Recursion CS 201

Introduction

- Recursion is an extremely powerful problem-solving technique
 - It breaks a problem into smaller identical problems and uses the same function to solve these smaller problems
 - It is an alternative to iterative solutions, which use loops

- Facts about recursive solutions
 - A recursive function calls itself.
 - Each recursive call solves an identical but a smaller problem
 - Base case must be defined (it enables to stop the recursive calls)
 - Eventually, one of the smaller problems must be the base case

Simple example: Write a global function that displays a given C-style string backward

Recursive solution:

- Each recursive call diminishes the string length by 1
- Base case: displaying the empty string backward

```
void displayBackward( char* str ) {
  if ( str[0] == '\0' ) null character
    return;

  displayBackward( str + 1 );
  cout << str[0];
}</pre>
```

Recursion and efficiency: Fibonacci function

Recurrence relation:

```
F(n) = F(n-1) + F(n-2)
```

Base cases:

```
F(1) = 1
F(2) = 1
```

```
int recursiveFib( int n ) {
  if ( n <= 2 )
    return 1;

return recursiveFib( n - 1) + recursiveFib( n - 2 );
}</pre>
```

Recursion and efficiency

- Some recursive solutions are so inefficient that they should not be used
- Factors contributing to this inefficiency
 - Inherent inefficiency of some recursive algorithms (such as the recursiveFib function)
 - Overhead associated with function calls
- Do not use a recursive solution if it is inefficient and there is a clear and efficient iterative solution

More examples: Write a recursive function for the binary search algorithm

A high-level pseudocode for binary search

```
if ( anArray is of size 1 )
    determine if anArray's item is equal to the searched value
else {
    find the midpoint of anArray
    determine which half of anArray contains the searched value
    if ( the value is in the first half of anArray )
        binarySearch( first half of anArray, value )
    else
        binarySearch( second half of anArray, value )
}
```

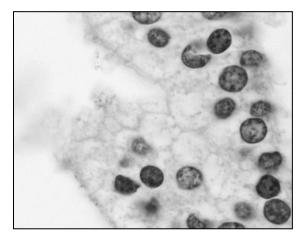
Implementation issues

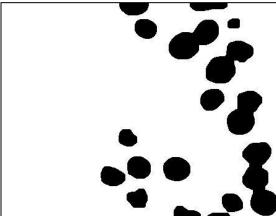
- How to pass "half of anArray" to the function?
- How to determine the base case(s)?
- How to return the result?

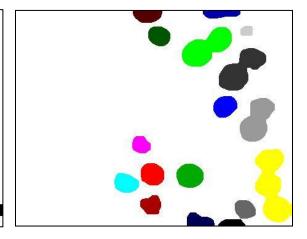
More examples: Write a recursive function for the binary search algorithm

```
int binarySearch( int* arr, int low, int high, int key ) {
   if (low > high)
      return -1:
   int mid = (low + high) / 2;
   if ( arr[mid] == key )
       return mid;
   if ( arr[mid] > key ) //search first half
       return binarySearch( arr, low, mid - 1, key);
                                //else search second half
   return binarySearch( arr, mid + 1, high, key );
                                                             //dont need else because of return
                                                             if(arr[mid] > key)
                                                             binarySearch(arr, low ,mid-1, key)
                                                             else
                                                             binarySearch(arr, mid+1, high, key)
```

<u>Application 1</u>: Suppose that we want to locate cell nuclei in a gray-level image whose pixel intensities are in between 0 and 255. To find the nucleus locations, one may first obtain a black-and-white image, whose intensities are either 0 or 1, using some image processing techniques (e.g., thresholding). Then, s/he may identify each connected component of the 1-pixels as a cell nucleus.



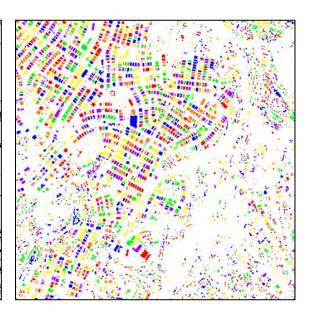




<u>Application 2</u>: Similarly, in the image below, we want to identify individual buildings. Connected component analysis can be used after obtaining a black-and-white image of buildings.







```
int** findConnectedComponents( int** arr, int row, int column ) {
   int** labels, i, j, currLabel;
   labels = new int*[ row ];
   for (i = 0; i < row; i++) {
     labels[ i ] = new int[ column ];
     for (j = 0; j < column; j++)
        labels[i][j] = 0;
  currLabel = 1;
   for (i = 0; i < row; i++)
     for (j = 0; j < column; j++)
         if ( arr[ i ][ j ] && !labels[ i ][ j ] )
           fourConnectivity( arr, labels, row, column, i, j, currLabel++ );
  return labels:
```

```
void fourConnectivity( int** arr, int** labels, int row, int column,
                      int i, int j, int currLabel ) {
   if ( arr[i][j] == 0 )
     return;
   if (labels[i][j] > 0)
     return;
   labels[i][j] = currLabel;
   if (i - 1 >= 0)
     fourConnectivity(arr, labels, row, column, i - 1, j, currLabel);
   if (i + 1 < row)
     fourConnectivity( arr, labels, row, column, i + 1, j, currLabel );
   if (j - 1 >= 0)
     fourConnectivity(arr, labels, row, column, i, j - 1, currLabel);
   if (j + 1 < column)
     fourConnectivity( arr, labels, row, column, i, j + 1, currLabel );
```