

# Statistical Inference Assignment - Part 1

*Tomás A. Maccor*

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## Synopsis

In this assignment we are going to verify if the postulates of the Central Limit Theorem (CLT) stand for an exponential distribution density. That is, as we obtain a higher **N** of random samples from an Exponential distribution, the distribution of the mean of each of these N random samples will approximate a Normal distribution (regardless of the fact that the samples are obtained from an exponential distribution density).

We will also try to prove another of the CLT postulates: that the average of the sample means will be the population mean. In other words, we add up the means from all of the samples, find the average —> and that average will be your actual population mean. The same can be applied for finding the standard deviation of your population (distribution, in this case)

## Basic Facts

### EXPONENTIAL distribution parameters

Mean =  $1/\lambda$

$\lambda$  (lambda) = rate parameter for the distribution St. dev. =  $1/\lambda$

We will work with an exponential distribution that has  $\lambda = 0.2$  Therefore, the mean of this particular distribution is 0.5 ( $1/0.2$ )

## Simulation

We will simulate obtaining 1000 samples from an exponential distribution with  $\lambda=0.2$ , each of size 40 ( $n=40$ ). So here we go:

```
averages <- NULL

for (i in 1:1000)
{
  averages <- c(averages, mean(rexp(40, 0.2)))
}

head(averages)

## [1] 4.298304 4.770915 5.559593 4.620831 4.935799 5.865961
```

The average of the 1000 sample means is This is almost identical to the theoretical mean for an exponential distribution with  $\lambda = 0.2$

Our original standard deviation is the same as the mean,  $1 / \lambda$ , so we just have to square it to get the variance for the exponential distribution with  $\lambda = 0.2$ :

```
theoreticalVariance <- (1/0.2)^2 / 40  
print(theoreticalVariance)
```

```
## [1] 0.625
```

If we then calculate the variance of our own sampling data, we get a close approximation:

```
print(var(averages))
```

```
## [1] 0.5904568
```