

HW2 陳偉博 110261035

Problem 1.

(a) $64 \Rightarrow 0100\ 0000$, $64+64 \Rightarrow 0100\ 0000+0100\ 0000=10000000$

(Overflow in signed number)

(b) $127 \Rightarrow 0111\ 1111$ 2' s complement $\Rightarrow -127 = 1000\ 0001$

$30 = 0001\ 1110$, $-127+30 = 1001\ 1111 = -97$ (Correct)

(c) In (b), -127 is known. $-127-1 = 1000\ 0001 - 0000\ 0001$

$= 1000\ 0000 = -128$ (Correct)

(d) $38 = 0010\ 0110$, $40 = 0010\ 1000$ 2' s complement \Rightarrow

$-40 = 1101\ 1000$,

$38+(-40) = 0010\ 0110+1101\ 1000=1111\ 1110 = -2$ (Correct)

Problem 2.

(a) Using a byte(8bits), $20 = 0001\ 0100 \Rightarrow -20 = 1000\ 1100$

In hexadecimal, $1110\ 1100 \Rightarrow 0xEC$

(b) Using a byte(8bits), $114 = 0111\ 0010$

In hexadecimal, $0111\ 0010 \Rightarrow 0x72$

(c) Using a byte(8bits), $-128 = 1000\ 0000$

In hexadecimal, $1000\ 0000 \Rightarrow 0x80$

(d) Using a half words(16bits),

$$129 = 0000\ 0000\ 1000\ 0001$$

$$\Rightarrow -129 = 1111\ 1111\ 0111\ 1111$$

In hexadecimal, 0xff7f

Problem 3.

In 6 bits system, if the number is out of range $-32 \sim 31$ in signed number or $0 \sim 63$ in unsigned number, Overflow Flag (OF) is set to be 1 and Carry Flag is set to be 1, respectively.

$$(a) -7 + (-29) = -36 \text{ OF}=1, \text{ CF}=1$$

$$(b) 31 + 11 = 42 \text{ OF}=1, \text{ CF}=0$$

$$(c) 15 - 19 = -4 \text{ OF}=0, \text{ CF}=1$$

Problem 4.

1 byte = 8 bits, 1 word = 4bytes (32bits), 1 half word = 2byte(16bits)

Range:

1 byte $\Rightarrow -128 \sim 127$, 1 word $\Rightarrow -2,147,483,648 \sim 2,147,483,647$

1 half word $\Rightarrow -32768 \sim 32767$

(a) -32765 included in a half word and a word

(b) 254 included in a half word and a word

(c)-1000000 included in word

(d)-128 included in a byte, a word and a half word

Problem 5.

1. $-A+B$ (where $B > A$)

$$A' + B = (2^n - 1 - A) + B = 2^n + (B - A) - 1$$

(The end-around carry which is equivalent to subtracting 2^n and adding 1)

2. $-A-B$ ($A+B < 2^{n-1}$)

$$A' + B' = (2^n - 1 - A) + (2^n - 1 - B) = 2^n + [2^n - 1 - (A+B)] - 1$$

After end-around carry, the answer is correct ($2^n - 1 - (A+B) = (A+B)'$)