 $1.59458 \times 10^{-8} \,, \, 8.97963 \times 10^{-10} \,, \, 5.05675 \times 10^{-11} \,, \, 2.84763 \times 10^{-12} \,, \, 1.6036 \times 10^{-13} \big\}$ 

Out[58]=  $\left\{0.5,\,0.0269685,\,0.0015775,\,0.000089261,\,5.02819\times10^{-6},\,2.83161\times10^{-7},\,\right.$  $\left.1.59458\times10^{-8},\,8.97963\times10^{-10},\,5.05675\times10^{-11},\,2.84763\times10^{-12},\,1.6036\times10^{-13}\right\}$ 

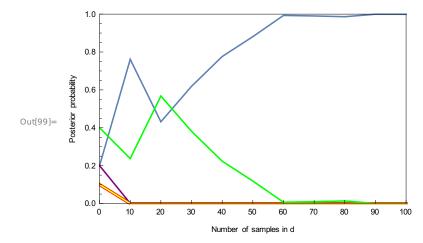


Q2a h2,P(h2)=0.2

In[80]:= binaryData2 = RandomChoice[{0.75, 0.25} → {0, 1}, 100]
myData21 = Array[f21, 10]

```
myData22 = Array[f22, 10]
myData23 = Array[f23, 10]
myData24 = Array[f24, 10]
myData25 = Array[f25, 10]
mySum2 = Array[s2, 10]
For[i = 1, i \le 10, i++, f21[i] = 1;
 For[j = 1, j \le i * 10, j + +, [f[binaryData2[[j]] == 0, f21[i] = f21[i] * 1, f21[i] = f21[i] * 0];
 f21[i] = f21[i] * 0.1]
For[i = 1, i \le 10, i++, f22[i] = 1;
 For[j = 1, j \le i * 10, j++, If[binaryData2[[j]] == 0, f22[i] = f22[i] * 0.75, f22[i] = f22[i] * 0.25];
 f22[i] = f22[i] * 0.2
For[i = 1, i \le 10, i++, f23[i] = 1;
 For[j = 1, j \le i * 10, j++, If[binaryData2[[j]] == 0, f23[i] = f23[i] * 0.5, f23[i] = f23[i] * 0.5];
 f23[i] = f23[i] * 0.4]
For[i = 1, i \le 10, i++, f24[i] = 1;
 For[j = 1, j \le i * 10, j++, If[binaryData2[[j]] == 0, f24[i] = f24[i] * 0.25, f24[i] = f24[i] * 0.75];
 f24[i] = f24[i] * 0.2]
For[i = 1, i \le 10, i++, f25[i] = 1;
 For[j = 1, j \le i * 10, j + *, If[binaryData2[[j]] == 0, f25[i] = f25[i] * 0, f25[i] = f25[i] * 1]];
 f25[i] = f25[i] * 0.1]
For[i = 1, i \le 10, i++, s2[i] = 0; s2[i] = s2[i] + f21[i] + f22[i] + f23[i] + f24[i] + f25[i]
For[i = 1, i \le 10, i++, f21[i] = f21[i]/s2[i];
 f22[i] = f22[i]/s2[i];
 f23[i] = f23[i]/s2[i];
 f24[i] = f24[i]/s2[i];
 f25[i] = f25[i] / s2[i]
myData21 = Prepend[myData21, 0.1]
myData22 = Prepend[myData22, 0.2]
myData23 = Prepend[myData23, 0.4]
myData24 = Prepend[myData24, 0.2]
myData25 = Prepend[myData25, 0.1]
Show[ListLinePlot[myData21, PlotStyle \rightarrow {Red, Thickness[0.01]}, PlotRange \rightarrow {{1, 11}, {0, 1}},
  Frame → True, FrameLabel → {"Number of samples in d", "Posterior probability"},
  FrameTicks → {{Automatic, None},
   \{\{\{1, 0\}, \{2, 10\}, \{3, 20\}, \}
    {4, 30}, {5, 40}, {6, 50}, {7, 60}, {8, 70}, {9, 80}, {10, 90}, {11, 100}}, None}}],
 ListLinePlot[myData22, PlotRange \rightarrow {{1, 11}, {0, 1}}],
 ListLinePlot[myData23, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Green],
 ListLinePlot[myData24, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Purple],
 ListLinePlot[myData25, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Yellow]]
```

- Out[82]= {0.761314, 0.431637, 0.618847, 0.776172, 0.88104, 0.993024, 0.990229, 0.98633, 0.999279, 0.998988}
- Out[83]= {0.237642, 0.56777, 0.381143, 0.223828, 0.11896, 0.00697551, 0.00977066, 0.0136704, 0.000720537, 0.00101182}
- Out[84]=  $\left\{0.00104433, 0.000592095, 0.0000104802, 1.62278 \times 10^{-7}, 2.27412 \times 10^{-9}, 3.90668 \times 10^{-13}, 4.32853 \times 10^{-14}, 4.79054 \times 10^{-15}, 7.3974 \times 10^{-19}, 8.21694 \times 10^{-20}\right\}$
- Out[85]= {0., 0., 0., 0., 0., 0., 0., 0., 0., 0.}
- Out[86]=  $\left\{0.00164375, 6.71873 \times 10^{-7}, 9.774 \times 10^{-10}, 1.62535 \times 10^{-12}, 2.98647 \times 10^{-15}, 4.97376 \times 10^{-17}, 3.46766 \times 10^{-20}, 2.42035 \times 10^{-23}, 4.4844 \times 10^{-25}, 3.11859 \times 10^{-28}\right\}$
- Out[95]= {0.2, 0.761314, 0.431637, 0.618847, 0.776172, 0.88104, 0.993024, 0.990229, 0.98633, 0.999279, 0.998988}
- Out[96]= {0.4, 0.237642, 0.56777, 0.381143, 0.223828, 0.11896, 0.00697551, 0.00977066, 0.0136704, 0.000720537, 0.00101182}
- Out[97]=  $\left\{0.2, 0.00104433, 0.000592095, 0.0000104802, 1.62278 \times 10^{-7}, 2.27412 \times 10^{-9}, 3.90668 \times 10^{-13}, 4.32853 \times 10^{-14}, 4.79054 \times 10^{-15}, 7.3974 \times 10^{-19}, 8.21694 \times 10^{-20}\right\}$



```
In[104]:= myPredict2 = Array[f2, 10]
         For[i = 1, i \le 10, i++, f2[i] = 0;
          f2[i] = f2[i] + 0 * f21[i] + 0.25 * f22[i] + 0.5 * f23[i] + 0.75 * f24[i] + 1 * f25[i]
         myPredict2 = Prepend[myPredict2, 0.5]
         ListLinePlot[myPredict2, PlotRange \rightarrow {{1, 11}, {0, 1}}, Frame \rightarrow True,
          FrameLabel → {"Number of samples in d", "Probability that next candy is lime"},
          FrameTicks → {{Automatic, None},
            \{\{\{1, 10\}, \{2, 20\}, \{3, 30\},
             {4, 40}, {5, 50}, {6, 60}, {7, 70}, {8, 80}, {9, 90}, {10, 100}}, None}}]
Out[104] = \{0.373299, 0.281886, 0.266012, 0.271924, \}
           0.260767, 0.289856, 0.252443, 0.25115, 0.25002, 0.250009
Out[106] = \{0.5, 0.373299, 0.281886, 0.266012, 0.271924, \}
           0.260767, 0.289856, 0.252443, 0.25115, 0.25002, 0.250009
            0.8
          that next candy is lime
            0.6
Out[107]=
            0.4
          Probability
            0.0
                    20
                          30
                                                             90
                                                                  100
                                           60
                                     Number of samples in d
         \bullet Q2 a h3,P(h3) = 0.4
In[228]:= binaryData3 = RandomChoice[\{0.5, 0.5\} \rightarrow \{0, 1\}, 100]
         myData31 = Array[f31, 10]
         myData32 = Array[f32, 10]
         myData33 = Array[f33, 10]
         myData34 = Array[f34, 10]
         myData35 = Array[f35, 10]
         mySum3 = Array[s3, 10]
         For[i = 1, i \le 10, i++, f31[i] = 1;
          For[j = 1, j \le i * 10, j + +, f[binaryData3[[j]] == 0, f31[i] = f31[i] * 1, f31[i] = f31[i] * 0]]
          f31[i] = f31[i] * 0.1]
         For[i = 1, i \le 10, i++, f32[i] = 1;
          For[j = 1, j \le i * 10, j++, If[binaryData3[[j]] == 0, f32[i] = f32[i] * 0.75, f32[i] = f32[i] * 0.25]];
          f32[i] = f32[i] * 0.2]
```

```
For[i = 1, i \le 10, i++, f33[i] = 1;
         For[j = 1, j \le i * 10, j++, If[binaryData3[[j]] == 0, f33[i] = f33[i] * 0.5, f33[i] = f33[i] * 0.5];
         f33[i] = f33[i] * 0.4]
        For[i = 1, i \le 10, i++, f34[i] = 1;
         For[j = 1, j \le i * 10, j++, If[binaryData3[[j]] == 0, f34[i] = f34[i] * 0.25, f34[i] = f34[i] * 0.75]];
         f34[i] = f34[i] * 0.2]
        For[i = 1, i \le 10, i++, f35[i] = 1;
         For[j = 1, j \le i * 10, j + +, [f[binaryData3[[j]] == 0, f35[i] = f35[i] * 0, f35[i] = f35[i] * 1]];
         f35[i] = f35[i] * 0.1]
        For[i = 1, i \le 10, i++, s3[i] = 0; s3[i] = s3[i] + f31[i] + f32[i] + f33[i] + f34[i] + f35[i]]
        For[i = 1, i \le 10, i++, f31[i] = f31[i]/s3[i];
         f32[i] = f32[i]/s3[i];
         f33[i] = f33[i]/s3[i];
         f34[i] = f34[i]/s3[i];
         f35[i] = f35[i]/s3[i]
       myData31 = Prepend[myData31, 0.1]
       myData32 = Prepend[myData32, 0.2]
       myData33 = Prepend[myData33, 0.4]
       myData34 = Prepend[myData34, 0.2]
       myData35 = Prepend[myData35, 0.1]
       Show[ListLinePlot[myData31, PlotStyle \rightarrow {Red, Thickness[0.01]}, PlotRange \rightarrow {{1, 11}, {0, 1}},
          Frame → True, FrameLabel → {"Number of samples in d", "Posterior probability"},
          FrameTicks → {{Automatic, None},
           \{\{\{1, 0\}, \{2, 10\}, \{3, 20\},
           {4, 30}, {5, 40}, {6, 50}, {7, 60}, {8, 70}, {9, 80}, {10, 90}, {11, 100}}, None}}],
         ListLinePlot[myData32, PlotRange \rightarrow {{1, 11}, {0, 1}}],
         ListLinePlot[myData33, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Green],
         ListLinePlot[myData34, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Purple],
         ListLinePlot[myData35, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Yellow]]
0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 0, 0, 1, 0, 0, 1, 0, 0, 1, 1, 1, 1, 1, 0,
         0, 1, 1, 1, 1, 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 1, 0, 1, 0, 0
3.29911 \times 10^{-6}, 7.84335 \times 10^{-7}, 1.86208 \times 10^{-7}, 4.41926 \times 10^{-8}, 3.14622 \times 10^{-8}}
Out[231] = \{0.480526, 0.304781, 0.846988, 0.985759, 
         0.996583, 0.997592, 0.999427, 0.999864, 0.999968, 0.999997
```

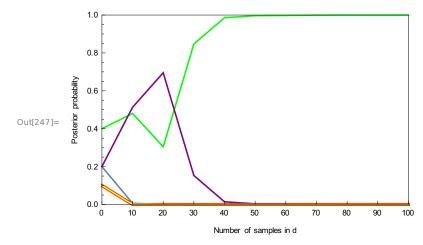
```
Out[232]= \{0.513139, 0.695113, 0.152802, 0.0140672, 0.00337488, 0.00240505, 0.00057178, 0.000135745, 0.0000322164, 2.54844 × <math>10^{-6}\}
```

Out[234]=  $\{0.000812912, 1.25162 \times 10^{-6}, 4.39828 \times 10^{-10}, 3.69054 \times 10^{-13}, 3.56489 \times 10^{-16}, 3.47782 \times 10^{-19}, 3.39007 \times 10^{-22}, 3.30917 \times 10^{-25}, 3.23128 \times 10^{-28}, 3.15545 \times 10^{-31}\}$ 

Out[243]=  $\{0.2, 0.00633505, 0.000105946, 0.000209605, 0.00017367, 0.0000416651, \\ 3.29911 \times 10^{-6}, 7.84335 \times 10^{-7}, 1.86208 \times 10^{-7}, 4.41926 \times 10^{-8}, 3.14622 \times 10^{-8}\}$ 

Out[244]= {0.4, 0.480526, 0.304781, 0.846988, 0.985759, 0.996583, 0.997592, 0.999427, 0.999864, 0.999968, 0.999997}

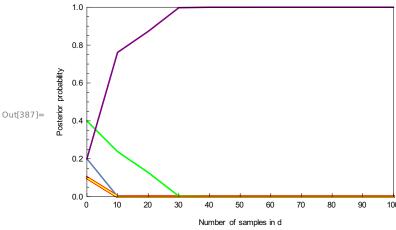
Out[245]=  $\{0.2, 0.513139, 0.695113, 0.152802, 0.0140672, 0.00337488, 0.00240505, 0.00057178, 0.000135745, 0.0000322164, 2.54844 <math>\times 10^{-6}\}$ 



```
In[252]:= myPredict3 = Array[f3, 10]
         For[i = 1, i \le 10, i++, f3[i] = 0;
          f3[i] = f3[i] + 0 * f31[i] + 0.25 * f32[i] + 0.5 * f33[i] + 0.75 * f34[i] + 1 * f35[i]
         myPredict3 = Prepend[myPredict3, 0.5]
         \label{listLinePlot} ListLinePlot[myPredict3\,,\ PlotRange \rightarrow \{\{1,\ 11\},\ \{0,\ 1\}\},\ Frame \ \rightarrow\ True,
          FrameLabel → {"Number of samples in d", "Probability that next candy is lime"},
          FrameTicks → {{Automatic, None},
             \{\{\{1, 10\}, \{2, 20\}, \{3, 30\},
             {4, 40}, {5, 50}, {6, 60}, {7, 70}, {8, 80}, {9, 90}, {10, 100}}, None}}]
Out[252] = \{0.556683, 0.549796, 0.513996, 0.503473,
           0.520943, 0.505309, 0.511072, 0.522515, 0.543624, 0.511941}
Out[254] = \{0.5, 0.556683, 0.549796, 0.513996, 0.503473, \}
           0.520943, 0.505309, 0.511072, 0.522515, 0.543624, 0.511941}
             0.8
          Probability that next candy is lime
Out[255]=
             0.4
             0.2
             0.0 L
10
                           30
                                                                    100
                                                              90
                                      Number of samples in d
In[538]:=
         \mathbf{Q} Q2 a h4,P(h4) = 0.2
ln[368]:= binaryData4 = RandomChoice[{0.25, 0.75} \rightarrow {0, 1}, 100]
         myData41 = Array[f41, 10]
         myData42 = Array[f42, 10]
         myData43 = Array[f43, 10]
         myData44 = Array[f44, 10]
         myData45 = Array[f45, 10]
         mySum4 = Array[s4, 10]
         For[i = 1, i \le 10, i++, f41[i] = 1;
          For[j = 1, j \le i * 10, j++, If[binaryData4[[j]] == 0, f41[i] = f41[i] * 1, f41[i] = f41[i] * 0]];
          f41[i] = f41[i] * 0.1]
         For[i = 1, i \le 10, i++, f42[i] = 1;
          For[j = 1, j \le i * 10, j++, If[binaryData4[[j]] == 0, f42[i] = f42[i] * 0.75, f42[i] = f42[i] * 0.25]];
```

f42[i] = f42[i] \* 0.2]

```
For[i = 1, i \le 10, i++, f43[i] = 1;
                    For[j = 1, j \le i * 10, j++, If[binaryData4[[j]] == 0, f43[i] = f43[i] * 0.5, f43[i] = f43[i] * 0.5];
                    f43[i] = f43[i] * 0.4]
                  For[i = 1, i \le 10, i++, f44[i] = 1;
                    For[j = 1, j \le i * 10, j + 1, f[binaryData4[[j]] == 0, f44[i] = f44[i] * 0.25, f44[i] = f44[i] * 0.75]];
                    f44[i] = f44[i] * 0.2]
                 For[i = 1, i \le 10, i++, f45[i] = 1;
                    For[j = 1, j \le i * 10, j + +, [f[binaryData4[[j]] == 0, f45[i] * f45[i] * 0, f45[i] * f45[i] * 1]];
                    f45[i] = f45[i] * 0.1
                  For[i = 1, i \le 10, i++, f41[i] = f41[i] / s4[i];
                    f42[i] = f42[i]/s4[i];
                    f43[i] = f43[i] / s4[i];
                    f44[i] = f44[i]/s4[i];
                    f45[i] = f45[i] / s4[i]
                 myData41 = Prepend[myData41, 0.1]
                 myData42 = Prepend[myData42, 0.2]
                 myData43 = Prepend[myData43, 0.4]
                 myData44 = Prepend[myData44, 0.2]
                 myData45 = Prepend[myData45, 0.1]
                 Show[ListLinePlot[myData41, PlotStyle \rightarrow {Red, Thickness[0.01]}, PlotRange \rightarrow {{1, 11}, {0, 1}},
                       Frame → True, FrameLabel → {"Number of samples in d", "Posterior probability"},
                       FrameTicks → {{Automatic, None},
                         \{\{\{1, 0\}, \{2, 10\}, \{3, 20\},
                          {4, 30}, {5, 40}, {6, 50}, {7, 60}, {8, 70}, {9, 80}, {10, 90}, {11, 100}}, None}}],
                    ListLinePlot[myData42, PlotRange \rightarrow {{1, 11}, {0, 1}}],
                    ListLinePlot[myData43, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Green],
                    ListLinePlot[myData44, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Purple],
                    ListLinePlot[myData45, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Yellow]]
1, 1, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1
Out[369]= \{0., 0., 0., 0., 0., 0., 0., 0., 0., 0.\}
Out[370]= \{0.00104433, 0.0000147754, 2.86072 \times 10^{-10}, 4.37067 \times 10^{-14}, 4.85604 \times 10^{-15}, 4.37067 \times 10^{-15}, 4.37067
                      6.66227 \times 10^{-18}, 1.12829 \times 10^{-22}, 1.54773 \times 10^{-25}, 1.91078 \times 10^{-27}, 2.62109 \times 10^{-30}
```



```
In[392]:= myPredict4 = Array[f4, 10]
         For[i = 1, i \le 10, i++, f4[i] = 0;
          f4[i] = f4[i] + 0 * f41[i] + 0.25 * f42[i] + 0.5 * f43[i] + 0.75 * f44[i] + 1 * f45[i]
         myPredict4 = Prepend[myPredict4, 0.5]
        ListLinePlot[myPredict4, PlotRange → {{1, 11}, {0, 1}}, Frame → True,
          FrameLabel → {"Number of samples in d", "Probability that next candy is lime"},
          FrameTicks → {{Automatic, None},
            \{\{\{1, 10\}, \{2, 20\}, \{3, 30\},
             {4, 40}, {5, 50}, {6, 60}, {7, 70}, {8, 80}, {9, 90}, {10, 100}}, None}}]
out[392] = \{0.626701, 0.718114, 0.654709, 0.728076, 0.739233, 0.74484, 0.749909, 0.749995, 0.749998, 0.75\}
Out[394] = \{0.5, 0.626701, 0.718114, 0.654709, 0.728076,
          0.739233, 0.74484, 0.749909, 0.749995, 0.749998, 0.75
            1.0
            0.8
          Probability that next candy is lime
            0.6
Out[395]=
            0.4
            0.2
            0.0 L
10
                          30
                                     50
                                           60
                                                 70
                                                            90
                                                                 100
                                    Number of samples in d
          = Q2a h5,P(h5) = 0.1 
In[416]:= binaryData5 = RandomChoice[{0, 1} \rightarrow {0, 1}, 100]
         myData51 = Array[f51, 10]
        myData52 = Array[f52, 10]
        myData53 = Array[f53, 10]
        myData54 = Array[f54, 10]
        myData55 = Array[f55, 10]
         mySum5 = Array[s5, 10]
         For[i = 1, i \le 10, i++, f51[i] = 1;
          For[j = 1, j \le i * 10, j + +, [f[binaryData5[[j]] == 0, f51[i] = f51[i] * 1, f51[i] = f51[i] * 0]];
          f51[i] = f51[i] * 0.1]
         For[i = 1, i \le 10, i++, f52[i] = 1;
          For[j = 1, j \le i * 10, j++, If[binaryData5[[j]] == 0, f52[i] = f52[i] * 0.75, f52[i] = f52[i] * 0.25]];
          f52[i] = f52[i] * 0.2]
         For[i = 1, i \le 10, i++, f53[i] = 1;
          For[j = 1, j \le i * 10, j ++, If[binaryData5[[j]] == 0, f53[i] = f53[i] * 0.5, f53[i] = f53[i] * 0.5]];
```

```
For[i = 1, i \le 10, i++, f54[i] = 1;
                    For[j = 1, j \le i * 10, j + +, f[binaryData5[[j]] == 0, f54[i] * f54[i] * 0.25, f54[i] * f54[i] * 0.75]];
                    f54[i] = f54[i] * 0.2]
                 For[i = 1, i \le 10, i++, f55[i] = 1;
                    For[j = 1, j \le i * 10, j++, If[binaryData5[[j]] == 0, f55[i] = f55[i] * 0, f55[i] = f55[i] * 1]];
                    f55[i] = f55[i] * 0.1]
                  For[i = 1, i \le 10, i++, s5[i] = 0; s5[i] = s5[i] + f51[i] + f52[i] + f53[i] + f54[i] + f55[i]]
                 For[i = 1, i \le 10, i++, f51[i] = f51[i]/s5[i];
                    f52[i] = f52[i]/s5[i];
                    f53[i] = f53[i]/s5[i];
                    f54[i] = f54[i]/s5[i];
                    f55[i] = f55[i]/s5[i]]
                 myData51 = Prepend[myData51, 0.1]
                 myData52 = Prepend[myData52, 0.2]
                 myData53 = Prepend[myData53, 0.4]
                 myData54 = Prepend[myData54, 0.2]
                 myData55 = Prepend[myData55, 0.1]
                 Show[ListLinePlot[myData51, PlotStyle → Red, PlotRange → {{1, 11}, {0, 1}},
                       Frame → True, FrameLabel → {"Number of samples in d", "Posterior probability"},
                      FrameTicks → {{Automatic, None},
                        \{\{\{1, 0\}, \{2, 10\}, \{3, 20\},
                         {4, 30}, {5, 40}, {6, 50}, {7, 60}, {8, 70}, {9, 80}, {10, 90}, {11, 100}}, None}}],
                    ListLinePlot[myData52, PlotRange \rightarrow {{1, 11}, {0, 1}}],
                    ListLinePlot[myData53, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Green],
                    ListLinePlot[myData54, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Purple],
                    ListLinePlot[myData55, PlotRange → {{1, 11}, {0, 1}}, PlotStyle → Yellow]]
Out[418]= \{1.70827 \times 10^{-6}, 1.80752 \times 10^{-12}, 1.7341 \times 10^{-18}, 1.65433 \times 10^{-24}, 1.57772 \times 10^{-30}, 1.65433 \times 10^{-
                     1.50463 \times 10^{-36}, 1.43493 \times 10^{-42}, 1.36846 \times 10^{-48}, 1.30506 \times 10^{-54}, 1.2446 \times 10^{-60}
Out[419]= \{0.00349855, 3.79064 \times 10^{-6}, 3.72396 \times 10^{-9}, 3.63791 \times 10^{-12}, 3.55271 \times 10^{-15}, 
                     3.46945 \times 10^{-18}, 3.38813 \times 10^{-21}, 3.30872 \times 10^{-24}, 3.23117 \times 10^{-27}, 3.15544 \times 10^{-30}
Out[420] = \{0.100872, 0.00630243, 0.000357037, 0.0000201128, 1.13264 \times 10^{-6}, 
                     6.37831 \times 10^{-8}, 3.59185 \times 10^{-9}, 2.0227 \times 10^{-10}, 1.13905 \times 10^{-11}, 6.4144 \times 10^{-13}
```

f53[i] = f53[i] \* 0.4

```
Out[421] = \{0.895628, 0.993694, 0.999643, 0.99998, 0.999999, 1., 1., 1., 1., 1.\}
Out[422] = \{0.111654, 0.100635, 0.100036, 0.100002, 0.1, 0.1, 0.1, 0.1, 0.1, 0.1\}
Out[431]= \{0.2, 1.70827 \times 10^{-6}, 1.80752 \times 10^{-12}, 1.7341 \times 10^{-18}, 1.65433 \times 10^{-24}, 1.57772 \times 10^{-30}, 1.65433 \times 10^{-24}, 1.65433 \times 
                                                                      1.50463 \times 10^{-36}, 1.43493 \times 10^{-42}, 1.36846 \times 10^{-48}, 1.30506 \times 10^{-54}, 1.2446 \times 10^{-60}
Out[432]= \{0.4, 0.00349855, 3.79064 \times 10^{-6}, 3.72396 \times 10^{-9}, 3.63791 \times 10^{-12}, 3.55271 \times 10^{-15}, 3.63791 \times 10^{-12}, 3.55271 \times 10^{-15}, 3.63791 \times 10^{-12}, 3.63791 \times 10^{-12}
                                                                     3.46945 \times 10^{-18}, 3.38813 \times 10^{-21}, 3.30872 \times 10^{-24}, 3.23117 \times 10^{-27}, 3.15544 \times 10^{-30}
 6.37831 \times 10^{-8}, 3.59185 \times 10^{-9}, 2.0227 \times 10^{-10}, 1.13905 \times 10^{-11}, 6.4144 \times 10^{-13}
 Out[434] = \{0.1, 0.895628, 0.993694, 0.999643, 0.99998, 0.999999, 1., 1., 1., 1., 1.\}
                                                                                 0.8
                                                             Posterior probability
                                                                                 0.6
 Out[435]=
                                                                                 0.4
                                                                                 0.2
                                                                                 0.0
```

30

50

Number of samples in d

40

80

90

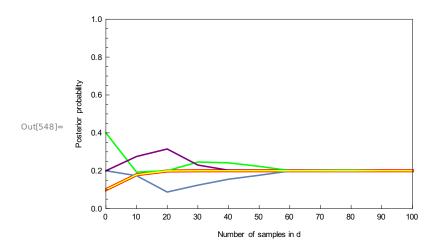
100

```
In[440]:= myPredict5 = Array[f5, 10]
         For[i = 1, i \le 10, i++, f5[i] = 0;
          f5[i] = f5[i] + 0 * f51[i] + 0.25 * f52[i] + 0.5 * f53[i] + 0.75 * f54[i] + 1 * f55[i]
         myPredict5 = Prepend[myPredict5, 0.5]
         ListLinePlot[myPredict5, PlotRange → {{1, 11}, {0, 1}}, Frame → True,
          FrameLabel → {"Number of samples in d", "Probability that next candy is lime"},
          FrameTicks → {{Automatic, None},
             \{\{\{1, 10\}, \{2, 20\}, \{3, 30\},
             \{4, 40\}, \{5, 50\}, \{6, 60\}, \{7, 70\}, \{8, 80\}, \{9, 90\}, \{10, 100\}\}, None\}\}
Out[440] = \{0.973031, 0.998422, 0.999911, 0.999995, 1., 1., 1., 1., 1., 1.\}
Out[442]= \{0.5, 0.973031, 0.998422, 0.999911, 0.999995, 1., 1., 1., 1., 1., 1.\}
             1.0
             0.8
          Probability that next candy is lime
             0.6
Out[443]=
             0.4
             0.0
                     20
                           30
                                 40
                                       50
                                             60
                                                   70
                                                              90
                                                                    100
                                     Number of samples in d
```

## ■ Q3 c

Red line indicates h1, blue line indicates h2, green line indicates h3, purple line indicates h4, yellow line indicates h5.

```
In[537]:= myReduction1 = Array[r1, 11]
                 myReduction2 = Array[r2, 11]
                 myReduction3 = Array[r3, 11]
                 myReduction4 = Array[r4, 11]
                 myReduction5 = Array[r5, 11]
                 For[i = 1, i \le 11, i++,
                   r1[i] = (myData11[[i]] + myData21[[i]] + myData31[[i]] + myData41[[i]] + myData51[[i]]) / 5]
                 For[i = 1, i \le 11, i++,
                   r2[i] = (myData12[[i]] + myData22[[i]] + myData32[[i]] + myData42[[i]] + myData52[[i]]) / 5]
                 For[i = 1, i \le 11, i++,
                   r3[i] = (myData13[[i]] + myData23[[i]] + myData33[[i]] + myData43[[i]] + myData53[[i]]) / 5]
                 For[i = 1, i \le 11, i++,
                    r4[i] = (myData14[[i]] + myData24[[i]] + myData34[[i]] + myData44[[i]] + myData54[[i]]) / 5] 
                 For[i = 1, i \le 11, i++,
                   r5[i] = (myData15[[i]] + myData25[[i]] + myData35[[i]] + myData45[[i]] + myData55[[i]]) / 5]
                 myData55[[11]]
                 Show[ListLinePlot[myReduction1, PlotStyle \rightarrow {Red, Thickness[0.01]}, PlotRange \rightarrow {{1, 11}, {0, 1}},
                      Frame → True, FrameLabel → {"Number of samples in d", "Posterior probability"},
                      FrameTicks → {{Automatic, None},
                        \{\{\{1, 0\}, \{2, 10\}, \{3, 20\},
                         {4, 30}, {5, 40}, {6, 50}, {7, 60}, {8, 70}, {9, 80}, {10, 90}, {11, 100}}, None}}],
                   ListLinePlot[myReduction2, PlotRange \rightarrow {{1, 11}, {0, 1}}},
                   ListLinePlot[myReduction3, PlotStyle \rightarrow Green, PlotRange \rightarrow {{1, 11}, {0, 1}}],
                   ListLinePlot[myReduction4, PlotStyle → Purple, PlotRange → {{1, 11}, {0, 1}}],
                   ListLinePlot[myReduction5, PlotStyle \rightarrow Yellow, PlotRange \rightarrow {{1, 11}, {0, 1}}]]
Out(537) = \{0.1, 0.179126, 0.198739, 0.199929, 0.199996, 0.2, 0.2, 0.2, 0.2, 0.2, 0.2\}
Out[538]= \{0.2, 0.173913, 0.0876121, 0.123883, 0.155273,
                    0.176216, 0.198606, 0.198046, 0.197266, 0.199856, 0.199798
Out[539]= \{0.4, 0.192561, 0.200015, 0.246132, 0.241944,
                    0.223146, 0.200919, 0.20184, 0.202707, 0.200138, 0.200202}
Out[540]= \{0.2, 0.275274, 0.314896, 0.230128, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791, 0.202791
                    0.200638, 0.200475, 0.200114, 0.200027, 0.200006, 0.200001}
Out[547]= 1.
```



In[627]:=