EECS 391

P2\_Write\_up

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1. **Noisy Fuel Guage**
2. P(B = 1) = 0.8 => P(B = 0) = 0.2

P(F = 1) = 0.9 => P(F = 0) = 0.1

P(G = 1 | B = 0, F = 0) = 0.1 => P(G = 0 | B = 0, F = 0) = 0.9

P(G = 1 | B = 1, F = 0) = 0.1 => P(G = 0 | B = 1, F = 0) = 0.9

P(G = 1 | B = 0, F = 1) = 0.2 => P(G = 0 | B = 0, F = 1) = 0.8  
 P(G = 1 | B = 1, F = 1) = 0.9 => P(G = 0 | B = 1, F = 1) = 0.1

1. Since P(X1, … , Xn) = , P(B, F, G) = P(B)P(F)P(G|B,F)

P(F|G = 0) =

=

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For simplicity, rewrite P(F|G= 0) =

Therefore, = 0.2941 which is consistent with (c).



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| F        |   phi(F) |

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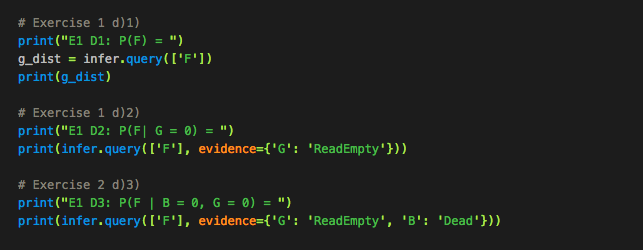
| F(Empty) |   0.2941 |

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| F(Full)  |   0.7059 |

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P(F = 0|G = 0) = 0.2941



1. P(F) and it is given in the question

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| F        |   phi(F) |

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| F(Empty) |   0.1000 |

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| F(Full)  |   0.9000 |

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1. P(F | G = 0) and it is the same as (c)

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| F        |   phi(F) |

+==========+==========+

| F(Empty) |   0.2941 |

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| F(Full)  |   0.7059 |

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1. P(F | B = 0, G= 0)

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| F        |   phi(F) |

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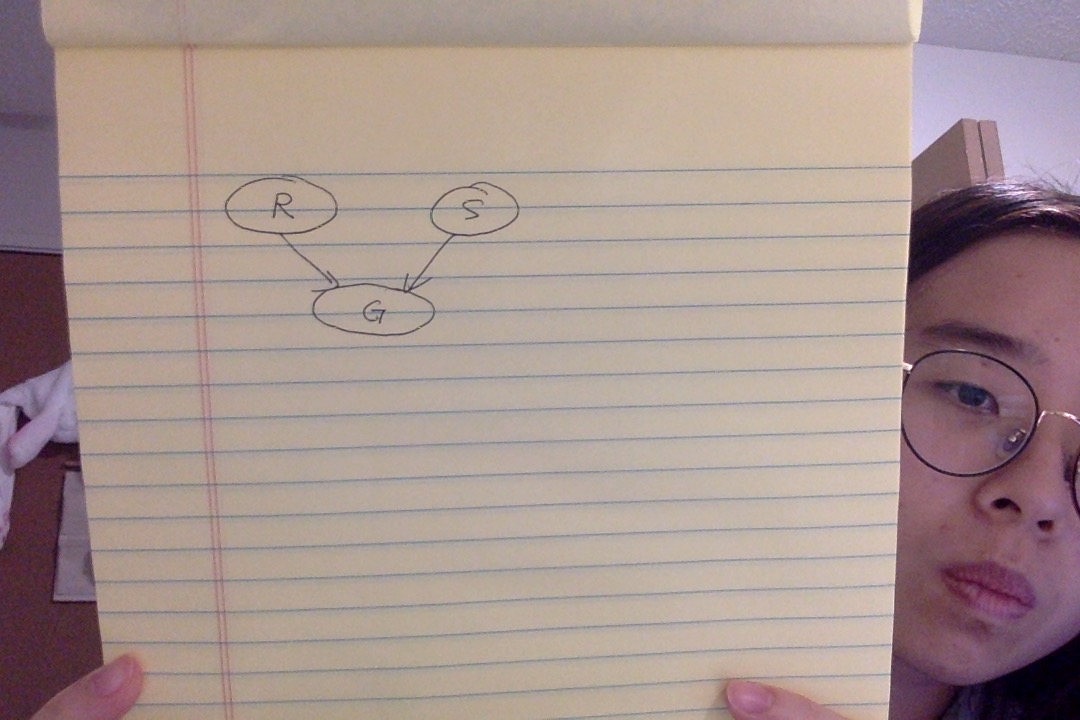
| F(Empty) |   0.1111 |

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| F(Full)  |   0.8889 |

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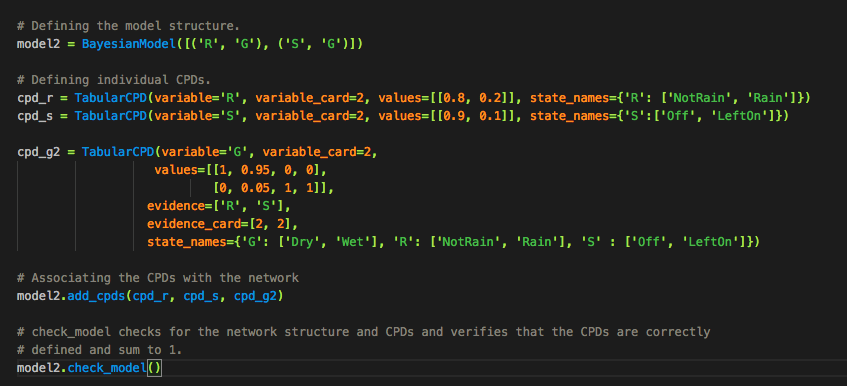
1. G is the common evidence(effect) of B and F. From d)2) to d)3), we have additional information about battery. Since the battery is dead, it is more likely that the guage does not work. Namely, the measurement from the guage is mostly incredulous (trustless). Therefore, our belief that the fuel tank is empty goes closer to when we have not made any observation. Namely, the probability moves from 0.2941 (d2) to 0.1111 that is closer to 0.1(d1).
2. The probability pf our belief if P(F|B=0). Since G has not been observed, B and F are independent. Therefore, P(F|B=0) = P(F). Namely, our belief that the fuel tank is empty is 0.1 and the fuel tank is full is 0.9.
3. **Wet Grass**

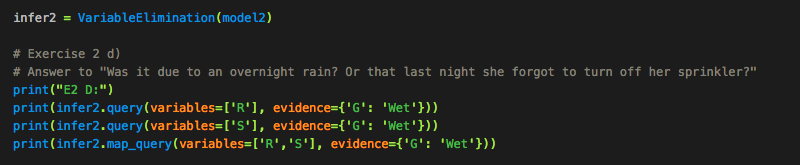


|  |  |
| --- | --- |
| P(R = 0) NotRain | P(R = 1) Rain |
| 0.8 | 0.2 |

|  |  |
| --- | --- |
| P(S = 0) Off | P(S = 1) LeftOn |
| 0.9 | 0.1 |

|  |  |  |
| --- | --- | --- |
|  | P(G = 0) Dry | P(G =1) Wet |
| R = 0, S = 0 | 1 | 0 |
| R = 0, S = 1 | 0.95 | 0.05 |
| R = 1, S = 0 | 0 | 1 |
| R = 1, S = 1 | 0 | 1 |





E2 D:

Finding Elimination Order: : 100%|██████████████| 1/1 [00:00<00:00, 2008.77it/s]

Eliminating: S: 100%|███████████████████████████| 1/1 [00:00<00:00, 1050.15it/s]

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| R          |   phi(R) |

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| R(NotRain) |   0.0196 |

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| R(Rain)    |   0.9804 |

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Finding Elimination Order: : 100%|██████████████| 1/1 [00:00<00:00, 2551.28it/s]

Eliminating: R: 100%|███████████████████████████| 1/1 [00:00<00:00, 1512.55it/s]

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| S         |   phi(S) |

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| S(Off)    |   0.8824 |

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| S(LeftOn) |   0.1176 |

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Finding Elimination Order: : : 0it [00:00, ?it/s]

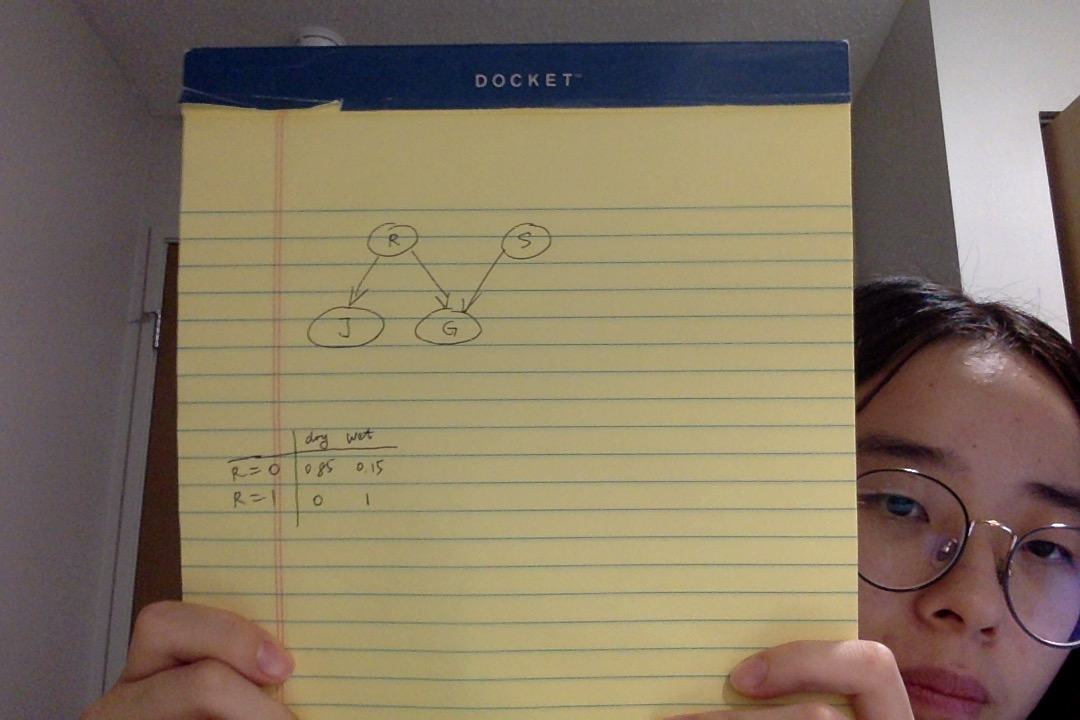
0it [00:00, ?it/s]

{'R': 'Rain', 'S': 'Off'}

Given that the grass is wet, P(NotRain|Wet) = 0.0196 and P(Rain|Wet) = 0.9804.

Given that the grass is wet, for the sprinkler, P(Off|Wet) = 0.8824 and P(LeftOn|Wet) = 0.1176.

Therefore, if Tracey sees that the grass is wet, it was most likely due to an overnight rain and the sprinkler was off.

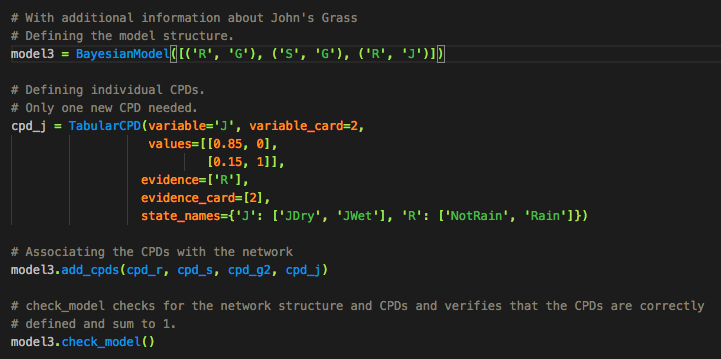


|  |  |
| --- | --- |
| P(R = 0) NotRain | P(R = 1) Rain |
| 0.8 | 0.2 |

|  |  |
| --- | --- |
| P(S = 0) Off | P(S = 1) LeftOn |
| 0.9 | 0.1 |

|  |  |  |
| --- | --- | --- |
|  | P(G = 0) Dry | P(G =1) Wet |
| R = 0, S = 0 | 1 | 0 |
| R = 0, S = 1 | 0.95 | 0.05 |
| R = 1, S = 0 | 0 | 1 |
| R = 1, S = 1 | 0 | 1 |

|  |  |  |
| --- | --- | --- |
|  | P(J = 0) JDry | P(J =1) JWet |
| R = 0 | 0.85 | 0.15 |
| R = 1 | 0 | 1 |



1. Since P(X1, … , Xn) = , P(J,R, G, S) = P(R)P(S)P(J|R)P(G|R,S)

P(S|G = 1, J = 1) =

=

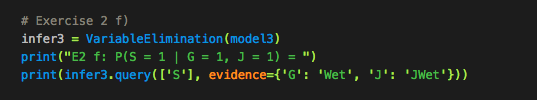
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For simplicity, rewrite P(S|G = 1, J = 1) =

Therefore, = 0.103 which is consistent with the value from toolbox.



E2 f: P(S = 1 | G = 1, J = 1) =

Finding Elimination Order: : 100%|██████████████| 1/1 [00:00<00:00, 1302.17it/s]

Eliminating: R: 100%|███████████████████████████| 1/1 [00:00<00:00, 1253.53it/s]

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| S         |   phi(S) |

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| S(Off)    |   0.8973 |

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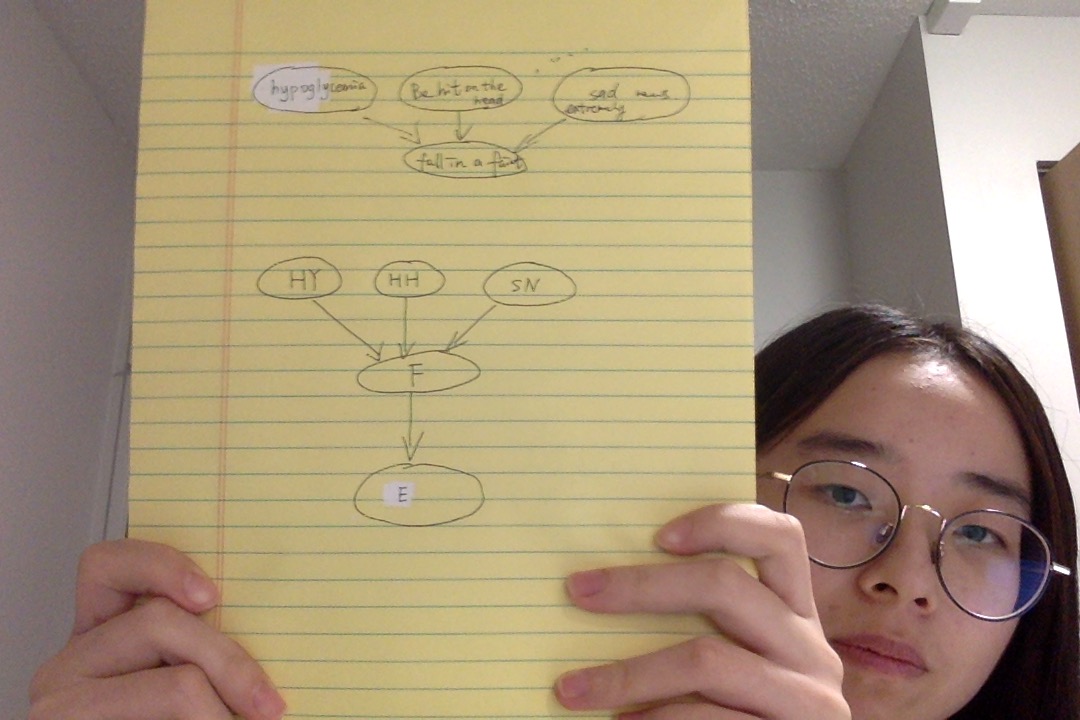
| S(LeftOn) |   0.1027 |

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1. We have additional information about the condition of John’s grass. Since J is only dependent on R, the probability that there was overnight rain increases. Since G is the common evidence(effect) of R and S and G has been observed, the influences flows from R to S. Therefore, S decreases. Namely, Tracery’s belief that she left the sprinkler on decreases.
2. **Extra**

Chris in on his way to Quad and he sees a girl fainted. He wonders: Was the faint due to hypoglycemia? Or she was hit on the head? Or she heard an extremely sad news?

The noisy-OR model of the Bayes net that models this scenario is shown below. Using the following variables: HY = the girl has hypoglycemia; HH = the girl’s head was hit; SN = the girl heard an extremely sad news; F = the girl falls in a faint.



Assumes that the parent causes of effect F contribute independently. Therefore, the probability that none of them caused effect F is simply the product of the probabilities that each one did not cause F. The probability that any of them caused F is just one minus the above.

|  |  |
| --- | --- |
| P(HY = 0) NoHypoglycemia | P(HY = 1) Hypoglycemia |
| 0.8 | 0.2 |

|  |  |
| --- | --- |
| P(HH = 0) NoHeadHit | P(HH = 1) HeadHit |
| 0.95 | 0.05 |

|  |  |
| --- | --- |
| P(SN = 0) NoSadNews | P(SN = 1) SadNews |
| 0.9 | 0.1 |

Conditional probability table for P(F|HY, HH, SN) as calculated from the noisy-OR model.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| HY | HH | SN | P(F) | P(F) |
| 0 | 0 | 0 | 0 | 1 |
| 0 | 0 | 1 | 0.2 | 0.8 |
| 0 | 1 | 0 | 0.9 | 0.1 |
| 0 | 1 | 1 | 1-(1-0.2)(1-0.9)= 0.92 | 0.08 |
| 1 | 0 | 0 | 0.7 | 0.3 |
| 1 | 0 | 1 | 1-(1-0.7)(1-0.2)= 0.76 | 0.24 |
| 1 | 1 | 0 | 1-(1-0.7)(1-0.9)= 0.97 | 0.03 |
| 1 | 1 | 1 | 1-(1-0.2)(1-0.9)(1-0.7))= 0.976 | 0.024 |