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ML:Clustering

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Unsupervised Learning: Introduction

Unsupervised learning is contrasted from supervised learning because it uses an **unlabeled** training set rather than a labeled one.

In other words, we don't have the vector y of expected results, we only have a dataset of features where we can find structure.

Clustering is good for:

- Market segmentation
- Social network analysis
- Organizing computer clusters
- Astronomical data analysis

K-Means Algorithm

The K-Means Algorithm is the most popular and widely used algorithm for automatically grouping data into coherent subsets.

- 1. Randomly initialize two points in the dataset called the *cluster centroids*.
- 2. Cluster assignment: assign all examples into one of two groups based on which cluster centroid the

example is closest to.

- 3. Move centroid: compute the averages for all the points inside each of the two cluster centroid groups, then move the cluster centroid points to those averages.
- 4. Re-run (2) and (3) until we have found our clusters.

Our main variables are:

K (number of clusters)

Training set $x^{(1)}, x^{(2)}, \dots, x^{(m)}$ Where $x^{(i)} \in \mathbb{R}^n$

Note that we will not use the $x_0 = 1$ convention.

The algorithm:

```
Randomly initialize K cluster centroids mu(1), mu(2), ..., mu(K)
Repeat:
   for i = 1 to m:
      c(i) := index (from 1 to K) of cluster centroid closest to x(i)
   for k = 1 to K:
      mu(k) := average (mean) of points assigned to cluster k
```

The **first for-loop** is the 'Cluster Assignment' step. We make a vector c where c(i) represents the centroid assigned to example x(i).

We can write the operation of the Cluster Assignment step more mathematically as follows:

$$c^{(i)} = \min_{k} ||x^{(i)} - \mu_{k}||^{2}$$

That is, each $c^{(i)}$ contains the $k^{(th)}$ centroid that has minimal distance to $x^{(i)}$.

By convention, we square the right-hand-side, which makes the function we are trying to minimize more sharply increasing. It is mostly just a convention.

The **second for-loop** is the 'Move Centroid' step where we move each centroid to the average of its group.

More formally, the equation for this loop is as follows:

$$\mu_k = \frac{1}{n} \left[x^{(k_1)} + x^{(k_2)} + \dots + x^{(k_n)} \right] \in \mathbb{R}^n$$

Where each of $x^{(k_1)}, x^{(k_2)}, \dots, x^{(k_n)}$ are the training examples assigned to group μ_k .

If you have a cluster centroid with **0 points** assigned to it, you can randomly **re-initialize** that centroid to a new point. You can also simply **eliminate** that cluster group.

After a number of iterations the algorithm will **converge**, where new iterations do not affect the clusters.

Note on non-separated clusters: some datasets have no real inner separation or natural structure. K-means can still evenly segment your data into K subsets, so can still be useful in this case.

Optimization Objective

Recall some of the parameters we used in our algorithm:

 $c^{(i)} = \text{index of cluster } (1,2,...,K) \text{ to which example } x^{(i)} \text{ is currently assigned}$

$$\mu_k = \text{cluster centroid } k \ (\mu_k \in \mathbb{R}^n)$$

 $\mu_{c^{(i)}}$ = cluster centroid of cluster to which example $x^{(i)}$ has been assigned

Using these variables we can define our **cost function**:

$$J(c^{(i)}, \dots, c^{(m)}, \mu_1, \dots, \mu_K) = \frac{1}{m} \sum_{i=1}^{m} ||x^{(i)} - \mu_{c^{(i)}}||^2$$

Our **optimization objective** is to minimize all our parameters using the above cost function:

$$min_{c,\mu} J(c,\mu)$$

That is, we are finding all the values in sets C, representing all our clusters, and μ , representing all our centroids, that will minimize **the average of the distances** of every training example to its corresponding cluster centroid.

The above cost function is often called the **distortion** of the training examples.

In the **cluster assignment step**, our goal is to:

Minimize
$$J(...)$$
 with $c^{(1)}, ..., c^{(m)}$ (holding $\mu_1, ..., \mu_K$ fixed)

In the **move centroid** step, our goal is to:

Minimize
$$J(...)$$
 with $\mu_1, ..., \mu_K$

With k-means, it is **not possible for the cost function to sometimes increase**. It should always descend.

Random Initialization

There's one particular recommended method for randomly initializing your cluster centroids.

- 1. Have K < m. That is, make sure the number of your clusters is less than the number of your training examples.
- 2. Randomly pick K training examples
- 3. Set μ_1, \dots, μ_k equal to these K examples.

K-means can get stuck in local optima. To decrease the chance of this happening, you can run the algorithm on many different random initializations.

```
for i = 1 to 100:

randomly initialize k-means

run k-means to get 'c' and 'm'

compute the cost function (distortion) J(c,m)

pick the clustering that gave us the lowest cost
```

Choosing the Number of Clusters

Choosing K can be quite arbitrary and ambiguous.

The elbow method: plot the cost J and the number of clusters K. The cost function should reduce as we increase the number of clusters, and then flatten out. Choose K at the point where the cost function starts to flatten out.

However, fairly often, the curve is **very gradual**, so there's no clear elbow.

Note: J will always decrease as K is increased. The one exception is if k-means gets stuck at a bad local optimum.

Another way to choose K is to observe how well k-means performs on a **downstream purpose**. In other words, you choose K that proves to be most useful for some goal you're trying to achieve from using these clusters.

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