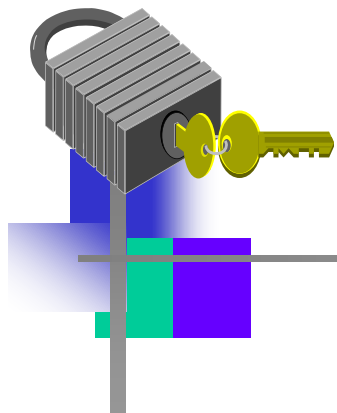


Computer and Information Security

Chapter 3 Symmetric Key Crypto

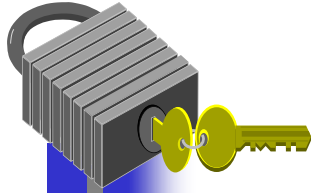


Chapter 3:

Symmetric Key Crypto

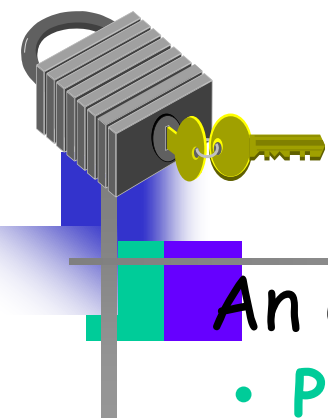
The chief forms of beauty are order and symmetry...
— Aristotle

“You boil it in sawdust: you salt it in glue:
You condense it with locusts and tape:
Still keeping one principal object in view —
To preserve its symmetrical shape.”
— Lewis Carroll, *The Hunting of the Snark*



Symmetric Encryption

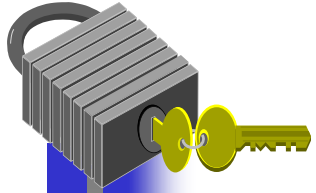
- Called conventional/private-key single-key encryption
- Sender and recipient share a common key
- All classical encryption algorithms are private-key
- Symmetric Encryption was the only type prior to invention of public-key in 1970's and is most widely used



Conventional Encryption Principles

An encryption scheme has five ingredients

- Plain text
- Encryption algorithms
- Public and private keys
- Cipher text
- Decryption algorithm
- Agents possess their private keys
- Access other public keys from a central repository
- Security depends on the secrecy of the **key**, not the secrecy of the algorithm



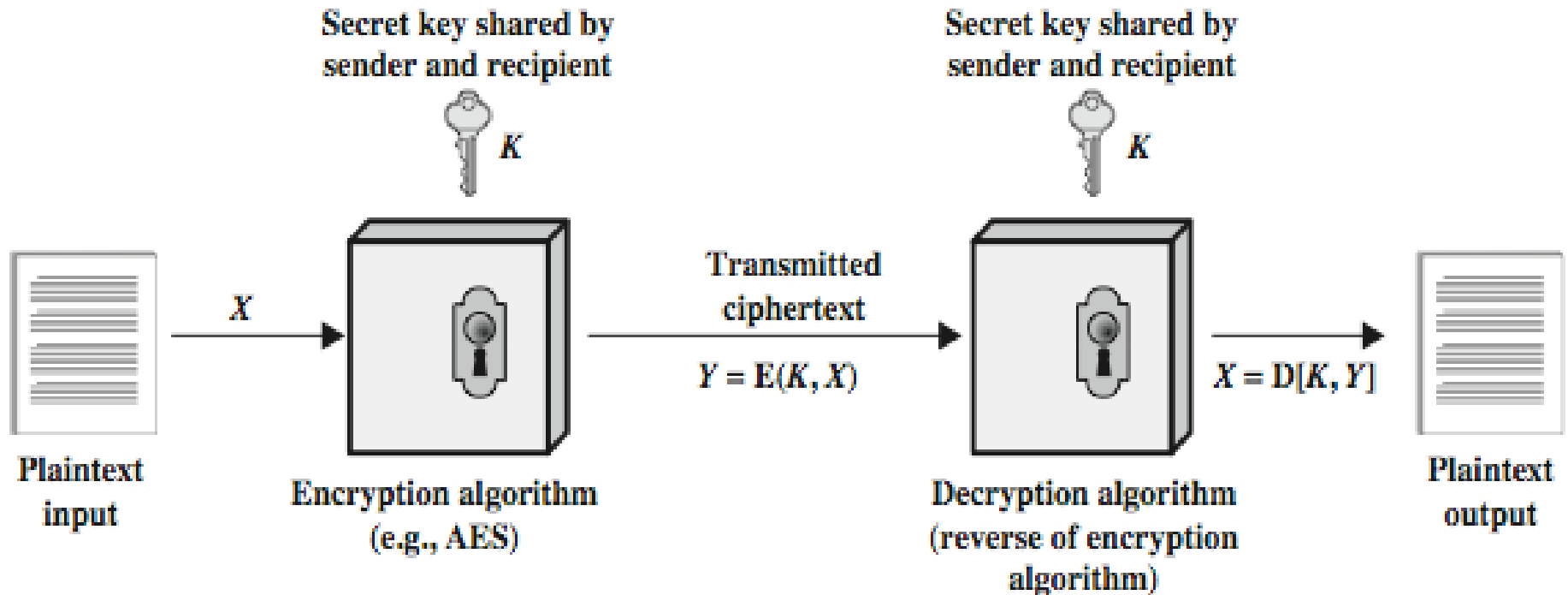
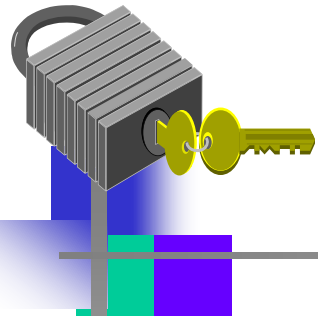
Conventional Encryption

Algorithm Components:

- **Plain Text**- original data or input
- **Encryption Algorithm**- performs substitutions or transformations on the plaintext
- **Public and Private Keys**- also input determines the substitutions/transpositions
- **Cipher Text**- scrambled message or output
- **Decryption Algorithm**- encryption algorithm run backward, taking the cipher text and producing the plain text.

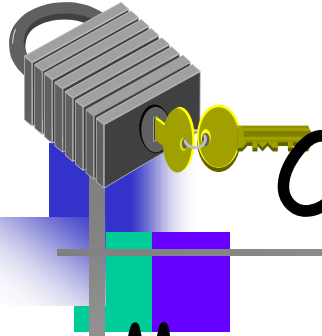
<https://www.youtube.com/watch?v=fNC3jCCGJ0o>

Conventional Encryption Principles



Asymmetric Encryption:

<https://www.youtube.com/watch?v=E5FEqGYLL0o>

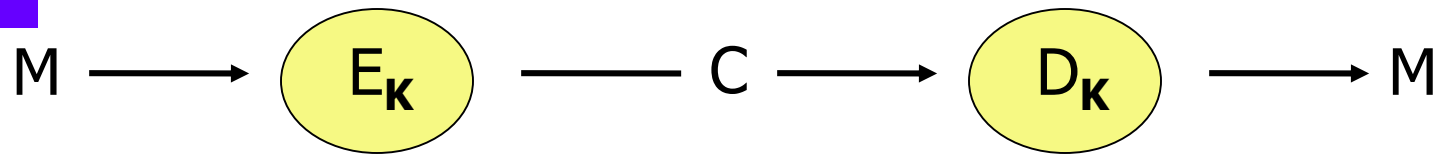


Conventional Encryption

- More rigorous definition
- Five components to the algorithm
 - A **Plaintext message space**, \mathcal{M}
 - A family of **enciphering transformations**, $E_K: \mathcal{M} \rightarrow \mathcal{C}$, where $K \in \mathcal{K}$
 - A **key space**, \mathcal{K}
 - A **ciphertext message space**, \mathcal{C}
 - A family of **deciphering transformations**, $D_K: \mathcal{C} \rightarrow \mathcal{M}$, where $K \in \mathcal{K}$



Conventional Encryption



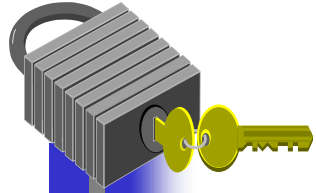
E_K defined by an encrypting algorithm E

D_K defined by a decrypting algorithm D

For given K , D_K is the **inverse** of E_K , i.e.,

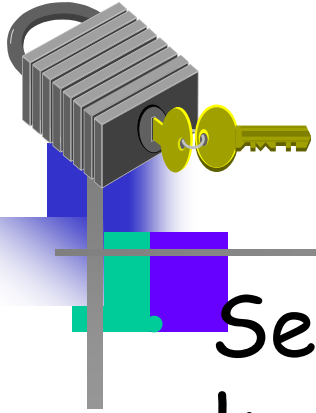
$$D_K(E_K(M)) = M$$

for every plain text message M



Requirements

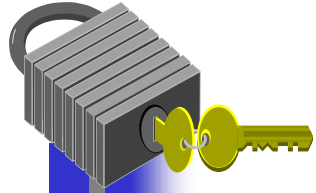
- Two requirements for secure use of symmetric encryption:
 - a strong encryption algorithm
 - a secret key known only to sender / receiver
- Mathematically have:
$$Y = E(K, X)$$
$$X = D(K, Y)$$
- Assume encryption algorithm is known
- Implies a secure channel to distribute key



Symmetric Encryption

Security depends on the secrecy of the key, NOT the secrecy of the algorithm

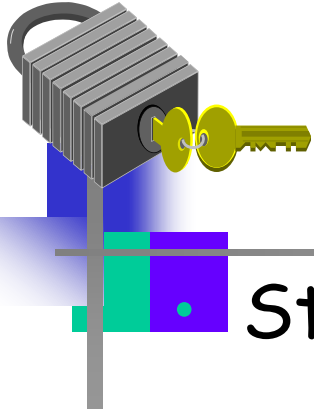
- Do not need to keep the algorithm secret- only the key
- This feature makes symmetric encryption feasible for widespread use.



Cryptography

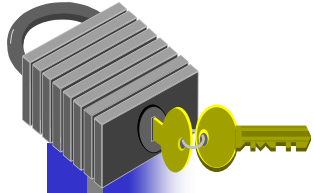
Classified according to three independent dimensions:

- The type of operations used for transforming plaintext to ciphertext
 - Substitution
 - Transposition
 - Product
- The number of keys used
 - **Symmetric** (single key or secret- key or private-key)
 - **Asymmetric** (two-keys, or public-key encryption)
- The way in which the plaintext is processed
 - Block- a block at a time
 - Stream- one element at a time



Symmetric Key Crypto

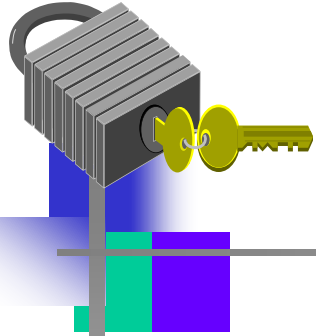
- Stream cipher — based on one-time pad
 - Except that key is relatively short
 - Key is stretched into a long **keystream**
 - Keystream is used just like a one-time pad
- Block cipher — based on codebook concept
 - Block cipher key determines a codebook
 - Each key yields a different codebook
 - Employs both “confusion” and “diffusion”



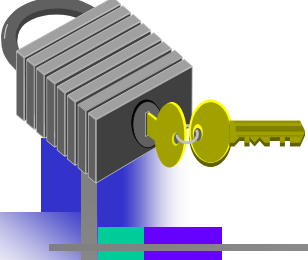
Random Numbers

- Many uses of random numbers in cryptography
 - nonces in authentication protocols to prevent replay
 - session keys
 - public key generation
 - keystream for a one-time pad
- Critical that these values be
 - statistically random, uniform distribution, independent (eg. Same number of 0's and 1's)
 - unpredictability of future values from previous values
- True random numbers provide this
- Care needed with generated random numbers

Pseudo Random Number Generators (PRNGs)



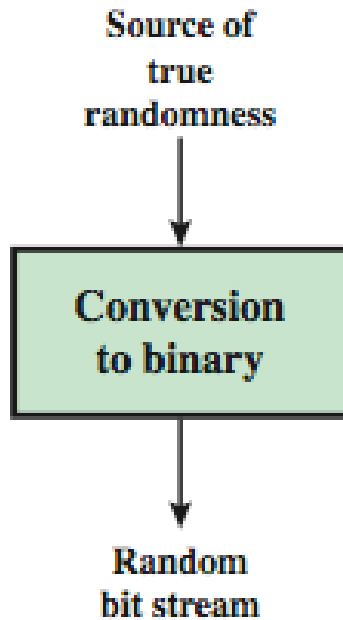
- Often use deterministic algorithmic techniques to create "random numbers"
 - although are not truly random
 - can pass many tests of "randomness"
- Known as "pseudorandom numbers"
- Created by "Pseudorandom Number Generators (PRNGs)"



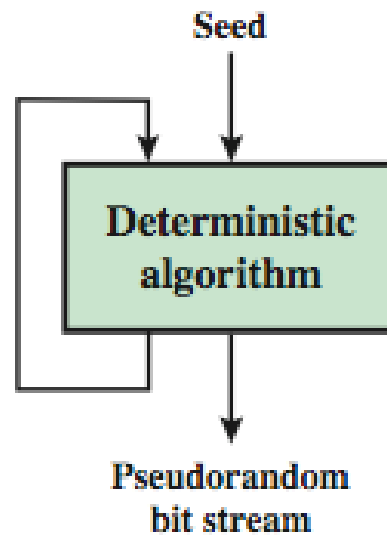
True and Pseudo Random Numbers

- TRNG - true random number generator
 - Takes a source that is random, entropy source, such as the system clock
- PRNG - pseudorandom number generator
 - Takes a fixed value called the seed
 - Produces output using a deterministic algorithm
- PRF - pseudorandom function
 - takes as input a seed plus some context specific values, such as a user ID or an application ID.

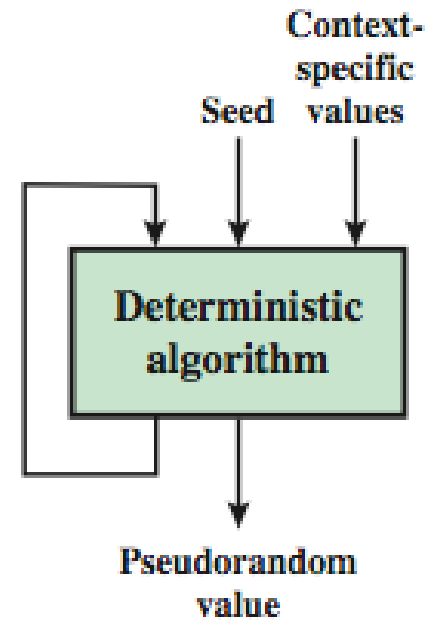
True and Pseudo Random Numbers



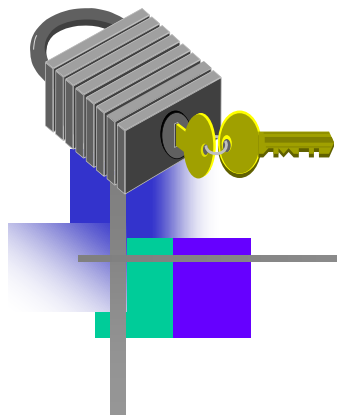
(a) TRNG



(b) PRNG



(c) PRF



Stream Ciphers

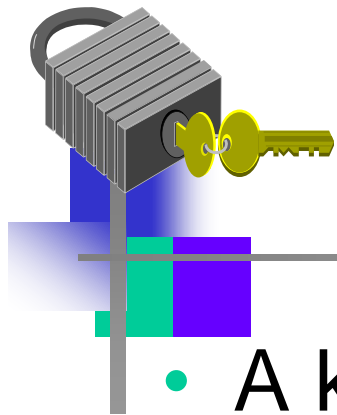




Stream Ciphers

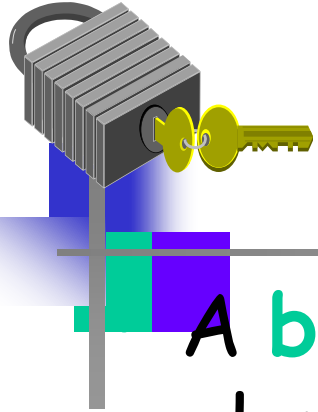
Once upon a time, not so very long ago, stream ciphers were the king of crypto

- Today, not as popular as block ciphers
- We'll discuss two stream ciphers...
- A5/1
 - Based on shift registers
 - Used in GSM mobile phone system
- RC4
 - Based on a changing lookup table
 - Used many places



Stream Cipher

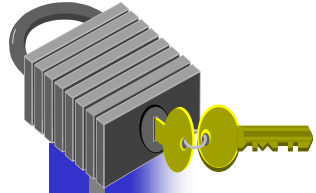
- A key is input to a pseudorandom bit generator that produces an apparently random keystream of bits.
- These bits are XOR'd with message to encrypt it,
- They are XOR'd again to decrypt it by the receiver.



Block and Stream Ciphers

A **block cipher** inputs a block of elements and produces an output block for each input block.

- A **stream cipher** processes the input elements continuously, producing output one element at a time.
- Block ciphers are more common, but there are applications which use stream ciphers.



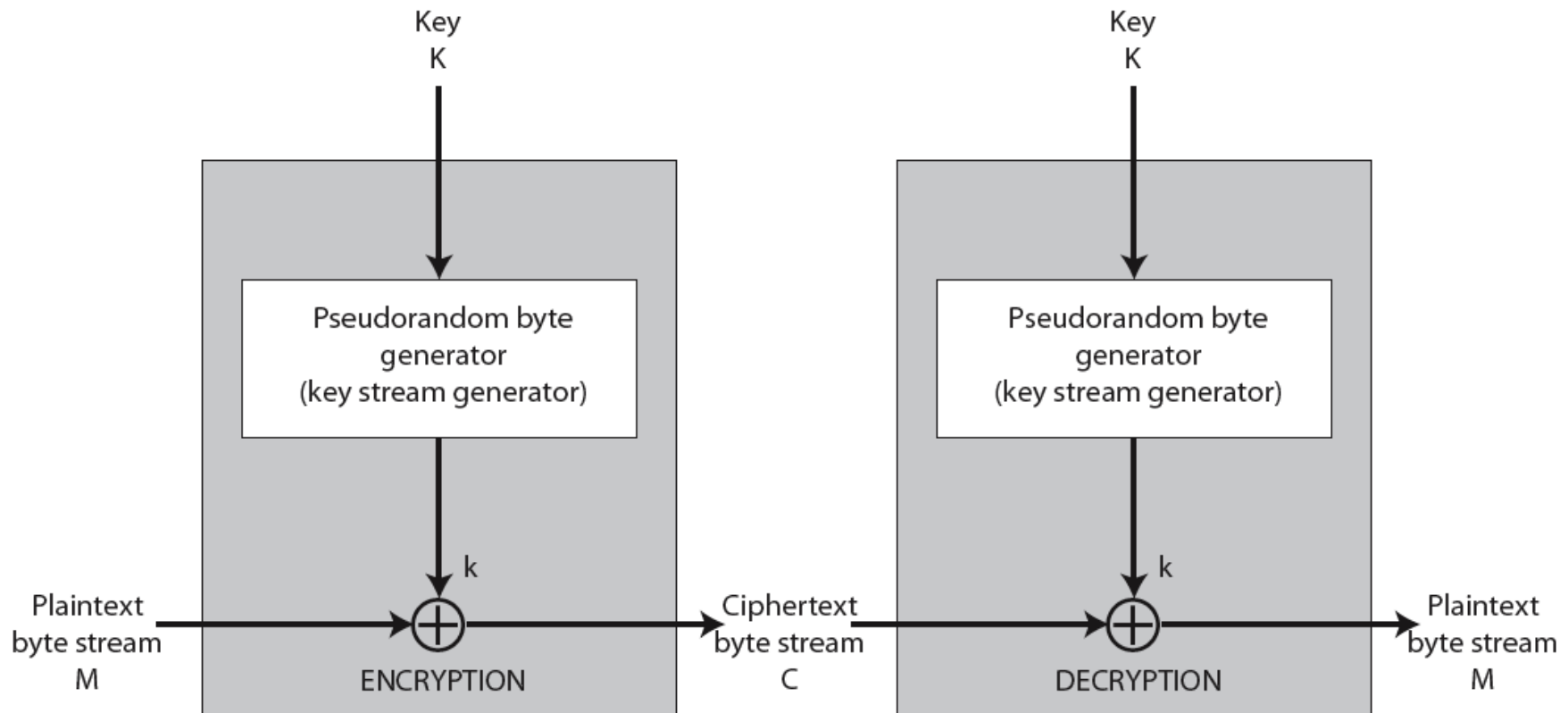
Stream Cipher Properties

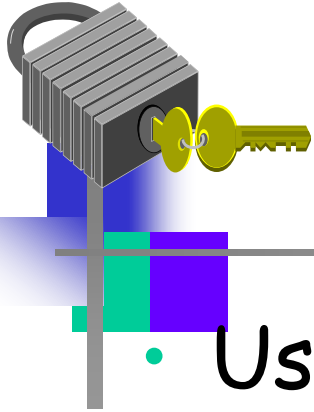
Some design considerations are:

- long period with no repetitions
- statistically random
- depends on large enough key
- large linear complexity
- Properly designed, can be as secure as a block cipher with same size key
- Usually simpler & faster



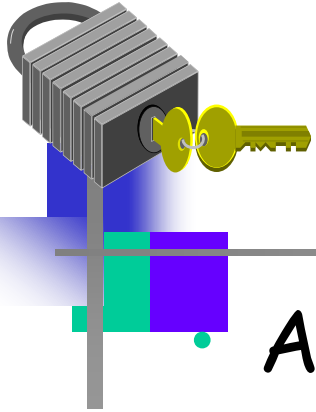
Stream Cipher Structure





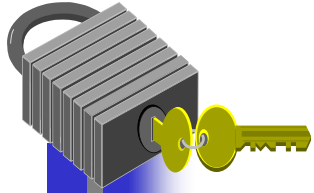
A5/1: Shift Registers

- Used for confidentiality in GSM (Global System for Mobile) cell phones
- A5/1 uses 3 *shift registers*
 - X: 19 bits ($x_0, x_1, x_2, \dots, x_{18}$)
 - Y: 22 bits ($y_0, y_1, y_2, \dots, y_{21}$)
 - Z: 23 bits ($z_0, z_1, z_2, \dots, z_{22}$)
 - *Note total bits = 64 (power of 2).



A5/1: Majority Function

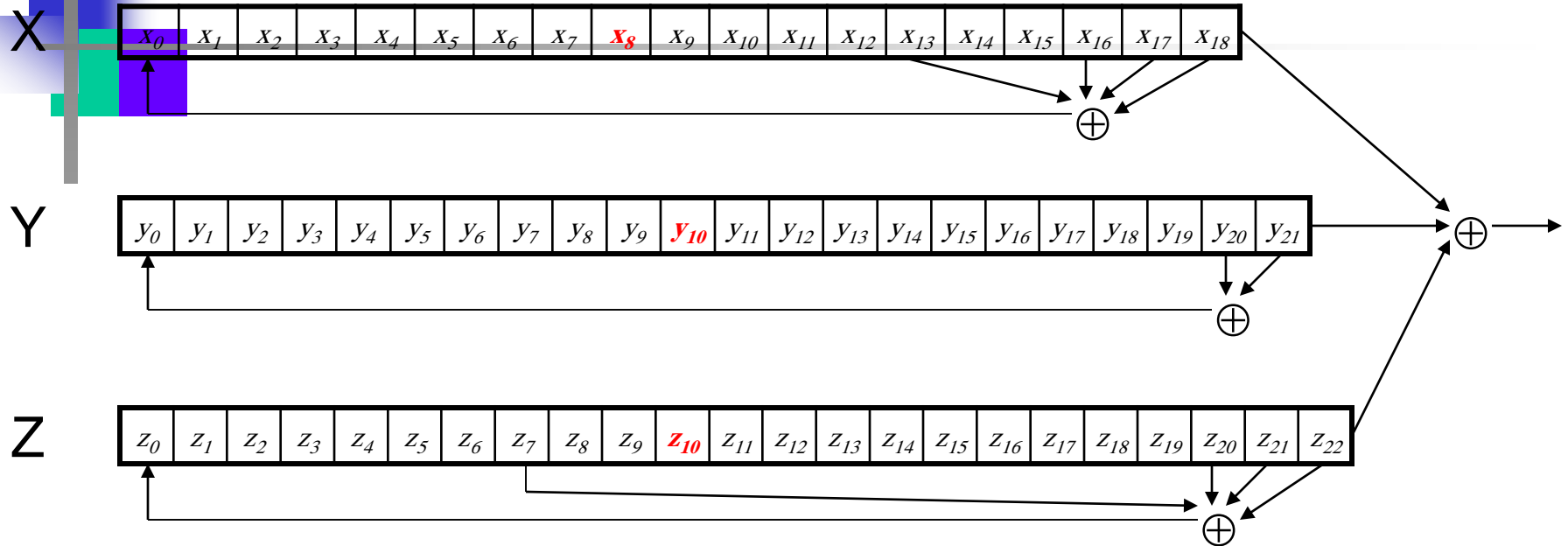
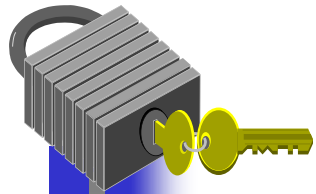
- A5/1 also uses a majority function
- A majority function such as $\text{maj}(x,y,z)$ is defined as a function from multiple inputs to one output.
- Its value is false when $n/2$ or more inputs are false and true otherwise.
- Here there are an odd number of bits so there cannot be a tie.



A5/1: Keystream

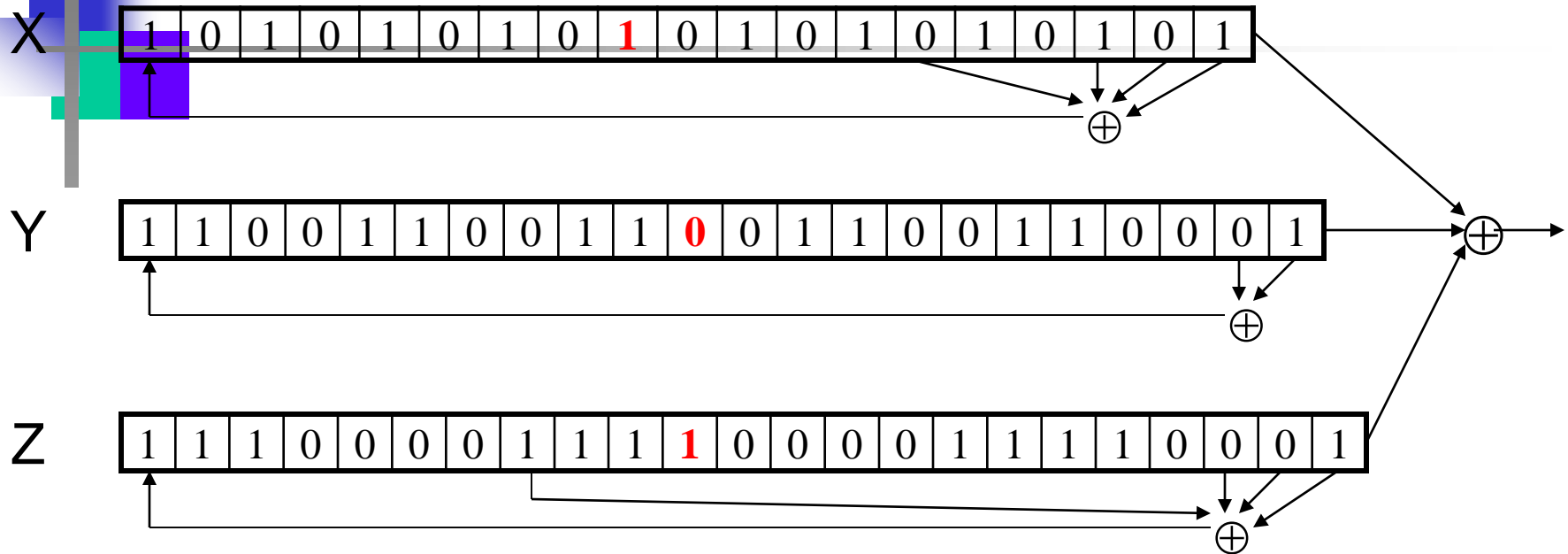
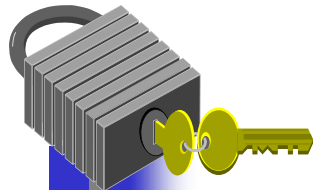
- At each step: $m = \text{maj}(x_8, y_{10}, z_{10})$
 - Examples: $\text{maj}(0,1,0) = 0$ and $\text{maj}(1,1,0) = 1$
- If $x_8 = m$ then **X steps**
 - $t = x_{13} \oplus x_{16} \oplus x_{17} \oplus x_{18}$
 - $x_i = x_{i-1}$ for $i = 18, 17, \dots, 1$ and $x_0 = t$
- If $y_{10} = m$ then **Y steps**
 - $t = y_{20} \oplus y_{21}$
 - $y_i = y_{i-1}$ for $i = 21, 20, \dots, 1$ and $y_0 = t$
- If $z_{10} = m$ then **Z steps**
 - $t = z_7 \oplus z_{20} \oplus z_{21} \oplus z_{22}$
 - $z_i = z_{i-1}$ for $i = 22, 21, \dots, 1$ and $z_0 = t$
- Keystream **bit** is $x_{18} \oplus y_{21} \oplus z_{22}$

A5/1

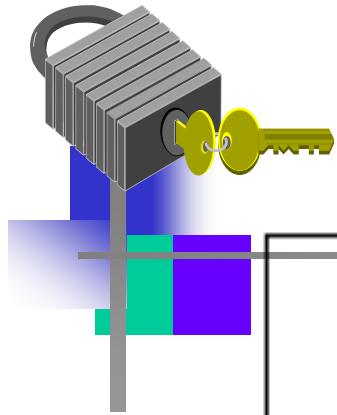


- Each variable here is a single bit
- Key is used as **initial fill** of registers
- Each register steps (or not) based on $\text{maj}(x_8, y_{10}, z_{10})$
- Keystream bit is XOR of rightmost bits of registers

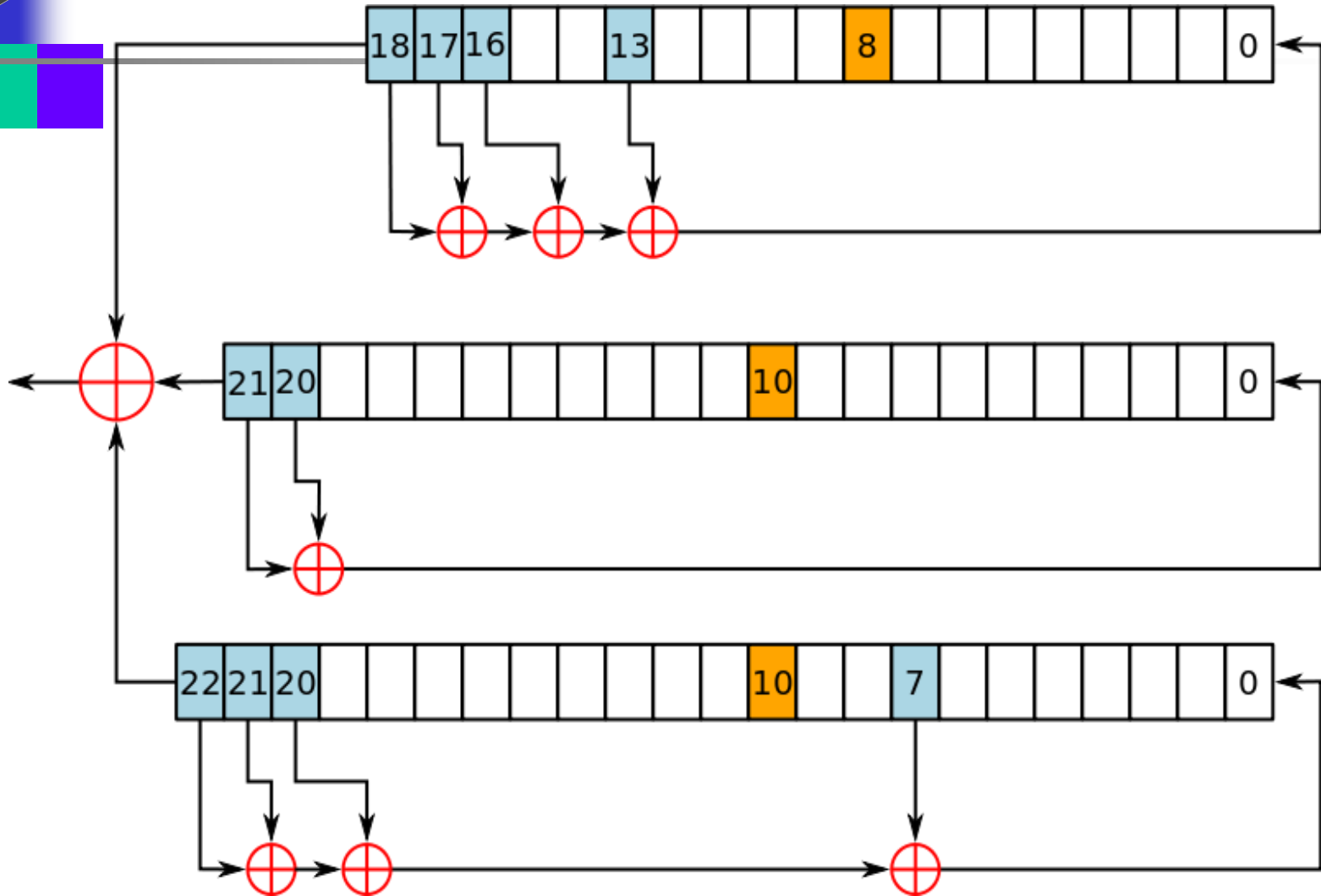
A5/1

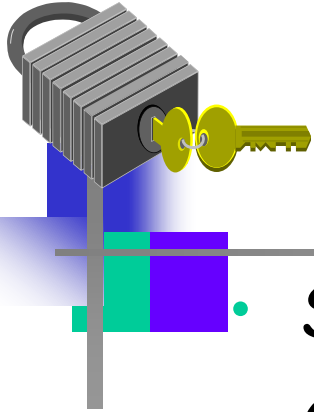


- In this example, $m = \text{maj}(x_8, y_{10}, z_{10}) = \text{maj}(\mathbf{1}, \mathbf{0}, \mathbf{1}) = \mathbf{1}$
- Register X steps, Y does not step, and Z steps
- Keystream bit is XOR of right bits of registers
- Here, keystream bit will be $0 \oplus 1 \oplus 0 = 1$



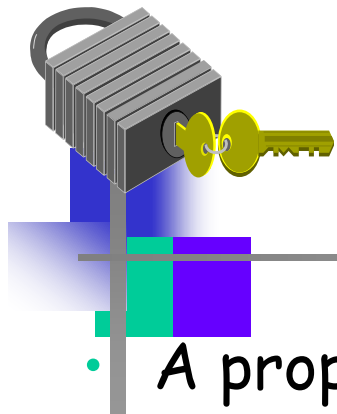
A5/1





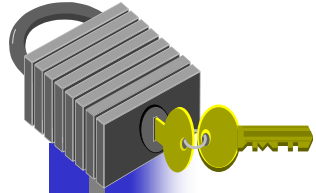
Shift Register Crypto

- Shift register crypto efficient in hardware
- Often, slow if implement in software
- In the past, very popular
- Today, more is done in software due to fast processors
- Shift register crypto still used some
 - Resource-constrained devices



RC4

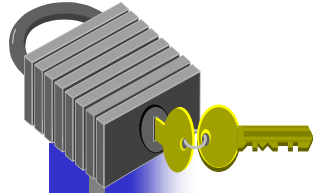
- A proprietary cipher owned by RSA Security
- A **Ron Rivest** design, simple but effective, based on random permutation
- Variable key size, byte-oriented stream cipher
- Widely used
 - SSL/TLS web security protocol
 - Wireless WEP/WPA LAN security protocols
- Key forms random permutation of all 8-bit values
- Uses that permutation to scramble input info processed a byte at a time
- Kept secret until anonymously posted on the Internet 30



RC4

A self-modifying lookup table

- Table always contains a permutation of the byte values $0, 1, \dots, 255$
- Initialize the permutation using key
- At each step, RC4 does the following
 - Swaps elements in current lookup table
 - Selects a key stream byte from table
- Each step of RC4 produces a **byte**
 - Efficient in **software**
- Each step of A5/1 produces only a bit
 - Efficient in **hardware**



RC4 Algorithm

- Starts with an array S of numbers $0..255$
- Use key to shuffle array
- S forms **internal state** of the cipher

for $i = 0$ to 255 do

// Initialization

$S[i] = i$

$T[i] = K[i \bmod \text{keylen}]$

$j = 0$

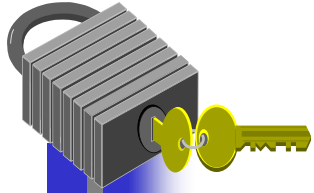
// Initial permutation of S

for $i = 0$ to 255 do

$j = (j + S[i] + T[i]) \bmod 256$

swap ($S[i], S[j]$)

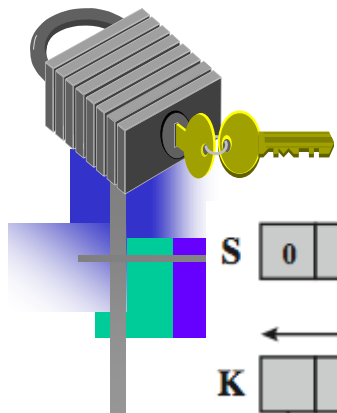
- Total number of possible states is $256!$



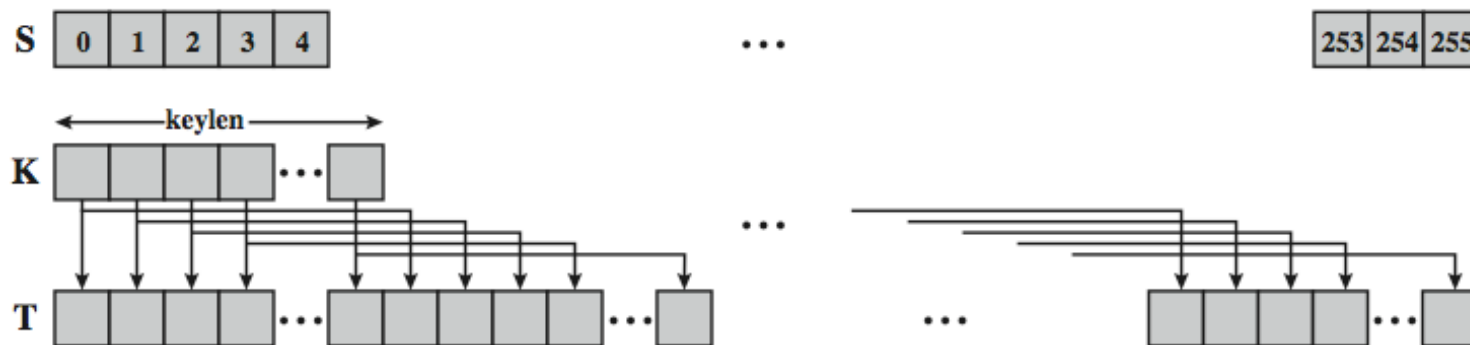
RC4 Encryption

- Encryption continues shuffling array values
- Sum of shuffled pair selects "stream key" value from permutation
- XOR $S[t]$ with next byte of message to en/decrypt

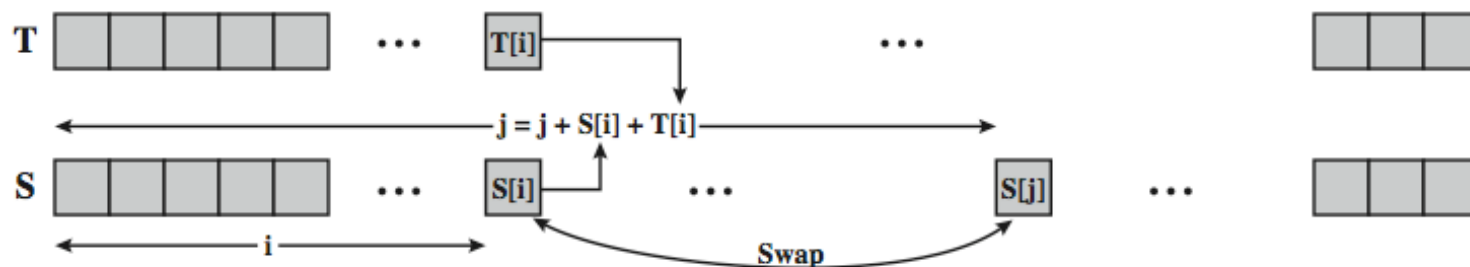
```
i = j = 0;                                //Stream Generation
while (true)                               //for each message byte  $M_i$ 
    i = (i + 1) (mod 256);
    j = (j + S[i]) (mod 256);
    swap(S[i], S[j]);
    t = (S[i] + S[j]) (mod 256);
    k = S[t];
     $C_i = M_i \text{ XOR } S[t]$    or  $M_i = C_i \text{ XOR } S[t]$ ; (to Encrypt/Decrypt)
```



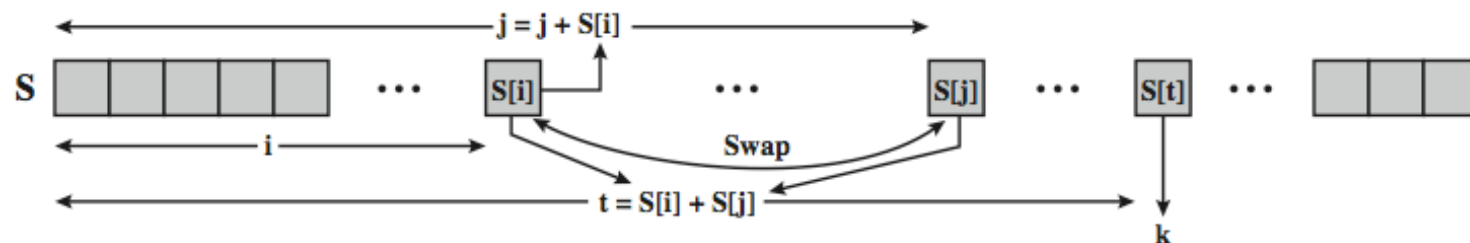
RC4 Overview



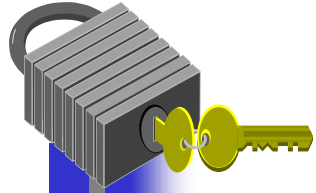
(a) Initial state of S and T



(b) Initial permutation of S

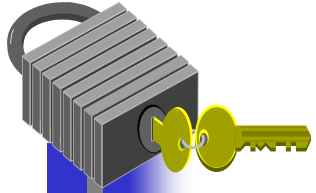


(c) Stream Generation



RC4 Security

- Claimed secure against known attacks
 - have some analyses, none practical
- Result is very non-linear
- Since RC4 is a stream cipher, must **never reuse a key**
- Concern with WEP, but due to key handling rather than RC4 itself
 - Secure with key length of at least 128 bits

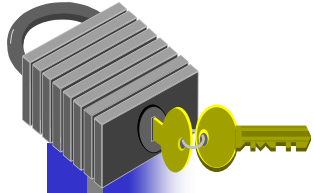


RC4 Initialization

`S[]` is permutation of $0, 1, \dots, 255$

- `key[]` contains N bytes of key

```
for i = 0 to 255
    S[i] = i
    K[i] = key[i mod N]
next i
j = 0
for i = 0 to 255
    j = (j + S[i] + K[i]) mod 256
    swap(S[i], S[j])
next i
i = j = 0
```



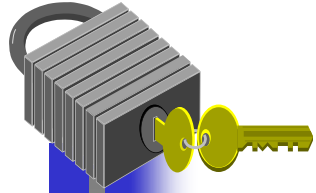
RC4 Keystream

For each keystream byte, swap elements in table and select byte

```
i = (i + 1) mod 256  
j = (j + S[i]) mod 256  
swap(S[i], S[j])  
t = (S[i] + S[j]) mod 256  
keystreamByte = S[t]
```

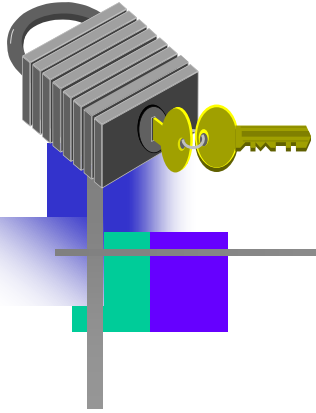
- Use keystream bytes like a one-time pad
- **Note:** first 256 bytes should be discarded
 - Otherwise, related key attack exists

<https://www.youtube.com/watch?v=riIp6EQOJOg>



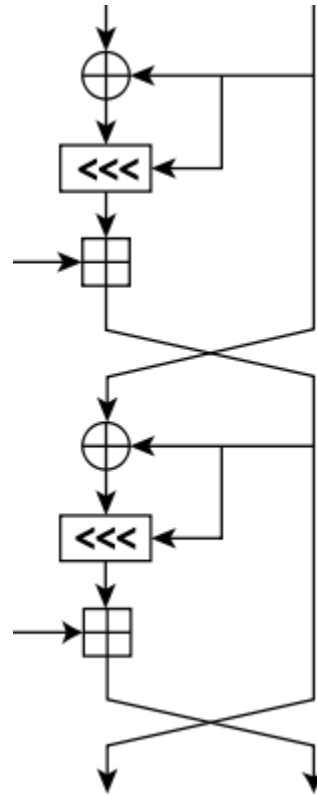
RC5

- **RC5 - designed by Ron Rivest (1994)**
 - Block cipher
 - Suitable for hardware and software
 - Fast, simple
 - Adaptable to processors of different word lengths
 - Variable block size (32, 64, 128 bits)
 - Variable number of rounds (0 to 255)
 - Variable-length key (0 to 2040 bits)
 - Low memory requirement, High security
 - Data-dependent rotations
 - Modulo additions and exclusive ORs (XOR)
 - **Feistel-like structure**

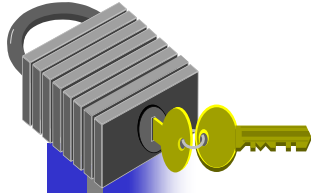


RC5

Two half- rounds of
RC5



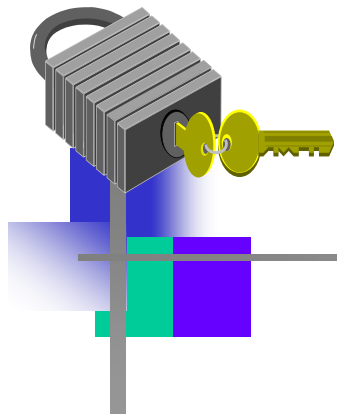
See <http://en.wikipedia.org/wiki/RC5> for details



Vigenere Cipher

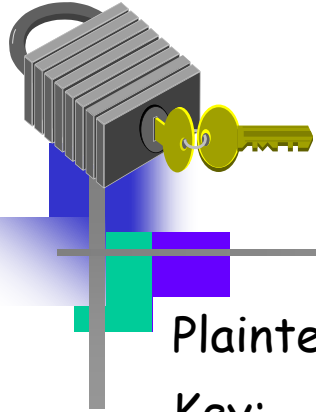
The **Vigenère cipher** is a method of encrypting alphabetic text by using a series of different Caesar ciphers based on the letters of a keyword. Its advantage is that it cannot be broken by frequency analysis.

- It is a simple form of polyalphabetic substitution.
- http://en.wikipedia.org/wiki/Vigen%C3%A8re_cipher
- Once considered unbreakable, but with modern computers it can be broken.
- See simple examples
- <http://www.youtube.com/watch?v=ijC2-JHz6Z4&NR=1&feature=endscreen> (4+ min)
- <http://www.youtube.com/watch?v=SseaQvc0aXo&feature=related>



Vigenere Table

| | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |



Vigenere Cipher

Plaintext:

ATTACKATDAWN

Key:

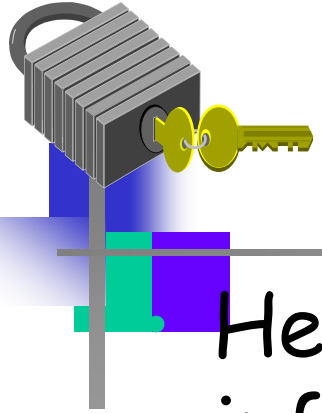
LEMONLEMONLE

Ciphertext:

LXFOPVEFRNHR

- Use key such as LEMON, repeated.
- To encrypt use the row of the key (L) and the column of the plaintext (A) to determine the cipher (L)
- To decrypt use the row of the key (L) and the column of the cipher text (L) to find the column label , which is the plaintext (A)
- Repeat for each letter in the message.

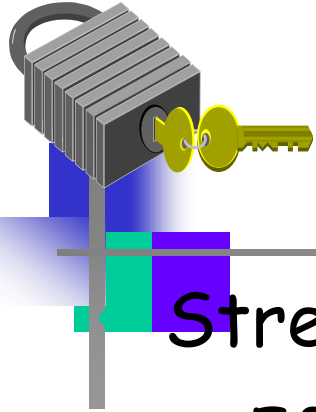
http://en.wikipedia.org/wiki/Vigen%C3%A8re_cipher



Vigenere Cipher Resources

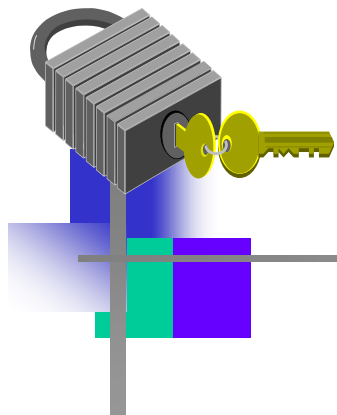
Here are some other sources for information and interaction with the Vigenere cipher:

- <http://www.cs.trincoll.edu/~crypto/historical/vigenere.html>
- <http://sharkysoft.com/misc/vigenere/>
- http://www.simonsingh.net/The_Black_Chamber/vigenere_cipher.html



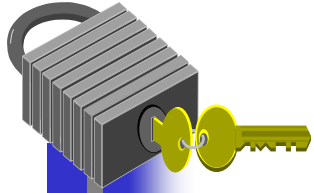
Stream Ciphers

- Stream ciphers were popular in the past
 - Efficient in hardware
 - Speed was needed to keep up with voice, etc.
 - Today, processors are fast, so software-based crypto is usually more than fast enough
- Future of stream ciphers?
 - Shamir declared "the death of stream ciphers"
 - May be greatly exaggerated...
 - http://en.wikipedia.org/wiki/Stream_cipher



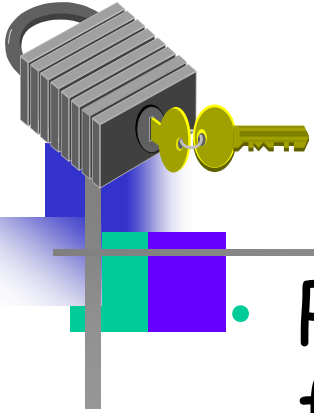
Block Ciphers





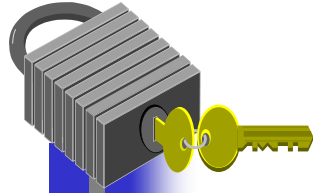
Block Ciphers

- Block Cipher is a symmetric key cipher operating on fixed-length groups of bits, called *blocks*, with an unvarying transformation. A block cipher encryption algorithm might take (for example) a 128-bit block of plaintext as input, and output a corresponding 128-bit block of cipher text. The exact transformation is controlled using a second input — the secret key.
- Short explanation
 - DES, 3DES, AES, IDEA



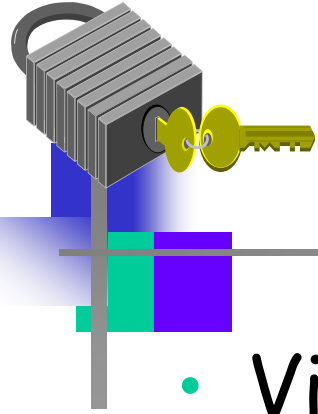
(Iterated) Block Cipher

- Plaintext and ciphertext consist of fixed-sized blocks
- Ciphertext obtained from plaintext by iterating a **round function**
- Input to round function consists of **key** and **output** of previous round
- Usually implemented in software



Feistel Cipher

- Horst Feistel devised the Feistel Cipher
 - based on concept of invertible product cipher
- Partitions input block into two halves
 - process through multiple rounds which
 - perform a substitution on left data half
 - based on round function of right half & subkey
 - then have permutation swapping halves
- Implements Shannon's S-P net concept
- <https://www.youtube.com/watch?v=ySZvE9vOfEQ>



Feistel Cipher Structure

- Virtually all conventional block encryption algorithms, including DES have a structure first described by Horst Feistel of IBM in 1973
- The realization of a Feistel Network depends on the choice of the following parameters and design features:
(see next slide)
- <http://www.youtube.com/watch?v=ySZvE9vOfEQ>



Feistel Cipher: Encryption

Feistel cipher is a type of block cipher, not a specific block cipher

- Split plaintext block into left and right halves: $P = (L_0, R_0)$

- For each round $i = 1, 2, \dots, n$, compute

$$L_i = R_{i-1}$$

$$R_i = L_{i-1} \oplus F(R_{i-1}, K_i)$$

where F is **round function** and K_i is **subkey**

- Ciphertext: $C = (L_n, R_n)$



Feistel Cipher: Decryption

Start with ciphertext $C = (L_n, R_n)$

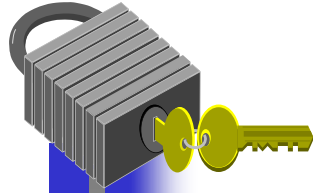
- For each round $i = n, n-1, \dots, 1$, compute

$$R_{i-1} = L_i$$

$$L_{i-1} = R_i \oplus F(R_{i-1}, K_i)$$

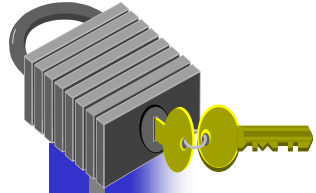
where F is round function and K_i is subkey

- Plaintext: $P = (L_0, R_0)$
- Formula “works” for any function F
 - But only secure for certain functions F



Feistel Cipher Structure

- **Block size:** larger block sizes mean greater security
- **Key Size:** larger key size means greater security
- **Number of rounds:** multiple rounds offer increasing security
- **Subkey generation algorithm:** greater complexity will lead to greater difficulty of cryptanalysis.
- **Fast software encryption/decryption:** the speed of execution of the algorithm becomes a concern



Feistel Cipher

- The plain text block is divided into two halves L_0 and R_0
- The two halves pass through n rounds of processing and then combine to produce the cipher text block.
- At each round a substitution is performed on the left half of the data by applying a round function F to the right half of the data and then XORing it with the left half

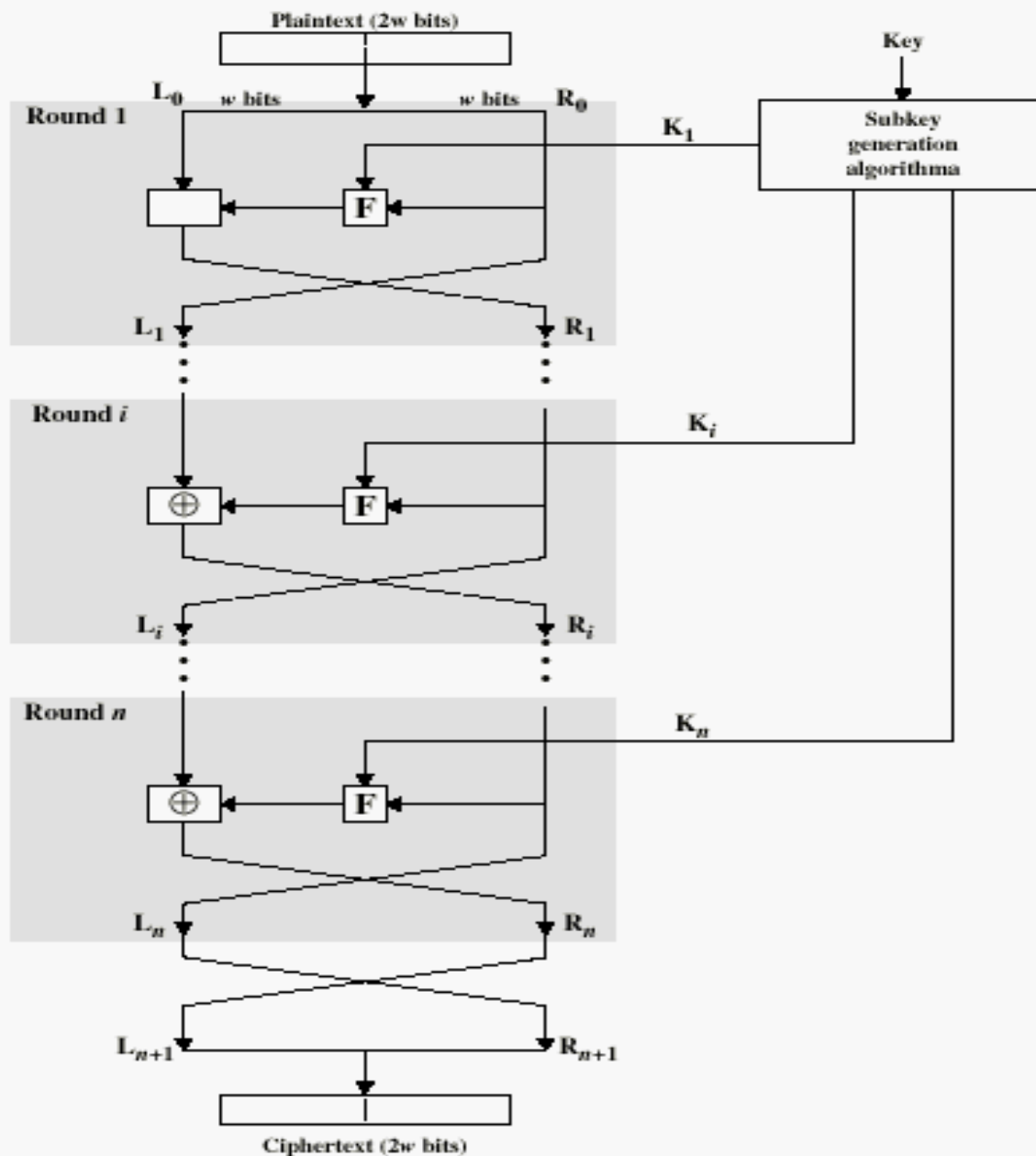
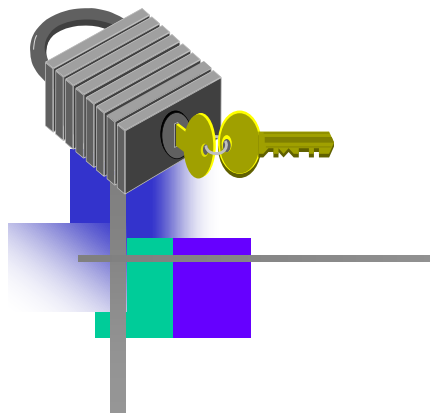
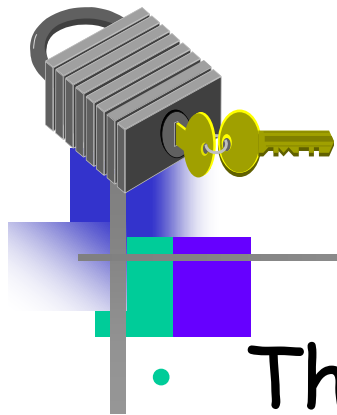


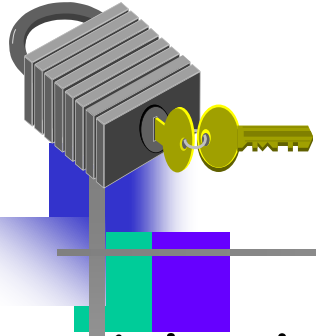
Figure 2.2 Classical Feistel Network



Feistel Structure

- The Feistel Structure is a general example used by all symmetric block ciphers:
- It is a series of rounds, each performing substitutions and permutations using a secret key value

Feistel Cipher Design Elements



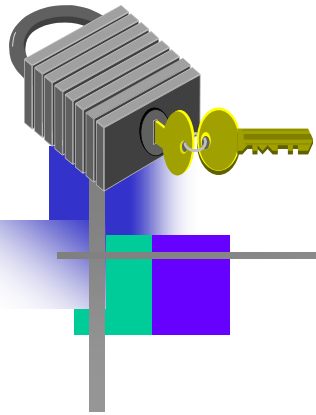
- block size
- key size
- number of rounds
- subkey generation algorithm
- round function

Increasing size means greater security, but slows cipher

Greater complexity, harder to decrypt

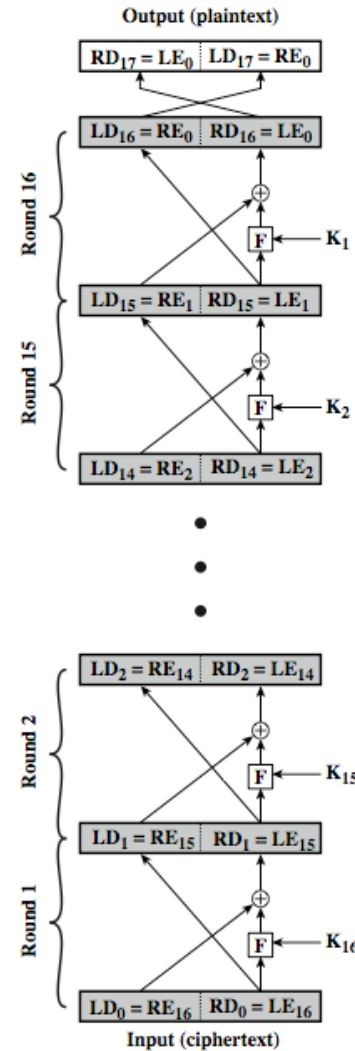
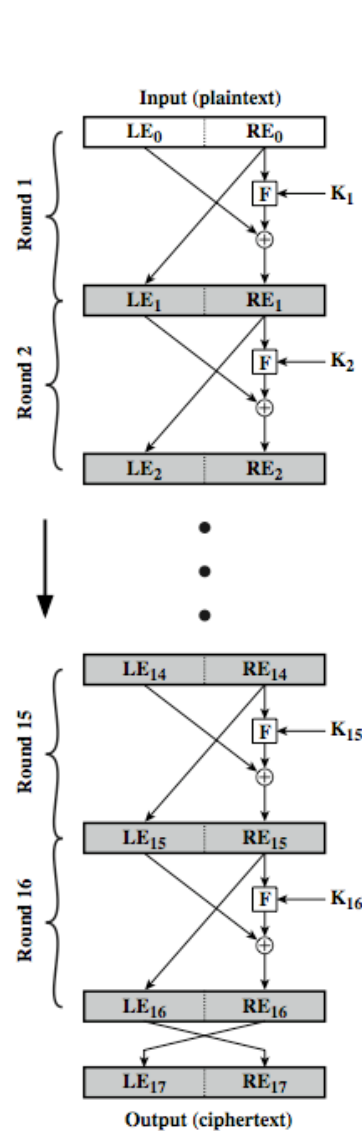
Other Considerations

- fast software en/decryption
- ease of analysis

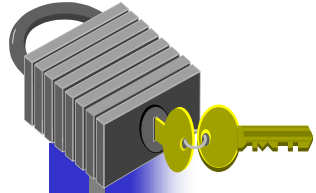


Feistel Cipher Structure

Encryption



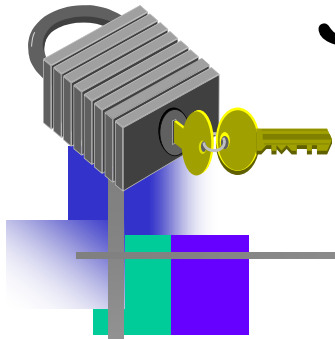
Decryption



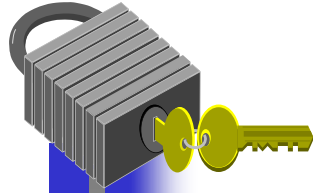
Feistel Algorithms

- Encryption and decryption algorithms are essentially the same
- To decrypt:
 - Use the ciphertext as input
 - Use the sub-keys in reverse order ($K_n, K_{n-1} \dots$)
- Advantage:
 - Only one algorithm is needed for encryption and decryption

Symmetric Block Encryption Algorithms



- Most common symmetric encryption algorithms are block ciphers.
- Block Ciphers process plaintext input in fixed size blocks and produce a block of equal size cipher text.
 - DES - Data Encryption Standard
 - 3DES - Triple DES
 - AES - Advanced Encryption Standard



Data Encryption Standard

- **DES** developed in 1970's
 - Based on IBM's Lucifer cipher
 - DES was U.S. government standard
 - DES development was controversial
 - NSA secretly involved
 - Design process was secret
 - Key length reduced from 128 to 56 bits
 - Subtle changes to Lucifer algorithm

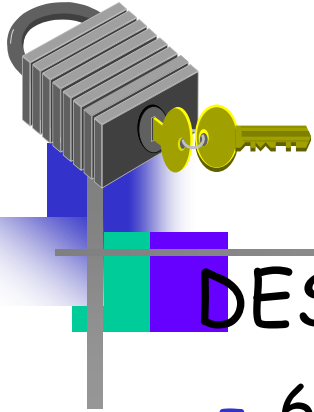
https://www.youtube.com/watch?v=G_guTnTcoqg



Conventional Symmetric Encryption Algorithms

Data Encryption Standard (DES)- 1977

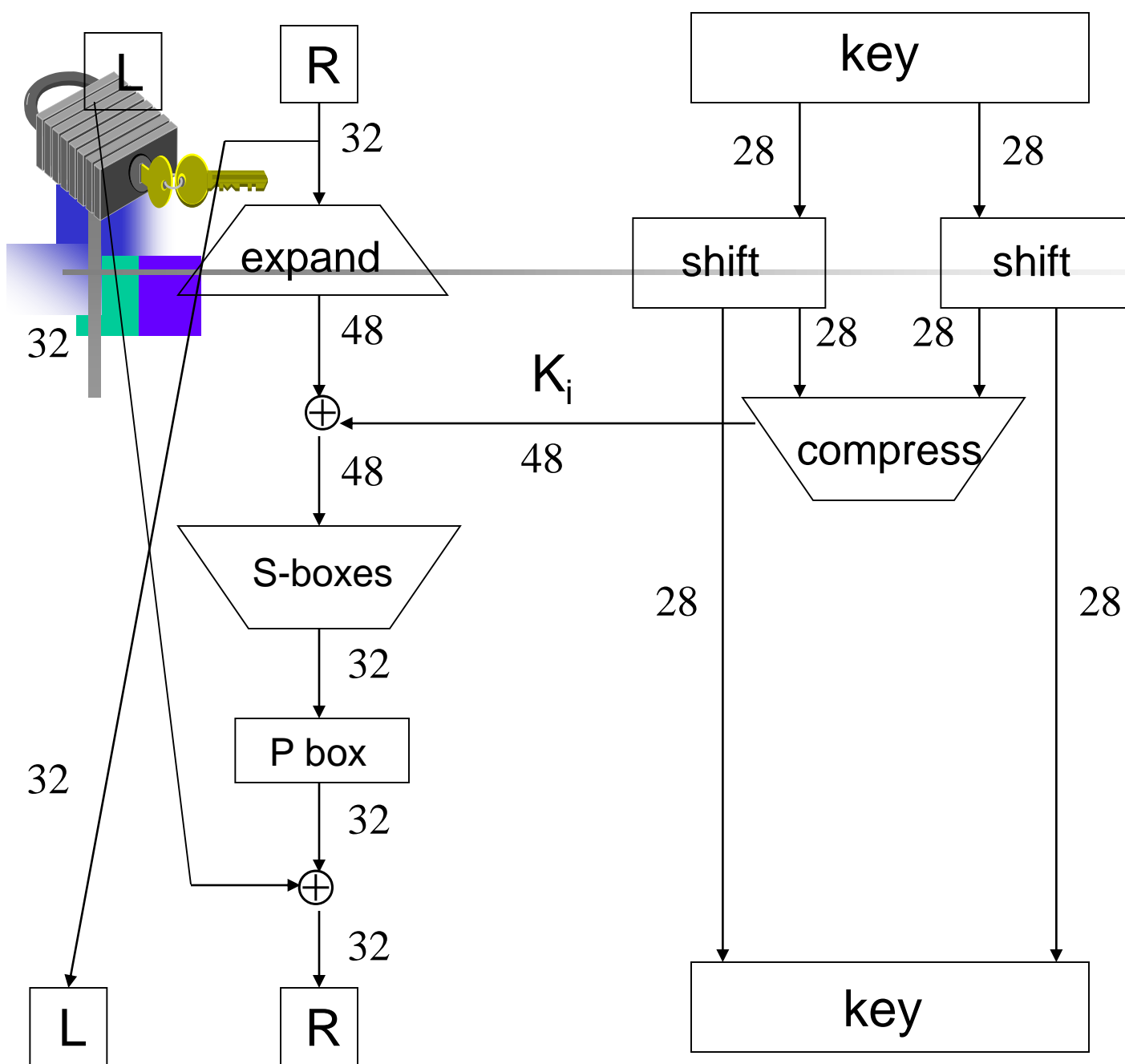
- The most widely used encryption scheme
- The algorithm is referred to the Data Encryption Algorithm (DEA)
- DES is a block cipher
- Variation of Feistel Cipher
- The plaintext is processed in 64-bit blocks
- The key is 56-bits in length
- 16 subkeys used in 16 rounds
- No longer used for government transmissions
- Controversy over security



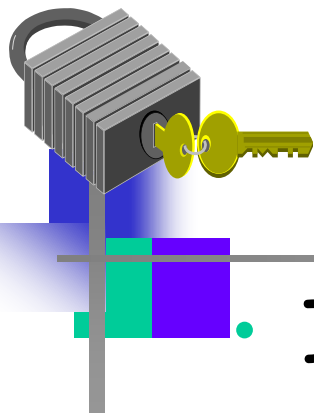
DES Numerology

DES is a Feistel cipher with...

- 64 bit block length
- 56 bit key length
- 16 rounds
- 48 bits of key used each round (subkey)
- Each round is simple (for a block cipher)
- Security depends heavily on "S-boxes"
 - Each S-boxes maps 6 bits to 4 bits



One Round of DES



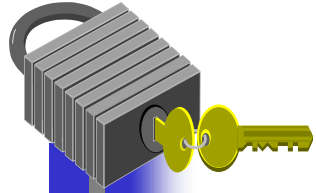
DES Expansion Permutation

- Input 32 bits

| | | | | | | | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 |

- Output 48 bits

| | | | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|----|----|
| 31 | 0 | 1 | 2 | 3 | 4 | 3 | 4 | 5 | 6 | 7 | 8 |
| 7 | 8 | 9 | 10 | 11 | 12 | 11 | 12 | 13 | 14 | 15 | 16 |
| 15 | 16 | 17 | 18 | 19 | 20 | 19 | 20 | 21 | 22 | 23 | 24 |
| 23 | 24 | 25 | 26 | 27 | 28 | 27 | 28 | 29 | 30 | 31 | 0 |



DES S-box

- 8 "substitution boxes" or *S-boxes*
- Each S-box maps 6 bits to 4 bits
- S-box number 1

input bits (0,5)



input bits (1,2,3,4)

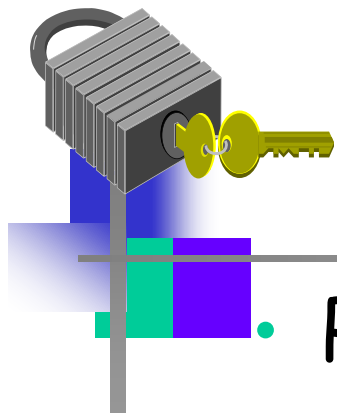
| 0000 0001 0010 0011 0100 0101 0110 0111 1000 1001 1010 1011 1100 1101
1110 1111

00 | 1110 0100 1101 0001 0010 1111 1011 1000 0011 1010 0110 1100 0101 1001
0000 0111

01 | 0000 1111 0111 0100 1110 0010 1101 0001 1010 0110 1100 1011 1001 0101
0011 1000

10 | 0100 0001 1110 1000 1101 0110 0010 1011 1111 1100 1001 0111 0011 1010
0101 0000

11 | 1111 1100 1000 0010 0100 1001 0001 0111 0101 1011 0011 1110 1010 0000
0110 1101



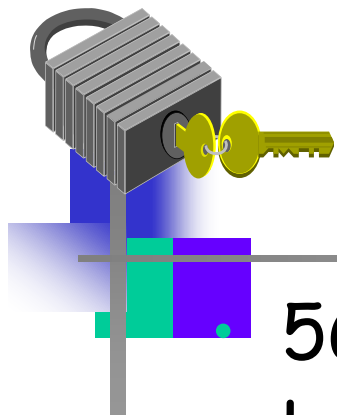
DES P-box

- P - **permutes** or rearranges the bits
- Input 32 bits

| | | | | | | | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 |

- Output 32 bits

| | | | | | | | | | | | | | | | |
|----|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 15 | 6 | 19 | 20 | 28 | 11 | 27 | 16 | 0 | 14 | 22 | 25 | 4 | 17 | 30 | 9 |
| 1 | 7 | 23 | 13 | 31 | 26 | 2 | 8 | 18 | 12 | 29 | 5 | 21 | 10 | 3 | 24 |



DES Subkey

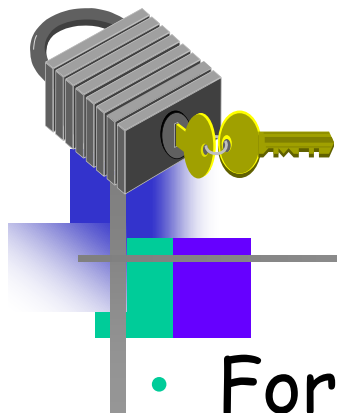
56 bit DES key, numbered 0,1,2,...,55

- Left half key bits, LK

| | | | | | | |
|----|----|----|----|----|----|----|
| 49 | 42 | 35 | 28 | 21 | 14 | 7 |
| 0 | 50 | 43 | 36 | 29 | 22 | 15 |
| 8 | 1 | 51 | 44 | 37 | 30 | 23 |
| 16 | 9 | 2 | 52 | 45 | 38 | 31 |

- Right half key bits, RK

| | | | | | | |
|----|----|----|----|----|----|----|
| 55 | 48 | 41 | 34 | 27 | 20 | 13 |
| 6 | 54 | 47 | 40 | 33 | 26 | 19 |
| 12 | 5 | 53 | 46 | 39 | 32 | 25 |
| 18 | 11 | 4 | 24 | 17 | 10 | 3 |



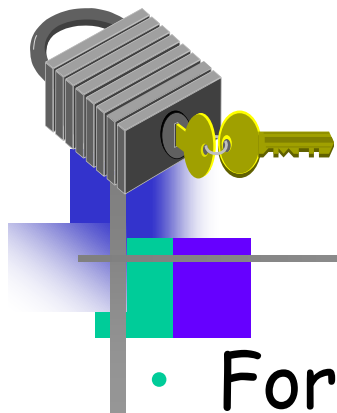
DES Subkey

- For rounds $i=1, 2, \dots, 16$
 - Let $LK = (LK \text{ circular shift left by } r_i)$
 - Let $RK = (RK \text{ circular shift left by } r_i)$
 - Left half of subkey K_i is of LK bits

13 16 10 23 0 4 2 27 14 5 20 9
22 18 11 3 25 7 15 6 26 19 12 1

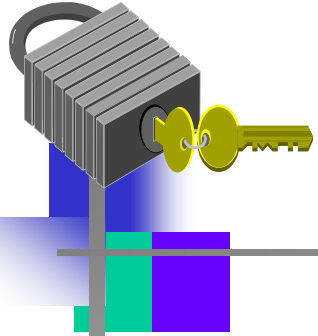
- Right half of subkey K_i is RK bits

12 23 2 8 18 26 1 11 22 16 4 19
15 20 10 27 5 24 17 13 21 7 0 3



DES Subkey

- For rounds 1, 2, 9 and 16 the shift r_i is 1, and in all other rounds r_i is 2
- Bits 8,17,21,24 of LK omitted each round
- Bits 6,9,14,25 of RK omitted each round
- **Compression permutation** yields 48 bit subkey K_i from 56 bits of LK and RK
- **Key schedule** generates subkey



DES Last Word (Almost)

- An initial permutation before round 1
- Halves are swapped after last round
- A final permutation (inverse of initial perm) applied to (R_{16}, L_{16})
- None of this serves security purpose

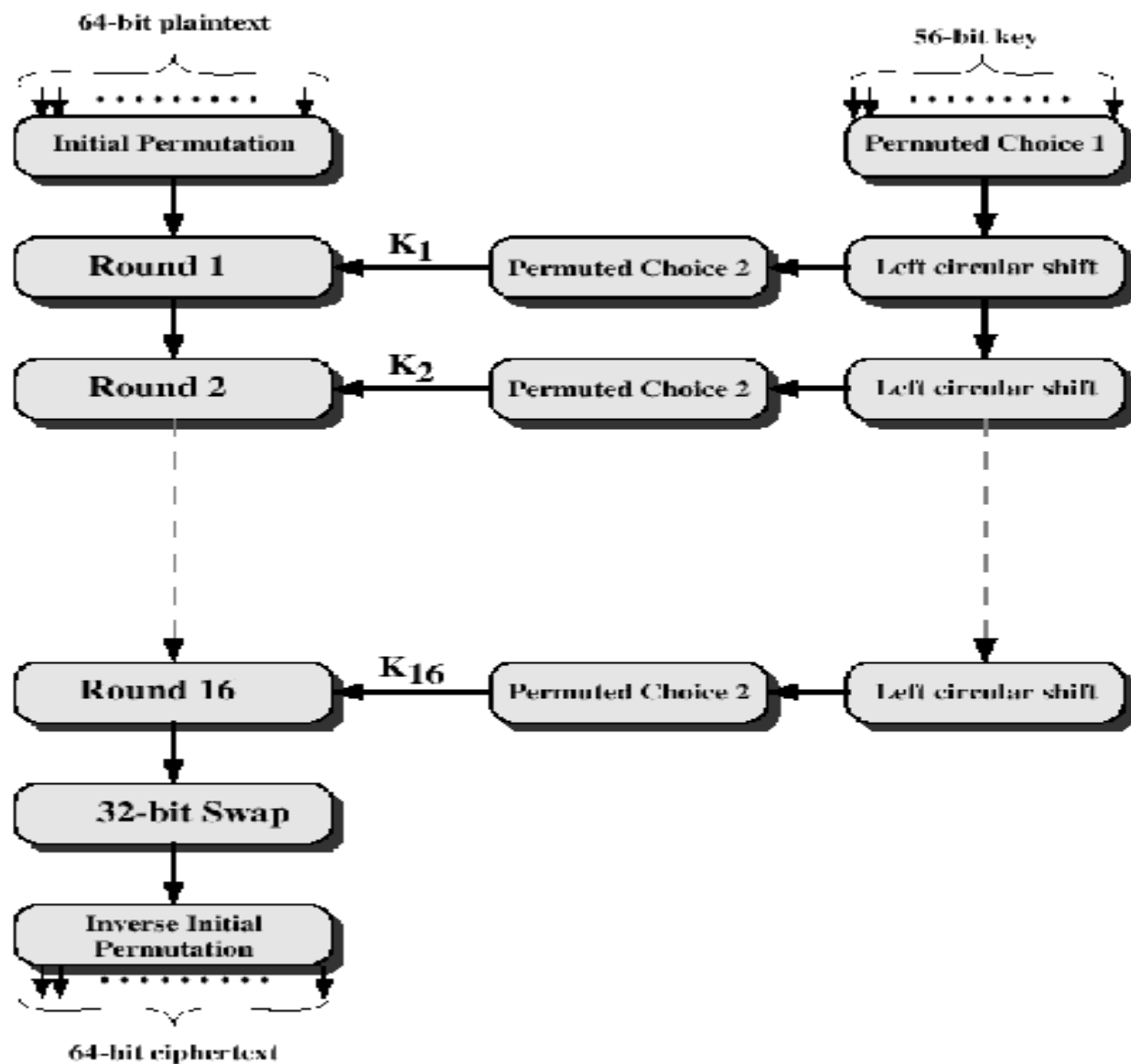
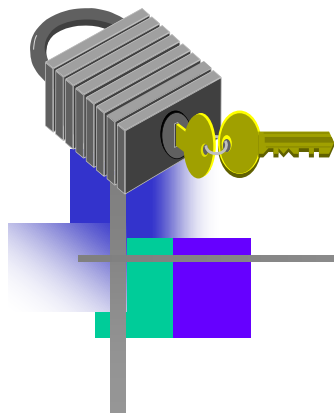


Figure 2.3 General Depiction of DES Encryption Algorithm

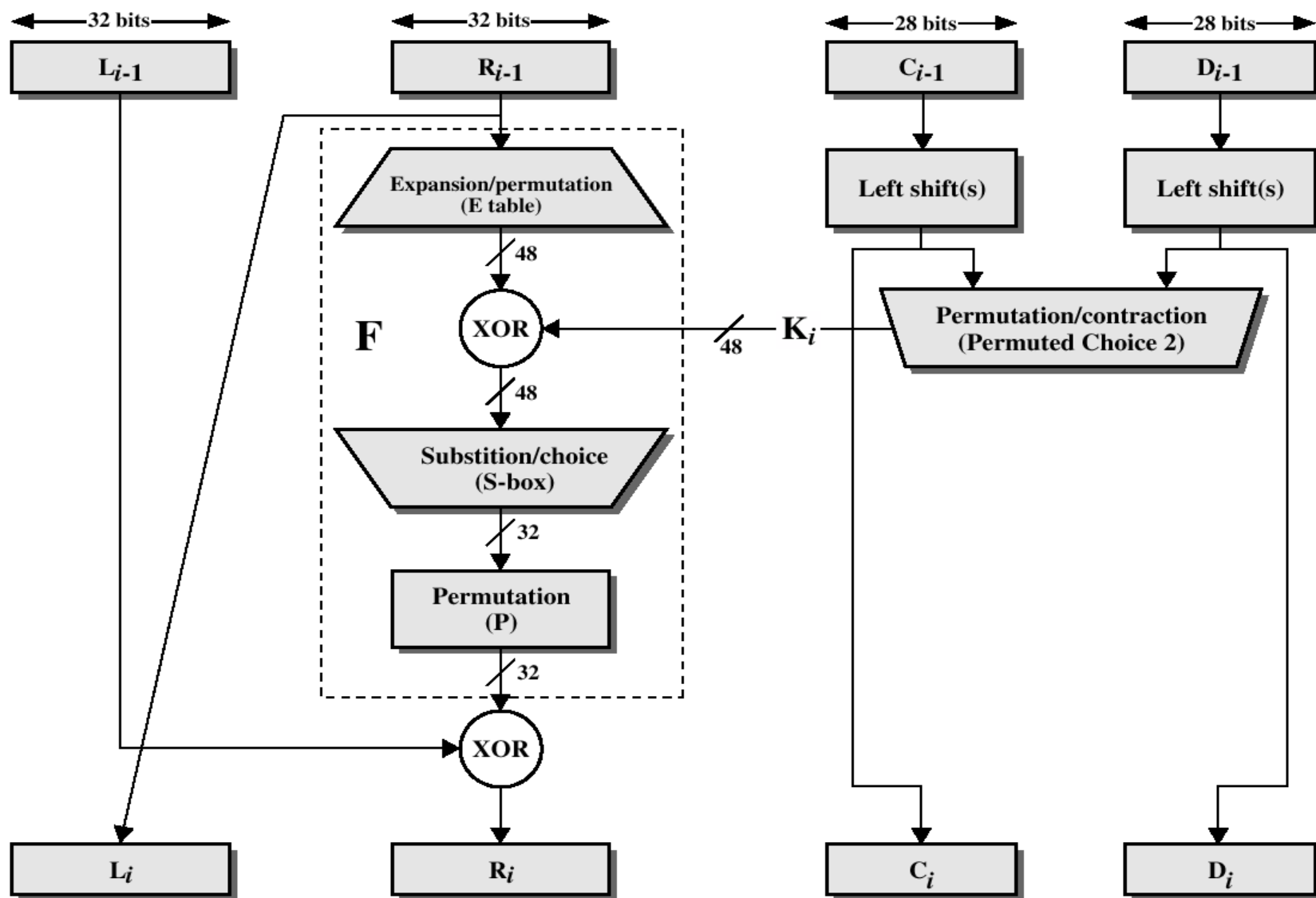
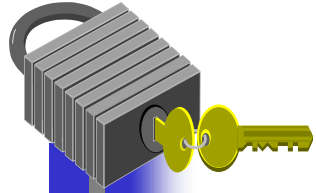


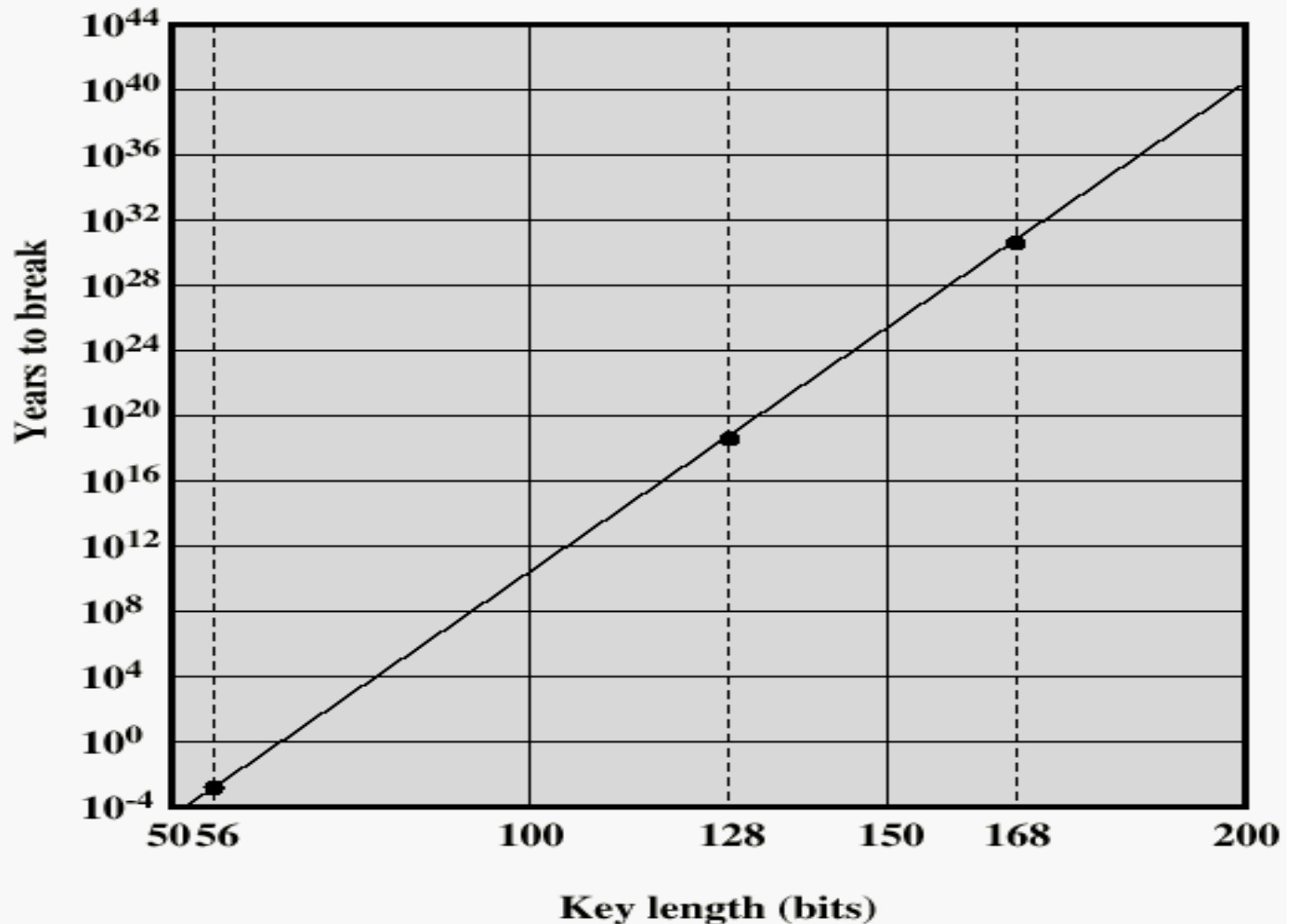
Figure 2.4 Single Round of DES Algorithm

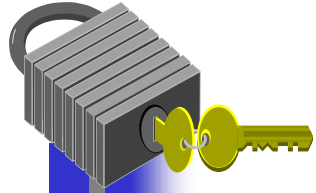


DES

- The overall processing at each iteration:
 - $L_i = R_{i-1}$
 - $R_i = L_{i-1} \quad F(R_{i-1}, K_i)$
- Concerns about:
 - The algorithm (since the design criteria were classified)
 - and the key length (56-bits) vs 128 bits

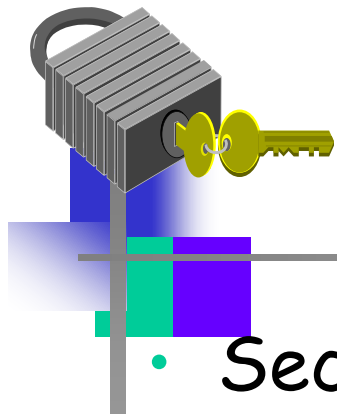
Time to break a code (10^6 decryptions/ μs)





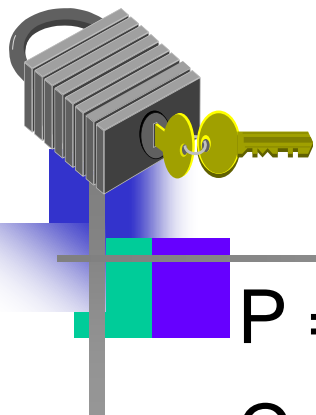
DES Concerns

- Although there are concerns about the DES design- no weakness has yet been discovered.
- With 56 bit keys- brute force is possible as demonstrated by "DES Cracker" in 1998 and machine speeds and costs will continue to improve.
- A 128 bit key is guaranteed to be unbreakable by brute force.



Security of DES

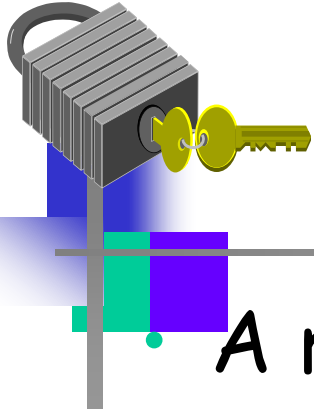
- Security depends heavily on S-boxes
 - Everything else in DES is linear
- Thirty+ years of intense analysis has revealed no “back door”
- Attacks, essentially exhaustive key search
- **Inescapable conclusions**
 - Designers of DES knew what they were doing
 - Designers of DES were way ahead of their time



Block Cipher Notation

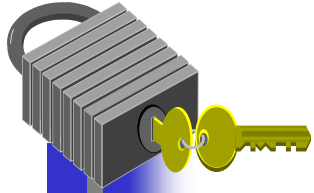
P = plaintext block

- C = ciphertext block
- Encrypt P with key K to get ciphertext C
 - $C = E(P, K)$
- Decrypt C with key K to get plaintext P
 - $P = D(C, K)$
- Note: $P = D(E(P, K), K)$ and $C = E(D(C, K), K)$
 - But $P \neq D(E(P, K_1), K_2)$ and $C \neq E(D(C, K_1), K_2)$ when $K_1 \neq K_2$



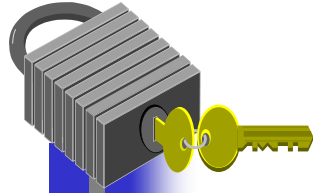
DES Alternatives

- A replacement for DES was needed
- Use multiple encryption with DES implementations - 3DES
- Design a new alternative- AES is a new cipher alternative
- 3DES
- https://www.youtube.com/watch?v=jQEx_vxLnrE



3DES with 2 Keys

- Use 3 encryptions
- Can use 2 keys with E-D-E sequence
 - $C = E_{K1}(D_{K2}(E_{K1}(P)))$
 - if $K1=K2$ then can work with single DES
- Standardized in ANSI X9.17 & ISO8732
- No current known practical attacks
 - several proposed impractical attacks might become basis of future attacks
 - Brute force search about 2^{112}



Triple DES

Use 3 keys and 3 executions of the DES algorithm (encrypt-decrypt-encrypt)

$$C = E_{K3}[D_{K2}[E_{K1}[P]]]$$

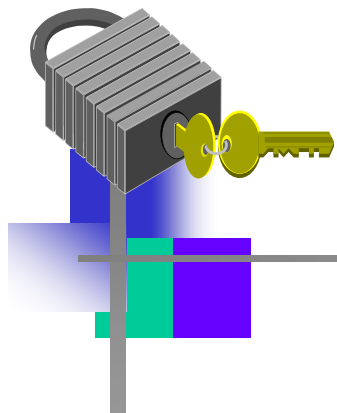
encrypt

- C = ciphertext
- P = Plaintext
- $EK[X]$ = encryption of X using key K
- $DK[Y]$ = decryption of Y using key K

$$P = D_{K1}[E_{K2}[D_{K3}[C]]]$$

decrypt

- Effective key length of 168 bits



Triple DES/DEA

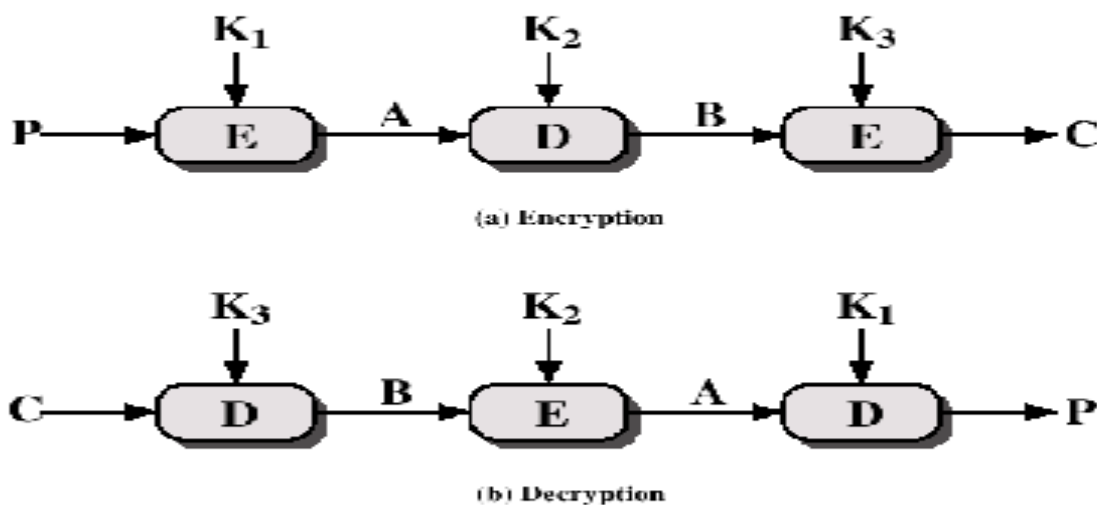
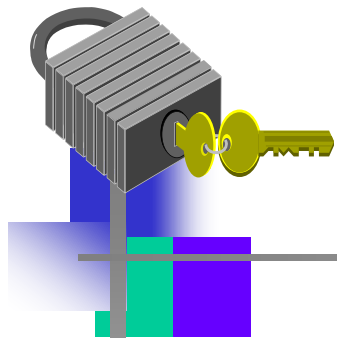
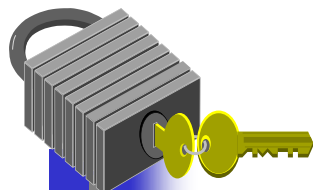


Figure 2.6 Triple DEA



Triple DES

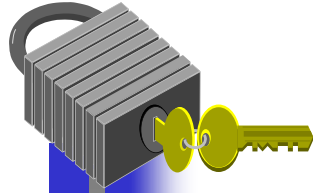
- 3 Key 3DES is the preferred alternative
- Approved for use in financial applications
- Adopted by some Internet applications, (eg. PGP, S/MIME)
- High level of confidence that 3DES is secure and resistant to cryptanalysis.
- Disadvantage - **slow**, small block size



Triple DES

Today, 56 bit DES key is too small

- Exhaustive key search is feasible
- But DES is everywhere, so what to do?
- **Triple DES** or **3DES** (112 bit key)
 - $C = E(D(E(P, K_1), K_2), K_1)$
 - $P = D(E(D(C, K_1), K_2), K_1)$
- Why Encrypt-Decrypt-Encrypt with 2 keys?
 - Backward compatible: $E(D(E(P, K), K), K) = E(P, K)$
 - And 112 bits is enough



3DES

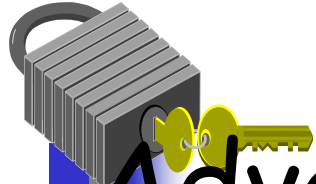
Why not $C = E(E(P, K), K)$?

- Trick question --- it's still just 56 bit key

- Why not $C = E(E(P, K_1), K_2)$?

- A (semi-practical) **known plaintext** attack

- Pre-compute table of $E(P, K_1)$ for every possible key K_1 (resulting table has 2^{56} entries)
- Then for each possible K_2 compute $D(C, K_2)$ until a match in table is found
- When match is found, have $E(P, K_1) = D(C, K_2)$
- Result gives us keys: $C = E(E(P, K_1), K_2)$



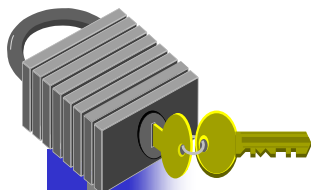
Advanced Encryption Standard

- Replacement for DES
 - AES competition (late 90's)
 - NSA openly involved
 - Transparent process
 - Many strong algorithms proposed
 - Rijndael Algorithm ultimately selected (pronounced like "Rain Doll" or "Rhine Doll")
 - Iterated block cipher (like DES)
 - Not a Feistel cipher (unlike DES)
 - <https://www.youtube.com/watch?v=ZhILF5Dhx74>



AES Overview

- **Block size:** 128 bits (others in Rijndael)
- **Key length:** 128, 192 or 256 bits (independent of block size)
- 10 to 14 rounds (depends on key length)
- Each round uses 4 functions (3 "layers")
 - ByteSub (nonlinear layer)
 - ShiftRow (linear mixing layer)
 - MixColumn (nonlinear layer)
 - AddRoundKey (key addition layer)

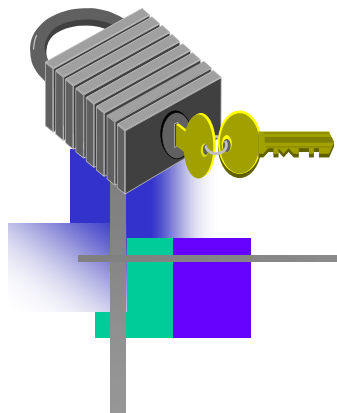


AES ByteSub

- Treat 128 bit block as 4x6 byte array

$$\begin{bmatrix} a_{00} & a_{01} & a_{02} & a_{03} \\ a_{10} & a_{11} & a_{12} & a_{13} \\ a_{20} & a_{21} & a_{22} & a_{23} \\ a_{30} & a_{31} & a_{32} & a_{33} \end{bmatrix} \longrightarrow \text{ByteSub} \longrightarrow \begin{bmatrix} b_{00} & b_{01} & b_{02} & b_{03} \\ b_{10} & b_{11} & b_{12} & b_{13} \\ b_{20} & b_{21} & b_{22} & b_{23} \\ b_{30} & b_{31} & b_{32} & b_{33} \end{bmatrix}$$

- ByteSub is AES's "S-box"
- Can be viewed as nonlinear (but invertible) composition of two math operations

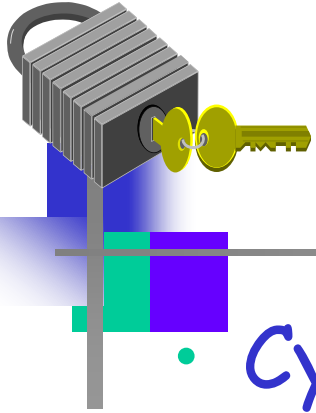


AES "S-box"

Last 4 bits of input

First 4
bits of
input

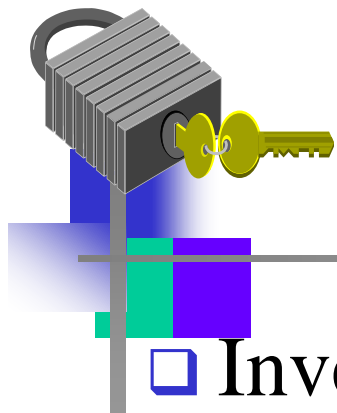
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | a | b | c | d | e | f |
|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 0 | 63 | 7c | 77 | 7b | f2 | 6b | 6f | c5 | 30 | 01 | 67 | 2b | fe | d7 | ab | 76 |
| 1 | ca | 82 | c9 | 7d | fa | 59 | 47 | f0 | ad | d4 | a2 | af | 9c | a4 | 72 | c0 |
| 2 | b7 | fd | 93 | 26 | 36 | 3f | f7 | cc | 34 | a5 | e5 | f1 | 71 | d8 | 31 | 15 |
| 3 | 04 | c7 | 23 | c3 | 18 | 96 | 05 | 9a | 07 | 12 | 80 | e2 | eb | 27 | b2 | 75 |
| 4 | 09 | 83 | 2c | 1a | 1b | 6e | 5a | a0 | 52 | 3b | d6 | b3 | 29 | e3 | 2f | 84 |
| 5 | 53 | d1 | 00 | ed | 20 | fc | b1 | 5b | 6a | cb | be | 39 | 4a | 4c | 58 | cf |
| 6 | d0 | ef | aa | fb | 43 | 4d | 33 | 85 | 45 | f9 | 02 | 7f | 50 | 3c | 9f | a8 |
| 7 | 51 | a3 | 40 | 8f | 92 | 9d | 38 | f5 | bc | b6 | da | 21 | 10 | ff | f3 | d2 |
| 8 | cd | 0c | 13 | ec | 5f | 97 | 44 | 17 | c4 | a7 | 7e | 3d | 64 | 5d | 19 | 73 |
| 9 | 60 | 81 | 4f | dc | 22 | 2a | 90 | 88 | 46 | ee | b8 | 14 | de | 5e | 0b | db |
| a | e0 | 32 | 3a | 0a | 49 | 06 | 24 | 5c | c2 | d3 | ac | 62 | 91 | 95 | e4 | 79 |
| b | e7 | c8 | 37 | 6d | 8d | d5 | 4e | a9 | 6c | 56 | f4 | ea | 65 | 7a | ae | 08 |
| c | ba | 78 | 25 | 2e | 1c | a6 | b4 | c6 | e8 | dd | 74 | 1f | 4b | bd | 8b | 8a |
| d | 70 | 3e | b5 | 66 | 48 | 03 | f6 | 0e | 61 | 35 | 57 | b9 | 86 | c1 | 1d | 9e |
| e | e1 | f8 | 98 | 11 | 69 | d9 | 8e | 94 | 9b | 1e | 87 | e9 | ce | 55 | 28 | df |
| f | 8c | a1 | 89 | 0d | bf | e6 | 42 | 68 | 41 | 99 | 2d | 0f | b0 | 54 | bb | 16 |



AES ShiftRow

- Cyclic shift rows

$$\begin{bmatrix} a_{00} & a_{01} & a_{02} & a_{03} \\ a_{10} & a_{11} & a_{12} & a_{13} \\ a_{20} & a_{21} & a_{22} & a_{23} \\ a_{30} & a_{31} & a_{32} & a_{33} \end{bmatrix} \xrightarrow{\text{ShiftRow}} \begin{bmatrix} a_{00} & a_{01} & a_{02} & a_{03} \\ a_{11} & a_{12} & a_{13} & a_{10} \\ a_{22} & a_{23} & a_{20} & a_{21} \\ a_{33} & a_{30} & a_{31} & a_{32} \end{bmatrix} \leftarrow$$

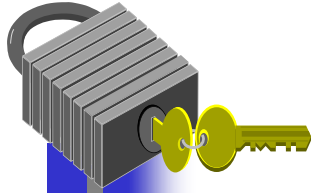


AES MixColumn

- Invertible, linear operation applied to each column

$$\begin{bmatrix} a_{0i} \\ a_{1i} \\ a_{2i} \\ a_{3i} \end{bmatrix} \rightarrow \text{MixColumn} \rightarrow \begin{bmatrix} b_{0i} \\ b_{1i} \\ b_{2i} \\ b_{3i} \end{bmatrix} \quad \text{for } i = 0, 1, 2, 3$$

- Implemented as a (big) lookup table



AES AddRoundKey

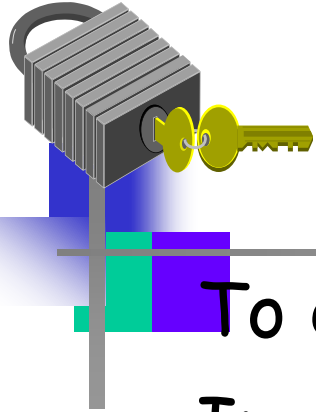
- XOR subkey with block

$$\begin{bmatrix} a_{00} & a_{01} & a_{02} & a_{03} \\ a_{10} & a_{11} & a_{12} & a_{13} \\ a_{20} & a_{21} & a_{22} & a_{23} \\ a_{30} & a_{31} & a_{32} & a_{33} \end{bmatrix} \oplus \begin{bmatrix} k_{00} & k_{01} & k_{02} & k_{03} \\ k_{10} & k_{11} & k_{12} & k_{13} \\ k_{20} & k_{21} & k_{22} & k_{23} \\ k_{30} & k_{31} & k_{32} & k_{33} \end{bmatrix} = \begin{bmatrix} b_{00} & b_{01} & b_{02} & b_{03} \\ b_{10} & b_{11} & b_{12} & b_{13} \\ b_{20} & b_{21} & b_{22} & b_{23} \\ b_{30} & b_{31} & b_{32} & b_{33} \end{bmatrix}$$

Block

Subkey

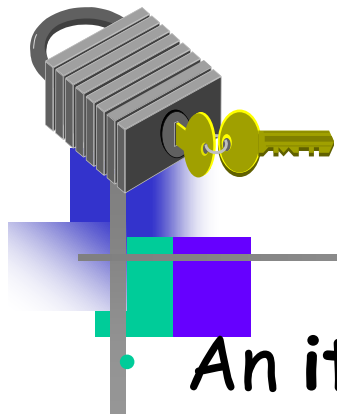
- RoundKey (subkey) determined by **key schedule** algorithm



AES Decryption

To decrypt, process must be invertible

- Inverse of MixAddRoundKey is easy, since " \oplus " is its own inverse
- MixColumn is invertible (inverse is also implemented as a lookup table)
- Inverse of ShiftRow is easy (cyclic shift the other direction)
- ByteSub is invertible (inverse is also implemented as a lookup table)



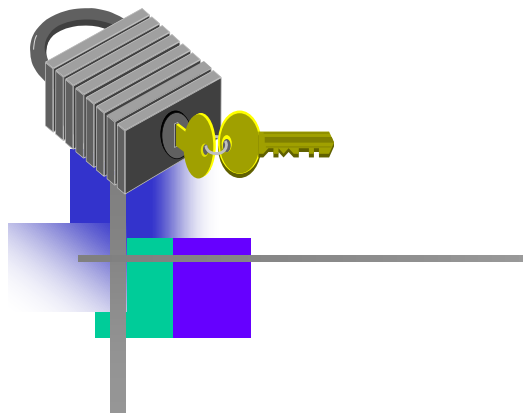
AES Cipher

- An **iterative** rather than **feistel** cipher
 - Operates on entire block in every round rather than halves
 - Processes data as block of 4 columns of 4 bytes
- Designed Criteria:
 - Resistant against known attacks
 - Speed and code compactness on many CPUs
 - Design simplicity

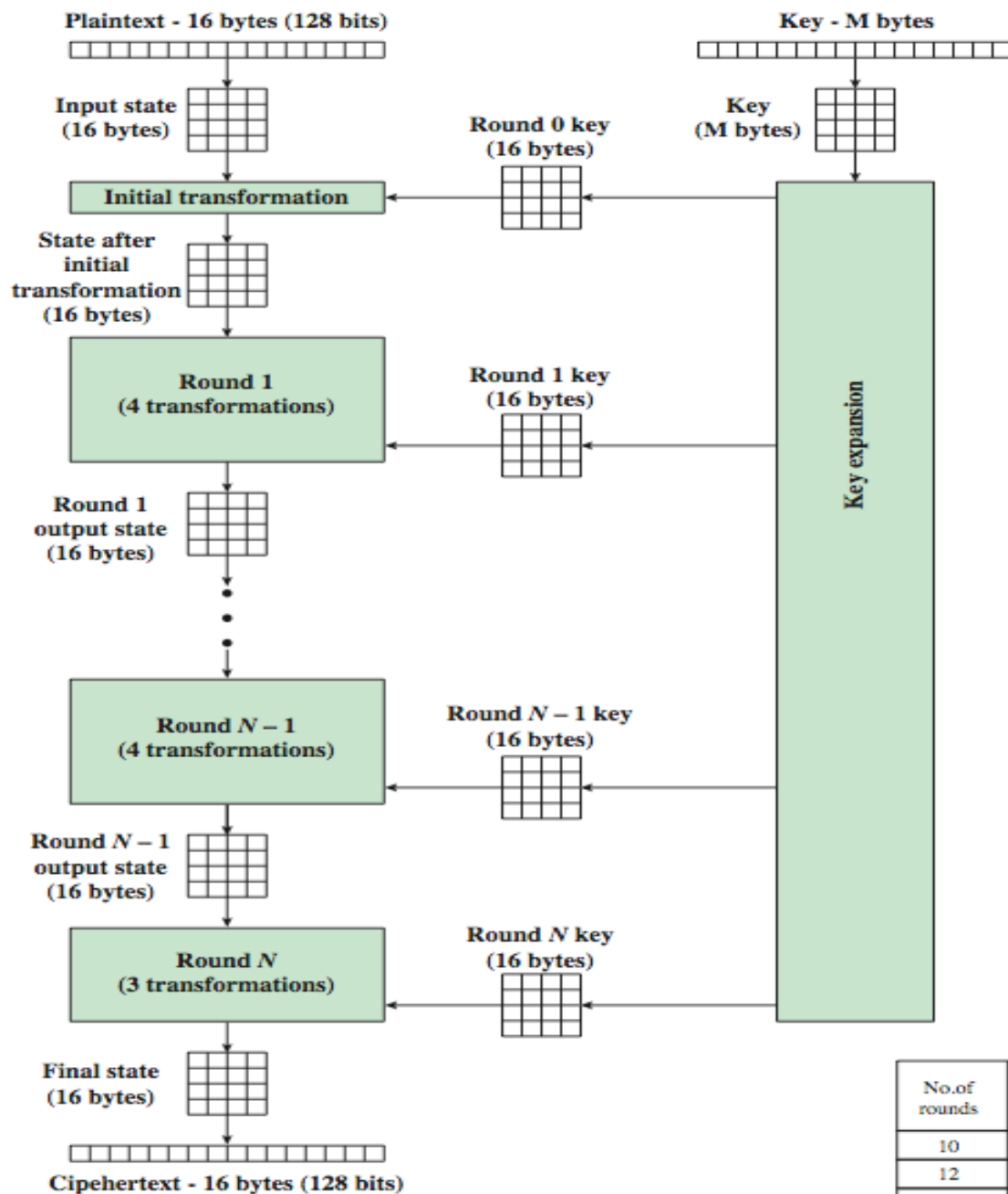


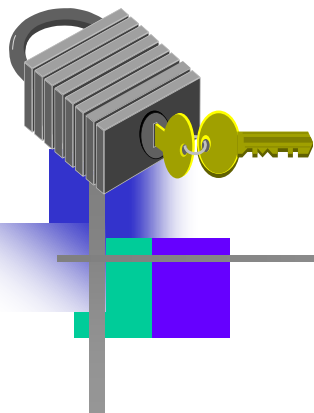
AES Cipher Stages

- 4 Stages are used(1 permutation, 3 substitution):
1. **Substitute** bytes (S-box)
 2. Shift rows (row-by-row permutation)
 3. **Mix columns** (substitution using function of all bytes in the column)
 4. **Add Round Key** (bitwise XOR with key)

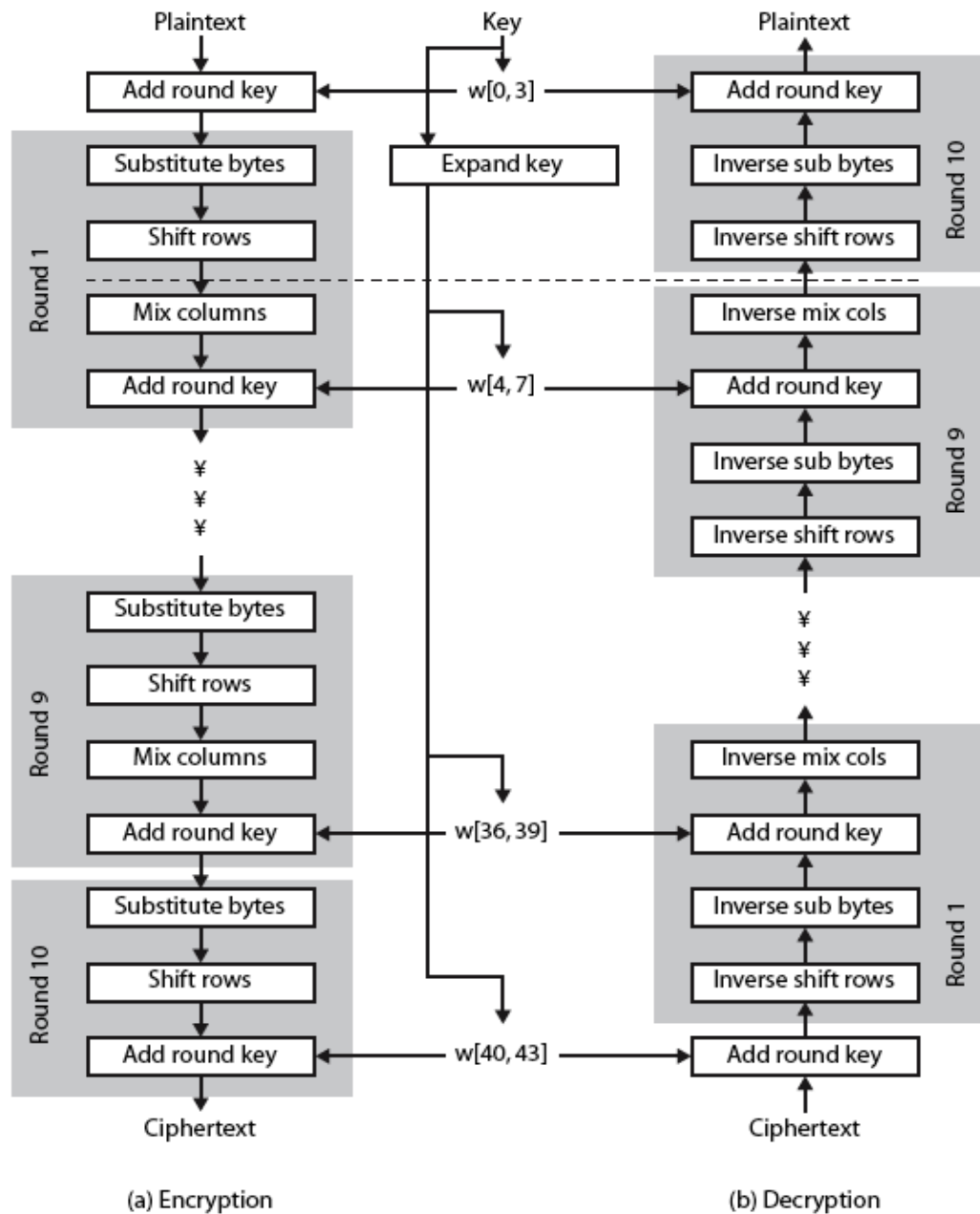


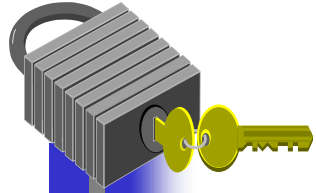
AES Encryption Process





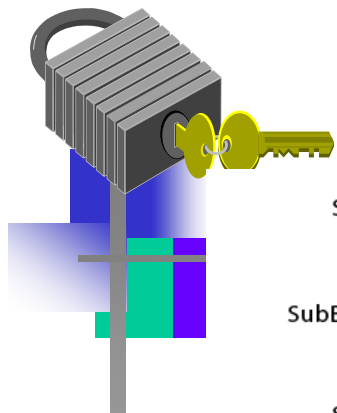
AES Structure



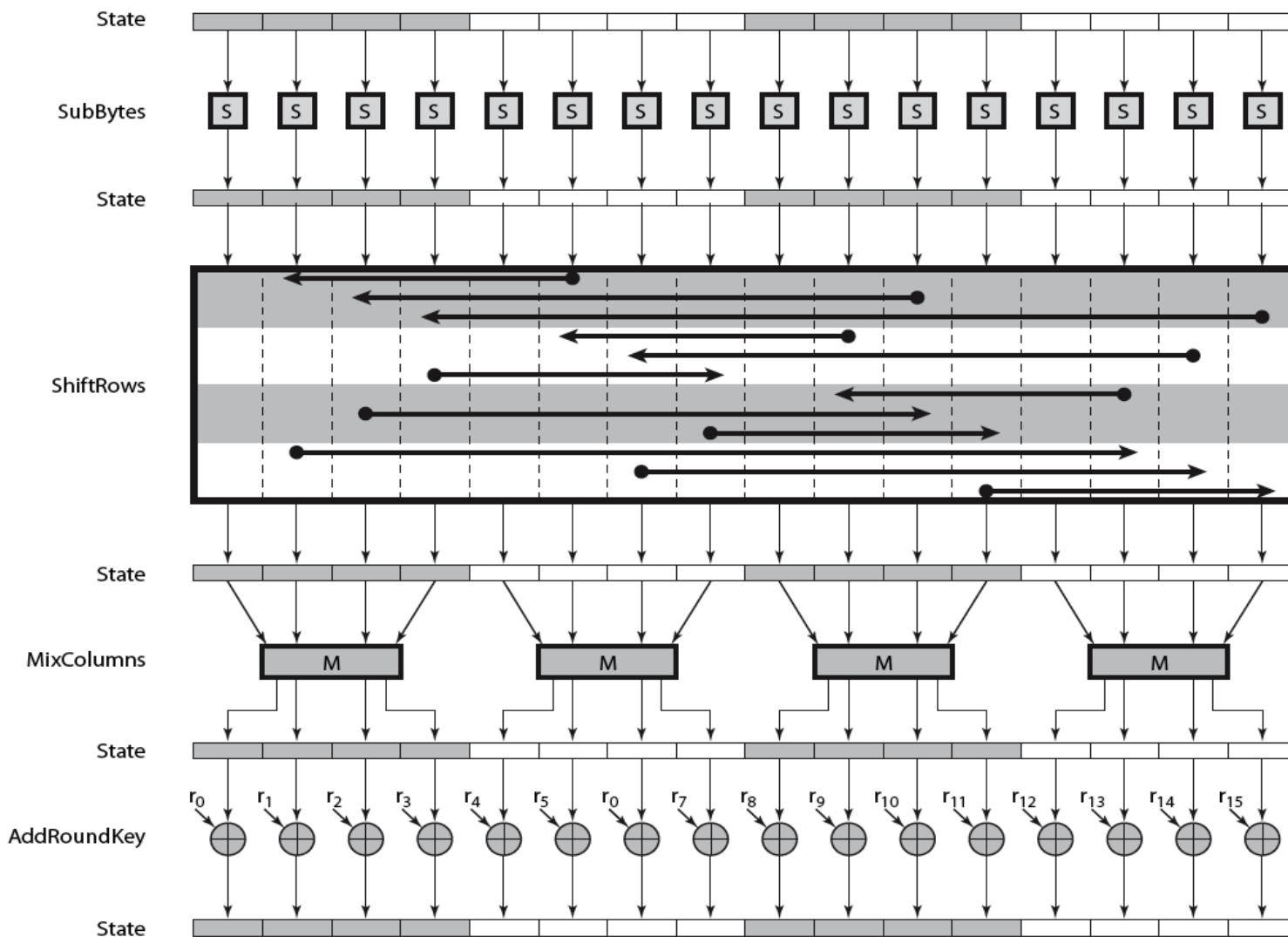


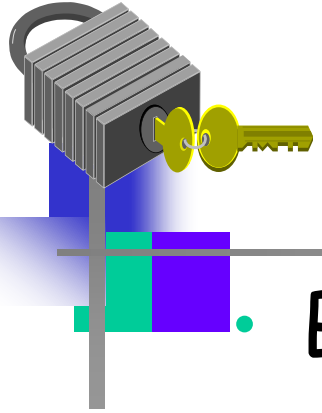
AES Algorithm

- Input is a single 128 bit block (square matrix)
- Block is copied into the *STATE* array
- At each stage the *STATE* array is modified by encryption or decryption
- After the final stage the *STATE* array is copied to an output matrix.
- The key is also a square matrix of 128 bits



AES Round

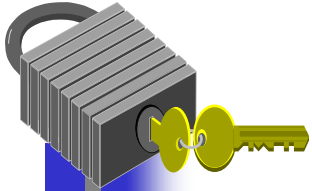




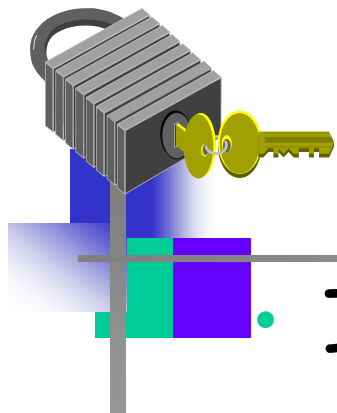
A Few Other Block Ciphers

- Briefly...
 - IDEA
 - Blowfish
 - RC6
- More detailed...
 - TEA

Other Symmetric Block Ciphers

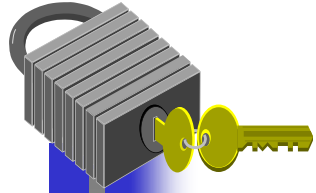


- International Data Encryption Algorithm (IDEA)
 - 128-bit key
 - Used in PGP
- Blowfish
 - Easy to implement
 - High execution speed
 - Run in less than 5K of memory
- CAST-128
 - Key size from 40 to 128 bits
 - The round function differs from round to round



IDEA

- Invented by James Massey
 - One of the giants of modern crypto
- IDEA has 64-bit block, 128-bit key
- IDEA uses **mixed-mode arithmetic**
- Combine different math operations
 - IDEA the first to use this approach
 - Frequently used today



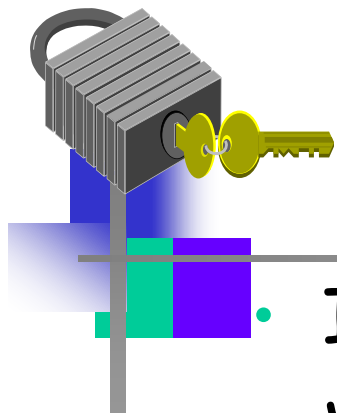
Blowfish

- Blowfish encrypts 64-bit blocks
- Key is variable length, up to 448 bits
- Invented by Bruce Schneier
- Almost a Feistel cipher

$$R_i = L_{i-1} \oplus K_i$$

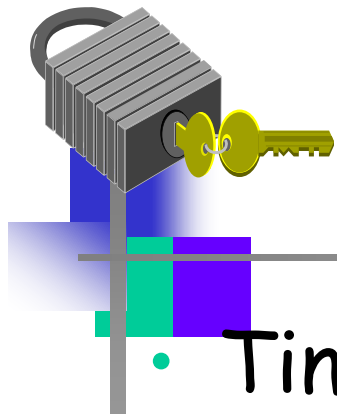
$$L_i = R_{i-1} \oplus F(L_{i-1} \oplus K_i)$$

- The round function F uses 4 S-boxes
 - Each S-box maps 8 bits to 32 bits
- **Key-dependent S-boxes**
 - S-boxes determined by the key



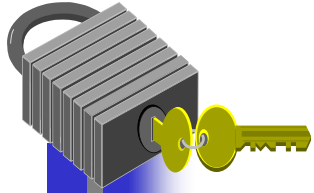
RC6

- Invented by Ron Rivest (of RSA fame)
- Variables
 - Block size
 - Key size
 - Number of rounds
- An AES finalist
- Uses **data dependent rotations**
 - Unusual for algorithm to depend on plaintext



Time for TEA

- Tiny Encryption Algorithm (TEA)
- 64 bit block, 128 bit key
- Assumes 32-bit arithmetic
- Number of rounds is variable (32 is considered secure)
- Uses “weak” round function, so large number of rounds required



TEA Encryption

Assuming 32 rounds:

$(K[0], K[1], K[2], K[3]) = 128 \text{ bit key}$

$(L, R) = \text{plaintext (64-bit block)}$

$\text{delta} = 0x9e3779b9$

$\text{sum} = 0$

for $i = 1$ to 32

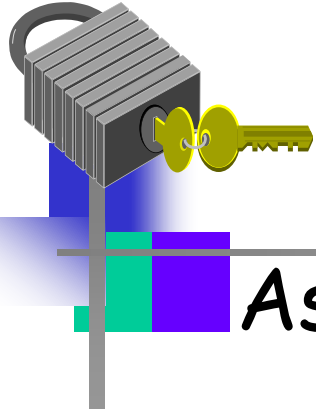
$\text{sum} += \text{delta}$

$L += ((R \ll 4) + K[0]) \wedge (R + \text{sum}) \wedge ((R \gg 5) + K[1])$

$R += ((L \ll 4) + K[2]) \wedge (L + \text{sum}) \wedge ((L \gg 5) + K[3])$

next i

ciphertext = (L, R)



TEA Decryption

Assuming 32 rounds:

$(K[0], K[1], K[2], K[3]) = 128 \text{ bit key}$

$(L, R) = \text{ciphertext (64-bit block)}$

$\text{delta} = 0x9e3779b9$

$\text{sum} = \text{delta} \ll 5$

for $i = 1$ to 32

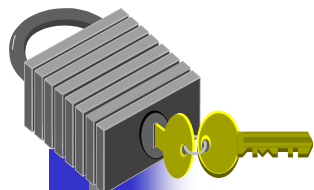
$R \leftarrow ((L \ll 4) + K[2]) \wedge (L + \text{sum}) \wedge ((L \gg 5) + K[3])$

$L \leftarrow ((R \ll 4) + K[0]) \wedge (R + \text{sum}) \wedge ((R \gg 5) + K[1])$

$\text{sum} \leftarrow \text{sum} + \text{delta}$

next i

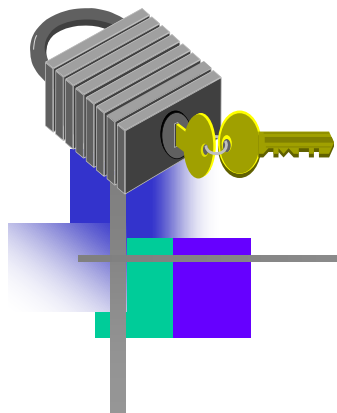
plaintext = (L, R)



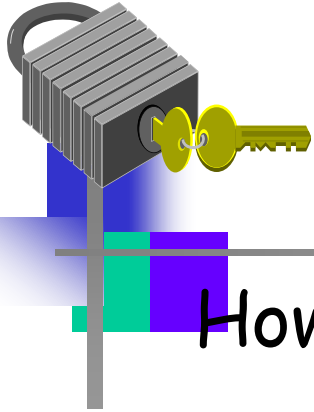
TEA Comments

Almost a Feistel cipher

- Uses + and - instead of \oplus (XOR)
- Simple, easy to implement, fast, low memory requirement, etc.
- Possibly a “related key” attack
- eXtended TEA (XTEA) eliminates related key attack (slightly more complex)
- Simplified TEA (STEAL) — insecure version used as an example for cryptanalysis



Block Cipher Modes



Multiple Blocks

How to encrypt multiple blocks?

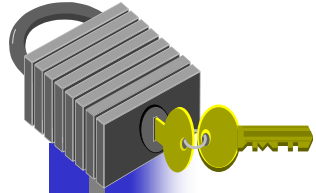
- Do we need a new key for each block?
 - As bad as (or worse than) a one-time pad!
- Encrypt each block independently?
- Make encryption depend on previous block?
 - That is, can we "chain" the blocks together?
- How to handle partial blocks?
 - We won't discuss this issue



Modes of Operation

- The different ways an encryption algorithm can be used are modes of operation
- NIST SP 800-38A defines 5 modes:
 1. Electronic codebook (ECB) mode
 2. Cipher Block Chaining (CBC) mode
 3. Cipher Feedback (CFB) mode
 4. Output Feedback (OFB) mode
 5. Counter (CTR) mode

See also http://en.wikipedia.org/wiki/Block_cipher_modes_of_operation



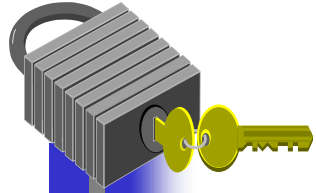
Modes of Operation

- In cryptography, **modes of operation** is the procedure of enabling the repeated and secure use of a block cipher under a single key.
- A block cipher by itself allows encryption only of a single data block of the cipher's block length.
- A mode of operation describes the process of encrypting each of these blocks, and generally uses randomization.
- http://en.wikipedia.org/wiki/Block_cipher_modes_of_operation



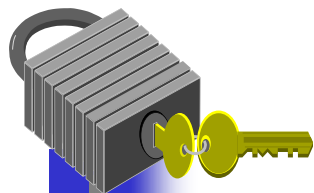
Modes of Operation

- Many modes — we discuss 3 most popular
- Electronic Codebook (**ECB**) mode
 - Encrypt each block independently
 - Most obvious, but has a serious weakness
- Cipher Block Chaining (**CBC**) mode
 - Chain the blocks together
 - More secure than ECB, virtually no extra work
- Counter Mode (**CTR**) mode
 - Block ciphers acts like a stream cipher
 - Popular for random access



Modes of Operation

- Block ciphers encrypt fixed size blocks
 - eg. DES encrypts 64-bit blocks with 56-bit key
 - AES uses 128 bit blocks
 - For larger sizes, break plain text into blocks
- Need some way to en/decrypt arbitrary amounts of data in practice
- have **block** and **stream** modes
- Cover a wide variety of applications
- Can be used with any block cipher



Electronic Codebook Mode (ECB)

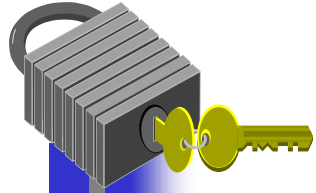
- Message is broken into independent blocks which are encrypted
- Each block is a value which is substituted, like a codebook, hence name
- Each block B is encoded or decoded independently of the other blocks:

$$C_i = E_k(P_i)$$

$$B_i = D_k(C_i)$$

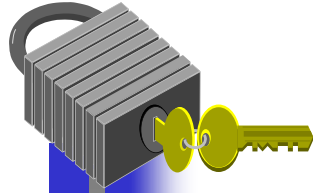
- Uses: secure transmission of single values

https://www.youtube.com/watch?v=qTjW_6q_61g



Electronic Codebook Mode

- Codebook- for a given key there is a unique cipher text for every b -bit block of plaintext.
- Advantages:
 - Simplicity
 - Tolerates block loss (eg. over network)
 - Used to send a few block of data
- Disadvantage:
 - ECB mode may reveal pattern in text, i.e. blocks that are identical, will be encrypted in the same way



ECB Mode

Notation: $C = E(P, K)$

- Given plaintext $P_0, P_1, \dots, P_m, \dots$
- Most obvious way to use a block cipher:

Encrypt

$$C_0 = E(P_0, K)$$

$$C_1 = E(P_1, K)$$

$$C_2 = E(P_2, K) \dots$$

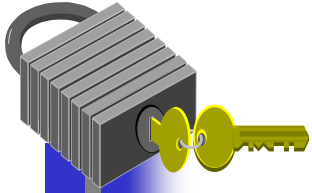
Decrypt

$$P_0 = D(C_0, K)$$

$$P_1 = D(C_1, K)$$

$$P_2 = D(C_2, K) \dots$$

- For fixed key K , this is “electronic” version of a codebook cipher (without additive)
 - With a different codebook for each key



ECB Cut and Paste

- Suppose plaintext is

Alice digs Bob. Trudy digs Tom.

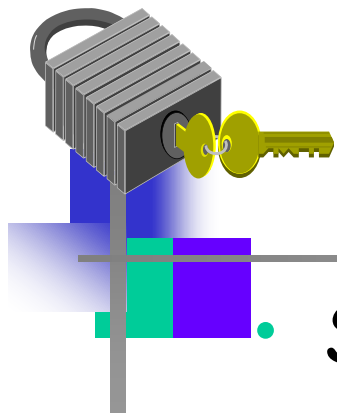
- Assuming 64-bit blocks and 8-bit ASCII:

P_0 = "Alice di", P_1 = "gs Bob. ",

P_2 = "Trudy di", P_3 = "gs Tom. "

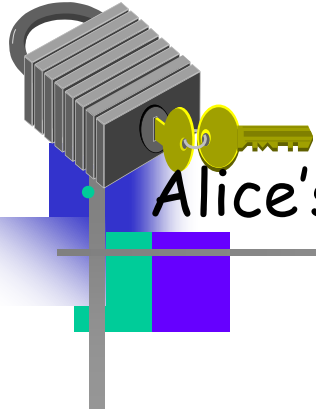
- Ciphertext: C_0, C_1, C_2, C_3
- Trudy cuts and pastes: C_0, C_3, C_2, C_1
- Decrypts as

Alice digs Tom. Trudy digs Bob



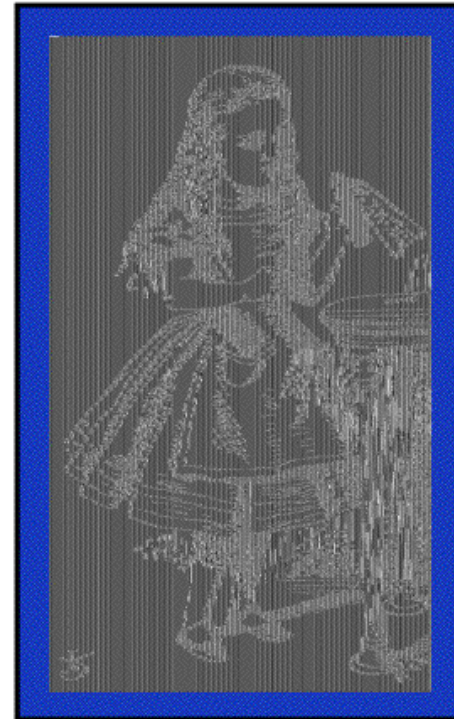
ECB Weakness

- Suppose $P_i = P_j$
- Then $C_i = C_j$ and Trudy knows $P_i = P_j$
- This gives Trudy some information, even if she does not know P_i or P_j
- Trudy might know P_i
- Is this a serious issue?



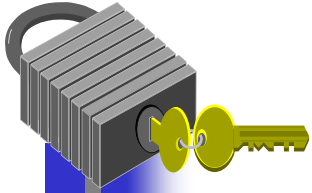
Alice Hates ECB Mode

Alice's uncompressed image, and ECB encrypted (TEA)



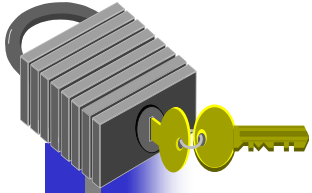
- ❑ Why does this happen?
- ❑ Same plaintext yields same ciphertext!

Cipher Block Chaining Mode of Operation



- Message is broken into blocks
- Linked together in encryption operation
- Each previous cipher block is chained with current plaintext block, hence name
- Use Initial Vector (IV) to start process
- Input to encryption algorithm bears no relationship to plaintext block
- Uses: bulk data encryption, authentication

Cipher Block Chaining Mode of Operation



- Cipher Block Chaining Mode (CBC)
 - The input to the encryption algorithm is the XOR of the current plaintext block and the preceding ciphertext block.
 - Repeating pattern of 64-bits are not exposed

$$C_i = E_k[C_{i-1} \oplus P_i]$$

$$D_K[C_i] = D_K[E_K(C_{i-1} \oplus P_i)]$$

$$D_K[C_i] = (C_{i-1} \oplus P_i)$$

$$C_{i-1} \oplus D_K[C_i] = C_{i-1} \oplus C_{i-1} \oplus P_i = P_i$$

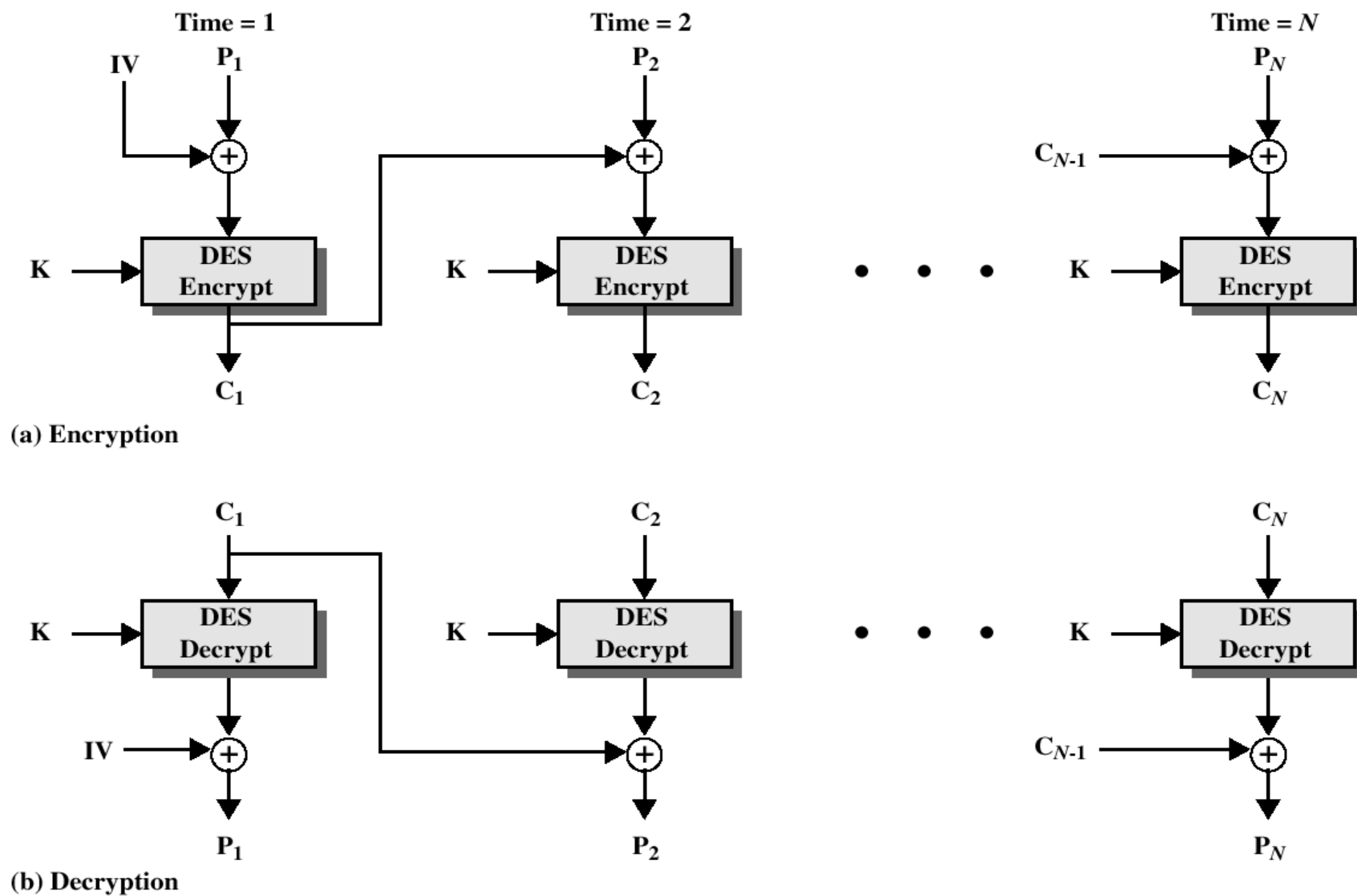
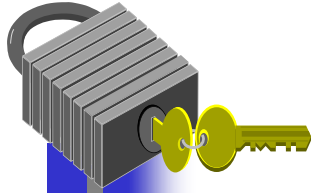


Figure 2.7 Cipher Block Chaining (CBC) Mode



CBC Mode

Blocks are “chained” together

- A random initialization vector, or IV, is required to initialize CBC mode
- IV is random, but not secret

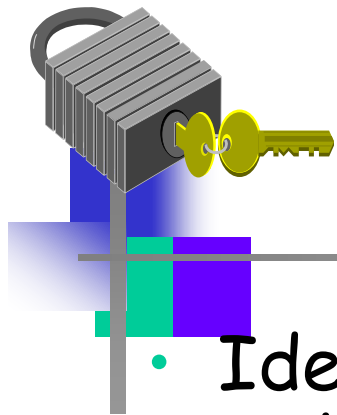
Encryption

$$\begin{aligned}C_0 &= E(\text{IV} \oplus P_0, K), \\C_1 &= E(C_0 \oplus P_1, K), \\C_2 &= E(C_1 \oplus P_2, K), \dots\end{aligned}$$

Decryption

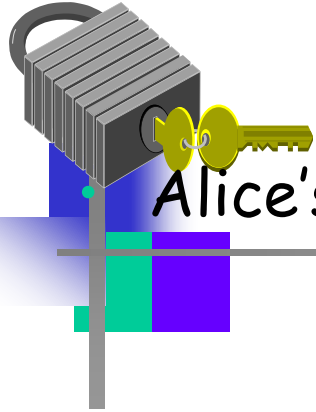
$$\begin{aligned}P_0 &= \text{IV} \oplus D(C_0, K), \\P_1 &= C_0 \oplus D(C_1, K), \\P_2 &= C_1 \oplus D(C_2, K), \dots\end{aligned}$$

- Analogous to classic codebook *with additive*



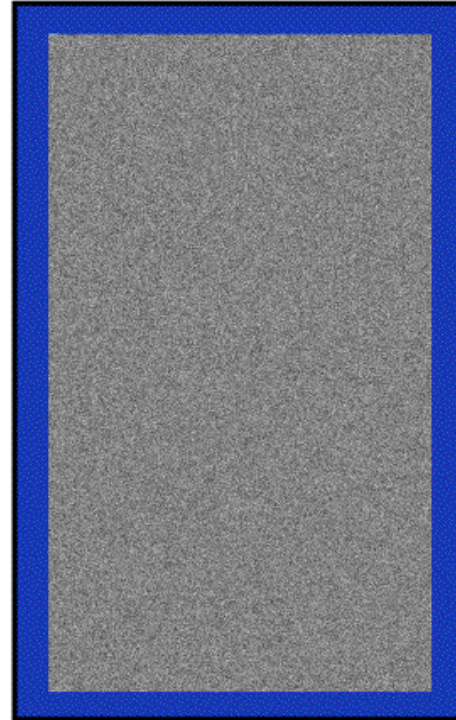
CBC Mode

- Identical plaintext blocks yield different ciphertext blocks — this is good!
- If C_1 is garbled to, say, G then
$$P_1 \neq C_0 \oplus D(G, K), P_2 \neq G \oplus D(C_2, K)$$
- But $P_3 = C_2 \oplus D(C_3, K), P_4 = C_3 \oplus D(C_4, K), \dots$
- Automatically recovers from errors!
- Cut and paste is still possible, but more complex (and will cause garbles)

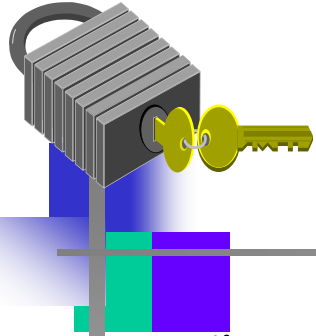


Alice Likes CBC Mode

Alice's uncompressed image, Alice CBC encrypted (TEA)



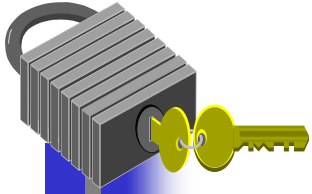
- ❑ Why does this happen?
- ❑ Same plaintext yields different ciphertext!



Counter (CTR)

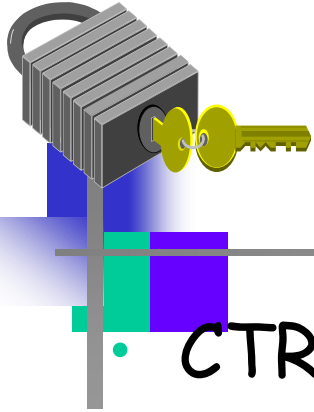
- A "new" mode, though proposed earlier
- Similar to Outback Feedback (OFB) but encrypts a counter value rather than any feedback value
- Must have a different key & counter value for every plaintext block (never reused)
$$O_i = E_K(i)$$
$$C_i = P_i \text{ XOR } O_i$$
- uses: high-speed network encryptions

Advantages and Limitations of CTR



• Efficiency

- can do parallel encryptions in h/w or s/w
- can preprocess in advance of need
- good for bursty high speed links
- Random access to encrypted data blocks
- Provable security (good as other modes)
- Must ensure never reuse key/counter values, otherwise could break, like OFB



Counter Mode (CTR)

- CTR is popular for random access
- Use block cipher like a stream cipher

Encryption

$$C_0 = P_0 \oplus E(\text{IV}, K),$$

$$C_1 = P_1 \oplus E(\text{IV}+1, K),$$

$$C_2 = P_2 \oplus E(\text{IV}+2, K), \dots$$

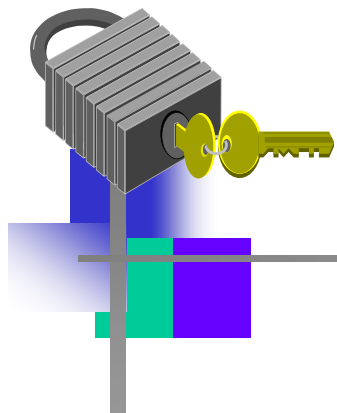
Decryption

$$P_0 = C_0 \oplus E(\text{IV}, K),$$

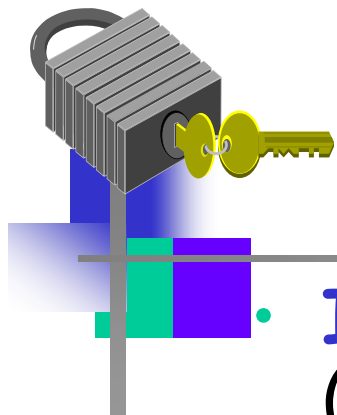
$$P_1 = C_1 \oplus E(\text{IV}+1, K),$$

$$P_2 = C_2 \oplus E(\text{IV}+2, K), \dots$$

- CBC can also be used for random access
 - With a significant limitation...

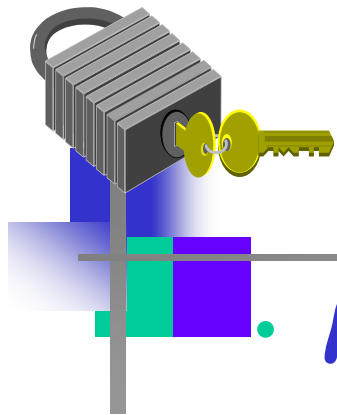


Integrity



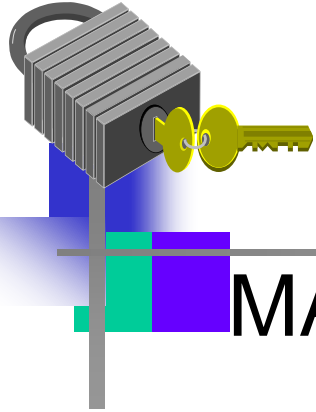
Data Integrity

- **Integrity** — detect unauthorized writing (i.e., modification of data)
- Example: Inter-bank fund transfers
 - Confidentiality may be nice, integrity is critical
- Encryption provides **confidentiality** (prevents unauthorized disclosure)
- Encryption alone does **not** provide integrity
 - One-time pad, ECB cut-and-paste, etc.



MAC

- **Message Authentication Code (MAC)**
 - Used for data **integrity**
 - Integrity **not** the same as confidentiality
- MAC is computed as **CBC residue**
 - That is, compute CBC encryption, saving only final cipher text block, the MAC



MAC Computation

MAC computation (assuming N blocks)

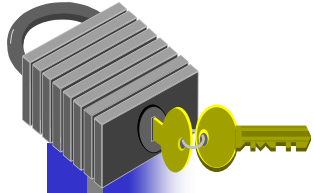
$$C_0 = E(\text{IV} \oplus P_0, K),$$

$$C_1 = E(C_0 \oplus P_1, K),$$

$$C_2 = E(C_1 \oplus P_2, K), \dots$$

$$C_{N-1} = E(C_{N-2} \oplus P_{N-1}, K) = \text{MAC}$$

- MAC sent with IV and plaintext
- Receiver does same computation and verifies that result agrees with MAC
- Note: receiver must know the key K



Does a MAC work?

Suppose Alice has 4 plaintext blocks

- Alice computes

$$C_0 = E(IV \oplus P_0, K), C_1 = E(C_0 \oplus P_1, K),$$

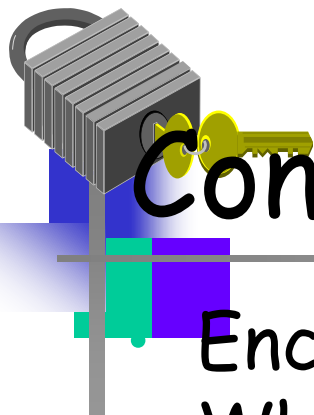
$$C_2 = E(C_1 \oplus P_2, K), C_3 = E(C_2 \oplus P_3, K) = \text{MAC}$$

- Alice sends IV, P_0, P_1, P_2, P_3 and **MAC** to Bob
- Suppose Trudy changes P_1 to X
- Bob computes

$$C_0 = E(IV \oplus P_0, K), C_1 = E(C_0 \oplus X, K),$$

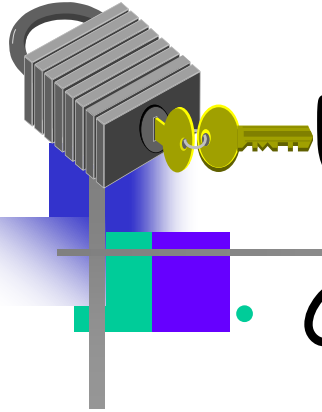
$$C_2 = E(C_1 \oplus P_2, K), C_3 = E(C_2 \oplus P_3, K) = \text{MAC} \neq \text{MAC}$$

- That is, error propagates into **MAC**
- Trudy can't make **MAC** == **MAC** without K



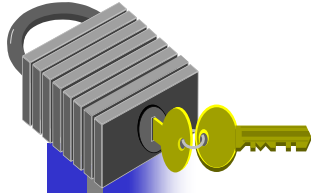
Confidentiality and Integrity

- Encrypt with one key, MAC with another key
- Why not use the same key?
 - Send last encrypted block (MAC) twice?
 - This cannot add any security!
- Using different keys to encrypt and compute MAC works, even if keys are related
 - But, twice as much work as encryption alone
 - Can do a little better — about 1.5 “encryptions”
- Confidentiality and integrity with same work as one encryption is a research topic



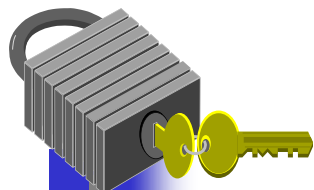
Uses for Symmetric Crypto

- Confidentiality
 - Transmitting data over insecure channel
 - Secure storage on insecure media
- Integrity (MAC)
- Authentication protocols (later...)
- Anything you can do with a hash function (upcoming chapter...)



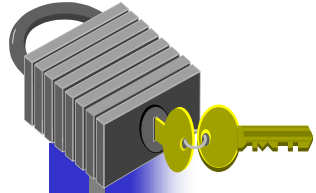
Recommended Reading

- Stallings, W. *Cryptography and Network Security: Principles and Practice*, 5th edition. Prentice Hall, 2011
- Schneier, B. *Applied Cryptography*, New York: Wiley, 1996
- Mel, H.X. Baker, D. *Cryptography Decrypted*. Addison Wesley, 2001
- Simon Singh, *The Code Book*, (on-line)
- <http://simonsingh.net/books/the-code-book/the-book/>
- David, Kahn, *The Codebreakers*, 1996.



Videos (Stamp)

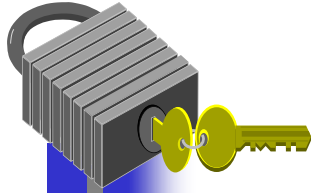
- **Crypto Basics -Mark Stamp- Info Security**
<http://www.youtube.com/watch?v=gnhTDFEQK8A&feature=related>
- Double Transposition - One Time Pad
http://www.youtube.com/watch?v=_8SQLjT_g9w&feature=related
- 3-1 Symmetric Key - Stream And Block Ciphers
http://www.youtube.com/watch?v=1GoP_HfF_v4&feature=related
- 3-2 Symmetric Key - Stream Ciphers- RC4
<http://www.youtube.com/watch?v=riIp6EQOJOg&feature=related>
- *3-3 Symmetric Key - Block Ciphers, Feistel cipher
<http://www.youtube.com/watch?v=ySZvE9vOfEQ&feature=related>
- 3-4 Symmetric key = Block Ciphers, DES
https://www.youtube.com/watch?v=G_guTnTcoqg
- 3-5 Symmetric Key -Block ciphers - DES, 3DES
http://www.youtube.com/watch?v=jQEx_vxLnrE&feature=related



Videos (Stamp)

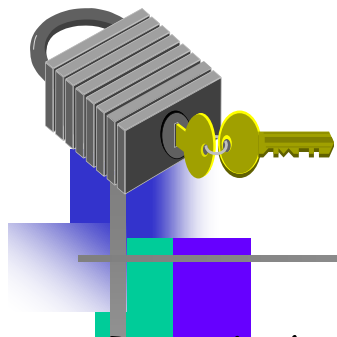
3-6 Symmetric Key -block, AES

- <https://www.youtube.com/watch?v=ZhILF5Dhx74>
- 3-7 Information Security: Principles and Practices
- <https://www.youtube.com/watch?v=aR29pnuJ6fQ>
- 3-8 Symmetric Key Crypto- block cipher modes, ECB
- https://www.youtube.com/watch?v=qTjW_6q_61g
- 3-9 Symmetric Key Crypto- block cipher, CBC, CTR
- <https://www.youtube.com/watch?v=057hz60lhZw>
- 3-10 Symmetric Key Crypto- integrity, message authentication code, MAC
- https://www.youtube.com/watch?v=8XcFiMju_94



More Video Resources

- <http://www.FreeSecurityPlus.com>
- One time pad demo
- <https://www.youtube.com/watch?v=3uJl2zutyO4>
- Block and Stream Ciphers
- https://www.youtube.com/watch?v=E_3M41NrtsU



More Resources

- RSA Laboratories <http://www.rsa.com/rsalabs/>
- <http://www.rsa.com/rsalabs/node.asp?id=2174> Stream ciphers
- Search Security - Tutorials and Information
- <http://searchsecurity.techtarget.com/tutorial/Information-security-tutorials>
- <http://searchsecurity.techtarget.com/definition/block-cipher>
- Stamp
- http://cs.sjsu.edu/~stamp/crypto/PowerPoint_PDF/5_StreamCiphers.pdf
- Stream vs Block
- <http://people.seas.harvard.edu/~salil/cs120/docs/lec13.pdf>
- Digital signatures
- <https://www.youtube.com/watch?v=HubAvQg6SPM>