

1. (2 points) Honor Code

I promise that I will complete this quiz independently and will not use any electronic products or paper-based materials during the quiz, nor will I communicate with other students during this quiz.

I will not violate the Honor Code during this quiz.

☒ True ☐ False

2. (18 points) True or False

(a) (1') A problem in NP is NP-Complete if any other problems in NP can be reduced to it in polynomial time.

☒ True ☐ False

(b) (1') A problem in NP is NP-Complete if it can be reduced to another problem in NP in polynomial time.

☐ True ☒ False

(c) (1') A problem in NP is NP-Complete if it can be reduced to the 3-SAT problem in polynomial time.

☐ True ☒ False

(d) (1') A problem in NP is NP-Complete if the 3-SAT problem can be reduced to it in polynomial time.

☒ True ☐ False

(e) (1') A problem in NP is NP-Complete if some problems in NP can be reduced to it in polynomial time.

☐ True ☒ False

(f) (1') A problem in NP is NP-Complete if there exists another NP-Complete problem which can be reduced to it in polynomial time.

☒ True ☐ False

(g) (1') According to the Cook-Levin Theorem, any problem in NP can be reduced to SAT in polynomial time.

☒ True ☐ False

(h) (1') If a problem is in NP-Complete, any NP-Complete problem can reduce to it in polynomial time.

☒ True ☐ False

(i) (1') Any problem in P is in NP.

☒ True ☐ False

(j) (1') If $L_1 \leq_p L_2$ and L_1 is in NP, then so is L_2 .

☐ True ☒ False

(k) (1') If $L_1 \leq_p L_2$ and L_1 is in NP-Complete, then so is L_2 .

☐ True ☒ False

(l) (1') If $L_1 \leq_p L_2$ and $L_1 \in P$, then $L_2 \in P$.

☐ True ☒ False

(m) (1') If $L_1 \leq_p L_2$ and $L_1 \notin P$, then $L_2 \notin P$.

☒ True ☐ False

(n) (1') For any positive integer $k \geq 2$, k-SAT \in NP.

☒ True ☐ False

(o) (1') For any positive integer $k \geq 2$, k-SAT \in NP-Complete.

☐ True ☒ False

(p) (1') For any problem $L \in$ NP, $L \leq_p$ 3-SAT.

☒ True ☐ False

(q) (1') 2-COLOR \leq_p 3-COLOR \leq_p 3-SAT.

☒ True ☐ False

(r) (1') If CLIQUE can be solved in polynomial time, then any problem in NP can be solved in polynomial time.

☒ True ☐ False

3. (10 points) P and NP worlds

Give out statements, please select their correctness from the four below.

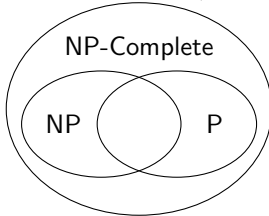
- A. True if and only if $P = NP$ B. True regardless of whether $P = NP$ or not
 C. False if and only if $P = NP$ D. False regardless of whether $P = NP$ or not

- (a) (2') There are problems in NP that cannot be solved in exponential time. D
 (b) (2') If problem $L_1 \in NP$, then for any problem $L_2 \in P$, L_2 can be reduced to L_1 in polynomial time. B
 (c) (2') Minimum Spanning Tree Problem is in NP. B
 (d) (2') Minimum Spanning Tree Problem is in NP-Complete. A
 (e) (2') $3\text{-SAT} \leq_p 2\text{-SAT}$. A

4. (10 points) Venn diagrams for P and NP

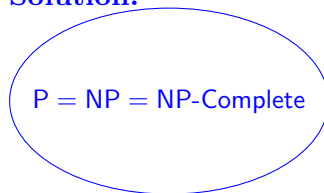
Draw Venn diagrams which represent the relationship among P, NP, and NP-Complete under 2 circumstances.

Example: If $A \neq B$, $A \cap B \neq \emptyset$, $A \subset C$, $B \subset C$, then the venn diagrams can be drawn like:



- (a) (4') If $P = NP$, draw Venn diagrams which represent the relationship among P, NP, and NP-Complete under 2 circumstances.

Solution:



- (b) (6') If $P \neq NP$, draw Venn diagrams which represent the relationship among P, NP, and NP-Complete under 2 circumstances.

Solution:

